

CSE 484: Computer Security and Privacy

# Cryptography

## [MACs and Hash Functions]

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...

# Admin

- Homework 2
  - Out soon™

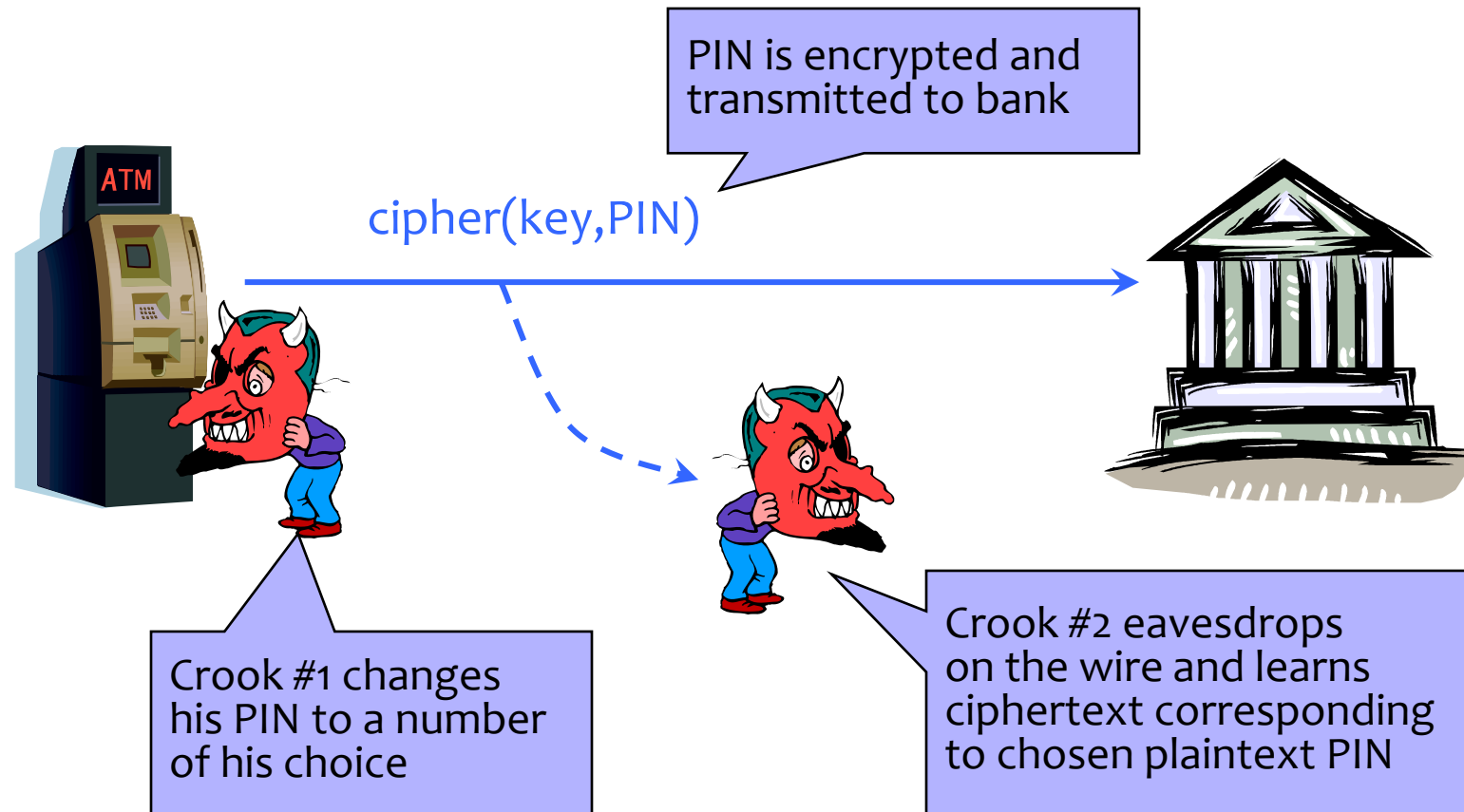
# When is an Encryption Scheme “Secure”?

- Hard to recover the key?
  - What if attacker can learn plaintext without learning the key?
- Hard to recover plaintext from ciphertext?
  - What if attacker learns some bits or some function of bits?

# How Can a Cipher Be Attacked?

- Attackers knows ciphertext and encryption algthm
  - **What else does the attacker know?** Depends on the application in which the cipher is used!

