Type-and-Effect Systems

Our plain-old type systems have judgments like \( \Gamma \vdash e : \tau \) to mean:

- \( e \) won’t get stuck
- If \( e \) produces a value, that value has type \( \tau \)

Adding effects reuses the “plumbing” of our typing rules to compute something about “how \( e \) executes”.

- There are many things we might want to conservatively approximate
  - Example: What exceptions might get thrown
- All effect systems are very similar, especially how they treat functions
  - Example: All values have no effect since their “computation” does nothing
First a type system

(In this example, exceptions raise constant strings $s$)

\[
\begin{align*}
\tau &::= \text{bool} \mid \tau \rightarrow \tau \mid \tau \ast \tau \\
e &::= x \mid \text{true} \mid \text{false} \mid \lambda x. \ e \mid e \ e \mid (e, e) \mid e.1 \mid e.2 \\
&\quad \mid \text{if } e \text{ then } e \text{ else } e \mid \text{raise } s \mid \text{try } e \text{ handle } s \ e
\end{align*}
\]

\[
\begin{array}{c}
\begin{array}{c}
\Gamma \vdash e : \tau \\
\end{array}
\begin{array}{c}
\begin{array}{c}
\Gamma \vdash x : \Gamma(x) \\
\end{array}
\begin{array}{c}
\Gamma, x : \tau_1 \vdash e : \tau_2 \\
\Gamma \vdash \lambda x. \ e : \tau_1 \rightarrow \tau_2 \\
\Gamma \vdash e_1 : \tau_1 \quad \Gamma \vdash e_2 : \tau_2 \\
\Gamma \vdash (e_1, e_2) : \tau_1 \ast \tau_2 \\
\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : \tau \quad \Gamma \vdash e_3 : \tau \\
\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : \tau \\
\Gamma \vdash \text{raise } s : \tau \\
\end{array}
\begin{array}{c}
\Gamma \vdash e_1 : \tau \quad \Gamma \vdash e_2 : \tau \\
\Gamma \vdash \text{try } e_1 \text{ handle } s \ e_2 : \tau
\end{array}
\end{array}
\end{array}
\]
Add effects

\[
\begin{align*}
\epsilon & ::= \ldots \text{sets of strings}\ldots \\
\tau & ::= \text{bool} \mid \tau \xrightarrow{\epsilon} \tau \mid \tau \star \tau \\
e & ::= x \mid \text{true} \mid \text{false} \mid \lambda x. e \mid e \ e \mid (e, e) \mid e.1 \mid e.2 \\
& \quad \mid \text{if } e \text{ then } e \text{ else } e \mid \text{raise } s \mid \text{try } e \text{ handle } s \ e
\end{align*}
\]

\[
\begin{array}{c}
\begin{array}{c}
\Gamma \vdash e : \tau; \epsilon \\
\hline \\
\Gamma \vdash x : \Gamma(x); \emptyset \\
\hline \\
\Gamma \vdash \text{true} : \text{bool}; \emptyset \\
\hline \\
\Gamma \vdash \text{false} : \text{bool}; \emptyset \\
\hline \\
\Gamma, x : \tau_1 \vdash e : \tau_2; \epsilon \\
\hline \\
\Gamma \vdash \lambda x. e : \tau_1 \xrightarrow{\epsilon} \tau_2; \emptyset \\
\hline \\
\Gamma \vdash e_1 : \tau_2 \xrightarrow{\epsilon_3} \tau_1; \epsilon_1 \\
\hline \\
\Gamma \vdash e_2 : \tau_2; \epsilon_2 \\
\hline \\
\Gamma \vdash e : \tau_1 \star \tau_2; \epsilon \\
\hline \\
\Gamma \vdash (e_1, e_2) : \tau_1 \star \tau_2; \epsilon_1 \cup \epsilon_2 \\
\hline \\
\Gamma \vdash e.1 : \tau_1; \epsilon \\
\hline \\
\Gamma \vdash e.2 : \tau_2; \epsilon \\
\hline \\
\Gamma \vdash e_1 : \text{bool}; \epsilon_1 \\
\hline \\
\Gamma \vdash e_2 : \tau; \epsilon_2 \\
\hline \\
\Gamma \vdash e_3 : \tau; \epsilon_3 \\
\hline \\
\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : \tau; \epsilon_1 \cup \epsilon_2 \cup \epsilon_3 \\
\hline \\
\Gamma \vdash \text{raise } s : \tau; \{s\} \\
\hline \\
\Gamma \vdash \text{try } e_1 \text{ handle } s \ e_2 : \tau; (\epsilon_1 - \{s\}) \cup \epsilon_2
\end{array}
\end{array}
\]
Key facts

Soundness: If $\cdot \vdash e : \tau; \epsilon$ and $e$ raises uncaught exception $s$, then $s \in \epsilon$.

