# Static and dynamic analysis: synergy and duality

Michael Ernst CSE 503, Winter 2018 Lecture 1

## **Static Dynamic Analysis**

- Static and dynamic analyses are more similar than many people believe
- Encourage blending of the techniques and communities
- Productive research avenue

#### **Outline**

Review of static and dynamic analysis

Synergy: combining static and dynamic analysis

- Aggregation
- Analogies
- Hybrids

Duality: subsets of behavior

Conclusion

## Static analysis

Examples: compiler optimizations, program verifiers

Examine program text (no execution)

Build a model of program state

• An abstraction of the run-time state

Reason over possible behaviors

• E.g., "run" the program over the abstract state

## **Abstract interpretation**

Typically implemented via dataflow analysis

Each program statement's *transfer function* indicates how it transforms state

Example: What is the transfer function for

$$y = x++;$$

?

### Selecting an abstract domain

```
\( x \text{ is odd; y is odd }\)
y = x++;
\( x \text{ is even; y is odd }\)
```

```
\( x is prime; y is prime \)
y = x++;
\( x is anything; y is prime \)
```

```
\langle x = \{ 3, 5, 7 \}; y = \{ 9, 11, 13 \} \rangle
\mathbf{y} = \mathbf{x++};
\langle x = \{ 4, 6, 8 \}; y = \{ 3, 5, 7 \} \rangle
```

$$\langle x=3, y=11 \rangle, \langle x=5, y=9 \rangle, \langle x=7, y=13 \rangle$$
 $\mathbf{y} = \mathbf{x}++;$ 
 $\langle x=4, y=3 \rangle, \langle x=6, y=5 \rangle, \langle x=8, y=7 \rangle$ 

$$\langle x_n = f(a_{n-1},...,z_{n-1}); y_n = f(a_{n-1},...,z_{n-1}) \rangle$$

$$\mathbf{y} = \mathbf{x} + + \mathbf{z}$$

$$\langle x_{n+1} = x_n + 1; y_{n+1} = x_n \rangle$$

## Research challenge: Choose good abstractions

The abstraction determines the expense (in time and space)

The abstraction determines the accuracy (what information is lost)

- Less accurate results are poor for applications that require precision
- Cannot conclude all true properties in the grammar

## Static analysis recap

- Slow to analyze large models of state, so use abstraction
- Conservative: account for abstracted-away state
- Sound: (weak) properties are guaranteed to be true
  - \*Some static analyses are not sound

## **Dynamic analysis**

Examples: profiling, testing

Execute program (over some inputs)

• The compiler provides the semantics

Observe executions

• Requires instrumentation infrastructure

2 research challenges:

- what to measure
- what test runs

## Research challenge: What to measure?

#### Coverage or frequency

• Statements, branches, paths, procedure calls, types, method dispatch

#### Values computed

• Parameters, array indices

Run time, memory usage

Test oracle results

Similarities among runs [Podgurski 99, Reps 97]

Like abstraction, determines what is reported

## Research challenge: Choose good tests

The test suite determines the expense (in time and space)

The test suite determines the accuracy (what executions are never seen)

- Less accurate results are poor for applications that require correctness
- Many domains do not require correctness!

\*What information is being collected also matters

## Dynamic analysis recap

- Can be as fast as execution (over a test suite, and allowing for data collection)
  - Example: aliasing
- Precise: no abstraction or approximation
- Unsound: results may not generalize to future executions
  - Describes execution environment or test suite

# Static analysis

Abstract domain slow if precise

Conservative due to abstraction

Sound

due to conservatism

# Dynamic analysis

Concrete execution slow if exhaustive

**Precise** 

no approximation

Unsound

does not generalize

#### **Outline**

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# Combining static and dynamic analysis

- Aggregation:
   Pre- or post-processing
- 2. Inspiring analogous analyses: Same problem, different domain
- 3. Hybrid analyses:
  Blend both approaches

# 1. Aggregation: Pre- or post-processing

Use output of one analysis as input to another Dynamic then static

- Profile-directed compilation: unroll loops, inline, reorder dispatch, ...
- Verify properties observed at run time

#### Static then dynamic

- Reduce instrumentation requirements
  - Efficient branch/path profiling
  - Discharge obligations statically (type/array checks)
- Type checking (e.g., Java, including generics)
- Indicate suspicious code to test more thoroughly

## 2. Analogous analyses: Same problem, different domain

Any analysis problem can be solved in either domain

- Type safety: no memory corruption or operations on wrong types of values
  - Static type-checking
  - Dynamic type-checking
- Slicing: what computations could affect a value
  - Static: reachability over dependence graph
  - Dynamic: tracing

## Memory checking

Goal: find array bound violations, uses of uninit. memory Purify [Hastings 92]: run-time instrumentation

- Tagged memory: 2 bits (allocated, initialized) per byte
- Each instruction checks/updates the tags
  - Allocate: set "A" bit, clear "I" bit
  - Write: require "A" bit, set "I" bit
  - Read: require "I" bit
  - Deallocate: clear "A" bit

LCLint [Evans 96]: compile-time dataflow analysis

- Abstract state contains allocated and initialized bits
- Each transfer function checks/updates the state

Identical analyses!

