Introduction to Database Systems CSE 444

Lecture 20: Query Execution: Relational Algebra

May 21, 2008

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DBMS Architecture

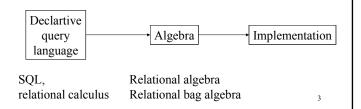
How does a SQL engine work?

- SQL query \rightarrow relational algebra plan
- Relational algebra plan → Optimized plan
- Execute each operator of the plan

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Relational Algebra

- Formalism for creating new relations from existing ones
- Its place in the big picture:



Relational Algebra

- Five operators:
 - Union: ○
 - Difference: -
 - Selection: σ
 - Projection: Π
 - Cartesian Product: ×
- Derived or auxiliary operators:
 - Intersection, complement
 - Joins (natural, equi-join, theta join, semi-join)
 - Renaming: ρ

1. Union and 2. Difference

- R1 ∪ R2
- Example:
 - ActiveEmployees \cup RetiredEmployees
- R1 R2
- Example:
 - AllEmployees -- RetiredEmployees

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3. Selection

- Returns all tuples which satisfy a condition
- Notation: $\sigma_c(R)$
- Examples
 - $\sigma_{Salary > 40000}$ (Employee)
 - $\sigma_{\text{name = "Smith"}} (Employee)$
- The condition c can be =, <, \le , >, \ge , <>

What about Intersection?

- It is a derived operator
- $R1 \cap R2 = R1 (R1 R2)$
- Also expressed as a join (will see later)
- Example
 - UnionizedEmployees ∩ RetiredEmployees

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| SSN | Name | Salary |
|---------|-------|--------|
| 1234545 | John | 200000 |
| 5423341 | Smith | 600000 |
| 4352342 | Fred | 500000 |

 $\sigma_{\text{Salary} > 40000}(Employee)$

| SSN | Name | Salary |
|---------|-------|--------|
| 5423341 | Smith | 600000 |
| 4352342 | Fred | 500000 |

4. Projection

• Eliminates columns, then removes duplicates

• Notation: $\Pi_{A1,...,An}(R)$

• Example: project social-security number and names:

- Π_{SSN, Name} (Employee)

- Output schema: Answer(SSN, Name)

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| SSN | Name | Salary |
|---------|------|--------|
| 1234545 | John | 200000 |
| 5423341 | John | 600000 |
| 4352342 | John | 200000 |

 $\Pi_{Name,Salary}$ (Employee)

| Name | Salary |
|------|--------|
| John | 20000 |
| John | 60000 |

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5. Cartesian Product

• Each tuple in R1 with each tuple in R2

• Notation: R1 × R2

• Example:

 $- \ Employee \times Dependents$

• Very rare in practice; mainly used to express joins

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Cartesian Product Example

Employee

| Name | SSN |
|------|----------|
| John | 99999999 |
| Tony | 77777777 |

Dependents

| EmployeeSSN | Dname | |
|-------------|-------|--|
| 99999999 | Emily | |
| 77777777 | Joe | |

Employee x Dependents

| Name | SSN | EmployeeSSN | Dname |
|------|-----------|-------------|-------|
| John | 999999999 | 99999999 | Emily |
| John | 99999999 | 77777777 | Joe |
| Tony | 77777777 | 99999999 | Emily |
| Tony | 77777777 | 77777777 | Joe |

Relational Algebra

- Five operators:
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Renaming

- Changes the schema, not the instance
- Notation: $\rho_{B1,...Bn}(R)$
- Example:
 - ρ_{LastName, SocSocNo} (Employee)
 - Output schema:Answer(LastName, SocSocNo)

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Renaming Example

| Em | pla | vee |
|----|-----|-----|
| | | |

| Name | SSN |
|------|----------|
| John | 99999999 |
| Tony | 77777777 |

$\rho_{\textit{LastName, SocSocNo}}$ (Employee)

| LastName | SocSocNo |
|----------|----------|
| John | 99999999 |
| Tony | 77777777 |

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Natural Join

• Notation: R1™R2

• Meaning: $R1 \bowtie R2 = \Pi_A(\sigma_C(R1 \times R2))$

- Where:
 - The selection $\sigma_{C}\, \text{checks}$ equality of all common attributes
 - The projection eliminates the duplicate common attributes

Natural Join Example

Employee

| Employee | | |
|----------|----------|--|
| Name | SSN | |
| John | 99999999 | |
| Tony | 77777777 | |

Dependents

| SSN | Dname |
|----------|-------|
| 99999999 | Emily |
| 77777777 | Joe |

Employee M Dependents =

 $\Pi_{Name, \ SSN, \ Dname}(\sigma_{\ SSN=SSN2}(Employee \times \rho_{SSN2, \ Dname}(Dependents))$

| Name | SSN | Dname |
|------|-----------|-------|
| John | 999999999 | Emily |
| Tony | 77777777 | Joe |

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Natural Join

| _ | | |
|----|---|---|
| S= | В | С |
| | Z | U |
| | V | W |
| | Z | V |

| D > 4C- | A | В | C |
|-----------------|---|---|---|
| • $R\bowtie S=$ | X | Z | U |
| | X | Z | V |
| | Y | Z | U |
| | Y | Z | V |
| | Z | V | W |

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Natural Join

- Given the schemas R(A, B, C, D), S(A, C, E), what is the schema of $R \bowtie S$?
- Given R(A, B, C), S(D, E), what is $R \bowtie S$?
- Given R(A, B), S(A, B), what is $R \bowtie S$?

