

CSE 442 - Data Visualization

Visual Encoding Design



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A Design Space of Visual Encodings

Mapping Data to Visual Variables

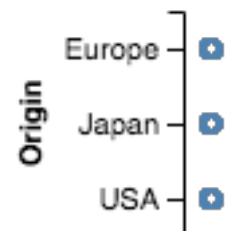
Assign **data fields** (e.g., with N , O , Q types) to **visual channels** (x , y , $color$, $shape$, $size$, ...) for a chosen **graphical mark** type ($point$, bar , $line$, ...).

Additional concerns include choosing appropriate **encoding parameters** ($log\ scale$, $sorting$, ...) and **data transformations** (bin , $group$, $aggregate$, ...).

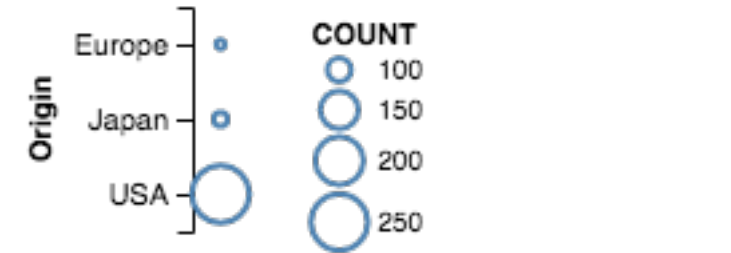
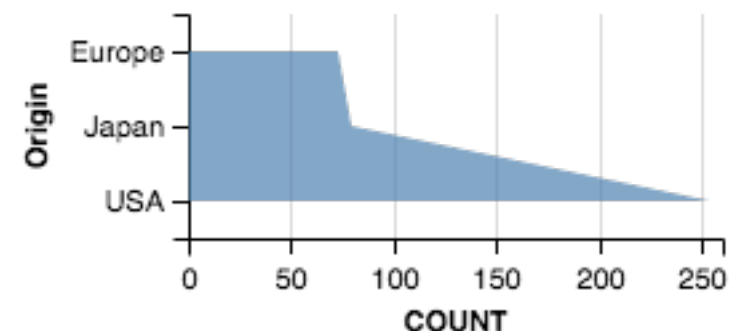
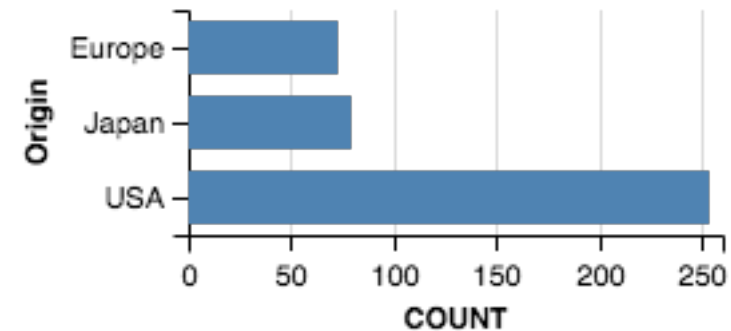
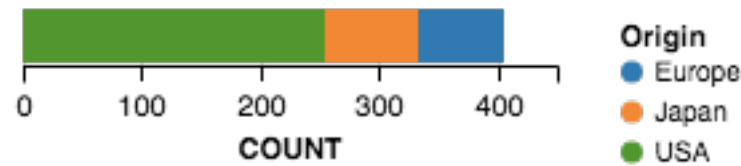
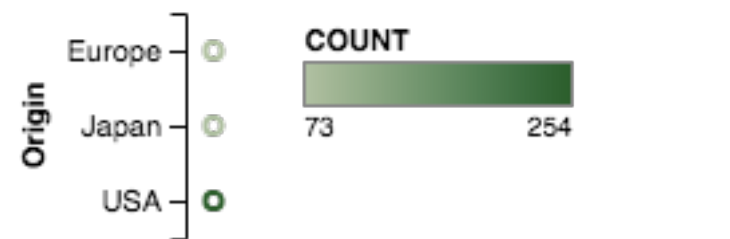
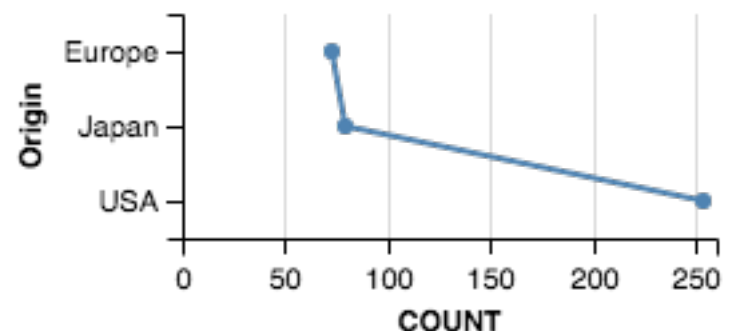
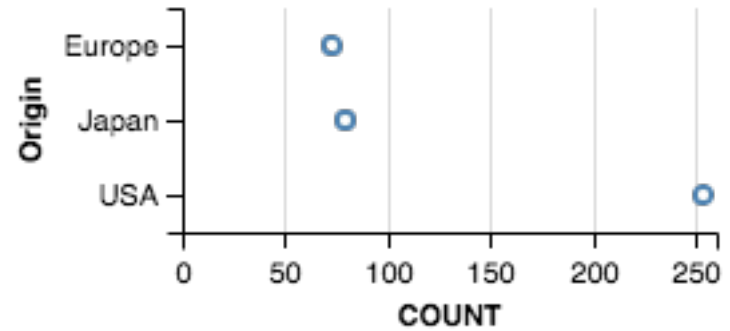
These options define a large combinatorial space, containing both useful and questionable charts!

1D: Nominal

Raw

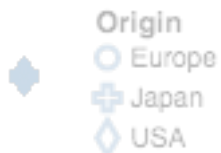
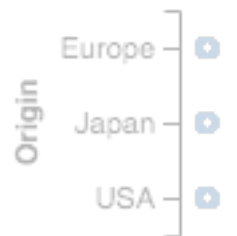


Aggregate (Count)

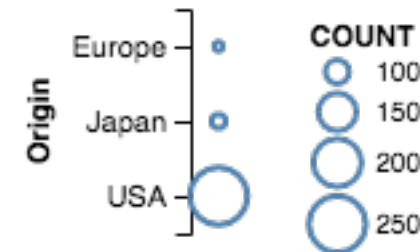
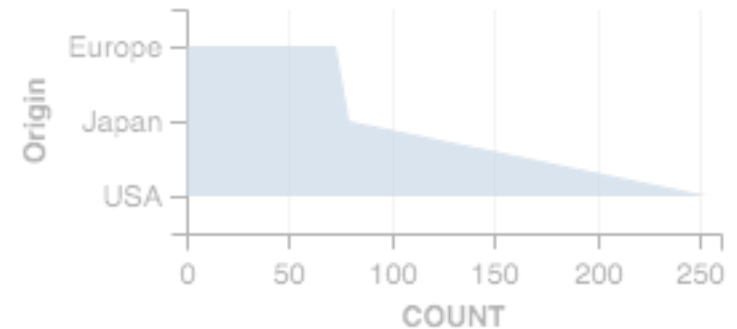
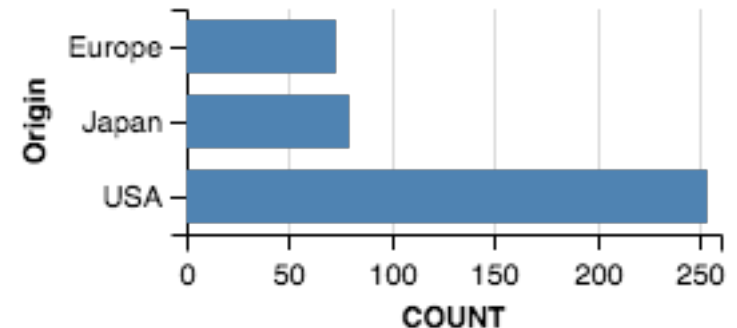
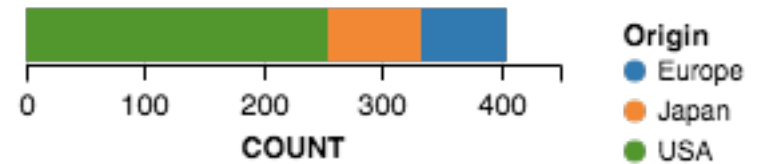
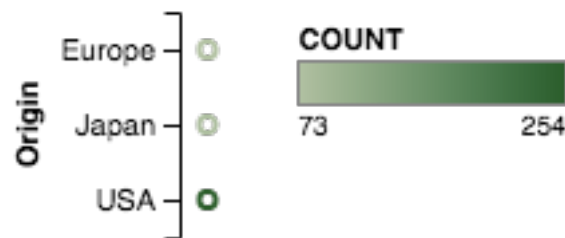
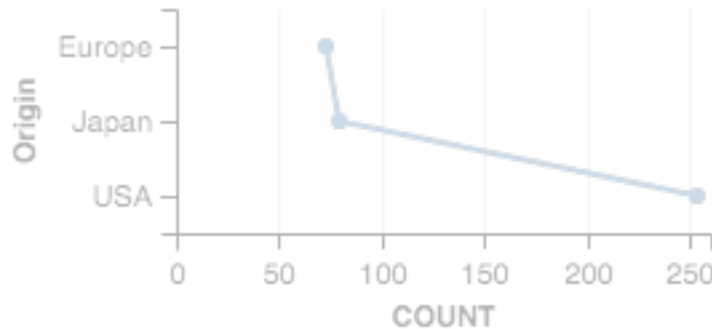
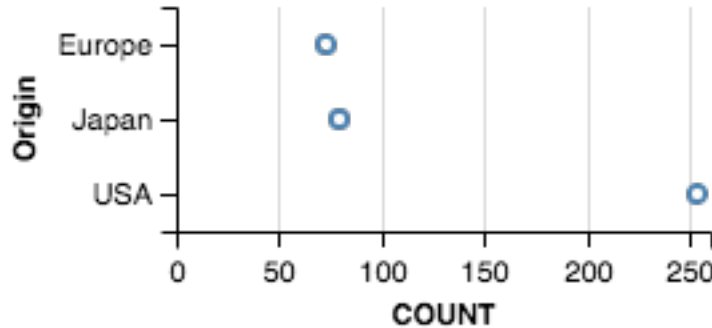


Expressive?