# Chosen Plaintext Attack



... repeat for any PIN value

# How Can a Cipher Be Attacked?

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- **Ciphertext-only attack**
- **KPA: Known-plaintext attack** (stronger)
  - Knows some plaintext-ciphertext pairs
- **CPA: Chosen-plaintext attack** (even stronger)
  - Can obtain ciphertext for any plaintext of his choice
- **CCA: Chosen-ciphertext attack** (very strong)
  - Can decrypt any ciphertext except the target

# Very Informal Intuition

Minimum security requirement for a modern encryption scheme

- Security against chosen-plaintext attack (CPA)
  - Ciphertext leaks no information about the plaintext
  - Even if the attacker correctly guesses the plaintext, he cannot verify his guess
  - Every ciphertext is unique, encrypting same message twice produces completely different ciphertexts
    - Implication: encryption must be randomized or stateful
- Security against chosen-ciphertext attack (CCA)
  - Integrity protection – it is not possible to change the plaintext by modifying the ciphertext

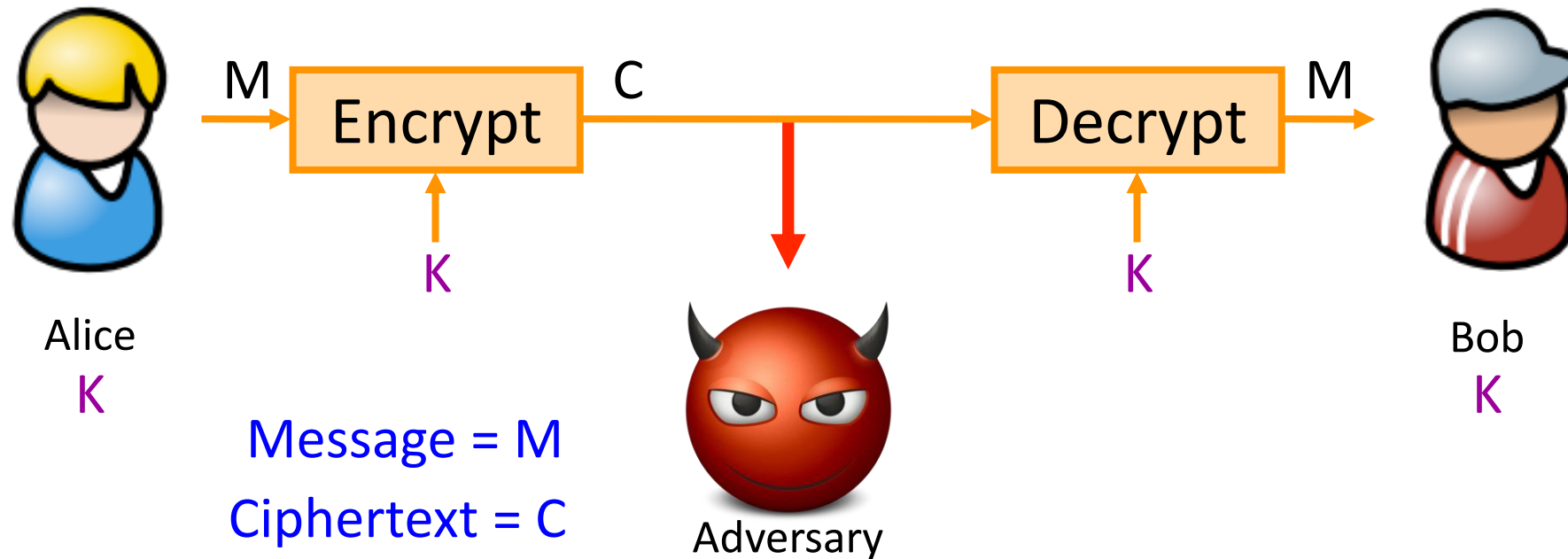
# The shape of the formal approach

- INDDistinguishability under Chosen Plaintext Attack
  - IND-CPA
- Formalized *cryptographic game*
- Adversary submits pairs of *plaintexts* ( $M_a, M_b$ )
  - Gets back ONE of the *ciphertexts* ( $C_x$ )
- Adversary must guess which ciphertext this is ( $C_a$  or  $C_b$ )
  - If they can do better than 50/50, they win