- Corollary to Preservation and Progress (once you define the operational semantics for exceptions)

All effect systems work this way:

- Values effectless
- Functions have *latent effects*
- Conservative due to if and try/handle
- Subeffecting (not shown) is sound and important
  - Functions covariant in effects

Only a couple rules special to this effect system

- Not always sets and $\cup$
Other effect systems

• Definitely terminates (0) or possibly diverges (1)
  – Give \texttt{fix} \( e \) effect 1
  – Give values effect 0
  – Treat \( \cup \) as max
  – No change to rules for functions, pairs, conditionals, etc.

• What type casts might occur (Nita POPL08)
• Are the right variables used in transactions (Moore POPL08)
• Does code obey a locking protocol
• ...

Really a general way to lift static analysis to higher-order functions

• And you want things like \textit{effect polymorphism} to give a useful type to functions like map
Concurrent and Parallelism

- PL support for concurrency/parallelism a huge topic
  - And increasingly important (not traditionally in 505)
- We’ll just do explicit threads plus:
  - Shared memory (locks and transactions)
  - Futures
  - Synchronous message passing (Concurrent ML)
- We’ll skip
  - Process calculi (foundational message-passing)
  - Asynchronous methods, join calculus, ...
  - Data-parallel languages (Snyder)
  - ...
- Mostly in ML syntax (inference rules where convenient)
Concurrency vs. Parallelism

My take on this (terminology not universal, but distinction important):

Software is **concurrent** if a primary intellectual challenge is responding to external events from multiple sources in a timely manner.

- Examples: operating system, shared hashtable, version control
- Key challenge is responsiveness
- Often provide responsiveness via threads

Software is **parallel** if a primary intellectual challenge is using extra computational resources to do more useful work per unit time.

- Examples: scientific computing, most graphics, a lot of servers
- Key challenge is Amdahl’s Law (no sequential bottlenecks)
- Often provide parallelism via threads on different processors
Threads

High-level: “Communicating sequential processes”

Low-level: “Multiple stacks plus communication”

From Caml’s thread.mli:

```ocaml
type t (* thread handle; remember we’re in module Thread *)
val create : ('a->'b) -> 'a -> t (* run new thread *)
val self : unit -> t (* what thread is executing this? *)
```

The code for a thread is in a closure (with hidden fields) and Thread.create actually spawns the thread.

Most languages make the same distinction, e.g., Java:

- Create a Thread object (just the code and data)
- Call its run method to actually spawn the thread
Why use threads?

One OR more of:

1. Performance (multiprocessor or mask I/O latency)
2. Isolation (separate errors or responsiveness)
3. Natural code structure (1 stack awkward)

It's not just performance.
One possible formalism (omitting thread-ids)

- Program state is one heap and multiple expressions
- Any $e_i$ might “take the next step” and potentially spawn a thread
- A value in the “thread-pool” is removable
- Nondeterministic with *interleaving granularity* determined by rules

Some example rules for $H; e \rightarrow H'; e'; o$ (where $o ::= \cdot \mid e$):

\[
\begin{align*}
H; !l & \rightarrow H; H(l); \cdot & \quad \quad H; e_1 & \rightarrow H'; e'_1; o \\
H; e_1 e_2 & \rightarrow H'; e'_1 e_2; o
\end{align*}
\]

\[
H; \text{spawn}(v_1, v_2) \rightarrow H; 0; (v_1 \ v_2)
\]
Formalism continued

The $H; e \rightarrow H'; e'; o$ judgment is just a helper-judgment for $H; T \rightarrow H'; T'$ where $T ::= \cdot \mid e; T$

\[
\frac{H; e \rightarrow H'; e'; \cdot}{H; e_1; \ldots; e; \ldots; e_n \rightarrow H'; e_1; \ldots; e'; \ldots; e_n}
\]

\[
\frac{H; e \rightarrow H'; e'; e''}{H'; e_1; \ldots; e; \ldots; e_n \rightarrow H'; e_1; \ldots; e'; \ldots; e_n; e''}
\]

\[
H; e_1; \ldots; e_{i-1}; v; e_{i+1}; \ldots; e_n \rightarrow H; e_1; \ldots; e_{i-1}; e_{i+1}; \ldots; e_n
\]

Program termination: $H; \cdot$
Equivalence just changed

Expressions equivalent in a single-threaded world are not necessarily equivalent in a multithreaded context!

