## CSE 442 - Data Visualization

## Data and Image Models



Jeffrey Heer University of Washington

## The Big Picture

task
questions, goals assumptions
data
physical data type
conceptual data type
domain
metadata
semantics
conventions
processing algorithms
image
visual channel graphical marks
mapping visual encoding

## Learning Goals

We should be able to answer these questions:
How can we encode abstract data within an image?
What are some foundational principles we can use to guide the visual encoding process?

## Topics

Properties of Data
Properties of Images
Mapping Data to Images

## Data Models

## Data Models / Conceptual Models

Data models are formal descriptions
Math: sets with operations on them
Example: integers with + and $x$ operators
Conceptual models are mental constructions Include semantics and support reasoning

Examples (data vs. conceptual)
1D floats vs. temperatures
3D vector of floats vs. spatial location

## Taxonomy of Data Types (?)

1D (sets and sequences)
Temporal
2D (maps)
3D (shapes)
nD (relational)
Trees (hierarchies)
Networks (graphs)
Are there others?
The eyes have it: A task by data type taxonomy for information visualization [Shneiderman 96]

Nominal, Ordinal \& Quantitative

## Nominal, Ordinal \& Quantitative

N-Nominal (labels or categories)

- Fruits: apples, oranges, ...


## Nominal, Ordinal \& Quantitative

N - Nominal (labels or categories)

- Fruits: apples, oranges, ...

O - Ordinal (rank ordered)

- Quality of meat: Grade A, AA, AAA


## Nominal, Ordinal \& Quantitative

N-Nominal (labels or categories)

- Fruits: apples, oranges, ...

O - Ordinal (rank ordered)

- Quality of meat: Grade A, AA, AAA

Q - Interval (location of zero arbitrary)

- Dates: Jan, 19, 2006; Location: (LAT 33.98, LONG -118.45)
- Only differences (i.e., intervals) may be compared


## Nominal, Ordinal \& Quantitative

N-Nominal (labels or categories)

- Fruits: apples, oranges, ...

O - Ordinal (rank ordered)

- Quality of meat: Grade A, AA, AAA

Q - Interval (location of zero arbitrary)

- Dates: Jan, 19, 2006; Location: (LAT 33.98, LONG -118.45)
- Only differences (i.e., intervals) may be compared

Q - Ratio (zero fixed)

- Physical measurement: Length, Mass, Time duration, ...
- Counts and amounts


## Nominal, Ordinal \& Quantitative

N - Nominal (labels or categories)

- Operations: =, $\neq$

O - Ordinal (rank ordered)

- Operations: $=, \neq,<,>$

Q - Interval (location of zero arbitrary)

- Operations: =, $\neq,<,>$, -
- Can measure distances or spans

Q - Ratio (zero fixed)

- Operations: =, $\neq,<,>,-, \%$
- Can measure ratios or proportions


## From Data Model to N, O, Q

Data Model
32.5, 54.0, -17.3, ...

Floating point numbers
Conceptual Model
Temperature ( ${ }^{\circ} \mathrm{C}$ )
Data Type
Burned vs. Not-Burned (N)
Hot, Warm, Cold (O)
Temperature Value (Q-interval)

## Dimensions \& Measures

Dimensions (~ independent variables)
Often discrete variables describing data (N, O)
Categories, dates, binned quantities
Measures ( ~ dependent variables)
Data values that can be aggregated (Q)
Numbers to be analyzed
Aggregate as sum, count, avg, std. dev...
Not a strict distinction. The same variable may be treated either way depending on the task.

## Example: U.S. Census Data

## Example: U.S. Census Data

People Count: \# of people in group
Year: 1850-2000 (every decade)
Age: 0-90+
Sex: Male, Female
Marital Status: Single, Married, Divorced, ...