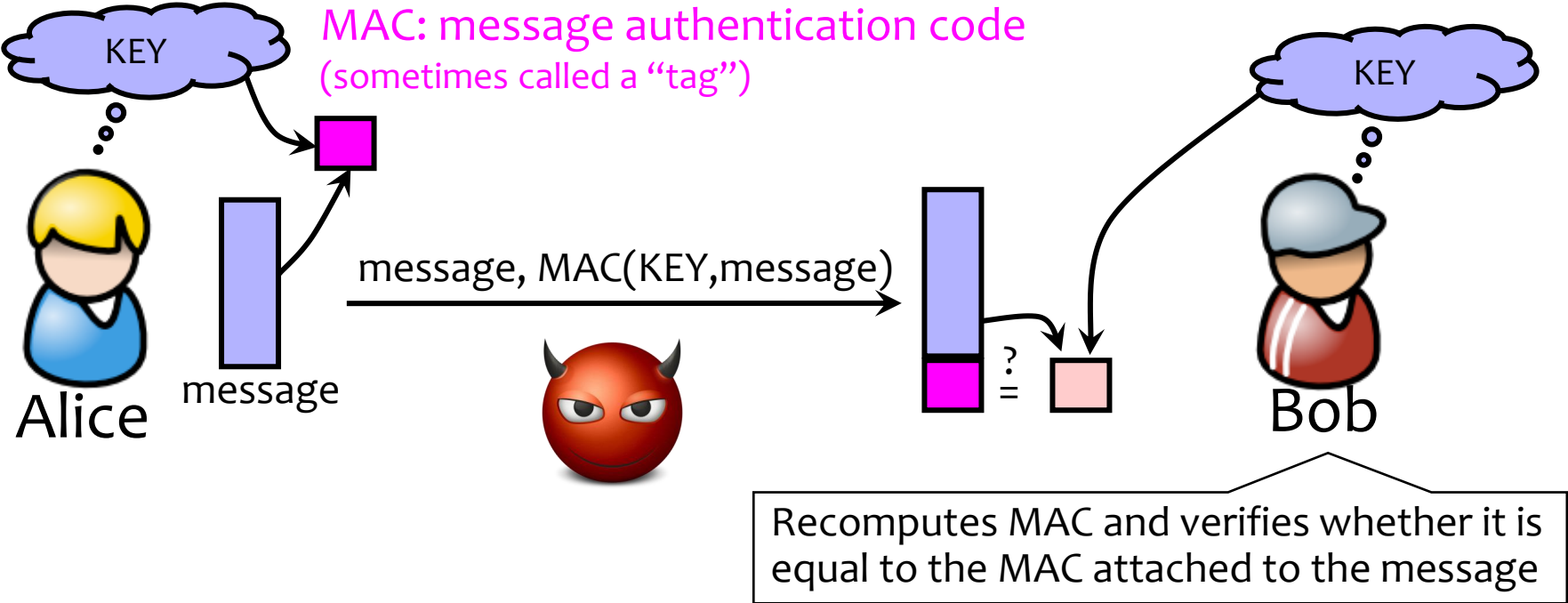
# So Far: Achieving Privacy

Encryption schemes: A tool for protecting **privacy**.



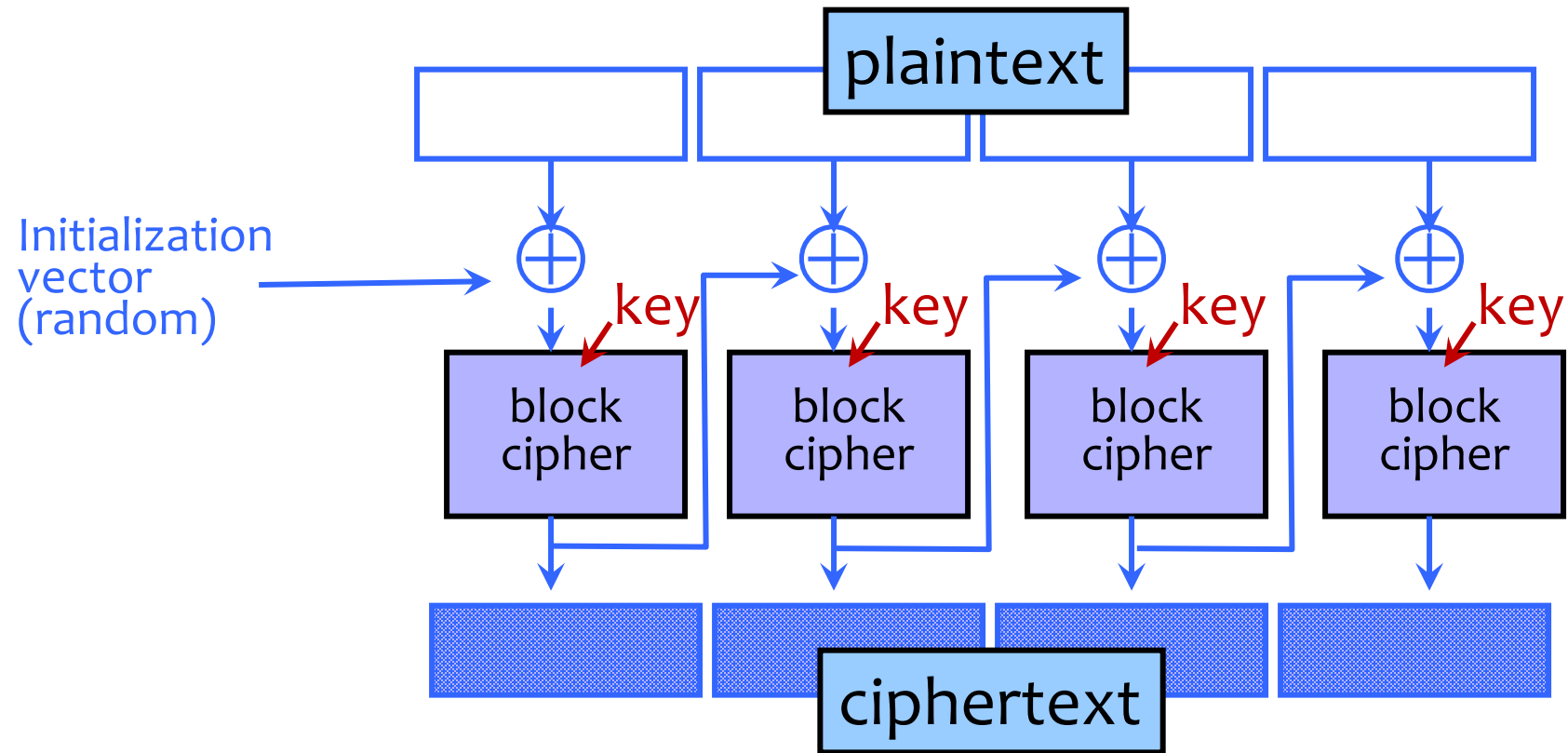
# Now: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



