

CSE 484: Computer Security and Privacy

# Cryptography 4

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Thanks to Franz Roesner, Dan Boneh, Dieter Gollmann, Dan Halperin, David Kohlbrenner, Yoshi Kohno, Ada Lerner, John Manferdelli, John Mitchell, Vitaly Shmatikov, Bennet Yee, and many others for sample slides and materials ...

# Logistics

- Lab 1b due Wednesday
- Homework 2 will go out today
  
- Lab 1a grades coming out ~today
  - 1a spoils are posted
  - 1a writeups out soon
  
- Things not going well? Please reach out to us ASAP!

# Defining the strength of a scheme

- *Effective Key Strength*
  - Amount of 'work' the adversary needs to do
- **DES**: 56-bits
  - $2^{56}$  encryptions to try 'all keys'
- **2DES**: 57-bits
  - $2 \cdot (2^{56})$  encryptions =  $2^{57}$
- **3DES**: 112-bits (or sometimes 80-bits)
  - Meet-in-the-middle + more work =  $2^{112}$  (for 3 keys, e.g. K1, K2, K3)
  - Various attacks =  $2^{80}$  (for 2 keys, e.g. K1, K2, K1)

# Standard Block Ciphers

- **DES: Data Encryption Standard**

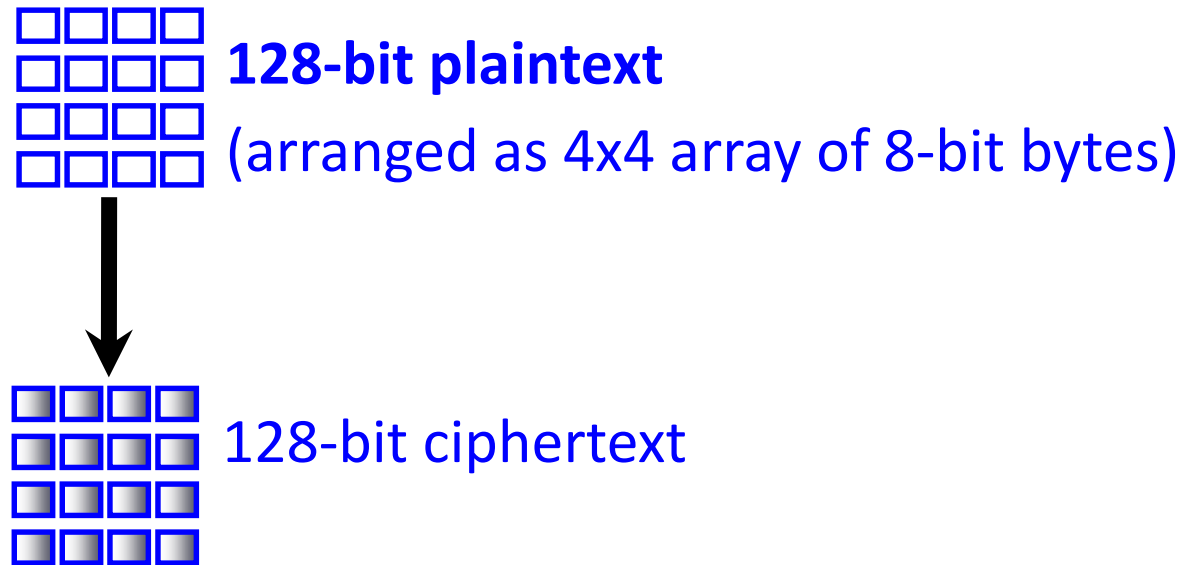
- Feistel structure: builds invertible function using non-invertible ones
- Invented by IBM, issued as federal standard in 1977
- 64-bit blocks, 56-bit key + 8 bits for parity

- **AES: Advanced Encryption Standard**

- New federal standard as of 2001
  - NIST: National Institute of Standards & Technology
- Based on the Rijndael algorithm
  - Selected via an open process
- 128-bit blocks, keys can be 128, 192 or 256 bits

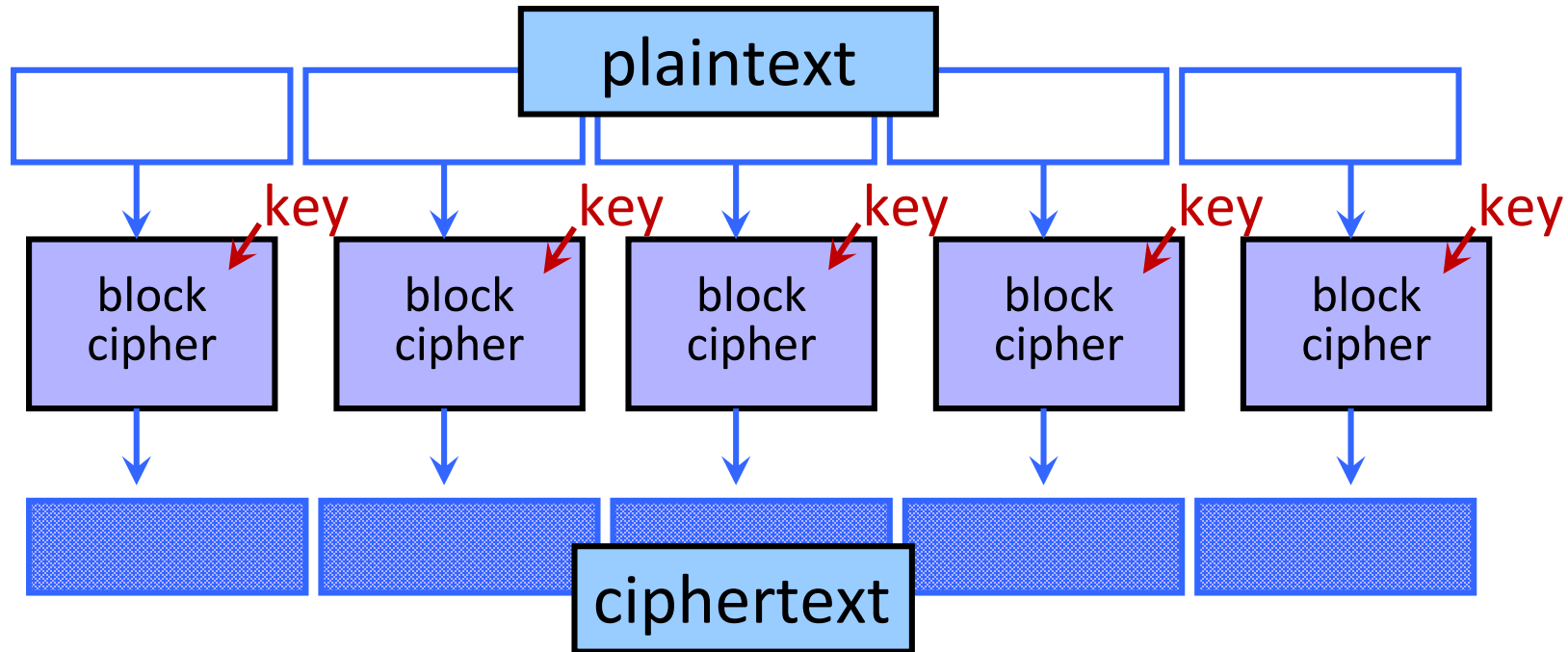
# Encrypting a Large Message

- So, we've got a good block cipher, but our plaintext is larger than 128-bit block size

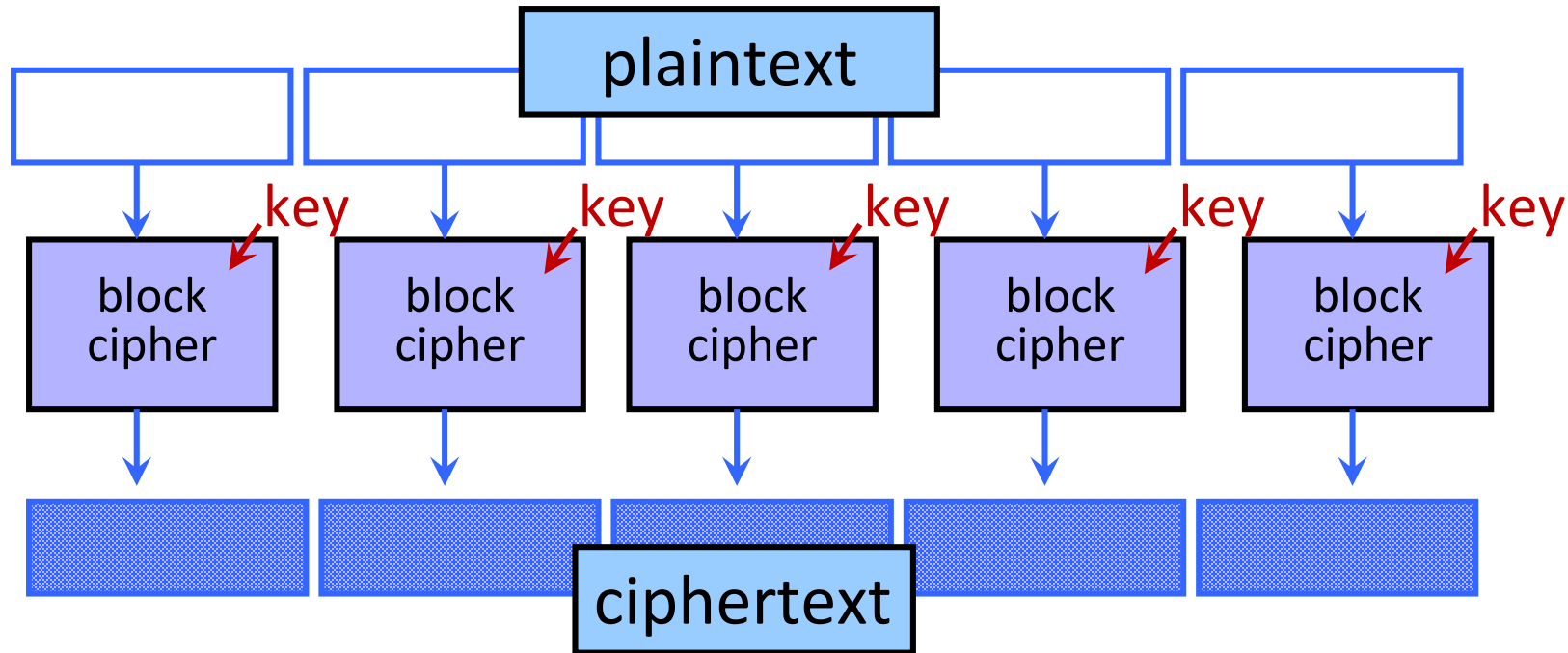


- What should we do?