## Example: U.S. Census

## People Count Year Age

 Sex Marital Status
## 2,348 data points

| T | A | B | C | D | E |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | year | age | marst | sex | people |
| 2 | 1850 | 0 | 0 | 1 | 1483789 |
| 3 | 1850 | 0 | 0 | 2 | 1450376 |
| 4 | 1850 | 5 | 0 | 1 | 1411067 |
| 5 | 1850 | 5 | 0 | 2 | 1359668 |
| 6 | 1850 | 10 | 0 | 1 | 1260099 |
| 7 | 1850 | 10 | 0 | 2 | 1216114 |
| 8 | 1850 | 15 | 0 | 1 | 1077133 |
| 9 | 1850 | 15 | 0 | 2 | 1110619 |
| 10 | 1850 | 20 | 0 | 1 | 1017281 |
| 11 | 1850 | 20 | 0 | 2 | 1003841 |
| 12 | 1850 | 25 | 0 | 1 | 862547 |
| 13 | 1850 | 25 | 0 | 2 | 799482 |
| 14 | 1850 | 30 | 0 | 1 | 730638 |
| 15 | 1850 | 30 | 0 | 2 | 639636 |
| 16 | 1850 | 35 | 0 | 1 | 588487 |
| 17 | 1850 | 35 | 0 | 2 | 505012 |
| 18 | 1850 | 40 | 0 | 1 | 475911 |
| 19 | 1850 | 40 | 0 | 2 | 428185 |
| 20 | 1850 | 45 | 0 | 1 | 384211 |
| 21 | 1850 | 45 | 0 | 2 | 341254 |
| 22 | 1850 | 50 | 0 | 1 | 321343 |
| 23 | 1850 | 50 | 0 | 2 | 286580 |
| 24 | 1850 | 55 | 0 | 1 | 194080 |
| 25 | 1850 | 55 | 0 | 2 | 187208 |
| 26 | 1850 | 60 | 0 | 1 | 174976 |
| 27 | 1850 | 60 | 0 | 2 | 162236 |
| 28 | 1850 | 65 | 0 | 1 | 106827 |
| 29 | 1850 | 65 | 0 | 2 | 105534 |
| 30 | 1850 | 70 | 0 | 1 | 73677 |
| 31 | 1850 | 70 | 0 | 2 | 71762 |
| 32 | 1850 | 75 | 0 | 1 | 40834 |
| 33 | 1850 | 75 | 0 | 2 | 40229 |
| 34 | 1850 | 80 | 0 | 1 | 23449 |
| 35 | 1850 | 80 | 0 | 2 | 22949 |
| 36 | 1850 | 85 | 0 | 1 | 8186 |
| 37 | 1850 | 85 | 0 | 2 | 10511 |
| 38 | 1850 | 90 | 0 | 1 | 5259 |
| 39 | 1850 | 90 | 0 | 2 | 6569 |
| 40 | 1860 | 0 | 0 | 1 | 2120846 |
| 41 | 1860 | 0 | 0 | 2 | 2092162 |

## Census: N, O, O-Interval, O-Ratio?

People Count
Year
Age
Sex
Marital Status

Q-Ratio
O-Interval (O)
Q-Ratio (O)
N
N

## Census: Dimension or Measure?

People Count
Year
Age
Sex
Marital Status

Measure
Dimension
Depends!
Dimension
Dimension

## Census Data Demo

## Data Tables \&

## Transformations

## Relational Data Model

Represent data as a table (or relation)
Each row (or tuple) represents a record Each record is a fixed-length tuple
Each column (or field) represents a variable Each field has a name and a data type

A table's schema is the set of names and types
A database is a collection of tables (relations)

## Relational Algebra [Codd '70] / SOL

Operations on Data Tables: table(s) in, table out

## Relational Algebra [Codd '70] / SQL

Operations on Data Tables: table(s) in, table out Project (select): select a set of columns
Filter (where): remove unwanted rows
Sort (order by): order records
Aggregate (group by, sum, min, max, ...):
partition rows into groups + summarize
Combine (join, union, ...):
integrate data from multiple tables

## Relational Algebra [Codd '70] / SOL

Project (select): select a set of columns select day, stock

| day | stock | price |
| :---: | :---: | ---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 3$ | MSFT | 74.26 |
| $10 / 4$ | AMZN | 965.45 |
| $10 / 4$ | MSFT | 74.69 |


| day | stock |
| :---: | :---: |
| $10 / 3$ | AMZN |
| $10 / 3$ | MSFT |
| $10 / 4$ | AMZN |
| $10 / 4$ | MSFT |

## Relational Algebra [Codd '70] / SOL

Filter (where): remove unwanted rows select * where price > 100

| day | stock | price |
| :---: | :---: | ---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 3$ | MSFT | 74.26 |
| $10 / 4$ | AMZN | 965.45 |
| $10 / 4$ | MSFT | 74.69 |


| day | stock | price |
| :---: | :---: | :---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 4$ | AMZN | 965.45 |