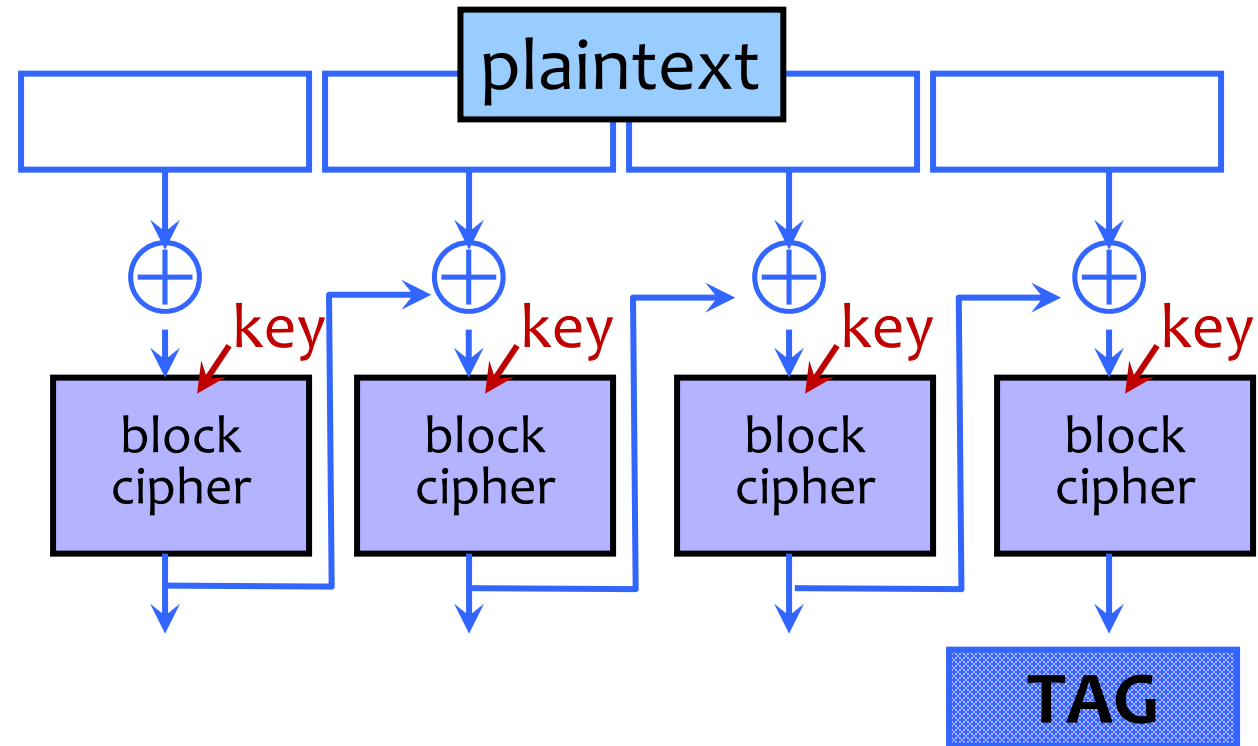
**Integrity and authentication:** only someone who knows KEY can compute correct MAC for a given message.

