Agent vs. Environment

- An **agent** is an entity that perceives and acts.
- A **rational agent** selects actions that maximize its utility function.
- Characteristics of the percepts, environment, and action space dictate techniques for selecting rational actions.

Types of Agents

- Reflex
- Goal oriented
- Utility-based

Goal Based Agents

- Plan ahead
- Ask “what if”
- Decisions based on (hypothesized) consequences of actions
- Must have a model of how the world evolves in response to actions
- Act on how the world WOULD BE

Search thru a Problem Space (aka State Space)

- **Input:**
  - Set of states
  - Operators [and costs]
  - Start state
  - Goal state [test]
- **Output:**
  - Path: start → a state satisfying goal test
    [May require shortest path]
    [Sometimes just need a state that passes test]
Example: Traveling in Romania

- State space:
  - Cities
- Successor function:
  - Roads: Go to adjacent city with cost = distance
- Start state:
  - Arad
- Goal test:
  - Is state == Bucharest?
- Solution?

Example: Simplified Pac-Man

- Input:
  - A state space
  - A successor function
  - A start state
  - A goal test
- Output:

State Space Sizes?

- Search Problem:
  - Eat all of the food
- Pacman positions: 10 x 12 = 120
- Pacman facing:
  - up, down, left, right
- Food configurations: $2^{10}$
- Ghost1 positions: 12
- Ghost 2 positions: 11

$120 \times 4 \times 2^{10} \times 12 \times 11 = 6.8 \times 10^{13}$

State Space Graphs

- State space graph:
  - Each node is a state
  - The successor function is represented by arcs
  - Edges may be labeled with costs
  - In a search graph, each state occurs only once!
  - We can rarely build this graph in memory (so we don’t)

Search Trees

- A search tree:
  - Start state at the root node
  - Children correspond to successors
  - Nodes contain states, correspond to PLANS to those states
  - Edges are labeled with actions and costs
  - For most problems, we can never actually build the whole tree

State Space Graphs vs. Search Trees

Each NODE in the search tree is an entire PATH in the state space graph.
We construct both as needed and we construct as little as possible.
State Space Graphs vs. Search Trees

Consider this 4-state graph:

Important: Lots of repeated structure in the search tree!

Tree Search

How big is its search tree (from $S$)?

Search Example: Romania

Searching with a Search Tree

- Search:
  - Expand out potential plans (tree nodes)
  - Maintain a fringe of partial plans under consideration
  - Try to expand as few tree nodes as possible

General Tree Search

- Important ideas:
  - Fringe
  - Expansion
  - Exploration strategy
- Main question: which fringe nodes to explore?

Tree Search Example
Search Algorithm Properties

- Complete: Guaranteed to find a solution if one exists?
- Optimal: Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?
- Cartoon of search tree:
  - b is the branching factor
  - m is the maximum depth
  - solutions at various depths
- Number of nodes in entire tree?
  - \[1 + b + b^2 + \ldots + b^m = O(b^m)\]

Depth-First Search (DFS) Properties

- What nodes does DFS expand?
  - Some left prefix of the tree.
  - Could process the whole tree!
  - If m is finite, takes time \(O(b^m)\)
- How much space does the fringe take?
  - Only has siblings on path to root, so \(O(bm)\)
- Is it complete?
  - \(m\) could be infinite, so only if we prevent cycles
- Is it optimal?
  - No, it finds the “leftmost” solution, regardless of depth or cost
Breadth-First Search

Strategy: Expand a shallowest node first.
Implementation: Fringe is a FIFO queue.

Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
  - Processes all nodes above shallowest solution
  - Let depth of shallowest solution be \( d \)
  - Search takes time \( O(b^d) \)

- How much space does the fringe take?
  - Has roughly the last tier, so \( O(b^d) \)

- Is it complete?
  - \( d \) must be finite if a solution exists, so yes!

- Is it optimal?
  - Only if costs are all 1 (more on costs later)

DFS vs BFS

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Complete</th>
<th>Optimal</th>
<th>Time</th>
<th>Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>BFS</td>
<td>Y</td>
<td>Y</td>
<td>( O(b^d) )</td>
<td>( O(b^d) )</td>
</tr>
<tr>
<td>DFS w/ Path Checking</td>
<td>N (unless finite)</td>
<td>N</td>
<td>( O(b^d) )</td>
<td>( O(b^d) )</td>
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</table>

Memory a Limitation?

- Suppose:
  - 4 GHz CPU
  - 32 GB main memory
  - 100 instructions / expansion
  - 5 bytes / node
  - 40 M expansions / sec
  - Memory filled in 160 sec ... 3 min

Iterative Deepening

Iterative deepening uses DFS as a subroutine:
1. Do a DFS which only searches for paths of length 1 or less.
2. If "1" failed, do a DFS which only searches paths of length 2 or less.
3. If "2" failed, do a DFS which only searches paths of length 3 or less.
   ... and so on.

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<tr>
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BFS vs. Iterative Deepening

- For $b = 10, d = 5$:
  - BFS = $1 + 10 + 100 + 1,000 + 10,000 + 100,000 = 111,111$
  - IDS = $6 + 50 + 400 + 3,000 + 20,000 + 100,000 = 123,456$
  - Overhead = $(123,456 - 111,111) / 111,111 = 11\%$
  - Memory BFS: 100,000; IDS: 50

Uniform Cost Search

Expand cheapest node first:
Fringe is a priority queue

Uniform Cost Search

- Strategy: expand a cheapest node first:
  - Fringe is a priority queue (priority: cumulative cost)

Uniform Cost Search (UCS) Properties

- What nodes does UCS expand?
  - Processes all nodes with cost less than cheapest solution
  - If that solution costs $c^*$ and arcs cost at least $c$, then the "effective depth" is roughly $c^*/c$
  - Takes time $O(b^{c^*/c})$ (exponential in effective depth)

- How much space does the fringe take?
  - Has roughly the last tier, so $O(b^{c^*/c})$

- Is it complete?
  - Assuming best solution has a finite cost and minimum arc cost is positive, yes!

- Is it optimal?
  - Yes!

Uniform Cost Search

- Strategy: expand lowest path cost
- The good: UCS is complete and optimal!
- The bad:
  - Explores options in every "direction"
  - No information about goal location
### Uniform Cost Search

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<td>$O(bm)$</td>
</tr>
<tr>
<td>UCS</td>
<td>Y*</td>
<td>Y</td>
<td>$O(b^{m^*})$</td>
<td>$O(b^{m^*})$</td>
</tr>
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$C^{m^*}$ tiers

### Uniform Cost: Pac-Man
- Cost of 1 for each action
- Explores all of the states, but one

![Pac-Man maze](image)

### The One Queue
- All these search algorithms are the same except for fringe strategies
  - Conceptually, all fringes are priority queues (i.e. collections of nodes with attached priorities)
  - Practically, for DFS and BFS, you can avoid the log(n) overhead from an actual priority queue, by using stacks and queues
  - Can even code one implementation that takes a variable queuing object

### To Do:
- Look at the course website:  
- Do the readings (Ch 3)
- Do Project 0 if new to Python
- Start Project 1, when it is posted