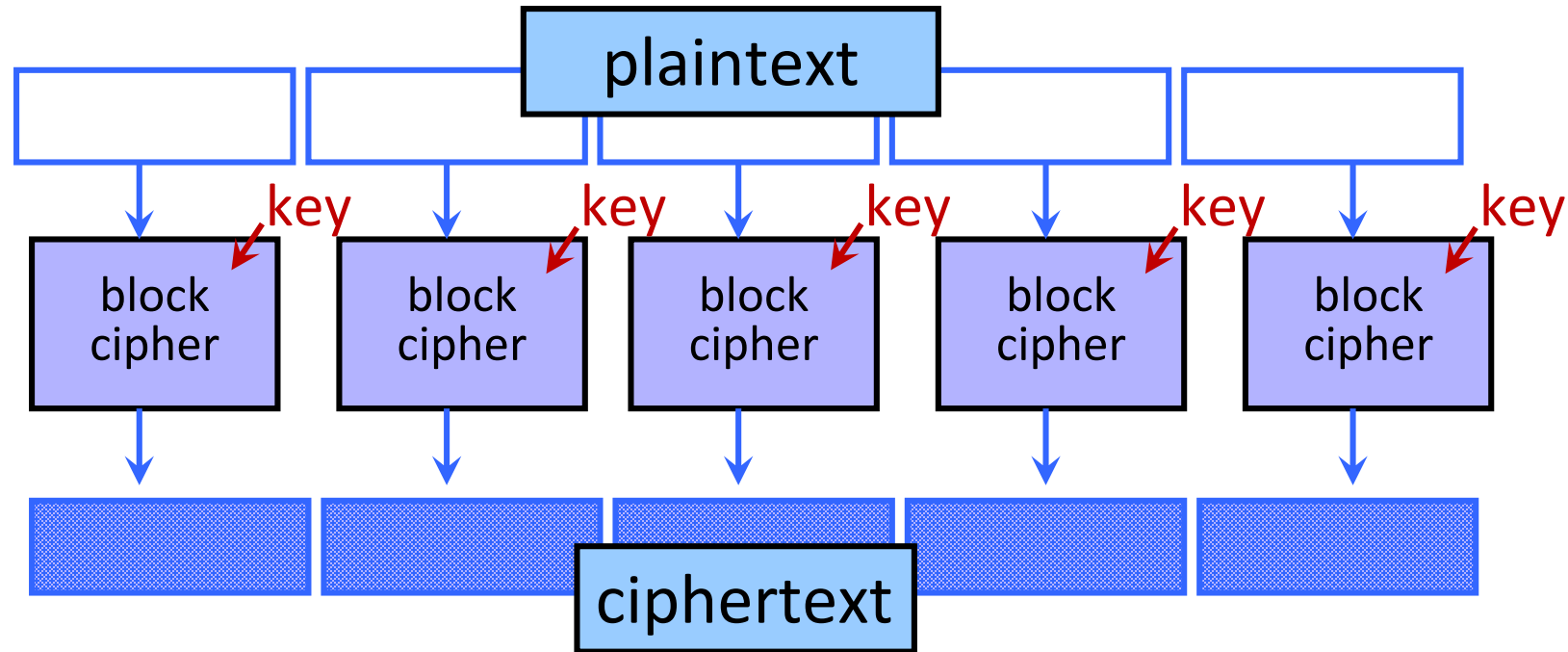
# Electronic Code Book (ECB) Mode



# Gradescope: What properties of ECB aren't great?



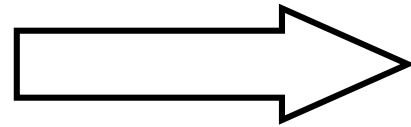
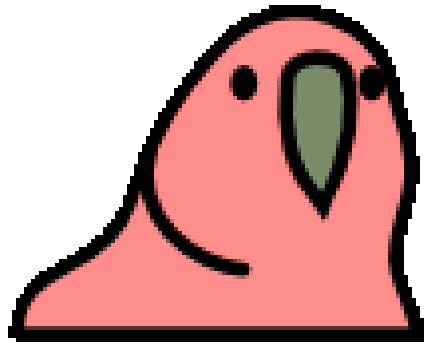
# Electronic Code Book (ECB) Mode



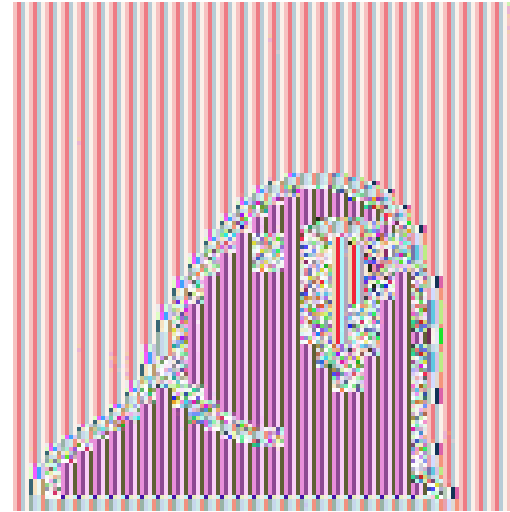
- Identical blocks of plaintext produce identical blocks of ciphertext
- No integrity checks: can mix and match blocks