# Reminder: CBC Mode Encryption



- Identical blocks of plaintext encrypted differently
- Last cipherblock depends on entire plaintext
  - Still does not guarantee integrity

# CBC-MAC



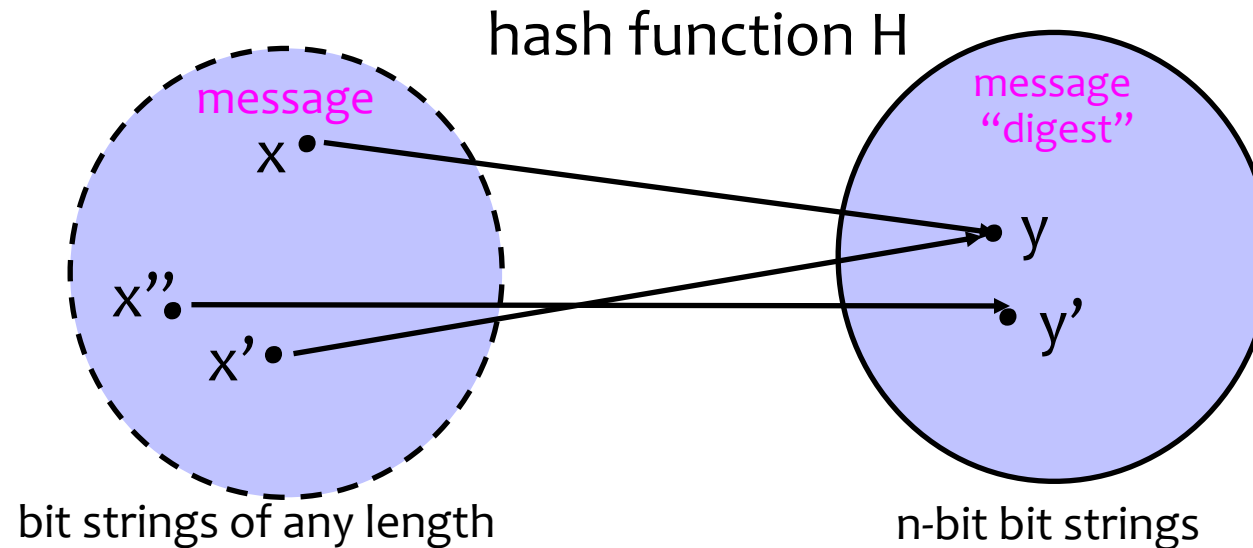
- Not secure when system may MAC messages of different lengths (*more in section!*).
- NIST recommends a derivative called CMAC [FYI only]

# Another Tool: Hash Functions

# You Just Did This

```
franzi@codered:~/sploits$ md5sum exploit0.c  
3a2e6ce795bce4d06df1ff6835d25cea  exploit0.c  
franzi@codered:~/sploits$ █
```

# Hash Functions: Main Idea



- Hash function  $H$  is a lossy compression function
  - Collision:  $h(x)=h(x')$  for distinct inputs  $x, x'$
- $H(x)$  should look "random"
  - Every bit (almost) equally likely to be 0 or 1
- Cryptographic hash function needs a few properties...

# Property 1: One-Way

- Intuition: hash should be hard to invert
  - “Preimage resistance”
  - Let  $h(x') = y \in \{0,1\}^n$  for a random  $x'$
  - Given  $y$ , it should be hard to find any  $x$  such that  $h(x)=y$
- How hard?
  - Brute-force: try every possible  $x$ , see if  $h(x)=y$
  - SHA-1 (common hash function) has 160-bit output
    - Expect to try  $2^{159}$  inputs before finding one that hashes to  $y$ .



# Property 2: Collision Resistance

- Should be hard to find  $x \neq x'$  such that  $h(x) = h(x')$

# Birthday Paradox

- Are there two people in the first 1/8 of this class that have the same birthday?
  - 365 days in a year (366 some years)
    - Pick one person. To find another person with same birthday would take on the order of  $365/2 = 182.5$  people
    - **Expect birthday “collision” with a room of only 23 people.**
    - For simplicity, approximate when we expect a collision as  **$\text{sqrt}(365)$** .
- Why is this important for cryptography?
  - $2^{128}$  different 128-bit values
    - Pick one value at random. To exhaustively search for this value requires trying on average  $2^{127}$  values.
    - **Expect “collision” after selecting approximately  $2^{64}$  random values.**
    - **64 bits** of security against collision attacks, not 128 bits.

# Property 2: Collision Resistance

- Should be hard to find  $x \neq x'$  such that  $h(x) = h(x')$
- Birthday paradox means that brute-force collision search is **only**  $O(2^{n/2})$ , *not*  $O(2^n)$ 
  - For SHA-1, this means  $O(2^{80})$  vs.  $O(2^{160})$

# One-Way vs. Collision Resistance

One-wayness does not imply collision resistance.

Collision resistance does not imply one-wayness.

You can prove this by constructing a function that has one property but not the other.

# Property 3: Weak Collision Resistance

- Given randomly chosen  $x$ , hard to find  $x'$  such that  $h(x)=h(x')$ 
  - Attacker must find collision for a specific  $x$ . By contrast, to break collision resistance it is enough to find any collision.
  - Brute-force attack requires  $O(2^n)$  time
- Weak collision resistance does not imply collision resistance.

