Announcements

Final

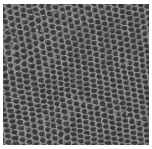
- Monday 10:30-12:20, in this room
- Closed book/notes
- Comprehensive (through today)
- Review today

Project 3 artifacts

Evals

- at end of class

Modeling Texture



What is texture?

How can we model it?

Markov Chains

Markov Chain

- a *sequence* of random variables $\mathbf{x}_1, \mathbf{x}_2, \ldots, \mathbf{x}_n$
- $\mathbf{x}_t$ is the **state** of the model at time t

$$\boxed{\mathbf{x}_1} \rightarrow \boxed{\mathbf{x}_2} \rightarrow \boxed{\mathbf{x}_3} \rightarrow \boxed{\mathbf{x}_4} \rightarrow \boxed{\mathbf{x}_5}$$

- **Markov assumption**: each state is dependent only on the previous one
  - dependency given by a **conditional probability**:

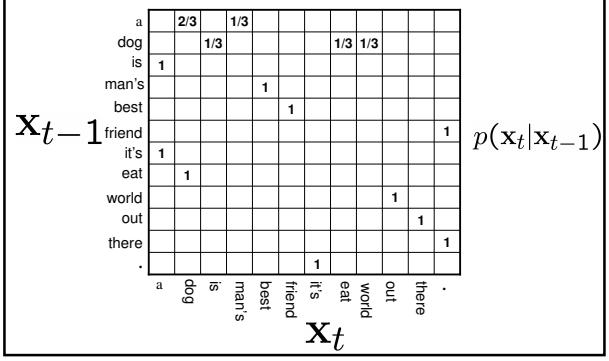
$$p(\mathbf{x}_t|\mathbf{x}_{t-1})$$

- The above is actually a *first-order* Markov chain
- An *N'th-order* Markov chain:

$$p(\mathbf{x}_t|\mathbf{x}_{t-1}, \ldots, \mathbf{x}_{t-N})$$

Markov Chain Example: Text

"A dog is a man's best friend. It's a dog eat dog world out there."



Text synthesis

Create plausible looking poetry, love letters, term papers, etc.

Most basic algorithm

1. Build probability histogram
   - find all blocks of N consecutive words/letters in training documents
   - compute probability of occurance $p(\mathbf{x}_t|\mathbf{x}_{t-1},\ldots,\mathbf{x}_{t-(n-1)})$
2. Given words $\mathbf{x}_1,\mathbf{x}_2,\ldots,\mathbf{x}_{k-1}$
   - compute $\mathbf{x}_k$ by sampling from $p(\mathbf{x}_t|\mathbf{x}_{t-1},\ldots,\mathbf{x}_{t-(n-1)})$

Example on board...

[Scientific American, June 1989, Dewdney]

"I Spent an Interesting Evening Recently with a Grain of Salt"

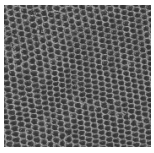
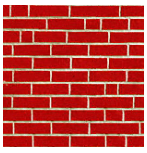
- Mark V. Shaney

(computer-generated contributor to UseNet News group called net.singles)

Output of 2nd order word-level Markov Chain after training on 90,000 word philosophical essay:

"Perhaps only the allegory of simulation is unendurable--more cruel than Artaud's Theatre of Cruelty, which was the first to practice deterrence, abstraction, disconnection, deterritorialisation, etc.; and if it were our own past. We are witnessing the end of the negative form. But nothing separates one pole from the very swing of voting "rights" to electoral..."

Modeling Texture

What is texture?

- An image obeying some statistical properties
- Similar structures repeated over and over again
- Often has some degree of randomness

Markov Random Field

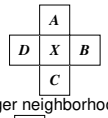
A Markov random field (MRF)

- generalization of Markov chains to two or more dimensions.

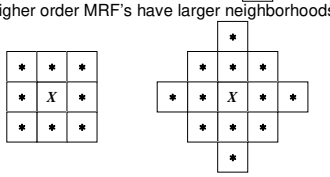
First-order MRF:

- probability that pixel *X* takes a certain value given the values of neighbors *A*, *B*, *C*, and *D*:

$$P(\mathbf{X}|\mathbf{A},\mathbf{B},\mathbf{C},\mathbf{D})$$

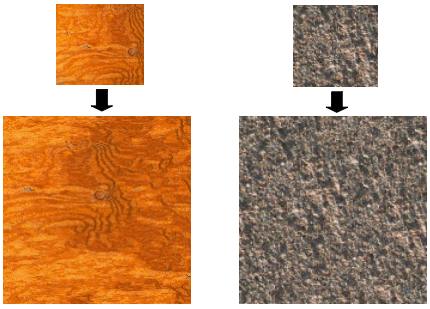


- Higher order MRF's have larger neighborhoods

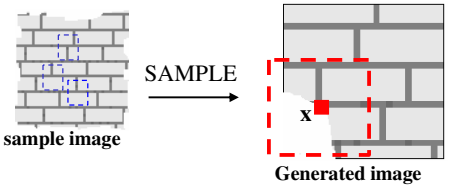


Texture Synthesis [Efros & Leung, ICCV 99]