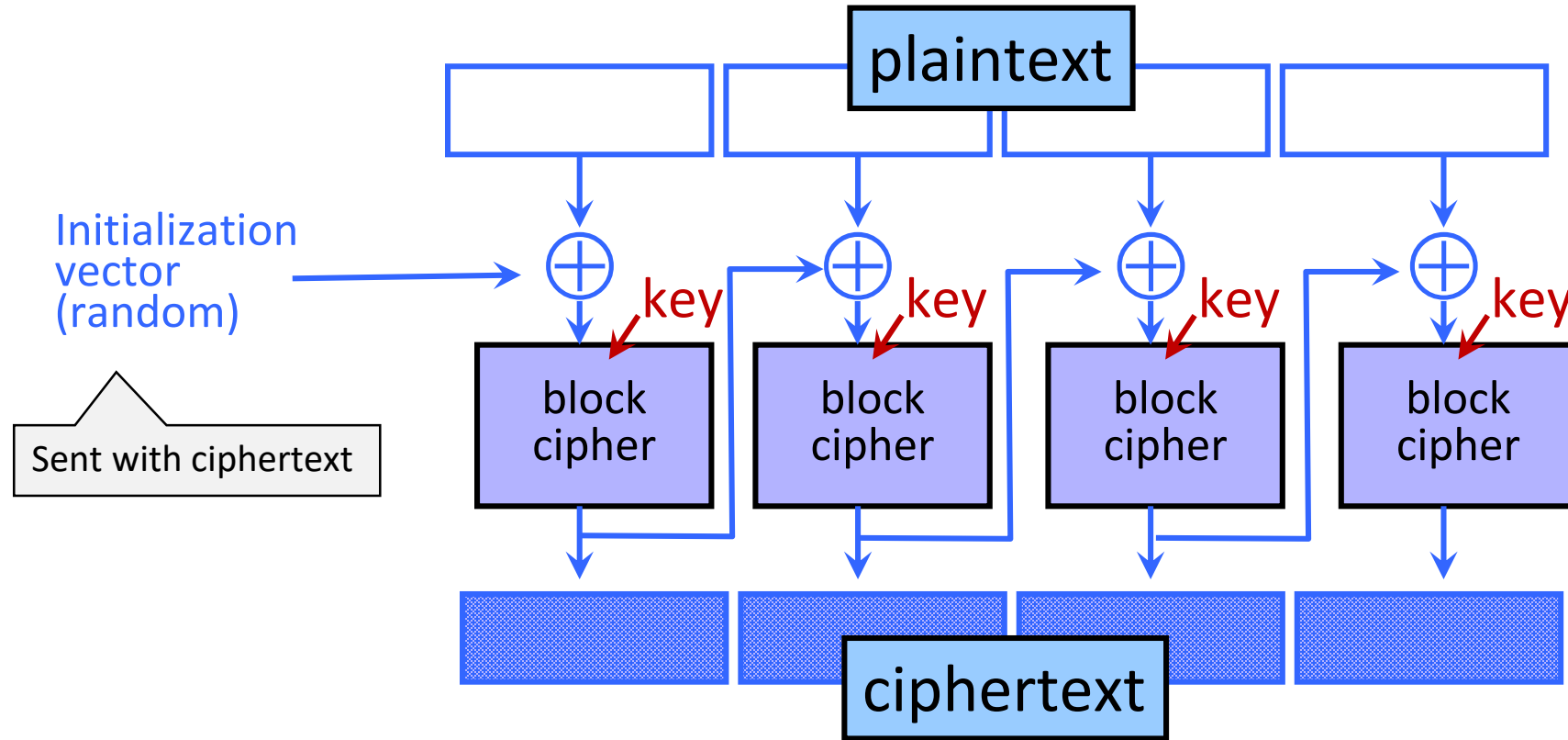
# Information Leakage in ECB Mode



Encrypt in ECB mode

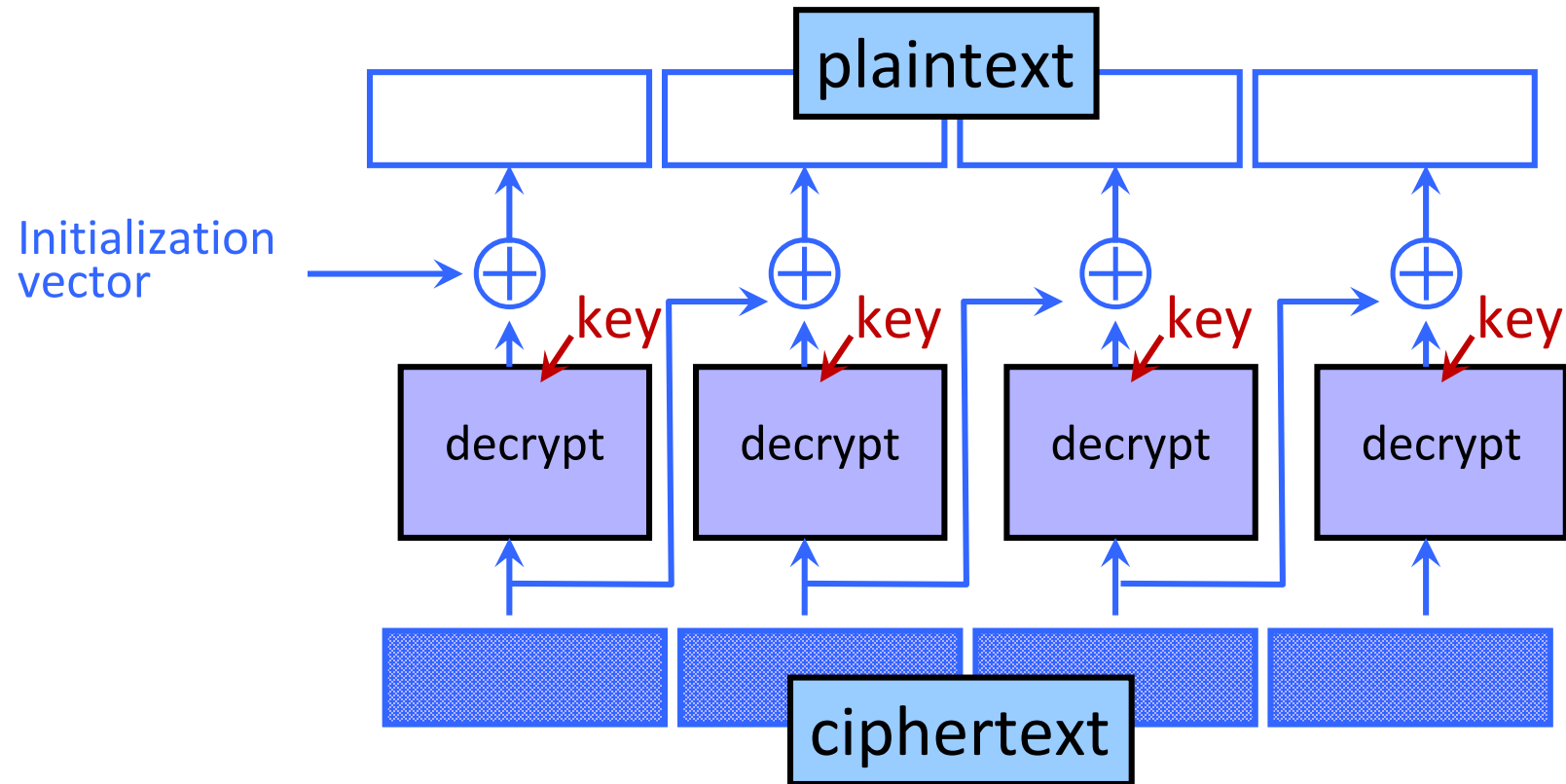


# Cipher Block Chaining (CBC) Mode: Encryption

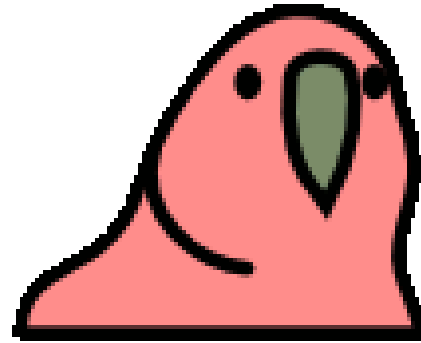


- Identical blocks of plaintext encrypted differently
- Last cipherblock depends on entire plaintext
  - Still does not guarantee integrity

# CBC Mode: Decryption

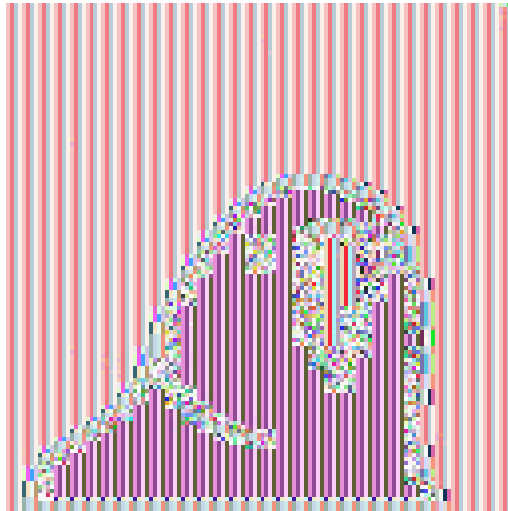


# ECB vs. CBC



AES in ECB mode

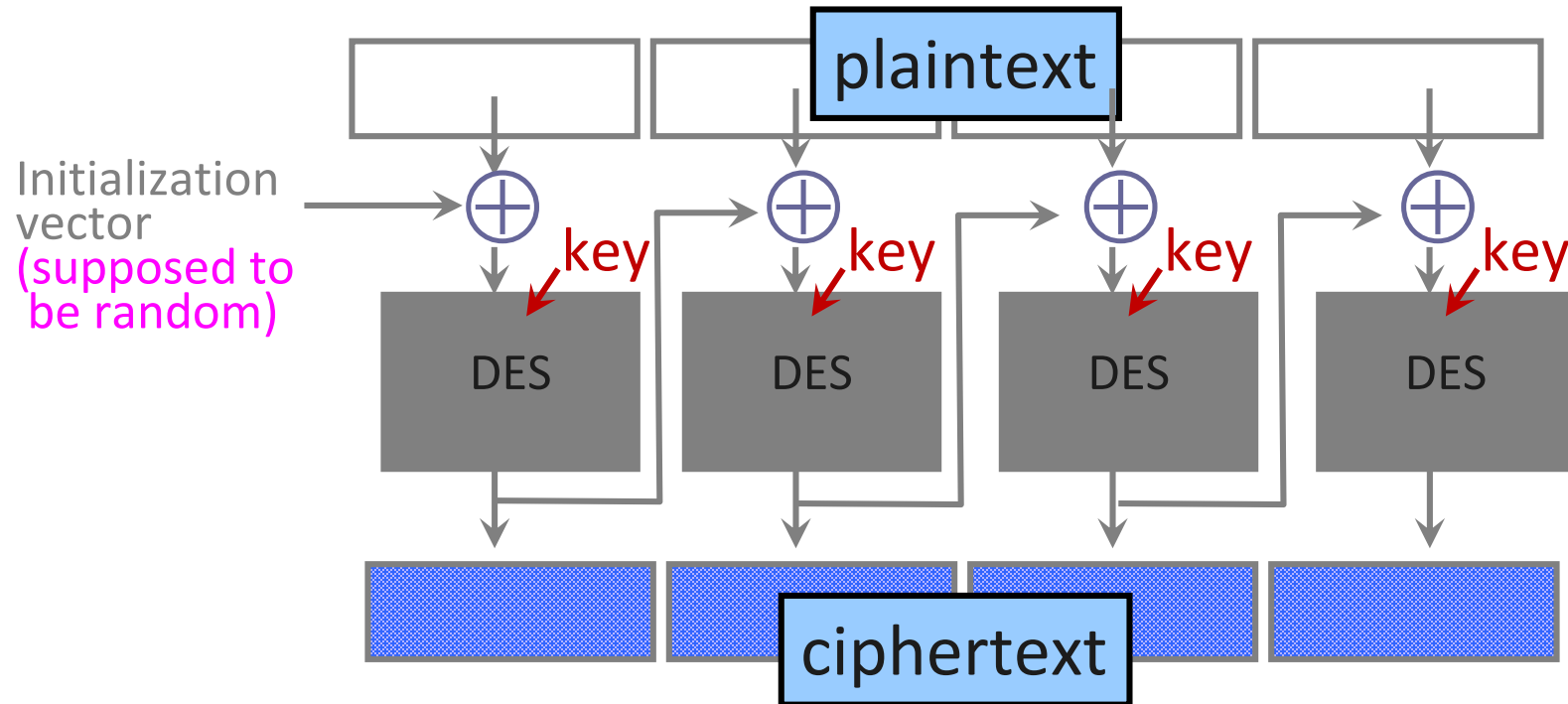
AES in CBC mode



Similar plaintext blocks produce similar ciphertext blocks (**not good!**)