# Hashing vs. Encryption

- Hashing is one-way. There is no “un-hashing”
  - A ciphertext can be decrypted with a decryption key... hashes have no equivalent of “decryption”
- Hash(x) looks “random” but can be compared for equality with Hash(x’)
  - Hash the same input twice → same hash value
  - Encrypt the same input twice → different ciphertexts
- Cryptographic hashes are also known as “cryptographic checksums” or “message digests”

# Application: Password Hashing

- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?

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- Instead of user password, store `hash(password)`
- When user enters a password, compute its hash and compare with the entry in the password file
- Why is hashing better than encryption here?
- System does not store actual passwords!
- Don't need to worry about where to store the key!
- Cannot go from hash to password!



# Application: Password Hashing

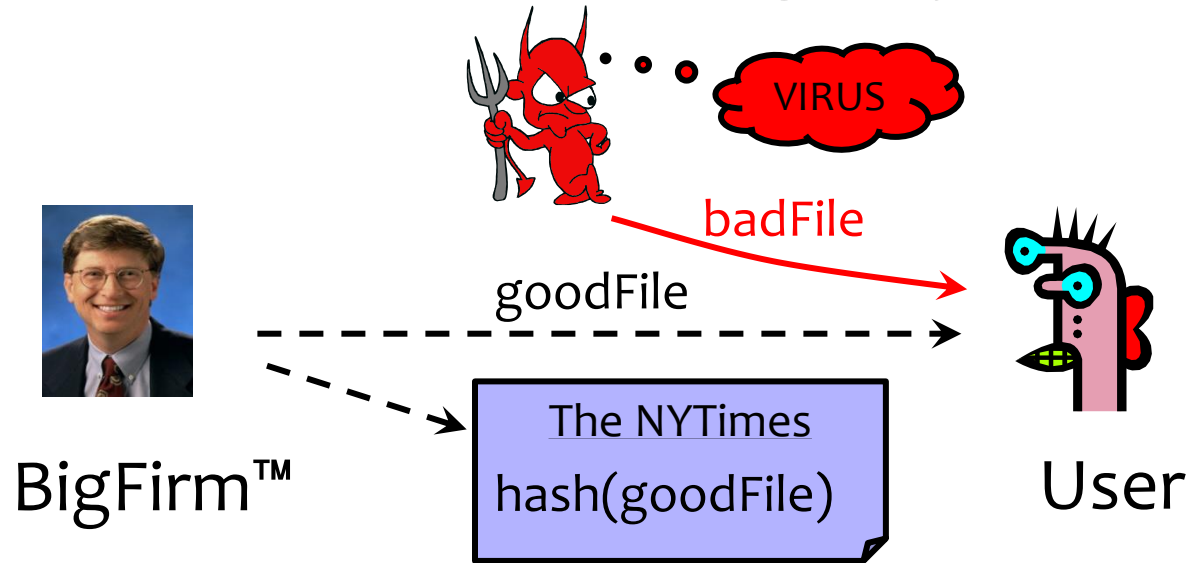
- Which property do we need?
  - One-wayness?
  - (At least weak) Collision resistance?
  - Both?

# Application: Password Hashing + Salting

- **Salting**

- We 'salt' hashes for password by adding a randomized suffix to the password
    - E.g. Hash("coolpassword"+"35B67C2A")
  - We then store the salt with the hashed password!
- 
- The goal is to prevent *precomputation attacks*
    - If the adversary doesn't know the salt, they can't precompute common passwords

# Application: Software Integrity



Goal: Software manufacturer wants to ensure file is received by users without modification.

Idea: given goodFile and hash(goodFile), very hard to find badFile such that hash(goodFile)=hash(badFile)

# Application: Software Integrity

- Which property do we need?
  - One-wayness?
  - (At least weak) Collision resistance?
  - Both?

# Which Property Do We Need?

One-wayness, Collision Resistance, Weak CR?

- UNIX passwords stored as hash(password)
  - **One-wayness:** hard to recover the/a valid password
- Integrity of software distribution
  - **Weak collision resistance**
  - But software images are not really random... may need **full collision resistance** if considering malicious developers

# Which Property Do We Need?

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  - But software images are not really random... may need **full collision resistance** if considering malicious developers
- Commitments (e.g. auctions)
  - Alice wants to bid  $B$ , sends  $H(B)$ , later reveals  $B$
  - **One-wayness:** rival bidders should not recover  $B$  (this may mean that she needs to hash some randomness with  $B$  too)
  - **Collision resistance:** Alice should not be able to change her mind to bid  $B'$  such that  $H(B)=H(B')$

# Common Hash Functions

- MD5 – **Don't Use!**
  - 128-bit output
  - Designed by Ron Rivest, used very widely
  - Collision-resistance broken (summer of 2004)
- RIPEMD
  - 160-bit version is OK
  - 128-bit version is *not* good
- SHA-1 (Secure Hash Algorithm) – **Don't Use!**
  - 160-bit output
  - US government (NIST) standard as of 1993-95
  - Theoretically broken 2005; practical attack 2017!
- **SHA-2: SHA-256, SHA-512, SHA-224, SHA-384**
- SHA-3: standard released by NIST in August 2015