Raw

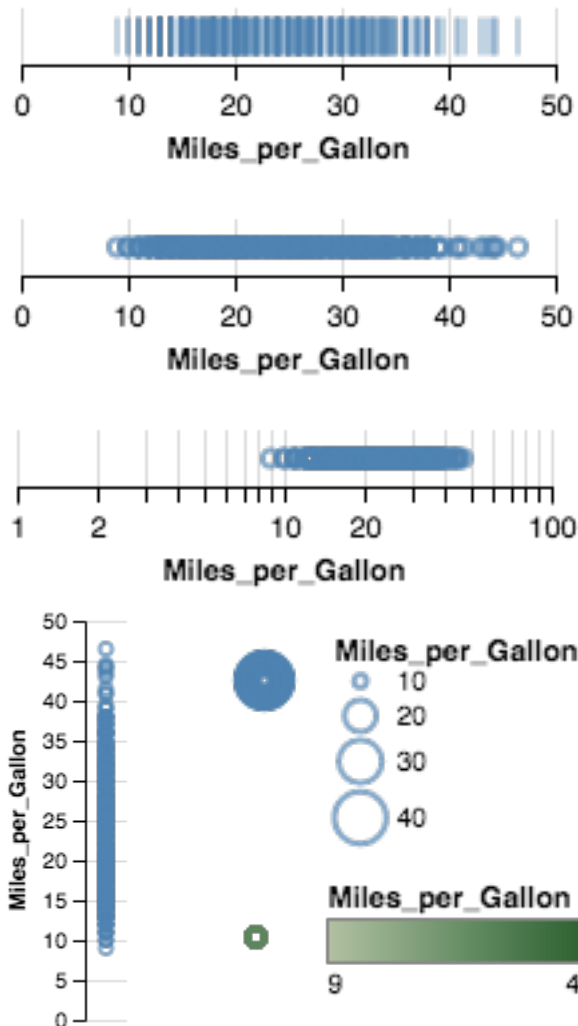


Aggregate (Count)

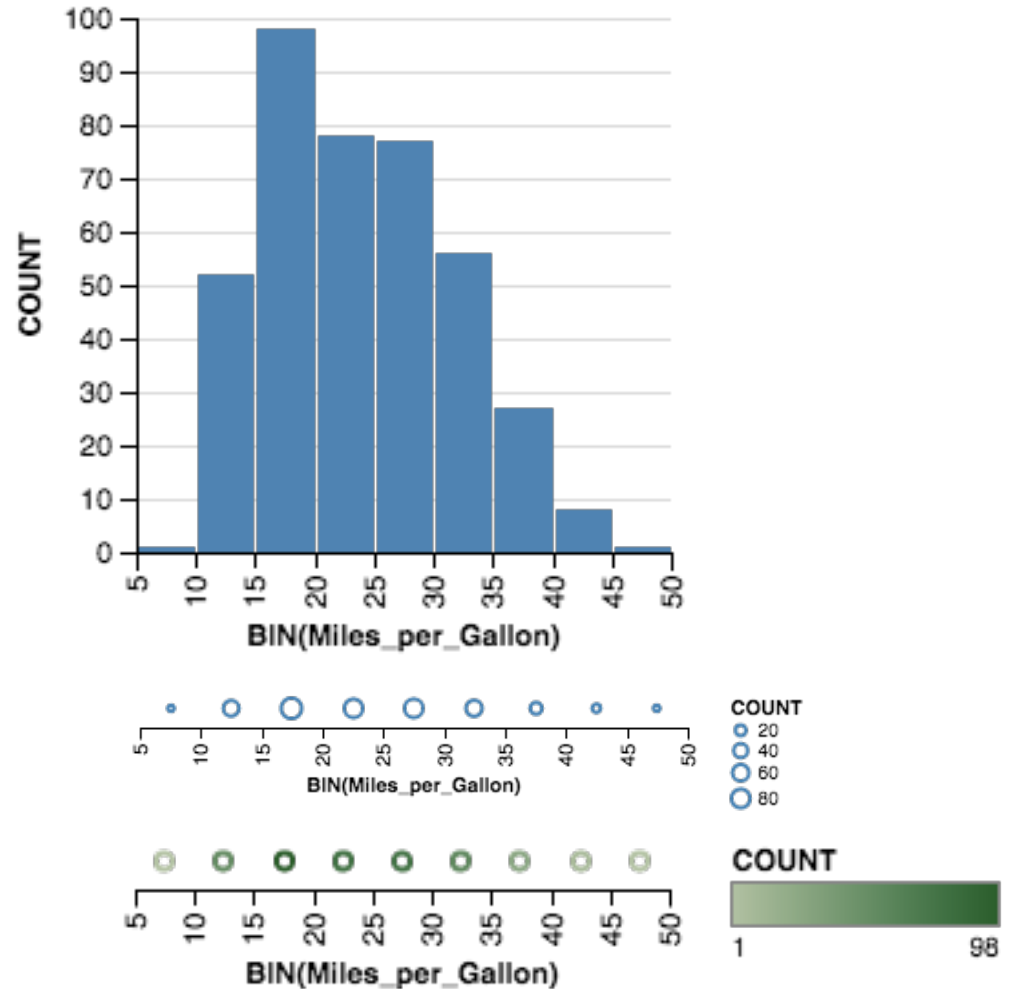


1D: Quantitative

Raw

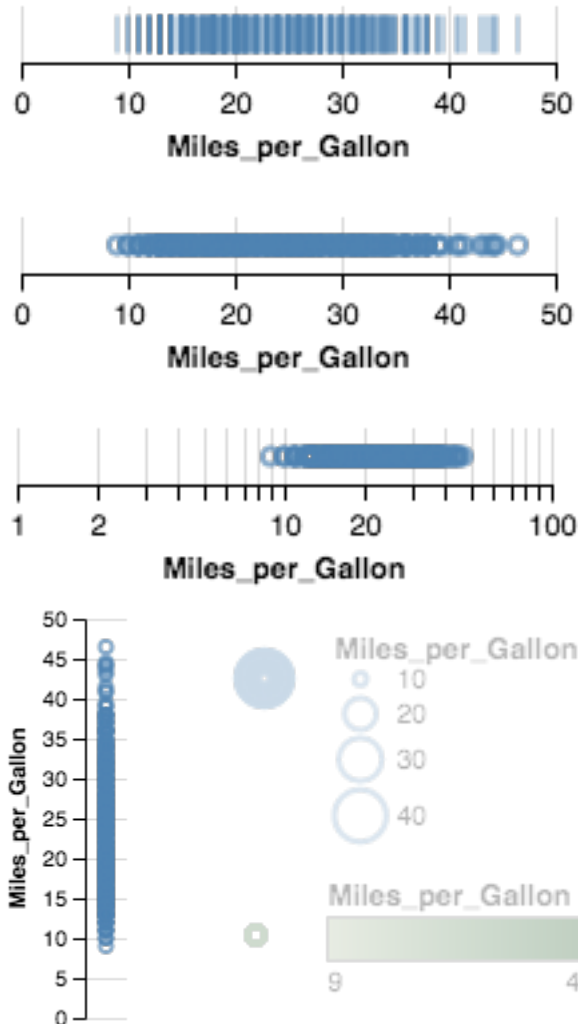


Aggregate (Count)

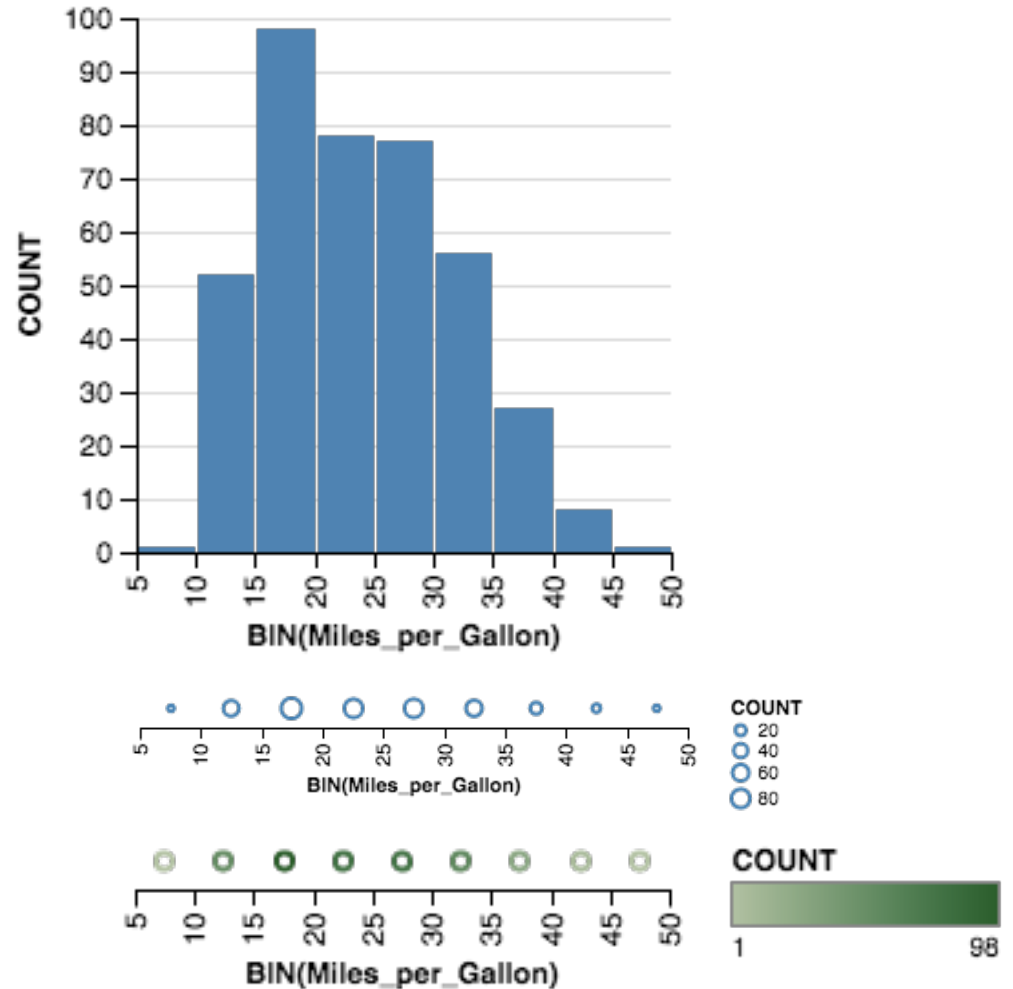


Expressive?

Raw

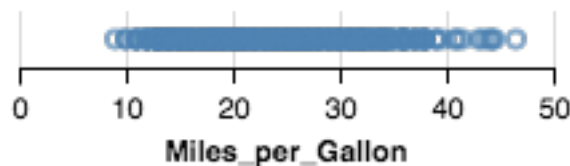
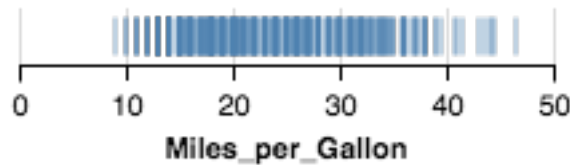


Aggregate (Count)

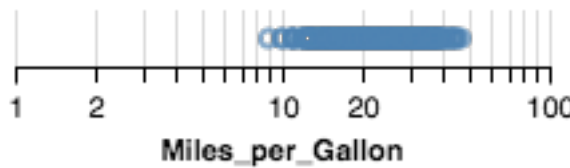


Effective?

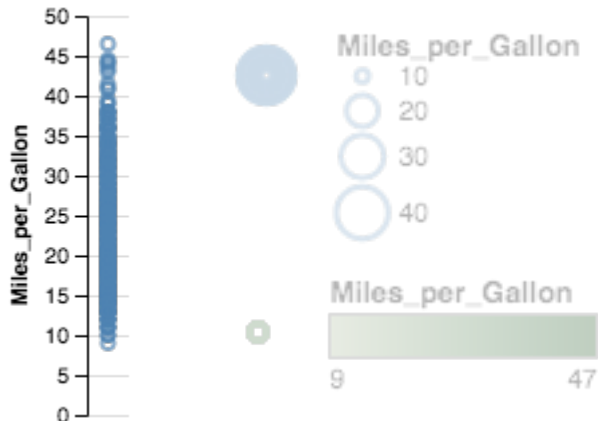
Raw



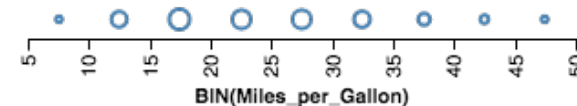
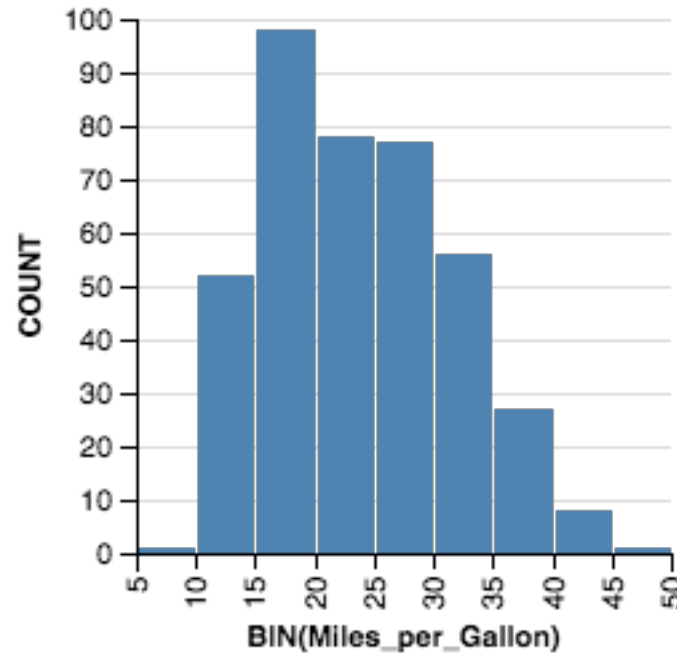
?