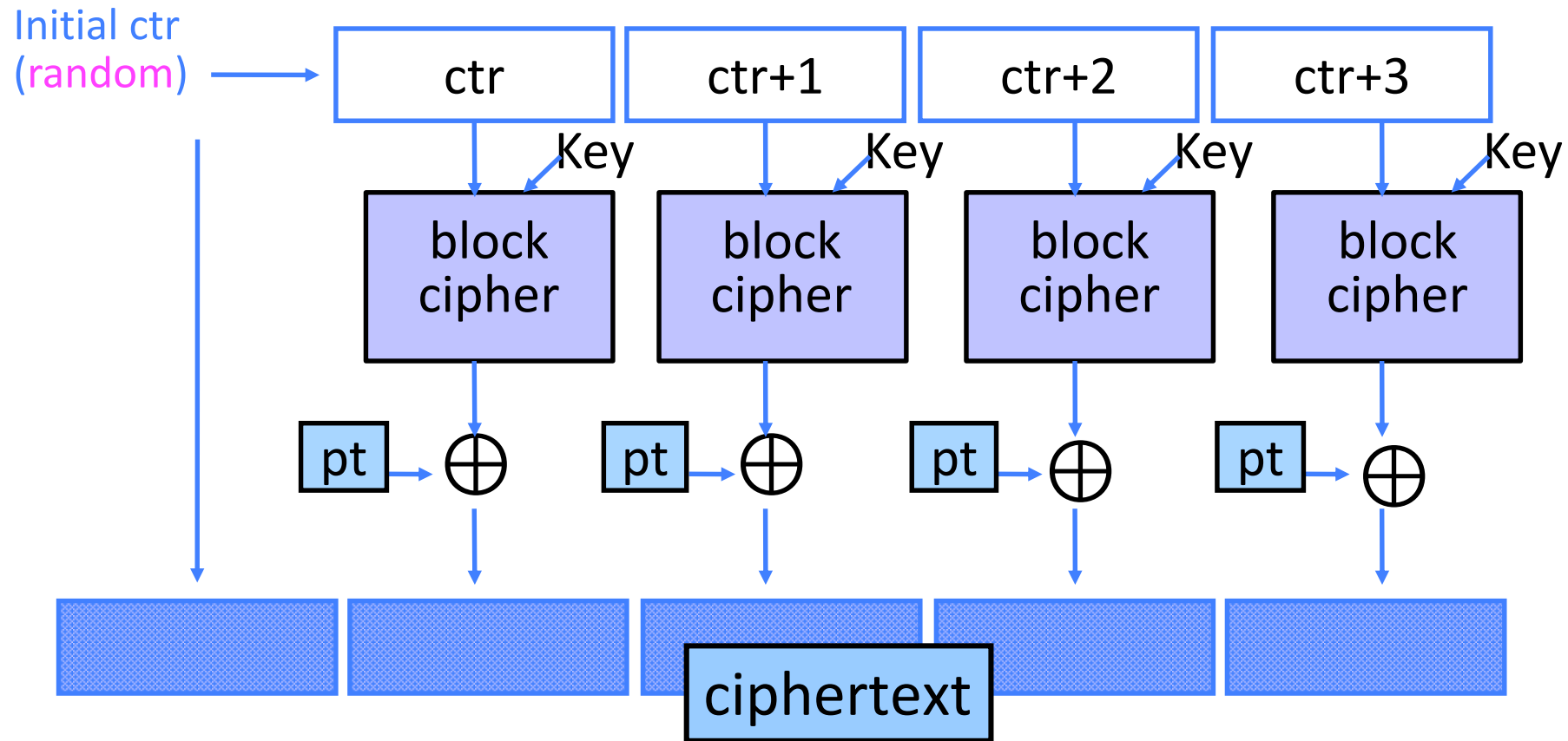
# Initialization Vector Dangers



Found in the source code for Diebold voting machines:

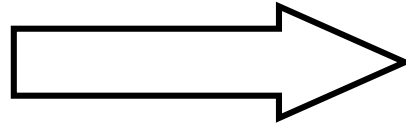
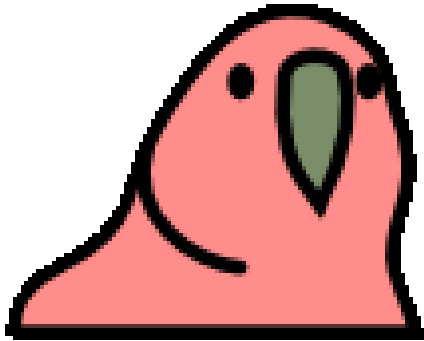
```
DesCBCEncrypt((des_c_block*)tmp, (des_c_block*)record.m_Data,  
totalSize, DESKEY, NULL, DES_ENCRYPT)
```

# Counter Mode (CTR): Encryption



- Identical blocks of plaintext encrypted differently
- **Still does not guarantee integrity; Fragile if ctr repeats**

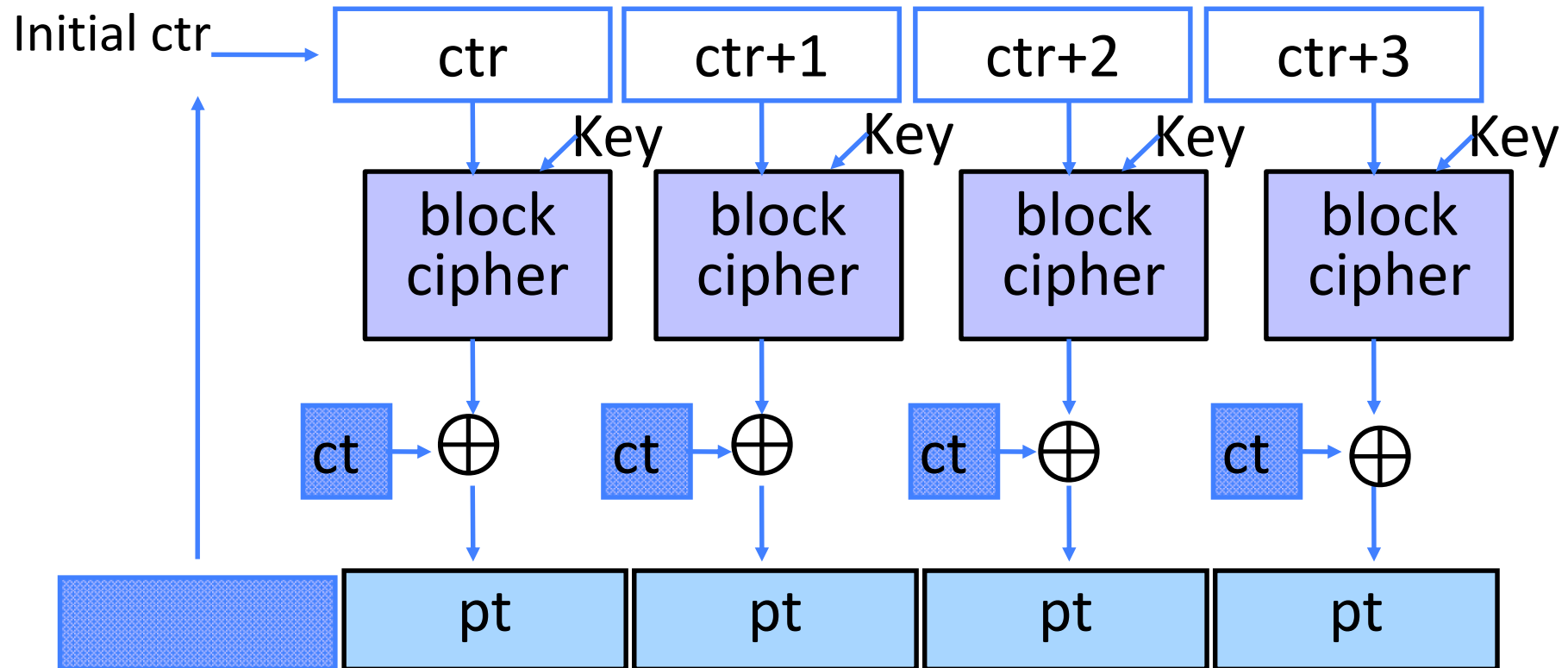
# Information Leakage in CTR Mode (poorly)



Encrypt in CTR mode:  
But with the same  
counter for each  
frame!



# Counter Mode (CTR): Decryption





# Ok, so what mode do I use?

- Don't choose a mode, use established libraries 😊
  - Libsodium's secretbox encryption solves 'all the problems' for example
- Good modes:
  - GCM - Galois/Counter Mode
  - CTR (sometimes)
  - Even ECB is fine in 'the right circumstance'
- AES-128 is standard
  - Be concerned if something says "AES 1024" ...

<https://research.kudelskisecurity.com/2022/05/11/practical-bruteforce-of-aes-1024-military-grade-encryption/>