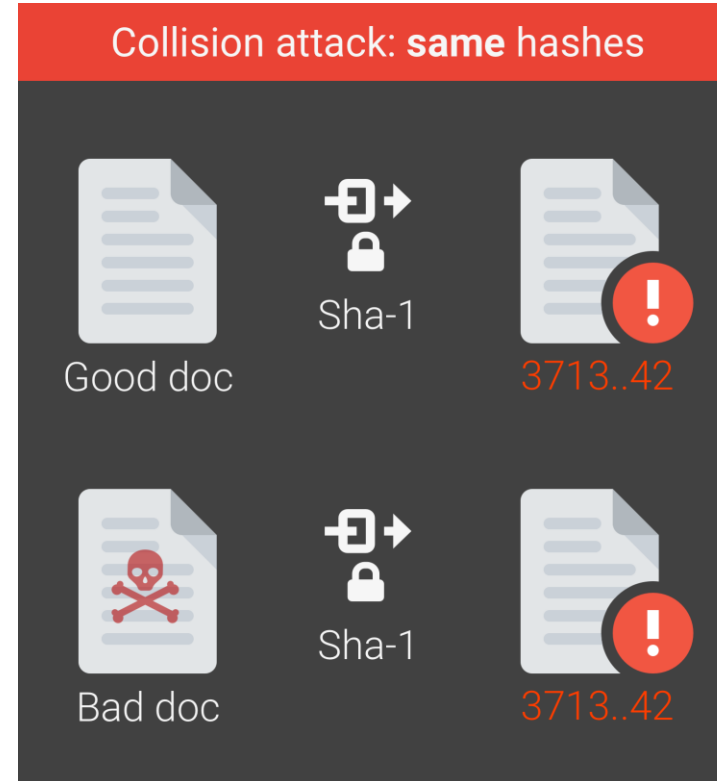
# SHA-1 Broken in Practice (2017)