Example in Caml:

let x, y = ref 0, ref 0 in 
create (fun () -> if (!y)=1 then x:=(!x)+1) ();
create (fun () -> if (!x)=1 then y:=(!y)+1) () (* 1 *)

Can we replace line (1) with:

create (fun () -> y:=(!y)+1; if (!x)<>1 then y:=(!y)-1) ()

For more compiler gotchas, see “Threads cannot be implemented as a library” by Hans-J. Boehm in PLDI2005

- Example: C bit-fields or other adjacent fields
Communication

If threads do nothing other threads need to “see,” we are done

- Best to do as little communication as possible
- E.g., do not mutate shared data unnecessarily, or hide mutation behind easier-to-use interfaces

One way to communicate: Shared memory

- One thread writes to a ref, another reads it
- Sounds nasty with pre-emptive scheduling
- Hence synchronization mechanisms
  - Taught in O/S for historical reasons!
  - Fundamentally about restricting interleavings
Join

“Fork-join” parallelism a simple approach good for “farm out subcomputations then merge results”

(* suspend caller until/unless arg terminates *)
val join : t -> unit

Common pattern:

val fork_join : ('a -> 'b array) -> (* divider *)
  ('b -> 'c) -> (* conqueror *)
  ('c array -> 'd) -> (* merger *)
  'a -> (* data *)
  'd

Apply the second argument to each element of the 'b array in parallel, then use third argument after they are done.

See lec14.ml for an (untested) implementation.
Futures

A different model for explicit parallelism without explicit shared memory or message sends.

- Easy to implement on top of either, but most models are easily inter-implementable.

type 'a promise;
val future : (unit -> 'a) -> 'a promise (*do in parallel*)
val force : 'a promise -> 'a (*may block*)

Essentially fork/join with a value returned?

- Returning a value more functional
- Less structured than “cobegin s1; s2; ... sn” form of fork/join
Locks (a.k.a. mutexes)

(* mutex.mli *)

type t (* a mutex *)
val create : unit -> t
val lock : t -> unit (* may block *)
val unlock : t -> unit

Caml locks do not have two common features:

- Reentrancy (changes semantics of lock)
- Banning nonholder release (changes semantics of unlock)

Also want condition variables (condition.mli), but skipping
Using locks

Among infinite correct idioms using locks (and more incorrect ones), the most common:

- Determine what data must be “kept in sync”
- Always acquire a lock before accessing that data and release it afterwards
- Have a *partial order* on all locks and if a thread holds $m_1$ it can acquire $m_2$ only if $m_1 < m_2$.

See canonical “bank account” example in lec14.ml.

Coarser locking (more data with same lock) trades off parallelism with synchronization. (Related: Performance-bug of *false sharing*.)
Getting it wrong

Races result from too little synchronization

- Data races: simultaneous read-write or write-write of same data
  - Lots of PL work in last 10 years on types and tools to prevent/detect
  - Provided language has some guarantees, may not be a bug
    * Canonical example: parallel search and “done” bits
- Higher-level races: much tougher to prevent in the language
  - Amount of correct nondeterminism inherently app-specific

Deadlock results from too much synchronization

- Cycle of threads waiting for someone else to do something
- Easy to detect dynamically with locks, but then what?
The Evolution Problem

Write a new function that needs to update $o_1$ and $o_2$ together.

- What locks should you acquire? In what order?

There may be no answer that avoids races and deadlocks without breaking old code. (Need a stricter partial order.)

See xfer code in lec14.ml, which is yet another binary-method problem for OOP. Real example from Java:

```java
synchronized append(StringBuffer sb) {
    int len = sb.length(); //synchronized call
    if(this.count+len > this.value.length) this.expand(...);
    sb.getChars(0,len,this.value,this.count); //synchronized call
    ...
}
```

Undocumented in 1.4; in 1.5 caller synchronizes on sb if necessary.
Software Transactions

One of the hottest areas in CS research right now (me too).

Java: atomic { s }

Caml: atomic : (unit -> ’a) -> ’a

Execute the body/thunk as though no interleaving from other threads.