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Theta Join

- A join that involves a predicate
- $R1 \underset{\theta}{\triangleright} R2 = \sigma_{\theta} (R1 \times R2)$
- Here θ can be any condition

Eq-join

- A theta join where θ is an equality
- R1 $\underset{A=B}{\bowtie}$ R2 = $\sigma_{A=B}$ (R1 × R2)
- Example:
 - Employee SN=SN Dependents
- Most useful join in practice

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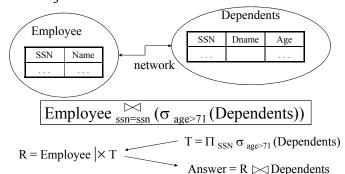
Semijoin

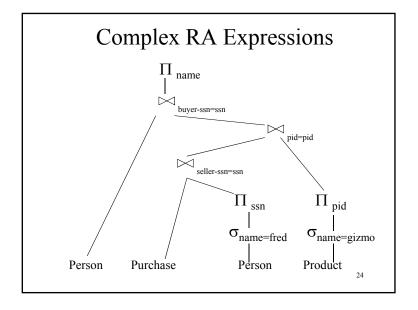
- $R \mid \times S = \prod_{A1,...,An} (R \bowtie S)$
- Where $A_1, ..., A_n$ are the attributes in R
- Example:
 - Employee |× Dependents

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Semijoins in Distributed Databases

• Semijoins are used in distributed databases





Operations on Bags

A **bag** = a set with repeated elements

All operations need to be defined carefully on bags

- $\{a,b,b,c\} \cup \{a,b,b,b,e,f,f\} = \{a,a,b,b,b,b,b,c,e,f,f\}$
- $\{a,b,b,c,c\} \{b,c,c,c,d\} = \{a,b,b\}$
- $\sigma_C(R)$: preserve the number of occurrences
- $\Pi_A(R)$: no duplicate elimination
- Cartesian product, join: no duplicate elimination Important! Relational Engines work on bags, not sets!

Reading assignment: 5.3 - 5.4

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Note: RA has Limitations!

• Cannot compute "transitive closure"

| Name1 | Name2 | Relationship |
|-------|-------|--------------|
| Fred | Mary | Father |
| Mary | Joe | Cousin |
| Mary | Bill | Spouse |
| Nancy | Lou | Sister |

- · Find all direct and indirect relatives of Fred
- Cannot express in RA!!! Need to write C program

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From SQL to RA Purchase(buyer, product, city) Person(name, age) SELECT DISTINCT P.buyer Gity='Seattle' and are > 20

FROM Purchase P, Person Q
WHERE P.buyer=Q.name AND
P.city='Seattle' AND
Q.age > 20

buyer

City='Seattle'
and age > 20

buyer=name

Purchase Person

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Also... Purchase(buyer, product, city) Person(name, age) SELECT DISTINCT P.buyer FROM Purchase P, Person Q WHERE P.buyer=Q.name AND P.city='Seattle' AND Q.age > 20 Ority='Seattle' age > 20 Purchase Person

Non-monontone Queries (in class)

Purchase(buyer, product, city) Person(name, age)

```
SELECT DISTINCT P.product
FROM Purchase P
WHERE P.city='Seattle' AND
not exists (select *
from Purchase P2, Person Q
where P2.product = P.product
and P2.buyer = Q.name
and Q.age > 20)
```

Extended Logical Algebra Operators (operate on Bags, not Sets)

- Union, intersection, difference
- Selection σ
- Projection Π
- Join ⋈
- Duplicate elimination δ
- Grouping γ
- Sorting τ

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Logical Query Plan

SELECT city, count(*)
FROM sales
GROUP BY city
HAVING sum(price) > 100

T3(city, c) $\Pi_{city, c}$ T2(city,p,c) $\sigma_{p>100}$ T1(city,p,c) $\gamma_{city, sum(price) \rightarrow p, count(*) \rightarrow c}$ sales(product, city, price)

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T1, T2, T3 = temporary tables

Logical v.s. Physical Algebra

- We have seen the logical algebra so far:
 - Five basic operators, plus group-by, plus sort
- The Physical algebra refines each operator into a concrete algorithm