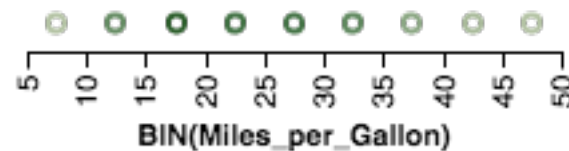
?



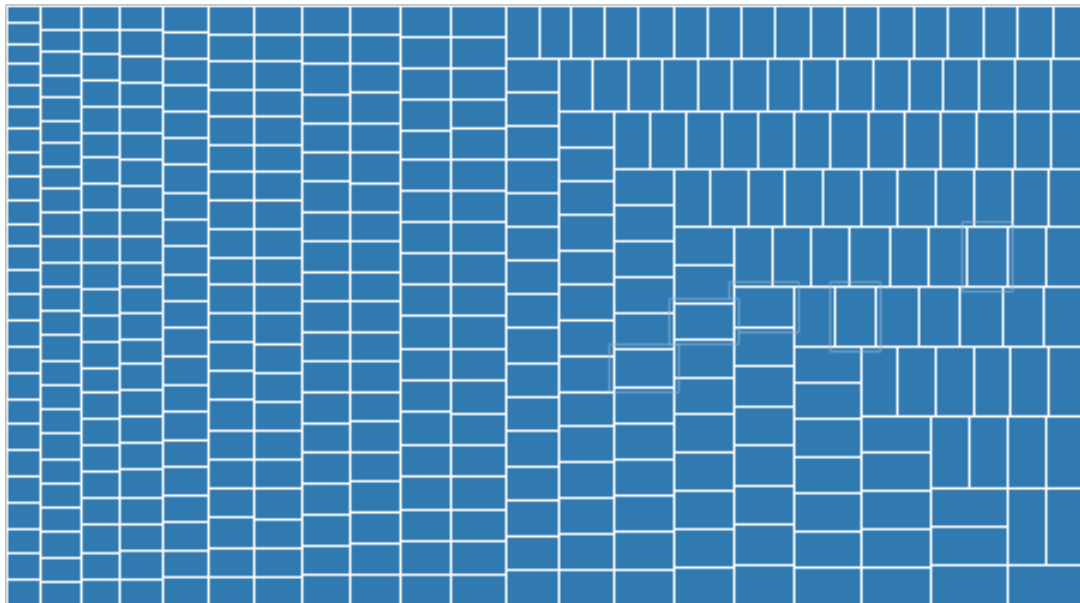
Aggregate (Count)



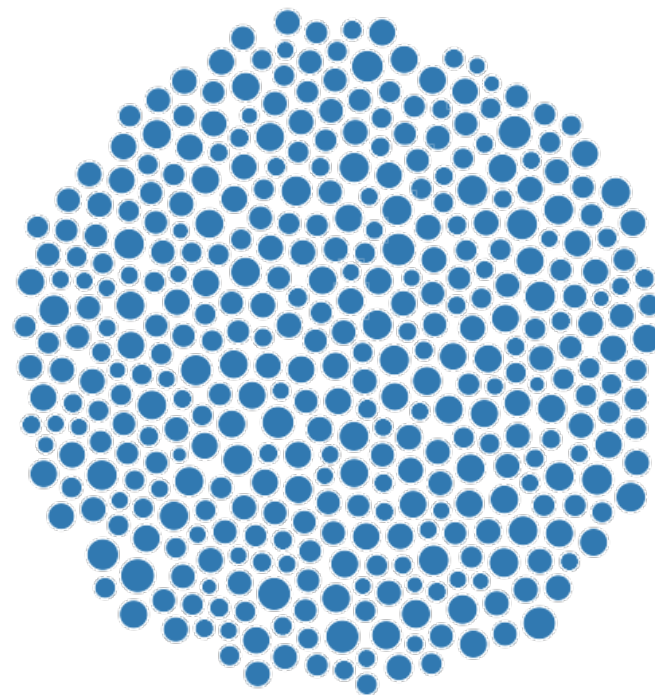
!?



Raw (with Layout Algorithm)

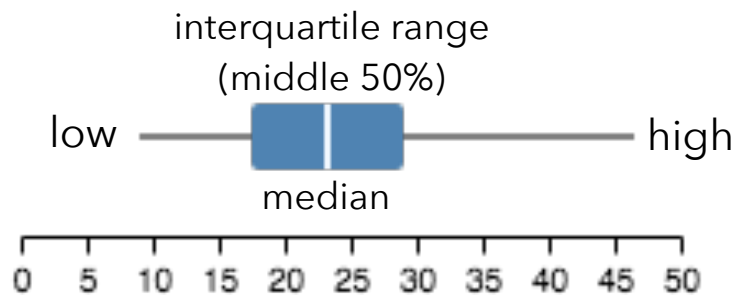


Treemap

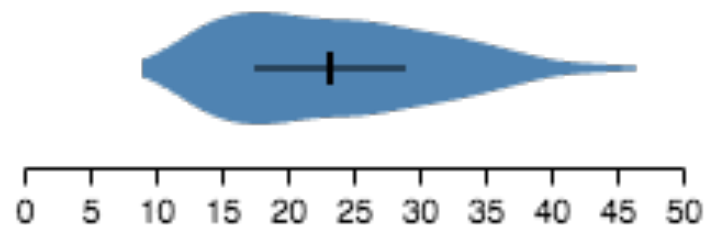


Bubble Chart

Aggregate (Distributions)



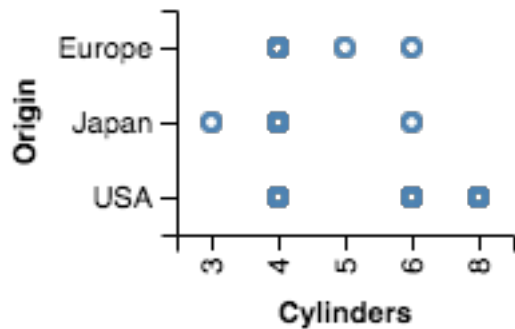
Box Plot



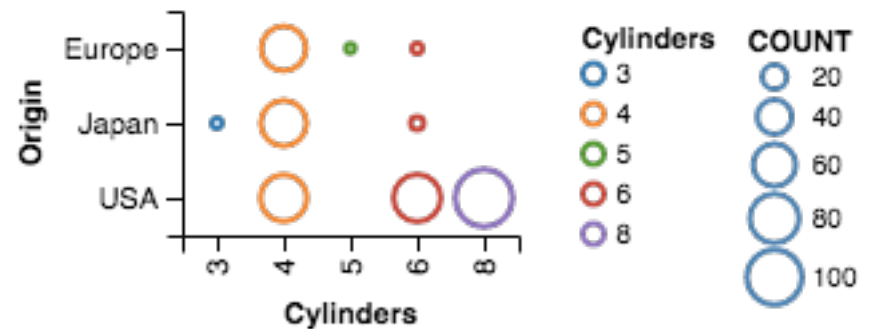
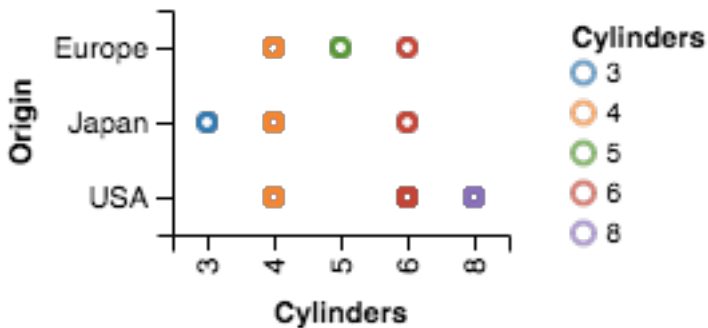
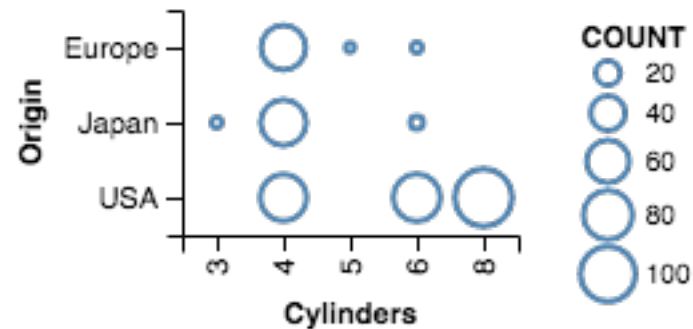
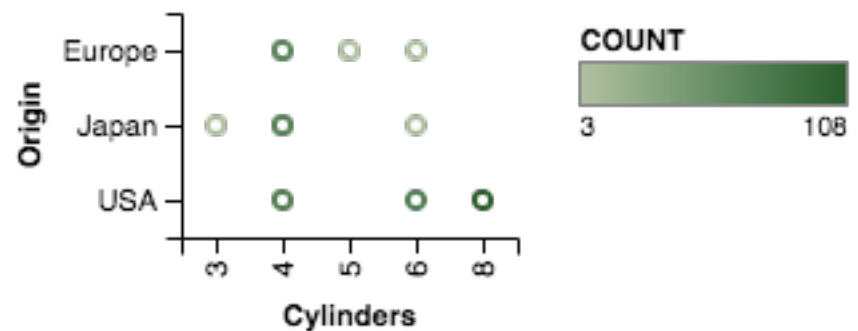
Violin Plot

2D: Nominal x Nominal

Raw

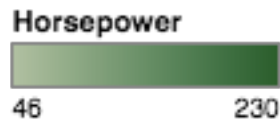
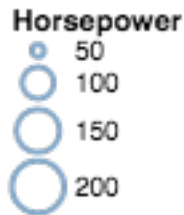
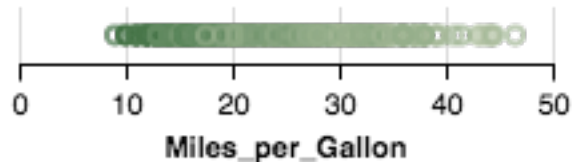
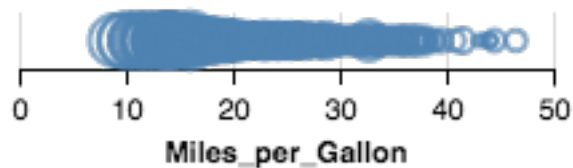
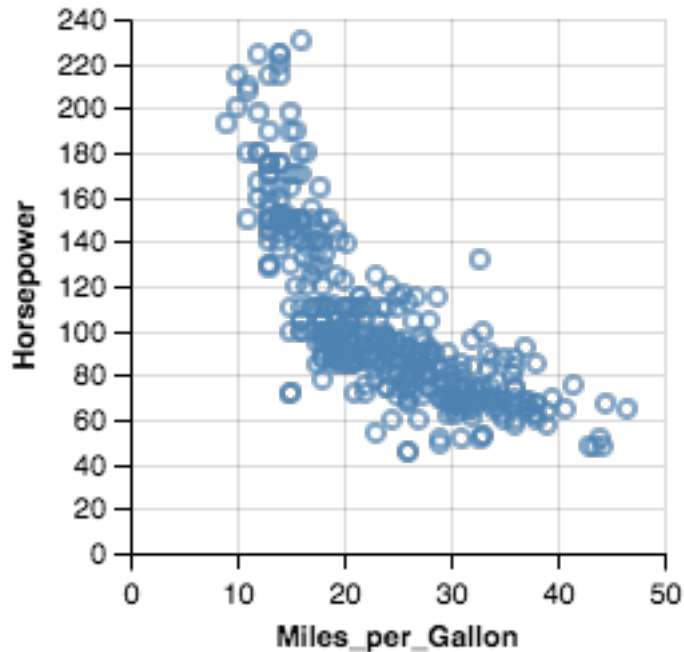