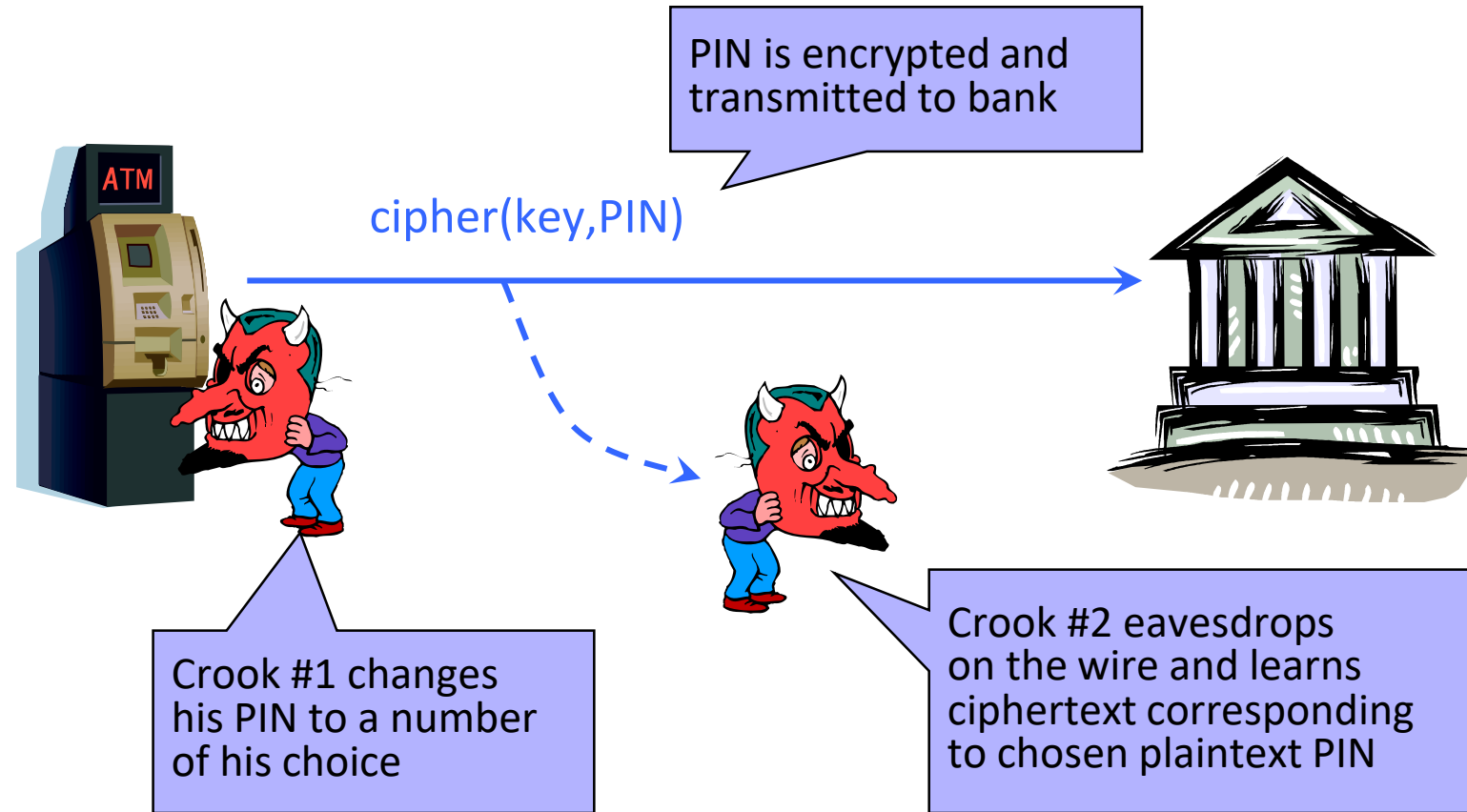
# When is an Encryption Scheme “Secure”?

- Hard to recover the key?
  - What if attacker can learn plaintext without learning the key?
- Hard to recover plaintext from ciphertext?
  - What if attacker learns some bits or some function of bits?

# How Can a Cipher Be Attacked?

- Attackers knows ciphertext and encryption algorithm
  - **What else does the attacker know?** Depends on the application in which the cipher is used!
- **Ciphertext-only attack**
- **KPA: Known-plaintext attack** (stronger)
  - Knows some plaintext-ciphertext pairs
- **CPA: Chosen-plaintext attack** (even stronger)
  - Can obtain ciphertext for any plaintext of choice
- **CCA: Chosen-ciphertext attack** (very strong)
  - Can decrypt any ciphertext except the target

# Chosen Plaintext Attack



... repeat for any PIN value

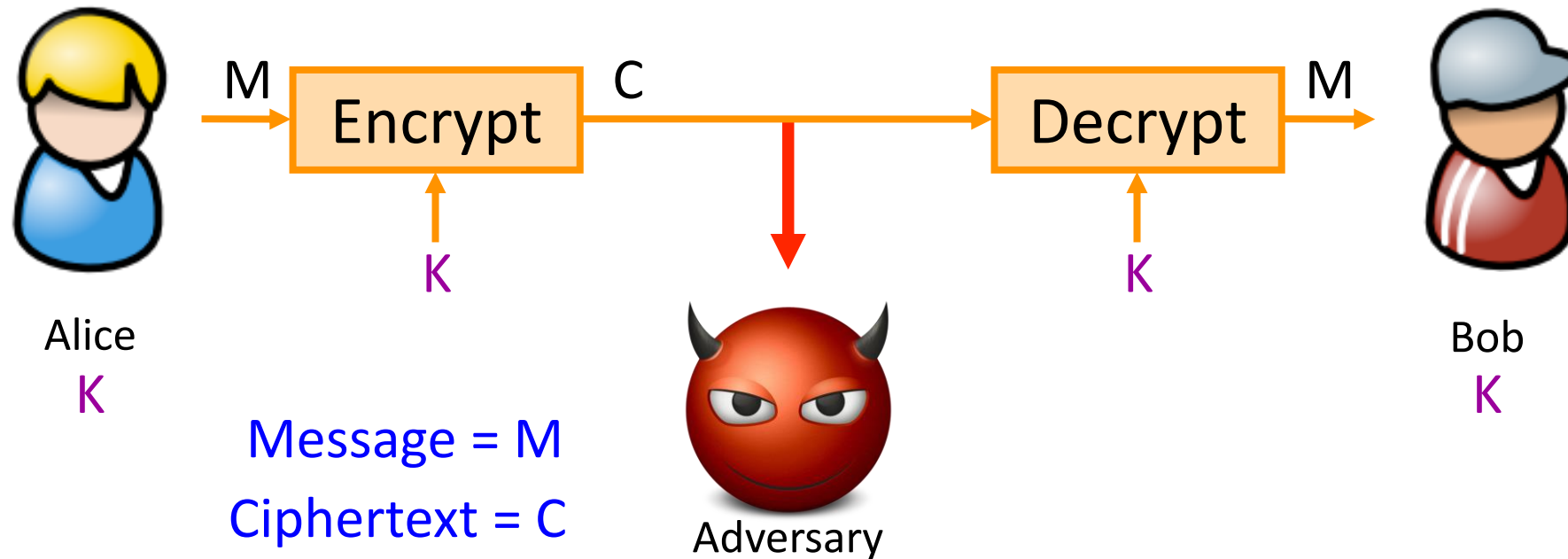
# Very Informal Intuition

Minimum security requirement for a modern encryption scheme

- Security against chosen-plaintext attack (CPA)
  - Ciphertext leaks no information about the plaintext
  - Even if the attacker correctly guesses the plaintext, he cannot verify his guess
  - Every ciphertext is unique, encrypting same message twice produces completely different ciphertexts
    - Implication: encryption must be randomized or stateful
- Security against chosen-ciphertext attack (CCA)
  - Integrity protection – it is not possible to change the plaintext by modifying the ciphertext

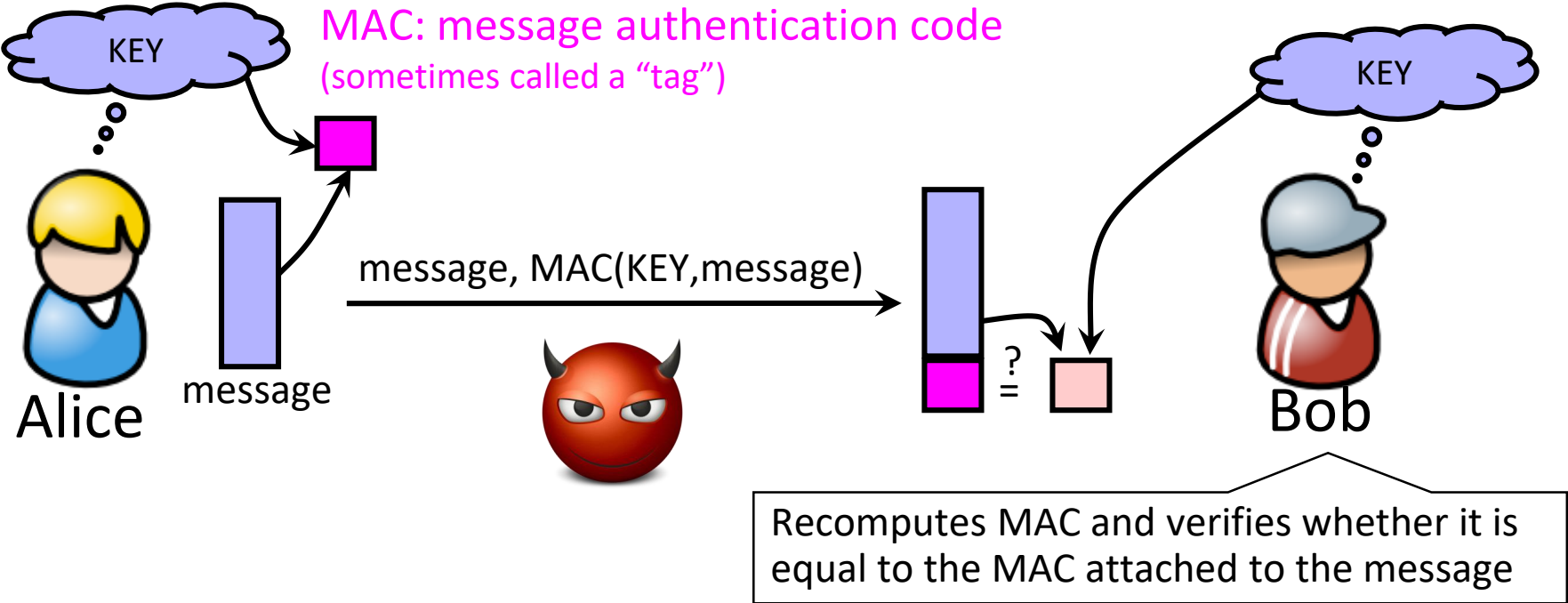
# So Far: Achieving Privacy

Encryption schemes: A tool for protecting **privacy**.