Can apply 2D version of text synthesis



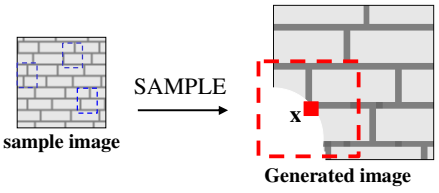
Synthesizing One Pixel



- What is $P(\mathrm{x}|\text{neighborhood of pixels around x})$?
- Find all the windows in the image that match the neighborhood
  - consider only pixels in the neighborhood that are already filled in
- To synthesize **x**
  - pick one matching window at random
  - assign **x** to be the center pixel of that window

Slides courtesy of Alyosha Efros

Really Synthesizing One Pixel

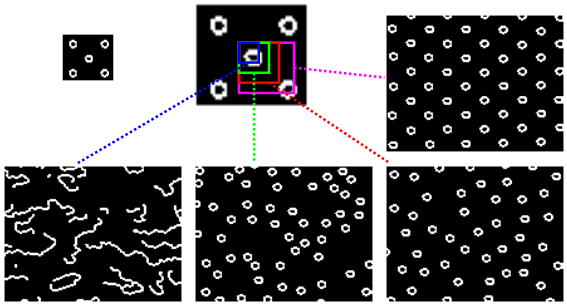


- An exact neighbourhood match might not be present
- So we find the **best** matches using SSD error and randomly choose between them, preferring better matches with higher probability

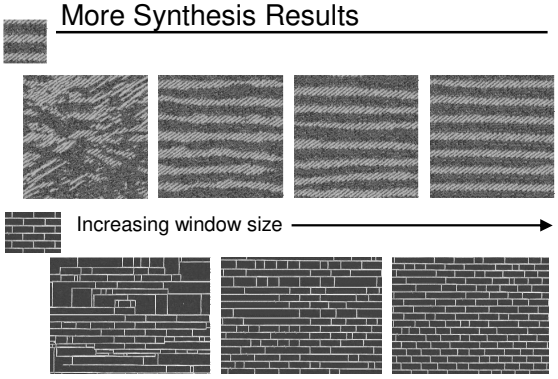
Growing Texture

- Starting from the initial image, "grow" the texture one pixel at a time

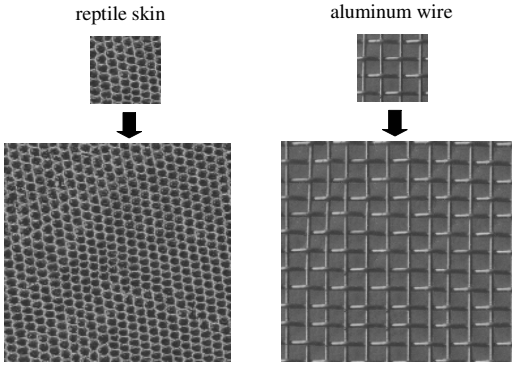
Window Size Controls Regularity



More Synthesis Results



More Results



Failure Cases

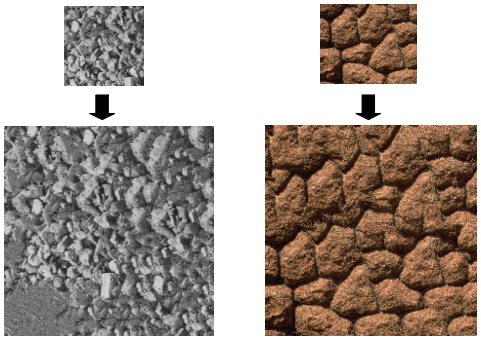
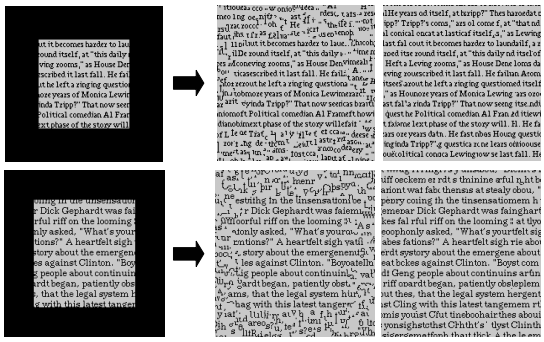
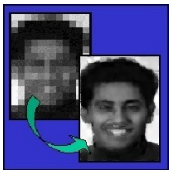


Image-Based Text Synthesis



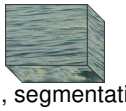
Applications of Texture Modeling

Super-resolution
- Freeman & Pasztor, 1999
- Baker & Kanade, 2000



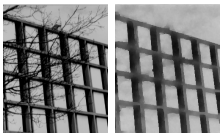
Image/video compression

Video Textures
- Wei & Levoy, 2000
- Schodl et al., 2000



Texture recognition, segmentation
- DeBonet

Restoration
- removing scratches, holes, filtering
- Zhu et al.



Art/entertainment