Aggregate (Count)

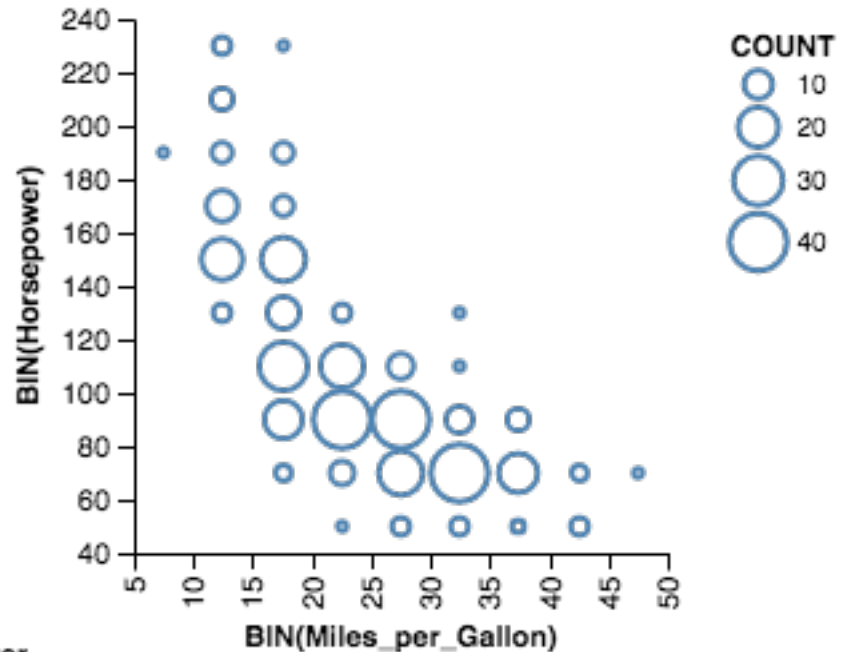


2D: Quantitative x Quantitative

Raw

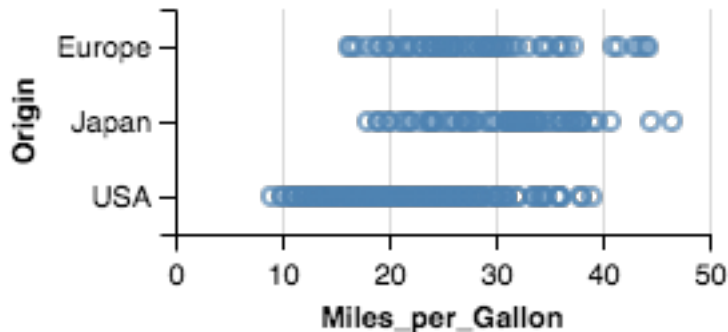


Aggregate (Count)

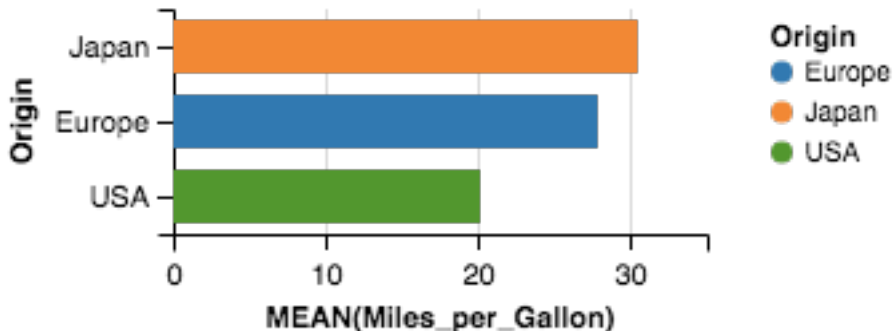
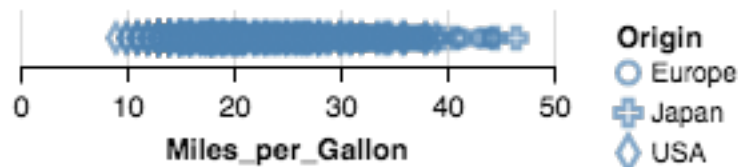
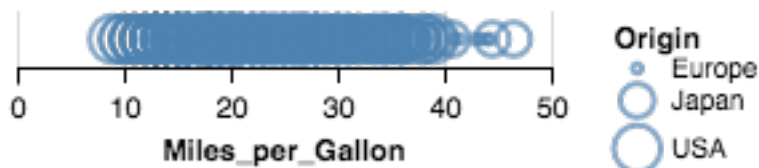
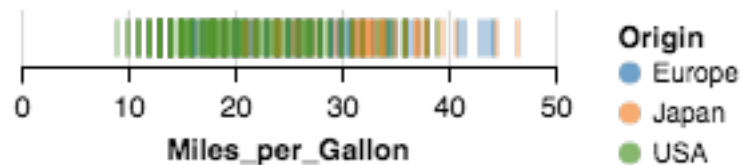
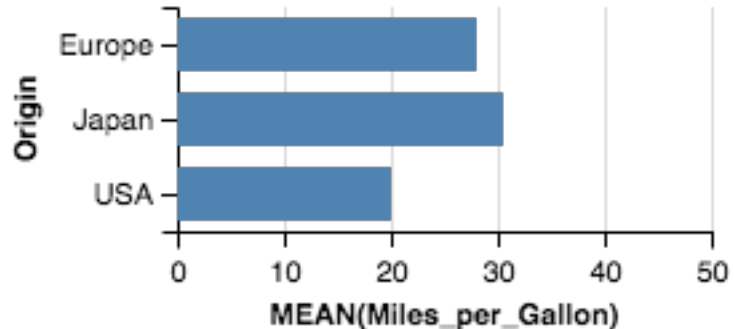


2D: Nominal x Quantitative

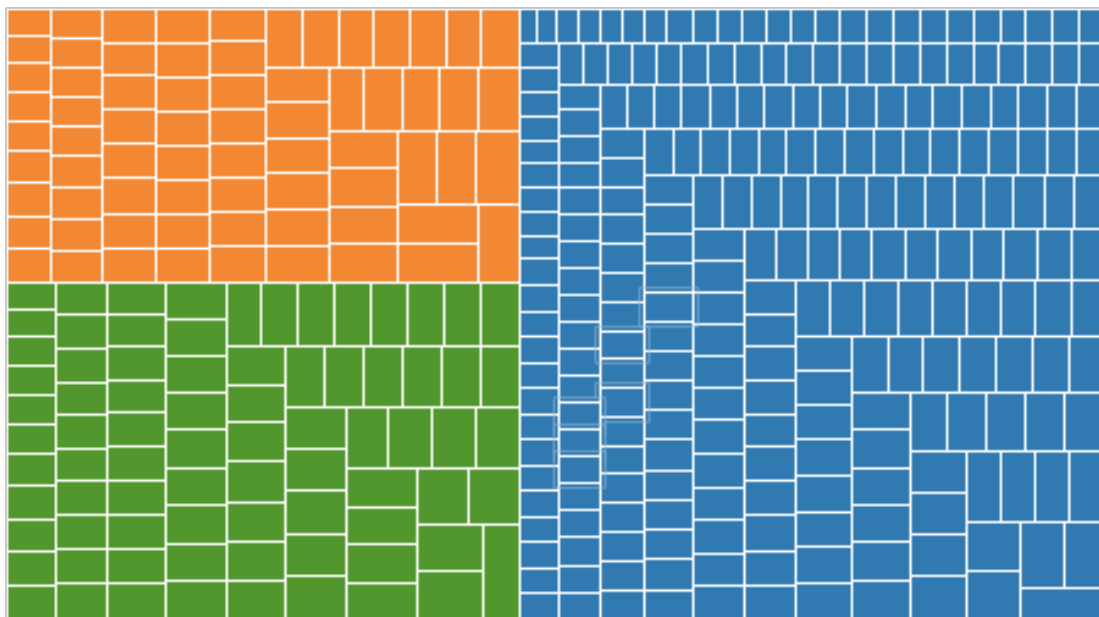
Raw



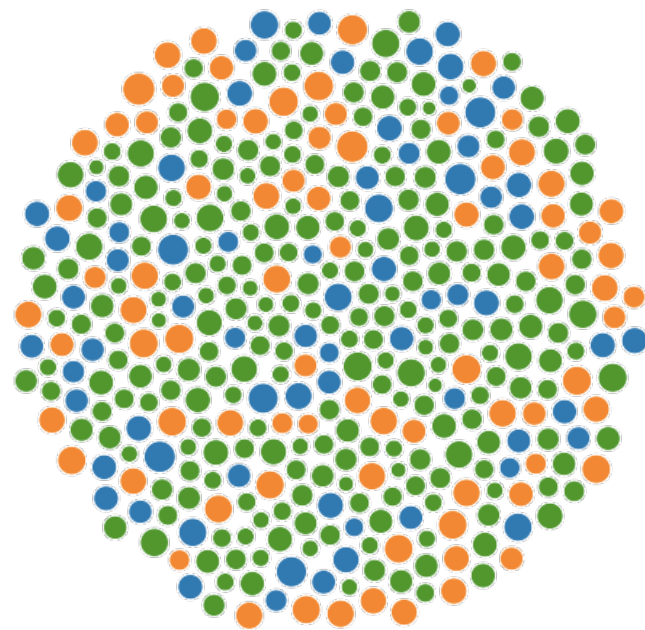
Aggregate (Mean)



Raw (with Layout Algorithm)

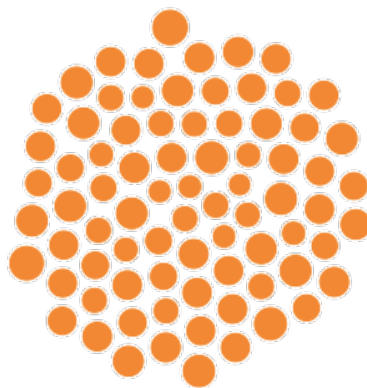
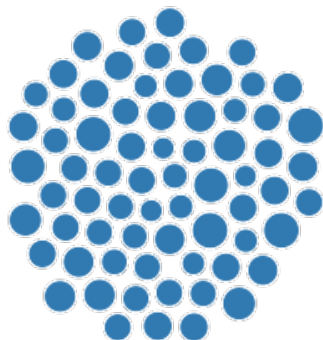


Treemap

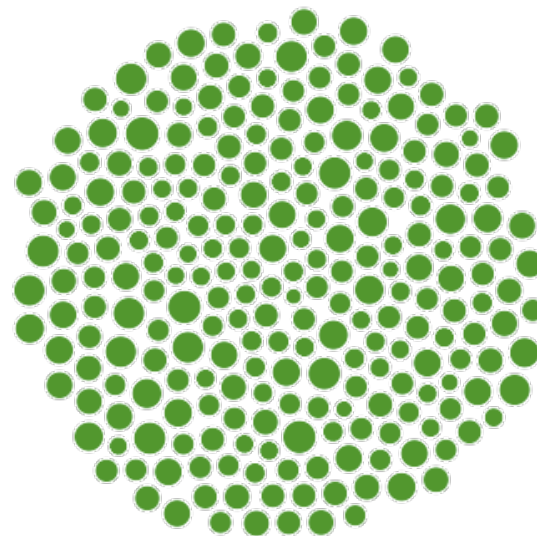


Bubble Chart

Origin
● Europe
● Japan
● USA



Beeswarm Plot



3D and Higher

Two variables [x,y]