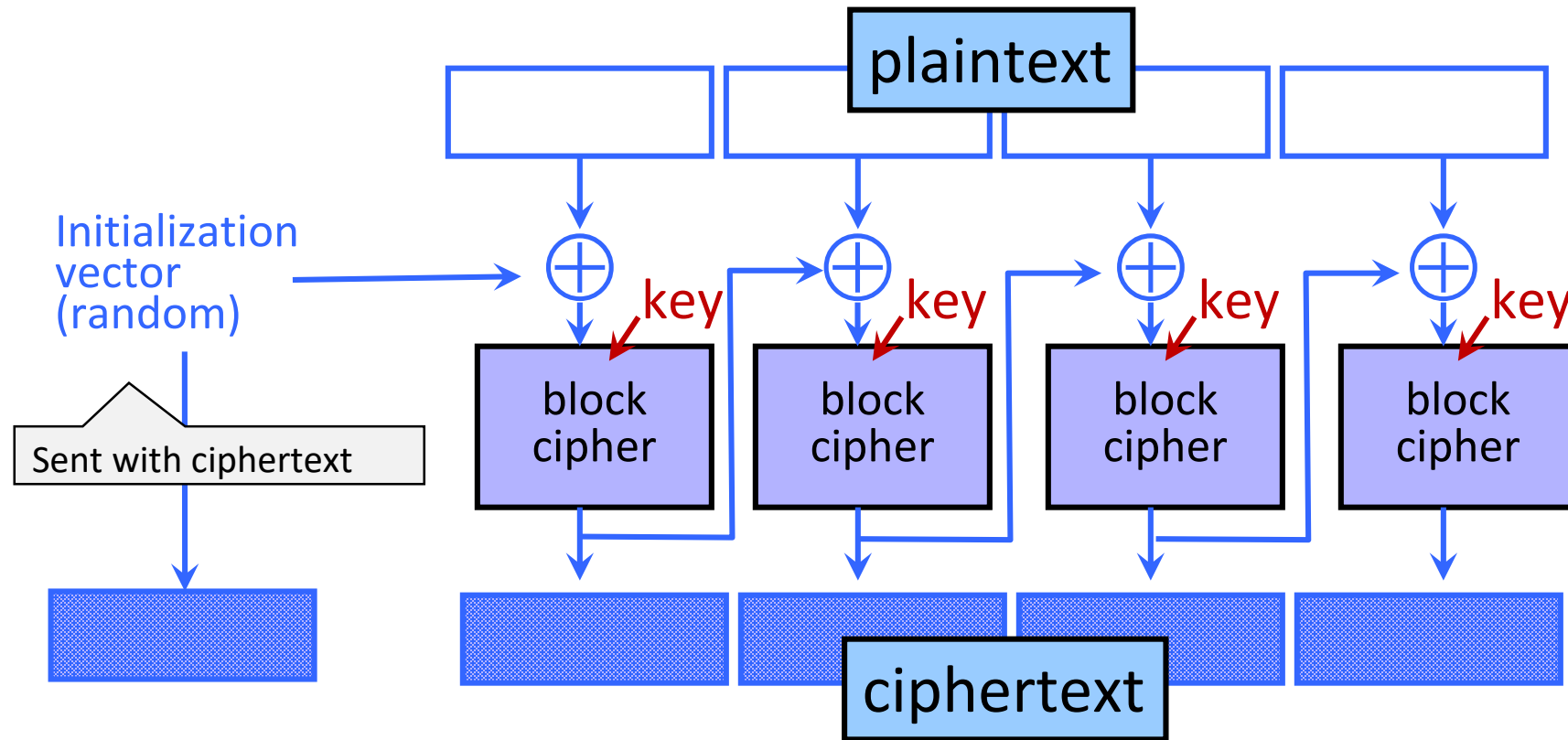
# Now: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



Integrity and authentication: only someone who knows KEY can compute correct MAC for a given message.

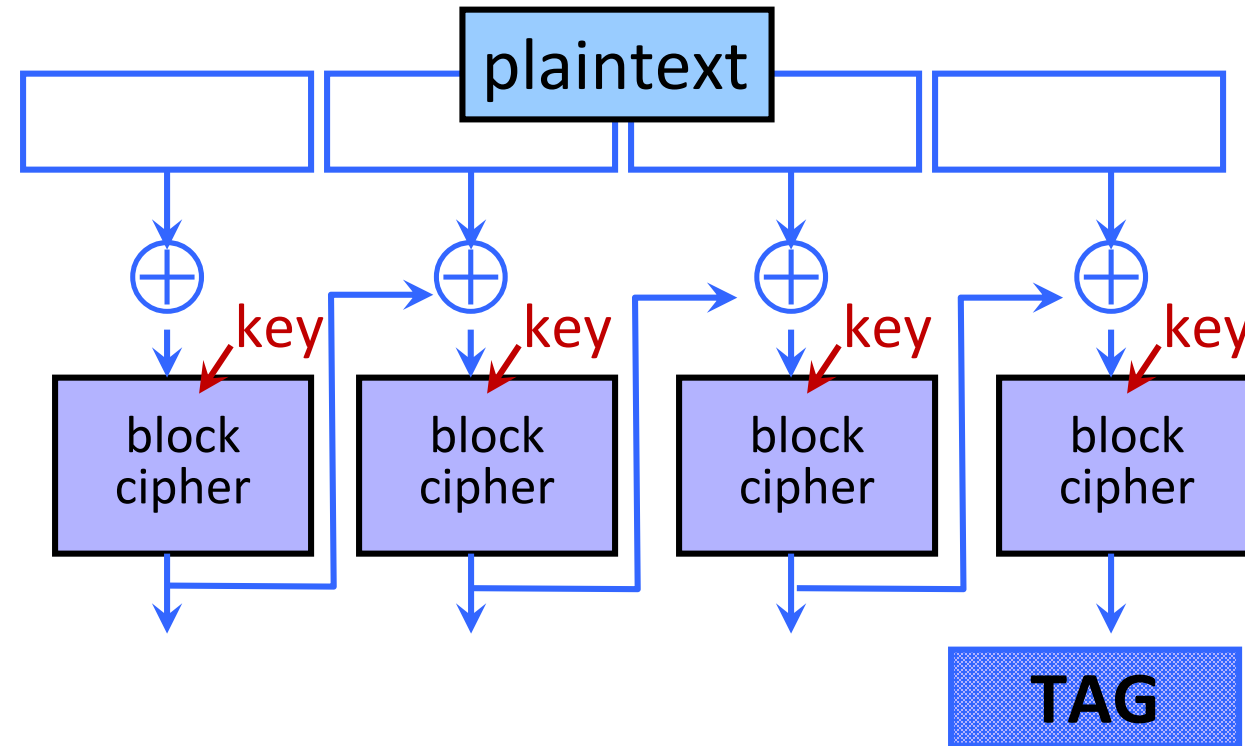
# Reminder: CBC Mode Encryption



- Identical blocks of plaintext encrypted differently
- Last cipherblock depends on entire plaintext
  - Still does not guarantee integrity



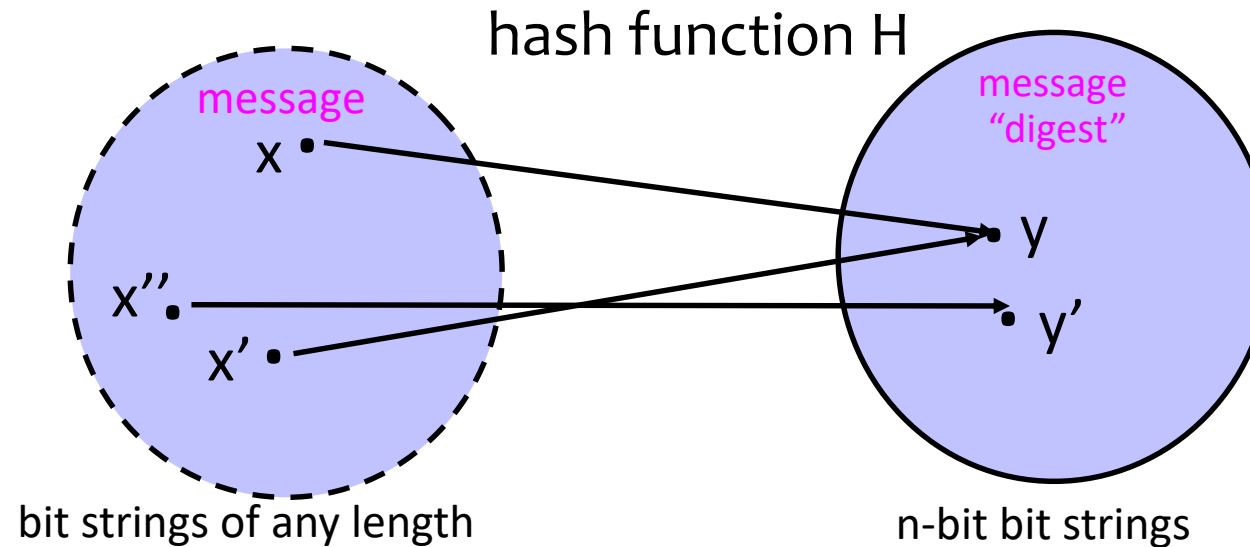
# CBC-MAC



- Not secure when system may MAC messages of different lengths
- Use a different key – not encryption key
- NIST recommends a derivative called CMAC [FYI only]

# Another Tool: Hash Functions

# Hash Functions: Main Idea



- Hash function  $H$  is a lossy compression function
  - Collision:  $h(x)=h(x')$  for distinct inputs  $x, x'$
- $H(x)$  should look “random”
  - Every bit (almost) equally likely to be 0 or 1
- Cryptographic hash function needs a few properties...

# Property 1: One-Way

- Intuition: hash should be hard to invert
  - “Preimage resistance”
  - Let  $h(x') = y$  in  $\{0,1\}^n$  for a random  $x'$
  - Given  $y$ , it should be hard to find any  $x$  such that  $h(x)=y$
- How hard?
  - Brute-force: try every possible  $x$ , see if  $h(x)=y$
  - SHA-1 (common hash function) has 160-bit output
    - Expect to try  $2^{159}$  inputs before finding one that hashes to  $y$ .