## Relational Algebra [Codd '70] / SOL

Sort (order by): order records select * order by stock, day

| day | stock | price |
| :---: | :---: | ---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 3$ | MSFT | 74.26 |
| $10 / 4$ | AMZN | 965.45 |
| $10 / 4$ | MSFT | 74.69 |


| day | stock | price |
| :---: | :---: | ---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 4$ | AMZN | 965.45 |
| $10 / 3$ | MSFT | 74.26 |
| $10 / 4$ | MSFT | 74.69 |

## Relational Algebra [Codd '70] / SOL

Aggregate (group by, sum, min, max, ...): select stock, min(price) group by stock

| day | stock | price |
| :---: | :---: | ---: |
| $10 / 3$ | AMZN | 957.10 |
| $10 / 3$ | MSFT | 74.26 |
| $10 / 4$ | AMZN | 965.45 |
| $10 / 4$ | MSFT | 74.69 |


| stock | $\min$ (price) |
| :---: | ---: |
| AMZN | 957.10 |
| MSFT | 74.26 |

## Roll-Up and Drill-Down

Want to examine population by year and age?
Roll-up the data along the desired dimensions


SELECT year, age, sum(people)
FROM census
GROUP BY year, age,
Dimensions

## Roll-Up and Drill-Down

Want to see the breakdown by marital status?
Drill-down into additional dimensions

SELECT year, age, marst, sum(people)
FROM census
GROUP BY year, age, marst

All Marital Status


All Marital Status


ORIGINAL

| YEAR | AGE | MARST | SEX | PEOPLE |
| :--- | :--- | :--- | :--- | :--- |
| 1850 | 0 | 0 | 1 | $1,483,789$ |
| 1850 | 5 | 0 | 1 | $1,411,067$ |
| 1860 | 0 | 0 | 1 | $2,120,846$ |
| 1860 | 5 | 0 | 1 | $1,804,467$ |
| $\ldots$ |  |  |  |  |

## PIVOTED (or CROSS-TABULATION)

AGE MARST
SEX 1850
1860
$\begin{array}{lllll}0 & 0 & 1 & 1,483,789 & 2,120,846 \ldots\end{array}$
$\begin{array}{lllll}5 & 0 & 1 & 1,411,067 & 1,804,467 \ldots\end{array}$

Which format might we prefer? Why?

## Tidy Data [Wickham 2014]

How do rows, columns, and tables match up with observations, variables, and types? In "tidy" data:

1. Each variable forms a column.
2. Each observation forms a row.
3. Each type of observational unit forms a table.

The advantage is that this provides a flexible starting point for analysis, transformation, and visualization.

Our pivoted table variant was not "tidy"!
(This is a variant of normalized forms in DB theory)

## Common Data Formats

## CSV: Comma-Separated Values

year,age, marst, sex, people
1850,0,0,1,1483789
1850,5,0,1,1411067

## Common Data Formats

CSV: Comma-Separated Values
year, age, marst, sex, people
1850,0,0,1,1483789
1850,5,0,1,1411067

## JSON: JavaScript Object Notation

[

$$
\begin{aligned}
& \text { \{"year":1850, "age":0, "marst":0, "sex":1, "people":1483789\}, } \\
& \text { \{"year":1850, "age":5, "marst":0, "sex":1, "people":1411067\}, }
\end{aligned}
$$

]

Administrivia

## A1: Visualization Design

Design a static visualization for a data set.
The climate of a place can have a tremendous impact on people's lived experience. You will examine average monthly climate measurements for six major U.S. cities, roughly covering the edges of the continental United States.

You must choose the message you want to convey. What question(s) do you want to answer? What insight do you want to communicate?

## A1: Visualization Design

Pick a guiding question, use it to title your vis.
Design a static visualization for that question.
You are free to use any tools (inc. pen \& paper).
Deliverables (upload to Gradescope; see A1 page) Image of your visualization (PNG or JPG format)
Short description + design rationale ( $\leq 4$ paragraphs)
Due by 11:59 pm, Friday January 12.

## Tableau Tutorial

Friday Jan. 12, 4:00-5:30pm on Zoom
Introduction to Tableau, a graphical visualization tool you may use for A1 or A2.

Led by Yilun.
Zoom link is available on Canvas.
The tutorial will be recorded.

## Course Participation

## Quizzes start this week! Due by Friday, 11:59pm.

## Image Models



## Visual Language is a Sign System



Jacques Bertin
Images perceived as a set of signs
Sender encodes information in signs
Receiver decodes information from signs

Sémiologie Graphique, 1967

## Bertin's Semiology of Graphics


"Resemblance, order and proportional are the three signfields in graphics." - Bertin


## Visual Encoding Variables

Position (x 2)
Size
Value
Texture
Color
Orientation
Shape


## Visual Encoding Variables

Position (x 2)
Size
Value
Texture
Color
Orientation
Shape

Others?