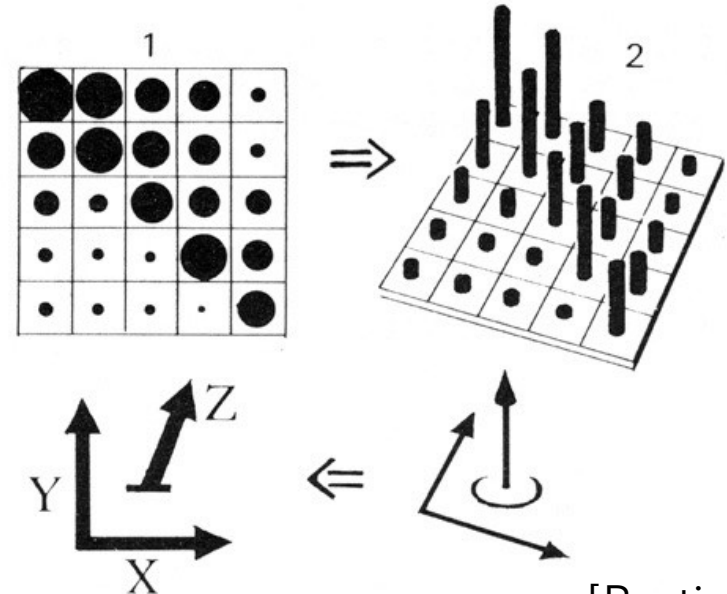
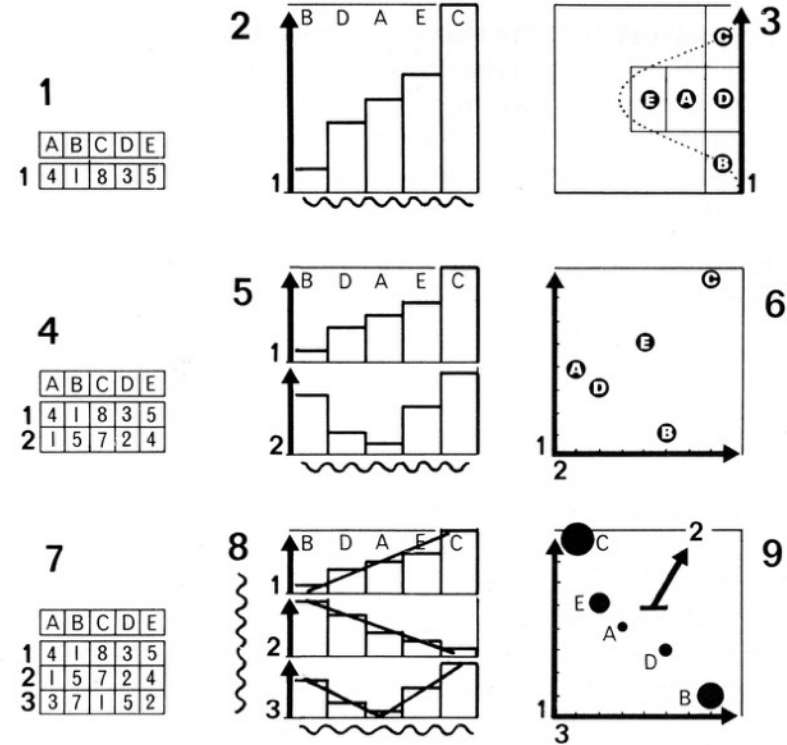
Can map to 2D points.

Scatterplots, maps, ...

Third variable [z]

Often use one of size, color, opacity, shape, etc. Or, one can further partition space.

What about 3D rendering?



Other Visual Encoding Channels?

wind map

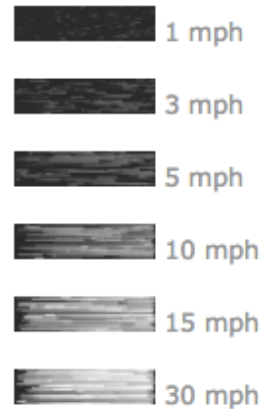
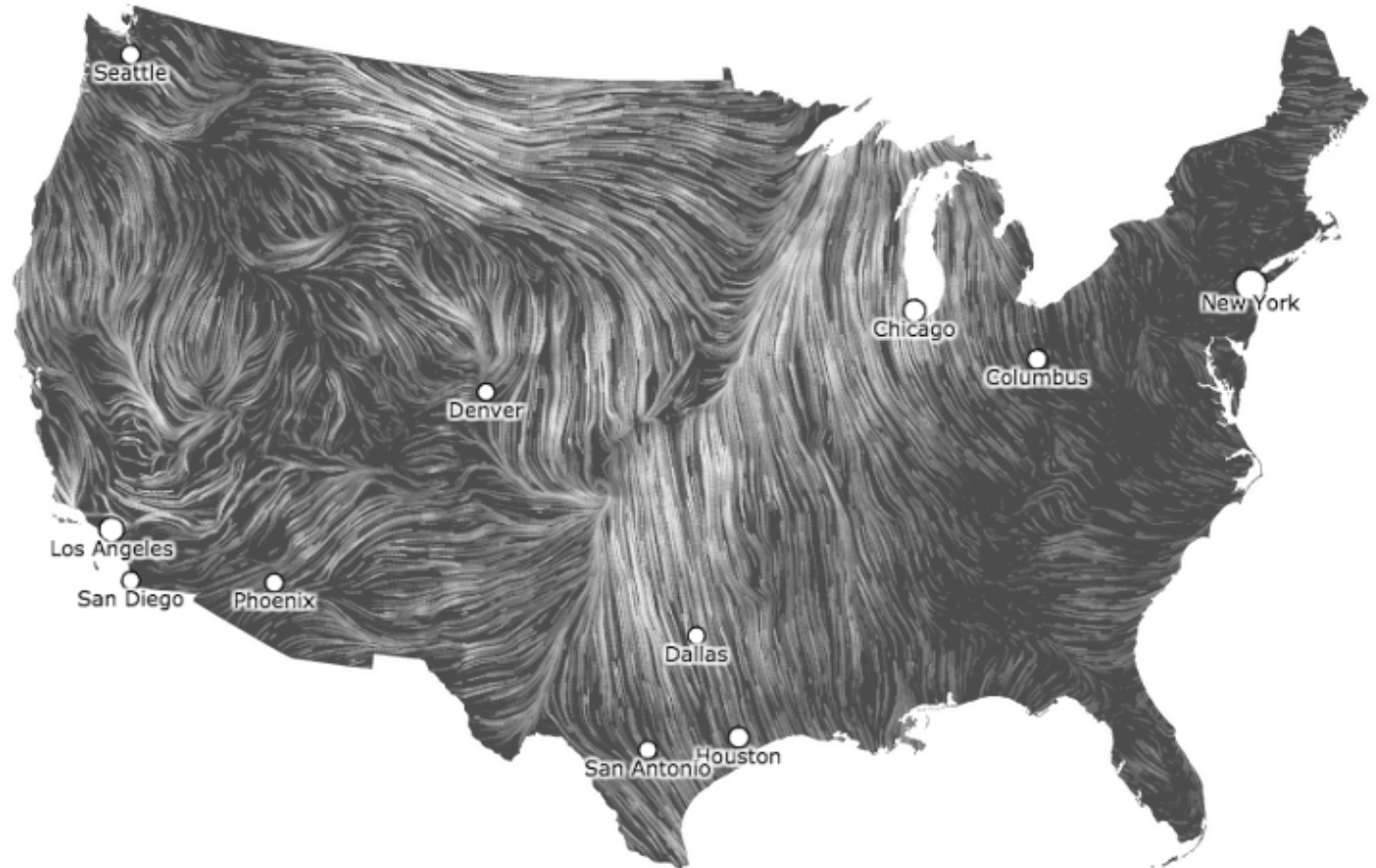
April 1, 2015

11:35 pm EST

(time of forecast download)

top speed: **30.5 mph**

average: **10.2 mph**



Encoding Effectiveness

Effectiveness Rankings [Mackinlay 86]

QUANTITATIVE

Position
Length
Angle
Slope
Area (Size)
Volume
Density (Value)
Color Sat
Color Hue
Texture
Connection
Containment
Shape

ORDINAL

Position
Density (Value)
Color Sat
Color Hue
Texture
Connection
Containment
Length
Angle
Slope
Area (Size)
Volume
Shape

NOMINAL

Position
Color Hue
Texture
Connection
Containment
Density (Value)
Color Sat
Shape
Length
Angle
Slope
Area
Volume

Effectiveness Rankings [Mackinlay 86]

QUANTITATIVE

Position

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NOMINAL

Position

Color Hue
Texture
Connection
Containment
Density (Value)
Color Sat
Shape
Length
Angle
Slope
Area
Volume

Effectiveness Rankings [Mackinlay 86]

QUANTITATIVE

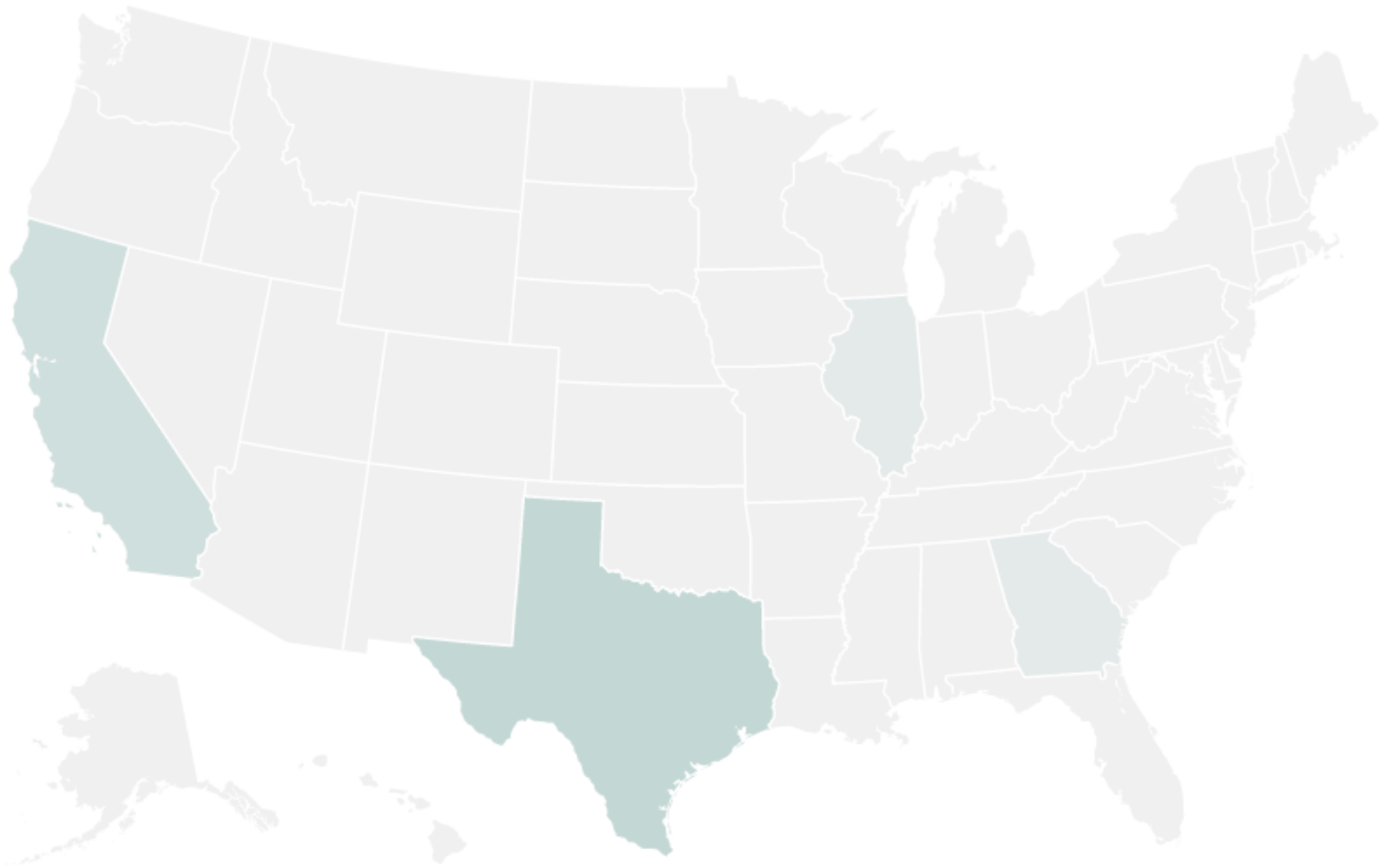
Position
Length
Angle
Slope
Area (Size)
Volume
Density (Value)
Color Sat
Color Hue
Texture
Connection
Containment
Shape