- Allow parallelism unless there are actual run-time memory conflicts (detect and abort/retry)

- Convenience of coarse-grained locking with parallelism of fine-grained locking

- But language implementation has to do more to detect conflicts (much like garbage collection is convenient but has costs)

Most research on implementation (preserve parallelism unless there are conflicts), but 505 not an implementation course.
Transactions make things easier

Problems like `append` and `xfer` become trivial.

So does mixing coarse-grained and fine-grained operations (e.g., hashtable lookup and hashtable resize).

Transactions *are* great, but not a panacea:

- Application-level races can remain
- Application-level deadlock can remain
- Implementations generally try-and-abort, which is hard for “launch missiles” (e.g., I/O)
- Many software implementations provide a weaker and under-specified semantics (come ask me)
- *Memory-consistency model* questions remain and may be worse than with locks...
Memory models

A memory-consistency model (or just memory model) for a concurrent shared-memory language specifies “which write a read can see”.

The gold standard is sequential consistency (Lamport): “the results of any execution is the same as if the operations of all the processors were executed in some sequential order, and the operations of each individual processor appear in this sequence in the order specified by its program”

Under sequential consistency, this assert cannot fail, despite data races:

```ocaml
let x, y = ref 0, ref 0
let _ = create (fun () -> x := 1; y := 1) ()
let _ = create (fun () -> let r = !y in let s = !x in
                 assert(s>=r) ()
```

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CSE505 Fall 2009, Lecture 14
Relaxed memory models

Modern imperative and OO languages do not promise sequential consistency (if they say anything at all)

- The hardware makes it prohibitively expensive
- Renders unsound almost every compiler optimization

Example: common-subexpression elimination

Initially a==b==0

<table>
<thead>
<tr>
<th>Thread 1</th>
<th>Thread 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>x=a+b;</td>
<td>b=1;</td>
</tr>
<tr>
<td>y=a;</td>
<td>a=1;</td>
</tr>
<tr>
<td>z=a+b;</td>
<td></td>
</tr>
<tr>
<td>assert(z&gt;=y);</td>
<td></td>
</tr>
</tbody>
</table>
Relaxed $\neq$ Nothing

But (especially in a safe language) have to promise something

- When is code “correctly synchronized”?
- What can a compiler do in the presence of races?
  - Cannot seg-fault Java or compromise the SecurityManager
  - Can a race between $x := 1$ and $!x$ cause the latter to produce a value “out of thin air” (Java: no).

The definitions are very complicated and programmers can usually ignore them, but do not assume sequential consistency.

See also Java’s volatiles and C++ atomics. C will likely adopt the C++ work.
In real languages

- **Java**: *If* every sequentially consistent execution of program $P$ is data-race free, *then* every execution of program $P$ is equivalent to some sequentially consistent execution.
  - Not the definition, a theorem about the definition.
  - Actual definition very complicated, balancing needs of code writers, compiler optimizers, and hardware.
    - Not defined in terms of “list of acceptable optimizations”
- **C++** (proposed): Roughly, any data race is as undefined as an array-bounds error. *No such thing as a benign data race* and **no** guarantees if you have one. (In practice, programmers will still assume things, like they do with casts.)
  - But same theorem as Java: “DRF $\Rightarrow$ SC”
- **Most languages**: Eerily silent.
Mostly functional wins again

If most of your data is immutable and most code is known to access only immutable data, then most code can be optimized without any concern for the memory model.

So can afford to be very conservative for the rest.

Example: A Caml program that uses mutable memory only for shared-memory communication.

Non-example: Java, which uses mutable memory for almost everything.

• Compilers try to figure out what is thread-local (again avoids memory-model issues), but it’s not easy
Ordering and atomic

Initially x==y==0

Thread 1                  Thread 2
x=1;                        r=y;

y=1;                        s=x;

Can s be less than r?

Yes.
Ordering and atomic

Initially $x==y==0$

Thread 1  Thread 2

$x=1;$  \hspace{1cm} \hspace{1cm} r=y;
\hspace{1cm} sync(1k)\{} \hspace{1cm} \hspace{1cm} sync(1k)\{}
\hspace{1cm} y=1; \hspace{1cm} \hspace{1cm} s=x;

Can $s$ be less than $r$?

In Java, no.
Ordering and atomic

Initially $x==y==0$

Thread 1 Thread 2

$x=1;$ $r=y;$

atomic{} atomic{}

$y=1;$ $s=x;$

Can $s$ be less than $r$?

Nobody has decided (in practice, yes)! (See my October 06 paper.)