Another example: atomicity checking [Flanagan 2003]

## **Specifications**

- Specification checking
  - Statically: theorem-proving
  - Dynamically: assert statement
- Specification generation
  - Statically: by hand or abstract interpretation [Cousot 77]
  - Dynamically: by invariant detection [Ernst 99], reporting unfalsified properties

### Your analogous analyses here

Look for gaps with no analogous analyses!
Try using the same analysis

• But be open to completely different approaches

There is still low-hanging fruit to be harvested

# 3. Hybrid analyses: Blending static and dynamic

Combine static and dynamic analyses

- Not mere aggregation, but a new analysis
- Disciplined trade-off between precision and soundness: find the sweet spot between them

## Possible starting points

Analyses that trade off run-time and precision

- Different abstractions (at different program points)
- Switch between static and dynamic at analysis time

Ignore some available information

• Examine only some paths [Evans 94, Detlefs 98, Bush 00]

Merge based on observation that both examine only a subset of executions (next section of talk)

- Problem: optimistic vs. pessimistic treatment
- Fine-grained aggregation (concolic execution)

More examples: (bounded) model checking, security analyses, delta debugging [Zeller 99], etc.

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# Dynamic analysis

Concrete execution slow if exhaustive

Precise

no approximation

Unsound

does not generalize

## Sound dynamic analysis

Observe every possible execution!

Problem: infinite number of executions

Solution: test case selection and generation

• Efficiency tweaks to an algorithm that works perfectly in theory but exhausts resources in practice

## Precise static analysis

Reason over full program state!

Problem: infinite number of executions

Solution: data or execution abstraction

• Efficiency tweaks to an algorithm that works perfectly in theory [Cousot 77] but exhausts resources in practice

## Dynamic analysis focuses on a subset of executions

The executions in the test suite

- Easy to enumerate
- Characterizes program use

Typically optimistic for other executions

## Static analysis focuses on a subset of data structures

More precise for data or control described by the abstraction

- Concise logical description
- Typically conservative elsewhere (safety net)

Example: *k*-limiting [Jones 81]

- Represents each object reachable by  $\leq k$  pointers
- Groups together (approximates) more distant objects

#### **Dual views of subsets**

Execution and data subsets are views on the same space Every execution subset corresponds to a data subset

Executions induce data structures and control flow

Every data subset corresponds to an execution subset

• A set of objects represents the executions that generate them

Subset description may be concise in one domain but complex in the other

• What if the test suite was generated from a specification? Any analysis may be conservative over other behaviors

## Differences between the approaches

Static and dynamic analysis communities work with different subsets

• Each subset and characterization is better for certain uses

What subsets have a concise description in both domains?

• Augment a test suite to fill out the data structures that it creates, making the data structure description a smaller logical formula

## A hybrid view of subsets

## Bring together static and dynamic analysis by unifying their subset descriptions

- Find subsets with small descriptions with respect to both data structures and executions
- Find a new, smaller description

#### Advantages of this approach

- Directly compare previous disparate analyses
- Directly apply analyses to other domain
- Switch between the approaches
- Obtain insight in order to devise and optimize analyses

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## Potential pitfalls

#### Analogies between analyses

- What applications tolerate unsoundness/imprecision?
- Any more low-hanging fruit?
- Most static and dynamic approaches differ

#### Hybrid analyses

- How to measure and trade off precision and soundness
  - What is "partial soundness"? What is in between?
- Not all static analyses are abstract interpretation
- Optimistic vs. pessimistic treatment of unseen executions

#### Subset characterization

• Find the unified characterization of behavior

#### Conclusion

Static and dynamic analysis share many similarities

Communities should be closer

Create analogous analyses

Many successes so far

Hybrid approach holds great promise

- Analyses increasingly look like points in this continuum
- Unified theory of subsets of executions/data is key

(Our) future work: explore this space

### **Discussion**