ORDINAL

Position
Density (Value)
Color Sat
Color Hue
Texture
Connection
Containment
Length
Angle
Slope
Area (Size)
Volume
Shape

NOMINAL

Position
Color Hue
Texture
Connection
Containment
Density (Value)
Color Sat
Shape
Length
Angle
Slope
Area
Volume



Color Encoding (Choropleth Map)

Effectiveness Rankings

QUANTITATIVE

Position

Length

Angle

Slope

Area (Size)

Volume

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Shape

ORDINAL

Position

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Length

Angle

Slope

Area (Size)

Volume

Shape

NOMINAL

Position

Color Hue

Texture

Connection

Containment

Density (Value)

Color Sat

Shape

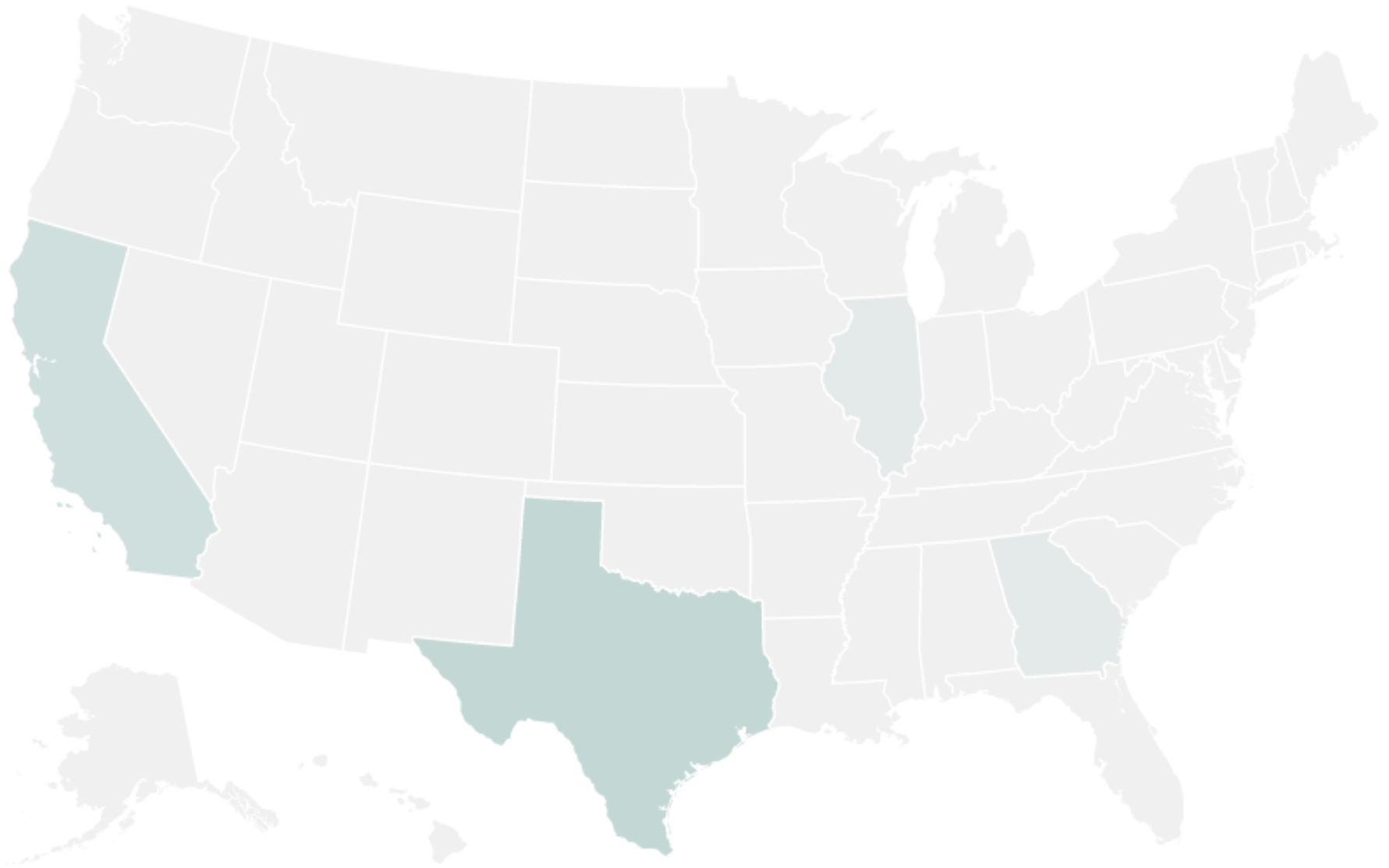
Length

Angle

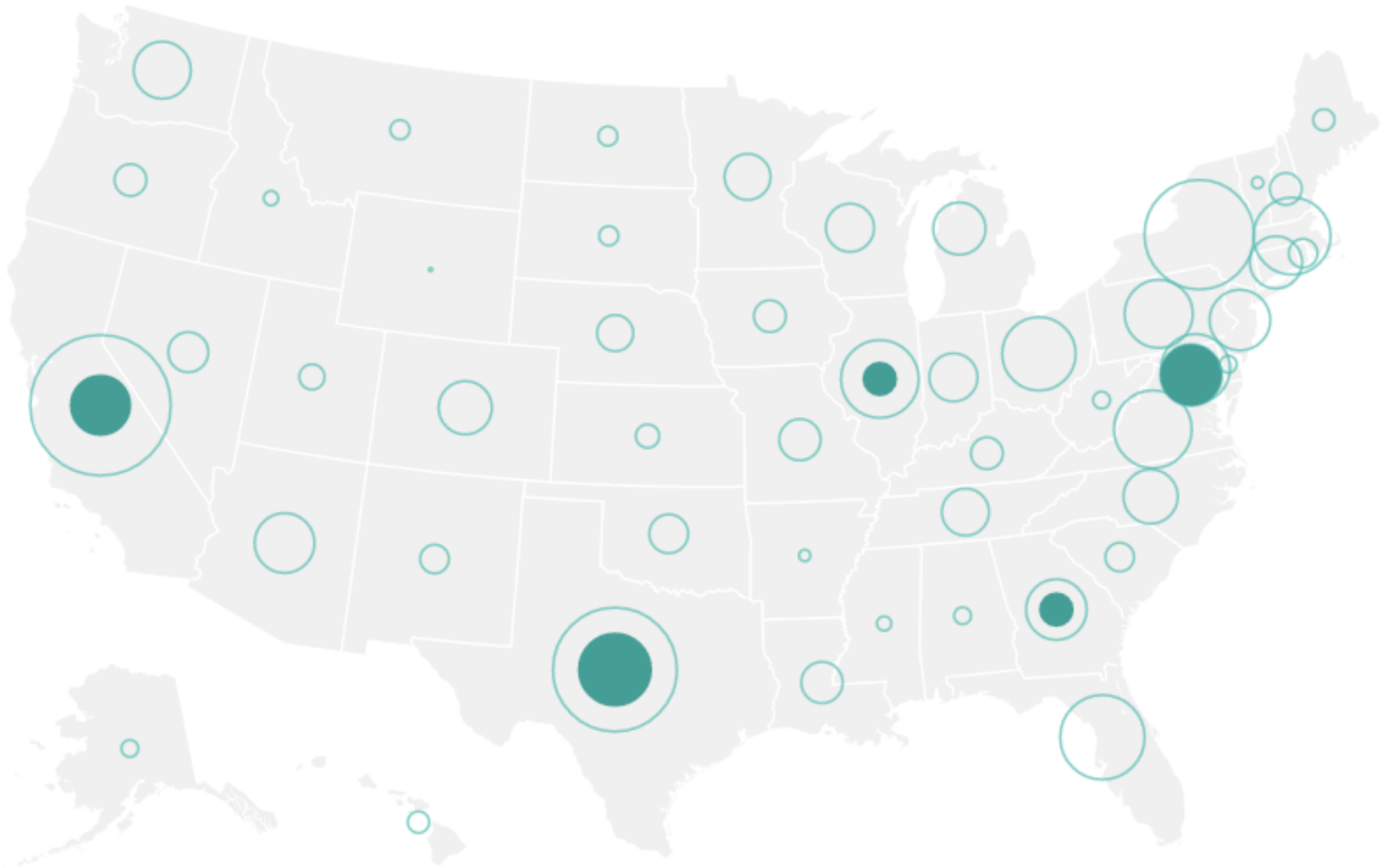
Slope

Area

Volume



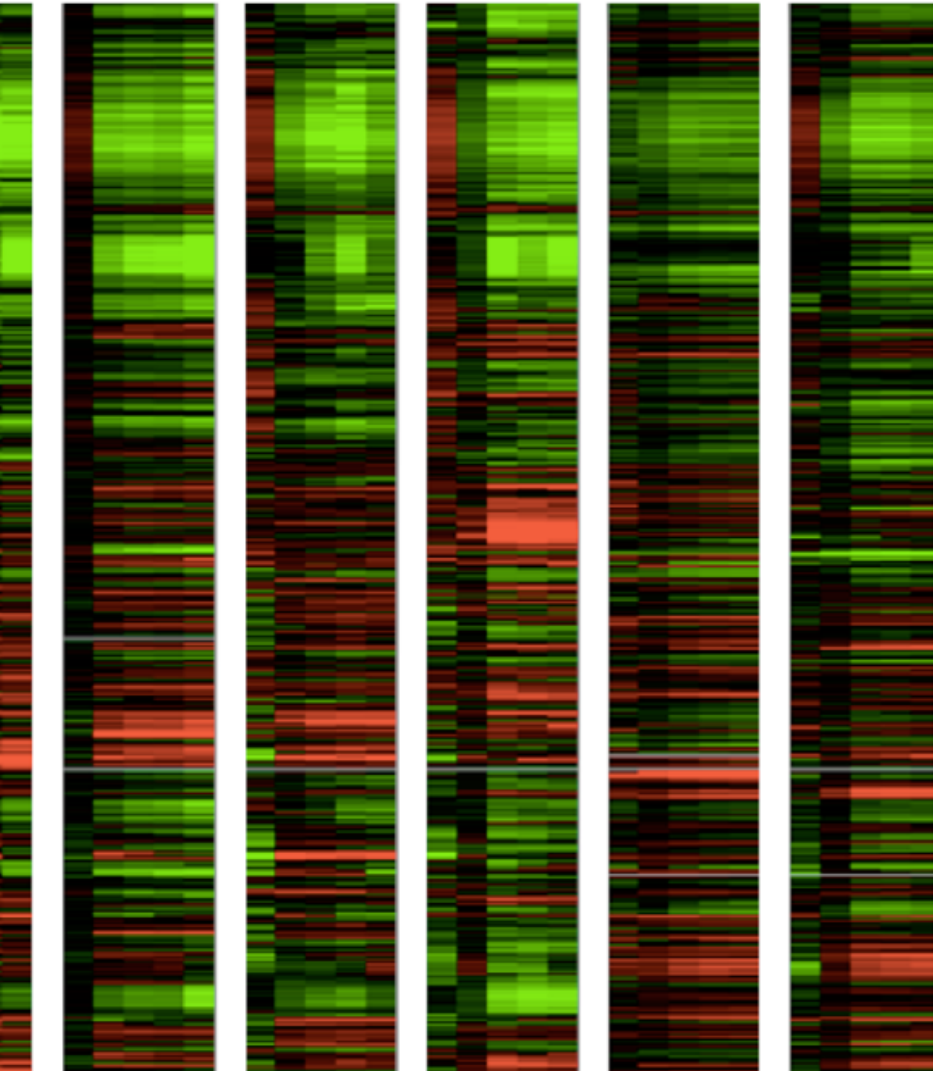
Color Encoding (Choropleth Map)



Area Encoding (Symbol Map)

Gene Expression Time-Series [Meyer et al '11]

Color Encoding



Effectiveness Rankings

QUANTITATIVE

Position

Length

Angle

Slope

Area (Size)

Volume

~~Density (Value)~~

Color Sat

~~Color Hue~~

Texture

Connection

Containment

Shape

ORDINAL

Position

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Length

Angle

Slope

Area (Size)