# Property 2: Collision Resistance

- Should be hard to find  $x \neq x'$  such that  $h(x) = h(x')$

# Birthday Paradox

- Are there two people in your part of the classroom that have the same birthday?
  - 365 days in a year (366 some years)
    - Pick one person. To find another person with same birthday would take on the order of  $365/2 = 182.5$  people
    - **Expect birthday “collision” with a room of only 23 people.**
    - For simplicity, approximate when we expect a collision as  **$\text{sqrt}(365)$** .
- Why is this important for cryptography?
  - $2^{128}$  different 128-bit values
    - Pick one value at random. To exhaustively search for this value requires trying on average  $2^{127}$  values.
    - **Expect “collision” after selecting approximately  $2^{64}$  random values.**
    - **64 bits** of security against collision attacks, not 128 bits.

# Property 2: Collision Resistance

- Should be hard to find  $x \neq x'$  such that  $h(x) = h(x')$
- Birthday paradox means that brute-force collision search is **only**  $O(2^{n/2})$ , *not*  $O(2^n)$ 
  - For SHA-1, this means  $O(2^{80})$  vs.  $O(2^{160})$

# One-Way vs. Collision Resistance

One-wayness does not imply collision resistance.

Collision resistance does not imply one-wayness.

You can prove this by constructing a function that has one property but not the other.



# One-Way vs. Collision Resistance

(Details here mainly FYI)

- One-wayness does not imply collision resistance
  - Suppose  $g$  is one-way
  - Define  $h(x)$  as  $g(x')$  where  $x'$  is  $x$  except drop the last bit
    - $h$  is one-way (to invert  $h$ , must invert  $g$ )
    - Collisions for  $h$  are easy to find: for any  $x$ ,  $h(x0)=h(x1)$
- Collision resistance does not imply one-wayness
  - Suppose  $g$  is collision-resistant
  - Define  $y=h(x)$  to be  $0x$  if  $x$  is  $n$ -bit long,  $1g(x)$  otherwise
    - Collisions for  $h$  are hard to find: if  $y$  starts with  $0$ , then there are no collisions, if  $y$  starts with  $1$ , then must find collisions in  $g$
    - $h$  is not one way: half of all  $y$ 's (those whose first bit is  $0$ ) are easy to invert (**how?**); random  $y$  is invertible with probability  $\frac{1}{2}$

# Property 3: Weak Collision Resistance

- Given randomly chosen  $x$ , hard to find  $x'$  such that  $h(x)=h(x')$ 
  - Attacker must find collision for a specific  $x$ . By contrast, to break collision resistance it is enough to find any collision.
  - Brute-force attack requires  $O(2^n)$  time
- Weak collision resistance does not imply collision resistance.

# Hashing vs. Encryption

- Hashing is one-way. There is no “un-hashing”
  - A ciphertext can be decrypted with a decryption key... hashes have no equivalent of “decryption”
- Hash(x) looks “random” but can be compared for equality with Hash(x’)
  - Hash the same input twice → same hash value
  - Encrypt the same input twice → different ciphertexts
- Cryptographic hashes are also known as “cryptographic checksums” or “message digests”

# Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?

# Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- **Why is hashing better than encryption here?**
- System does not store actual passwords!
- Don't need to worry about where to store the key!
- Cannot go from hash to password!

# Application: Password Hashing

- Which property do we need?
  - One-wayness?
  - (At least weak) Collision resistance?
  - Both?

# Application: Password Hashing + Salting

- **Salting**

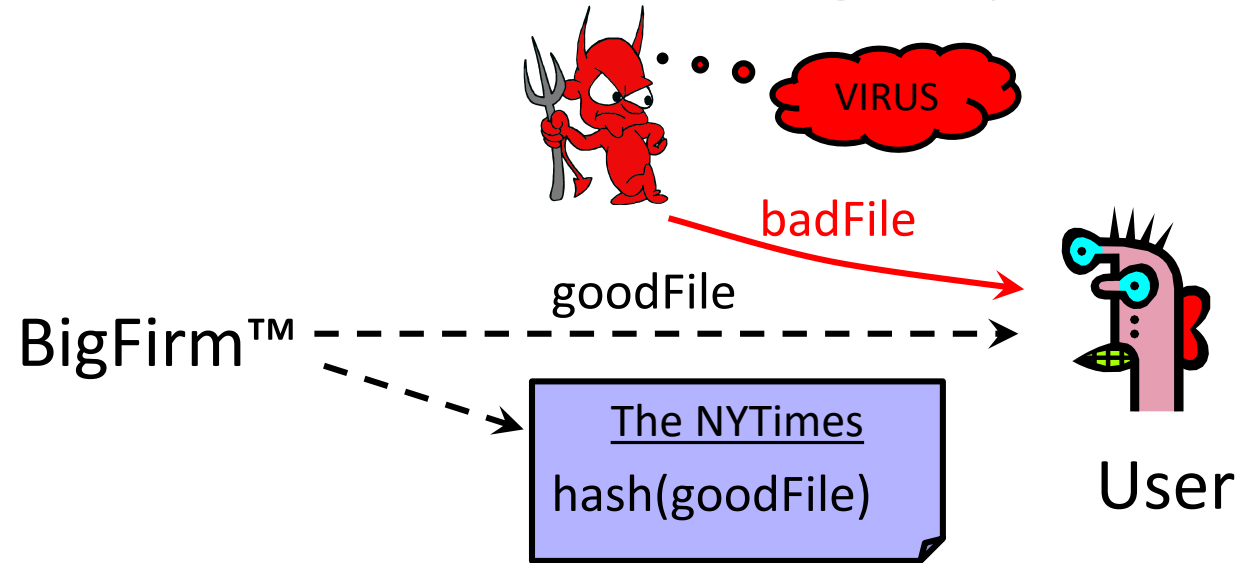
- We 'salt' hashes for password by adding a randomized suffix to the password
    - E.g. Hash("coolpassword"+"35B67C2A")
  - We then store the salt with the hashed password!
  - Server generates the salt
- 
- The goal is to prevent *precomputation attacks*
    - If the adversary doesn't know the salt, they can't *precompute* common passwords

# Hash Functions Review

- Map large domain to small range (e.g., range of all 160- or 256-bit values)
- Properties:
  - Collision Resistance: Hard to find two distinct inputs that map to same output
  - One-wayness: Given a point in the range (that was computed as the hash of a random domain element), hard to find a preimage
  - Weak Collision Resistance: Given a point in the domain and its hash in the range, hard to find a new domain element that maps to the same range element



# Application: Software Integrity



Goal: Software manufacturer wants to ensure file is received by users without modification.

Idea: given goodFile and hash(goodFile), very hard to find badFile such that  $\text{hash}(\text{goodFile}) = \text{hash}(\text{badFile})$

# Application: Software Integrity

- Which property do we need?
  - One-wayness?
  - (At least weak) Collision resistance?
  - Both?

# Which Property Do We Need?

One-wayness, Collision Resistance, Weak CR?

- UNIX passwords stored as hash(password)
  - **One-wayness**: hard to recover the/a valid password
- Integrity of software distribution
  - **Weak collision resistance**
  - But software images are not really random... may need **full collision resistance** if considering malicious developers

# Which Property Do We Need?

- UNIX passwords stored as hash(password)
  - **One-wayness:** hard to recover the/a valid password
- Integrity of software distribution
  - **Weak collision resistance**
  - But software images are not really random... may need **full collision resistance** if considering malicious developers
- Commitments (e.g. auctions)
  - Alice wants to bid B, sends  $H(B)$ , later reveals B
  - **One-wayness:** rival bidders should not recover B (this may mean that they need to hash some randomness with B too)
  - **Collision resistance:** Alice should not be able to change their mind to bid  $B'$  such that  $H(B)=H(B')$

# Commitments

# Common Hash Functions

- **SHA-2: SHA-256, SHA-512, SHA-224, SHA-384**
- **SHA-3: standard released by NIST in August 2015**
- MD5 – **Don't Use!**
  - 128-bit output
  - Designed by Ron Rivest, used very widely
  - Collision-resistance broken (summer of 2004)
- RIPEMD
  - 160-bit version is OK
  - 128-bit version is *not* good
- SHA-1 (Secure Hash Algorithm) – **Don't Use!**
  - 160-bit output
  - US government (NIST) standard as of 1993-95
  - Theoretically broken 2005; practical attack 2017!

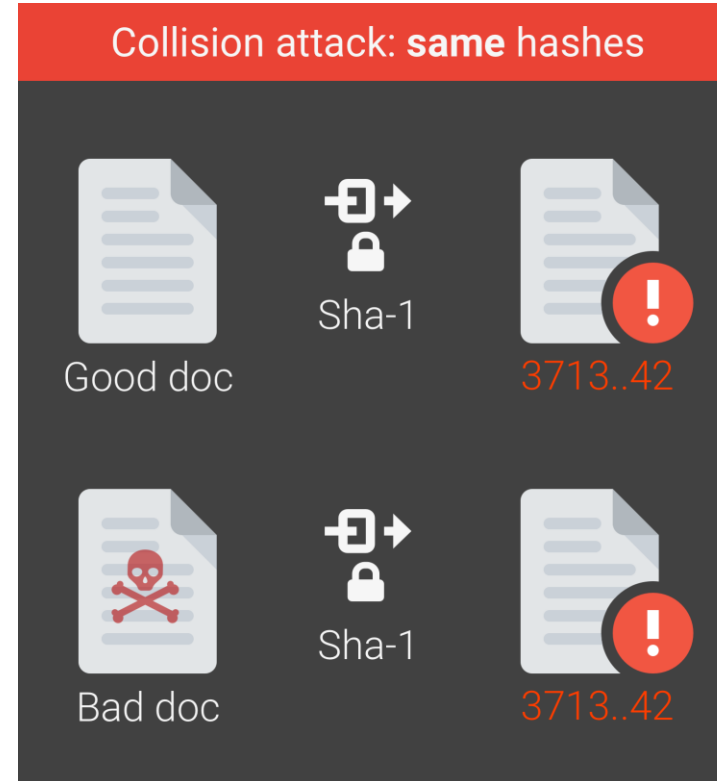
# SHA-1 Broken in Practice (2017)