**Google just cracked one of the building blocks of web encryption (but don't worry)**

*It's all over for SHA-1*

by [Russell Brandom](#) | [@russellbrandom](#) | Feb 23, 2017, 11:49am EST

<https://shattered.io>



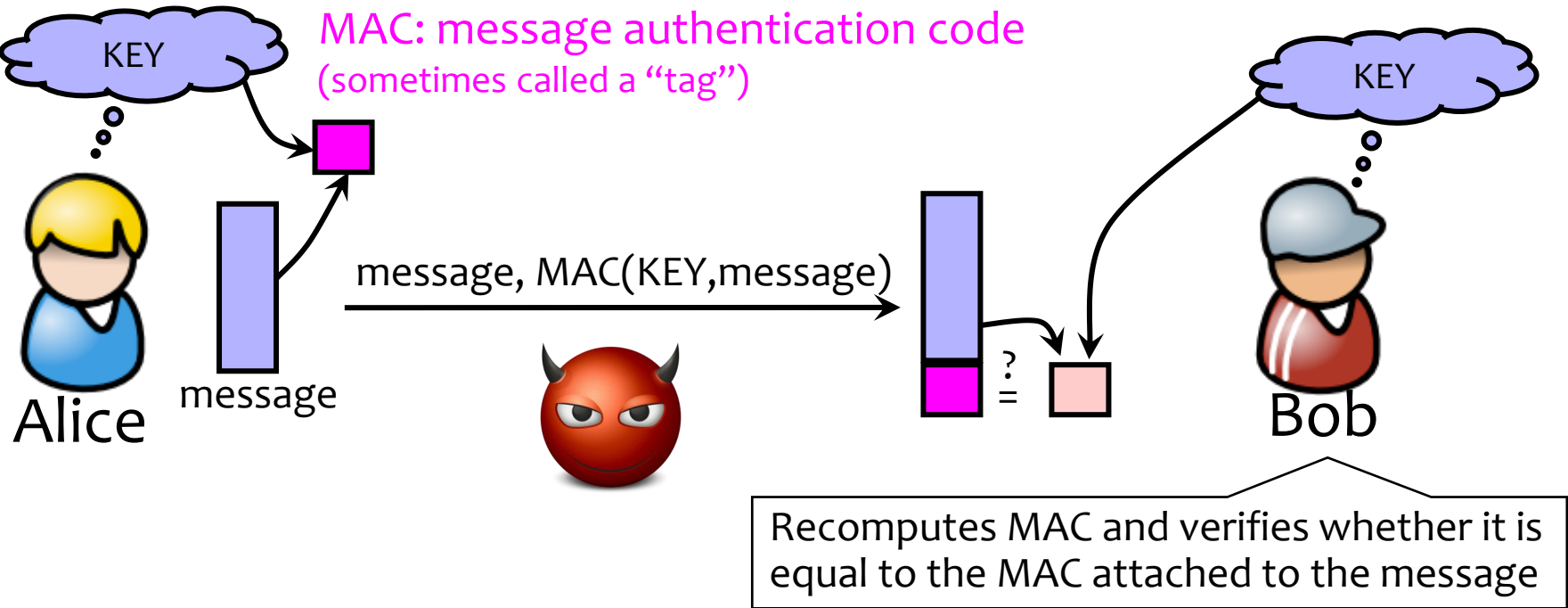


# Aside: How we evaluate hash functions

- Speed
  - Is it amenable to hardware implementations?
- Diffusion
  - Does changing 1 bit in the input affect all output bits?
- Resistance to attack approaches
  - Collisions?
  - Length extensions?
  - etc

# Recall: Achieving Integrity

Message authentication schemes: A tool for protecting integrity.



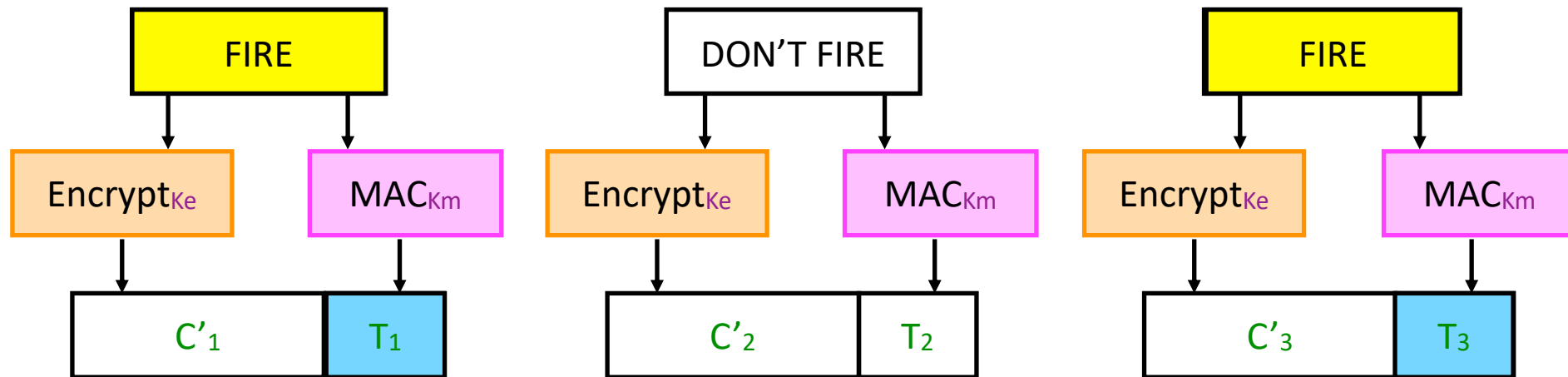
**Integrity and authentication:** only someone who knows KEY can compute correct MAC for a given message.

# HMAC

- Construct MAC from a cryptographic hash function
  - Invented by Bellare, Canetti, and Krawczyk (1996)
  - Used in SSL/TLS, mandatory for IPsec
- Why not encryption?
  - Hashing is faster than block ciphers in software
  - Can easily replace one hash function with another
  - There used to be US export restrictions on encryption

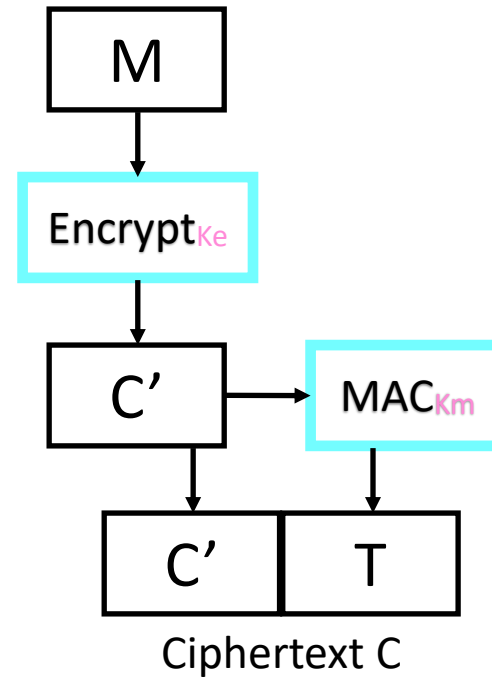
# Authenticated Encryption

- What if we want both privacy and integrity?
- Natural approach: combine **encryption scheme** and a **MAC**.
- **But be careful!**
  - Obvious approach: Encrypt-and-MAC
  - Problem: MAC is deterministic! same plaintext  $\rightarrow$  same MAC



# Authenticated Encryption

- Instead:  
**Encrypt *then* MAC.**
- (Not as good:  
MAC-then-Encrypt)



**Encrypt-then-MAC**