Volume

Shape

NOMINAL

Position

Color Hue

Texture

Connection

Containment

Density (Value)

Color Sat

Shape

Length

Angle

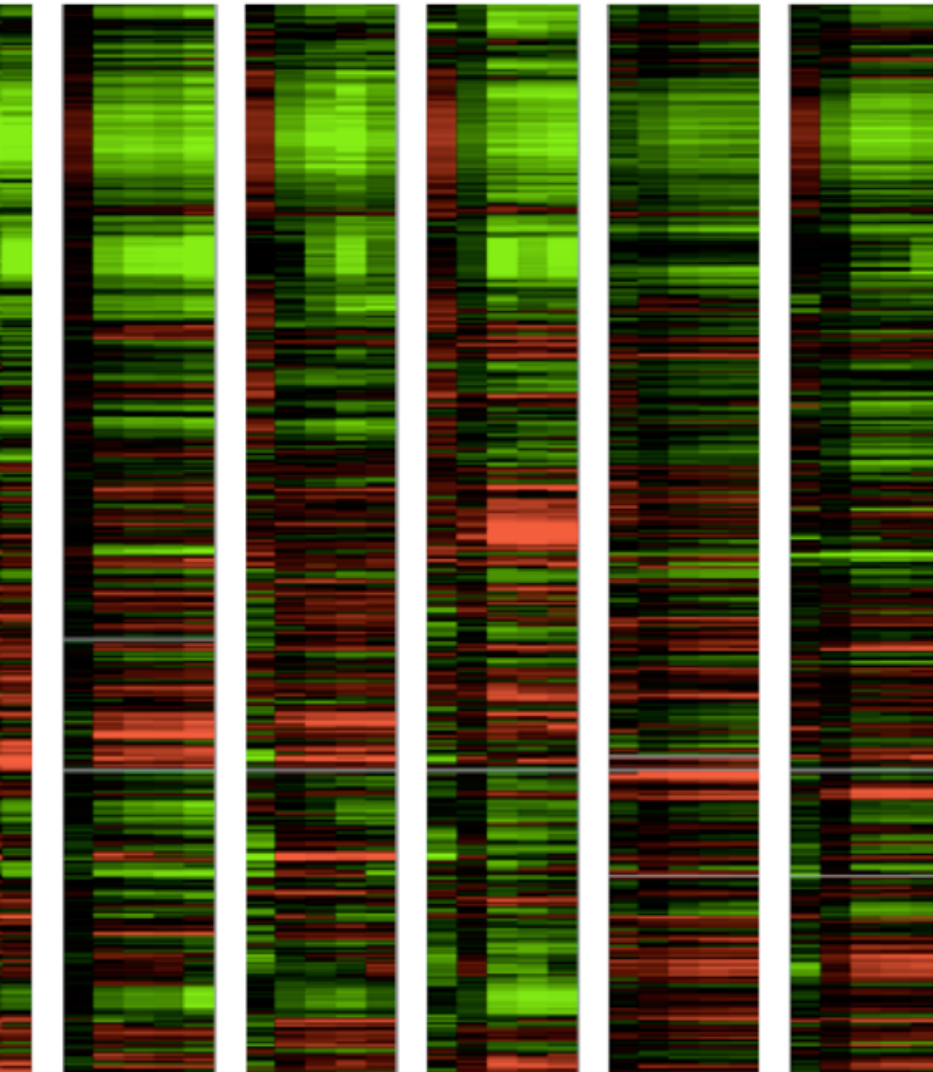
Slope

Area

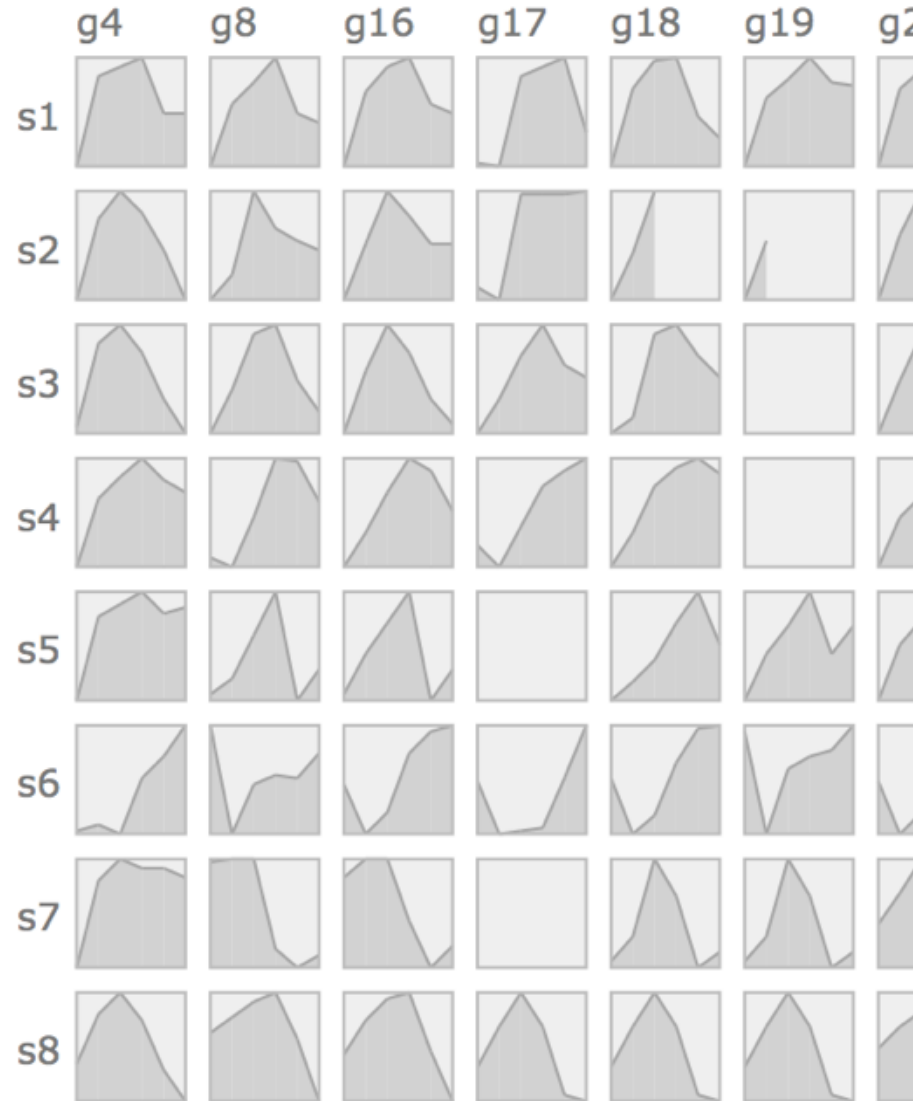
Volume

Gene Expression Time-Series [Meyer et al '11]

Color Encoding



Position Encoding

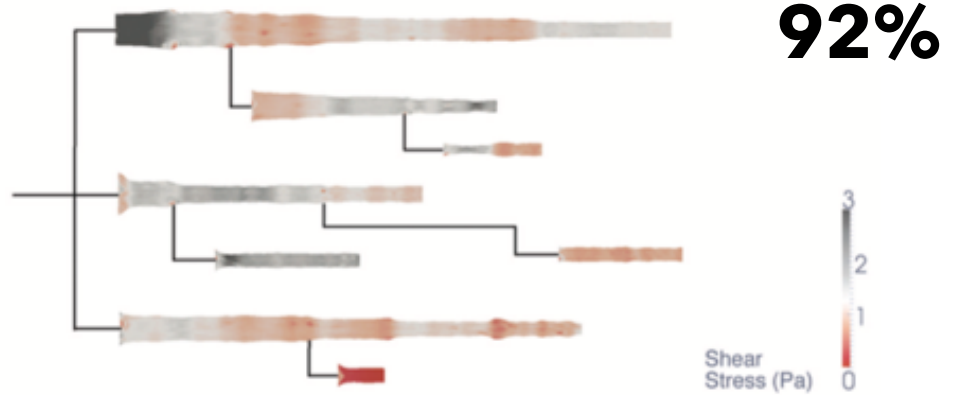


Artery Visualization [Borkin et al '11]

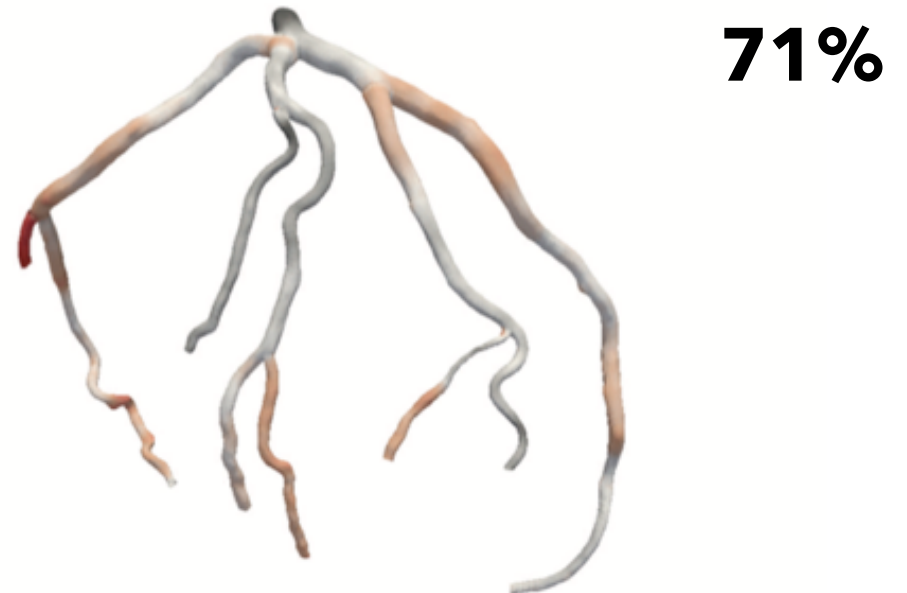
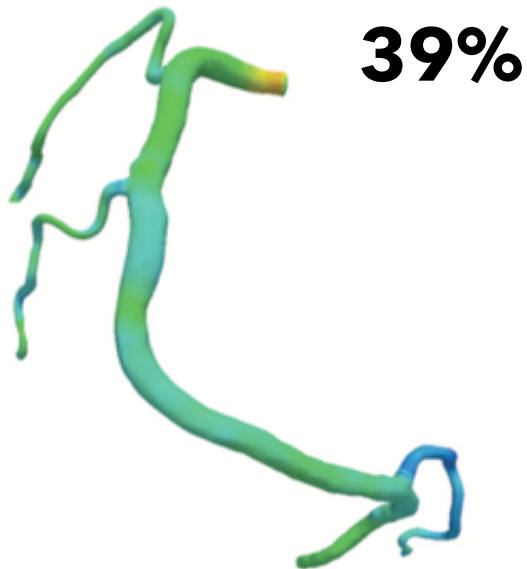
Rainbow Palette

Diverging Palette

2D



3D



Effectiveness Rankings

QUANTITATIVE

Position ↻

Length

Angle

Slope

Area (Size)

Volume

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Shape

ORDINAL

Position

Density (Value)

Color Sat

Color Hue

Texture

Connection

Containment

Length

Angle

Slope

Area (Size)

Volume

Shape

NOMINAL

Position

Color Hue

Texture

Connection

Containment

Density (Value)