**Google just cracked one of the building blocks of web encryption (but don't worry)**

*It's all over for SHA-1*

by [Russell Brandom](#) | [@russellbrandom](#) | Feb 23, 2017, 11:49am EST

<https://shattered.io>



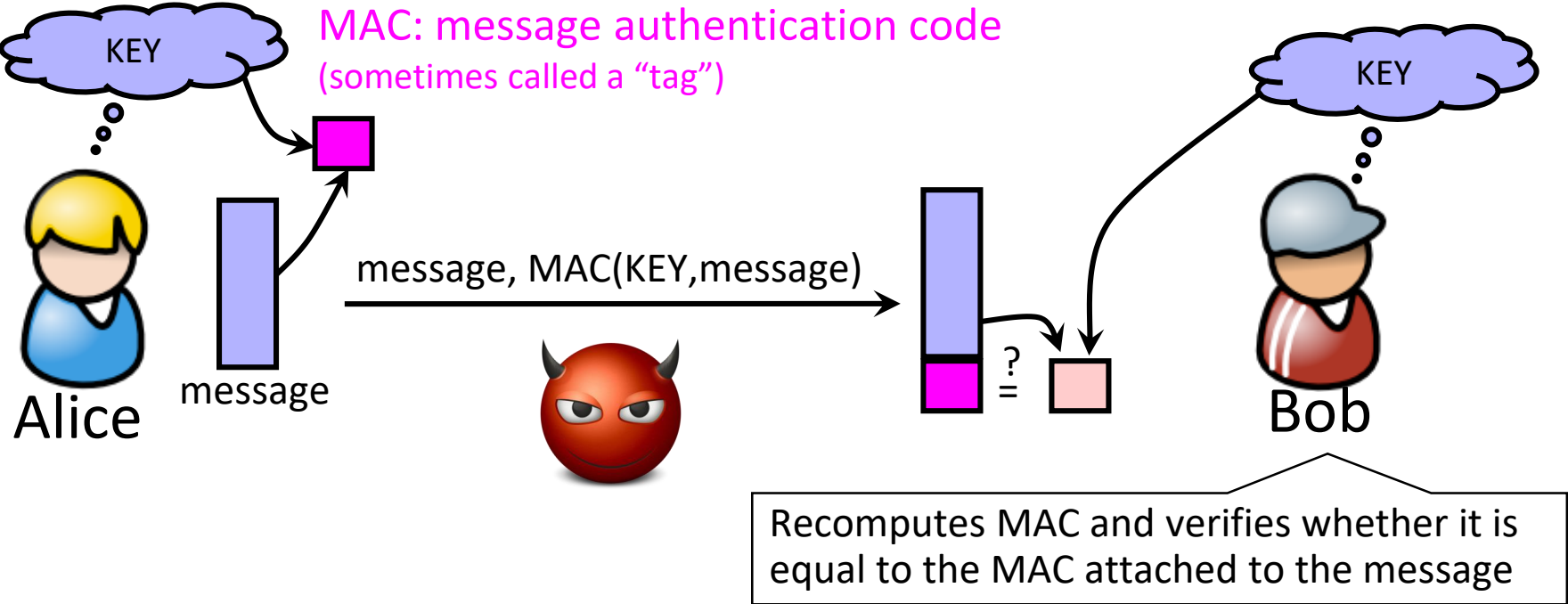
# Aside: How we evaluate hash functions

- Speed
  - Is it amenable to hardware implementations?
- Diffusion
  - Does changing 1 bit in the input affect all output bits?
- Resistance to attack approaches
  - Collisions?
  - Length extensions?
  - etc



# Recall: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



Integrity and authentication: only someone who knows KEY can compute correct MAC for a given message.

# HMAC

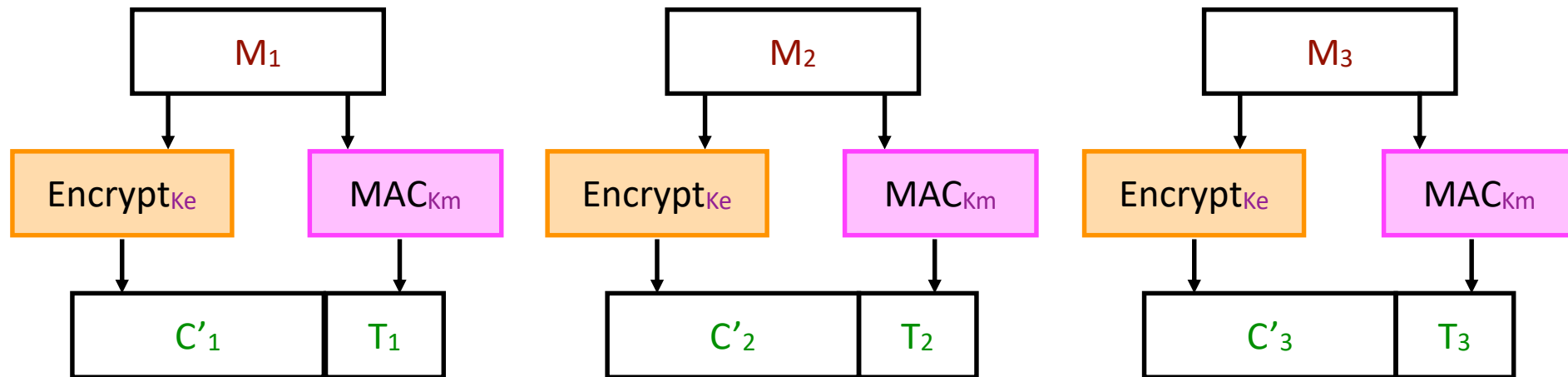
- Construct MAC from a cryptographic hash function
  - Invented by Bellare, Canetti, and Krawczyk (1996)
  - Used in SSL/TLS, mandatory for IPsec
- Why not encryption? (Historical reasons)
  - Hashing is faster than block ciphers in software
  - Can easily replace one hash function with another
  - There used to be US export restrictions on encryption

# MAC with SHA3

- $\text{SHA3}(\text{Key} || \text{Message})$
- SHA3 is designed to get the same safety properties as HMAC constructions

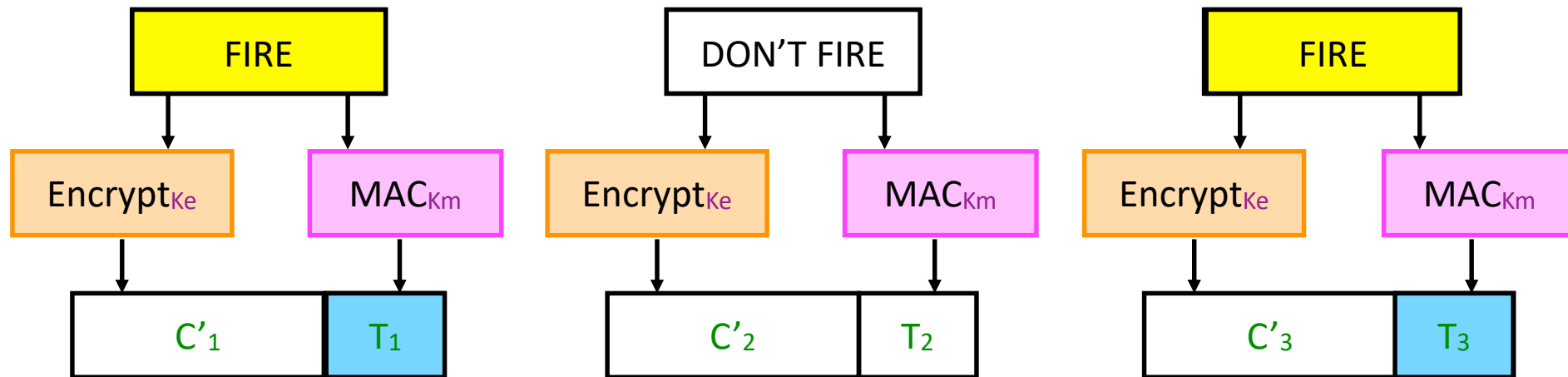
# Authenticated Encryption

- What if we want both privacy and integrity?
- Natural approach: combine **encryption scheme** and a **MAC**.
- Is this fine? (Pollev)



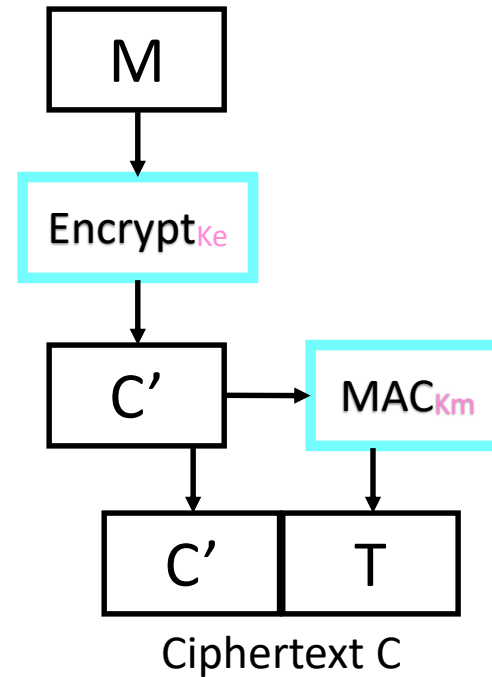
# Authenticated Encryption

- What if we want both privacy and integrity?
- Natural approach: combine **encryption scheme** and a **MAC**.
- **But be careful!**
  - Obvious approach: Encrypt-and-MAC
  - Problem: MAC is deterministic! same plaintext  $\rightarrow$  same MAC



# Authenticated Encryption

- Instead:  
**Encrypt *then* MAC.**
- (Not as good:  
MAC-then-Encrypt)



**Encrypt-then-MAC**