## Visual Encoding Variables

Position
Length
Area
Volume
Value
Texture
Color
Orientation
Shape
Transparency
Blur / Focus ...


## Information in Hue and Value

Value is perceived as ordered
$\therefore$ Encode ordinal variables (O)

$\therefore$ Encode continuous variables (Q) [not as well]


Hue is normally perceived as unordered
$\therefore$ Encode nominal variables ( N ) using color

$$
\square \square \square \square \square \square \square \square \square \square
$$

## Bertin's Levels of Organization

Position

Size

Value

Texture

Color

Orientation

Shape


Ordinal
Quantitative
Note: $\mathbf{O} \subset \mathbf{O} \subset \mathbf{N}$
Nominal

Deconstructions

Exports and Imports to and from DENMARK \& NORWAY from 1700 to 1780.


## William Playfair, 1786

Exports and Imports to and from DENMARK \& NORWAY from 1700 to 1780.


X-axis: year (Q)
Y-axis: currency (Q)
Color: imports/exports (N, O)

http://www.smartmoney.com/marketmap/

## Wattenberg's Map of the Market



Rectangle Area: market cap (Q)
Rectangle Position: market sector (N), market cap (Q)
Color Hue: loss vs. gain (N, O)
Color Value: magnitude of loss or gain (Q)

## Minard 1869: Napoleon's March






## Single-Axis Composition



## Mark Composition

Y-axis: temperature (Q)

Y X-axis: longitude (Q) / time (O)


Temp over space/time ( $\mathrm{O} \times \mathrm{Q}$ )

## Mark Composition

Y-axis: latitude (Q)

- X-axis: longitude (Q)

ـ Width: army size (Q)


Army position $(\mathrm{O} \times \mathrm{Q})$ and army size ( Q )


## Minard 1869: Napoleon's March



Depicts at least 5 quantitative variables. Any others?

## Formalizing Design

## Choosing Visual Encodings

Assume $k$ visual encodings and $n$ data attributes. We would like to pick the "best" encoding among a combinatorial set of possibilities of size $(n+1)^{k}$

## Principle of Consistency

The properties of the image (visual variables) should match the properties of the data.

Principle of Importance Ordering
Encode the most important information in the most effective way.

## Design Criteria [Mackinlay 86]

## Expressiveness

Effectiveness

## Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is expressible in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

Effectiveness

## Can not express the facts

A multivariate relation may be inexpressive in a single horizontal dot plot because multiple records are mapped to the same position.

|  | - | 000000000000000000000000000000000000000000000000000000000000000000 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | I |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 0 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 | 80 |
|  |  | Value |  |  |  |  |  |  |  |  |  |  |  |  |  |  |



## Expresses facts not in the data



A length is interpreted as a quantitative value.

## Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is expressible in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

Effectiveness

## Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is expressible in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

A visualization is more effective than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

## Design Criteria Translated

Tell the truth and nothing but the truth (don't lie, and don't lie by omission)

Use encodings that people decode better (where better $\approx$ faster and/or more accurate)

## Mackinlay's Ranking

Quantitative

Conjectured effectiveness of encodings by data type

## Mackinlay's Design Algorithm

APT - "A Presentation Tool", 1986
User formally specifies data model and type Input: ordered list of data variables to show

APT searches over design space Test expressiveness of each visual encoding Generate encodings that pass test Rank by perceptual effectiveness criteria

Output the "most effective" visualization

## APT

## Automatically generate chart for car data

## Input variables:

1. Price
2. Mileage
3. Repair
4. Weight

## Limitations of APT?

## Limitations of APT

Does not cover many visualization techniques
Networks, hierarchies, maps, diagrams
Also: 3D structure, animation, illustration, ...
Does not consider interaction
Does not consider semantics / conventions
Assumes single visualization as output
Still an active area of research, e.g., the
Draco visualization design knowledge base

## Summary: Data \& Image Models

Formal specification
Data model: relational data; N,O,O types Image model: visual encoding channels Encodings map data to visual variables

Choose expressive and effective encodings Rule-based tests of expressiveness Perceptual effectiveness rankings

Question: how do we establish effectiveness criteria? Subject of perception lectures...