Color Sat

Shape

Length

Angle

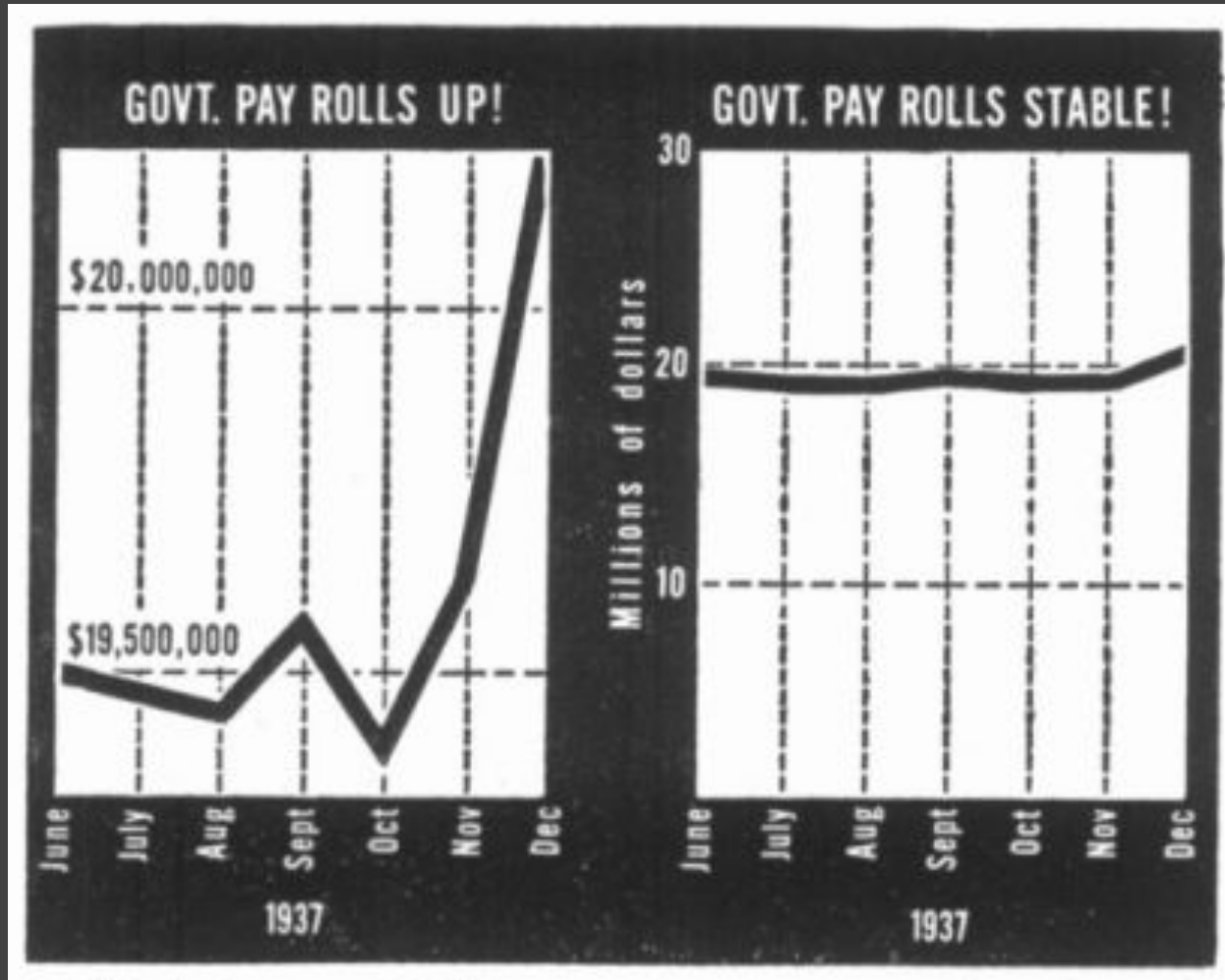
Slope

Area

Volume

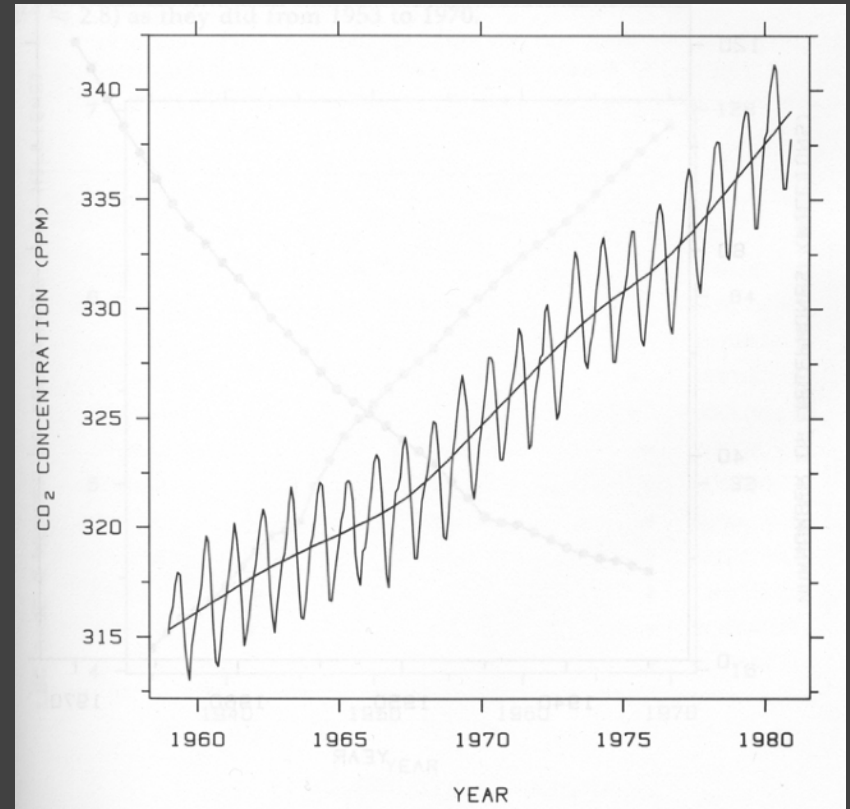
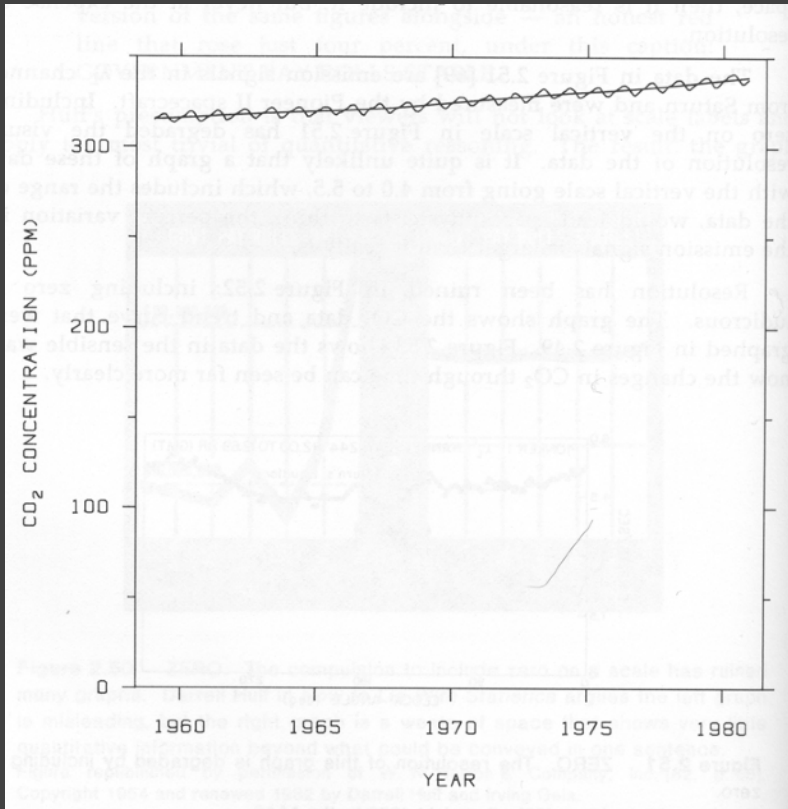
Scales & Axes

Include Zero in Axis Scale?



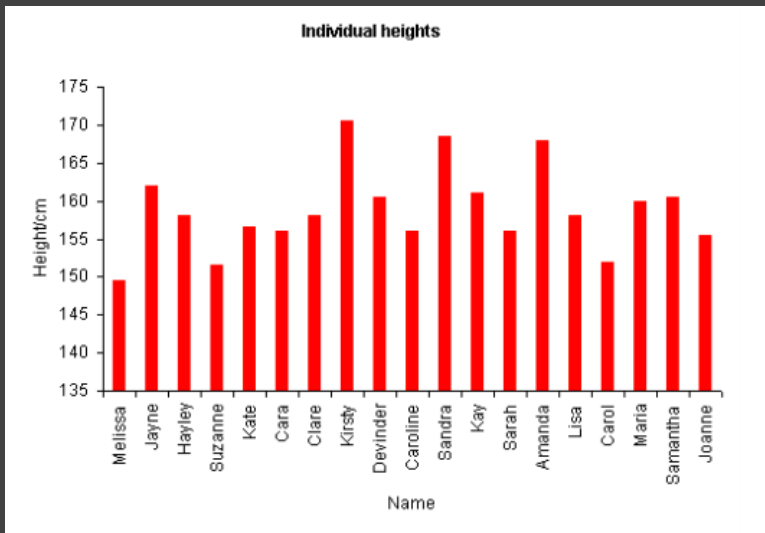
Government payrolls in 1937 [How To Lie With Statistics. Huff]

Include Zero in Axis Scale?



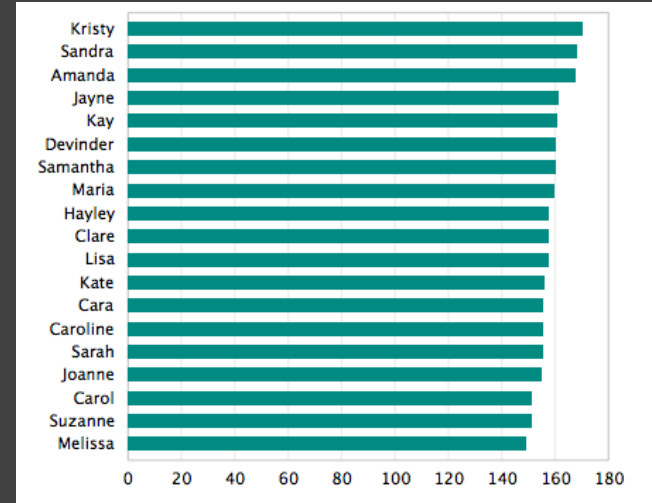
Yearly CO₂ concentrations [Cleveland 85]

Include Zero in Axis Scale?

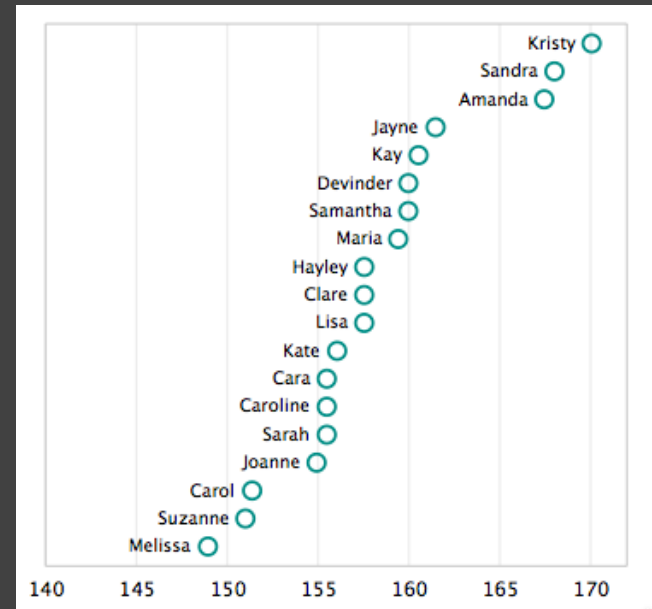


Violates Expressiveness Principle!

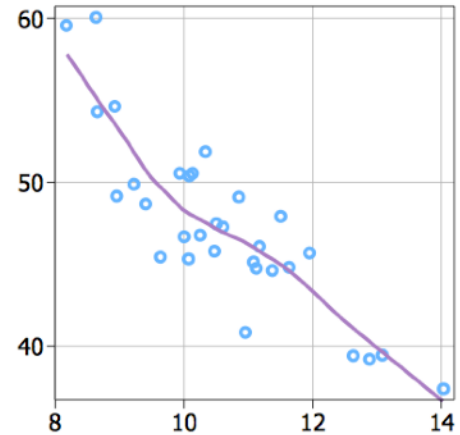
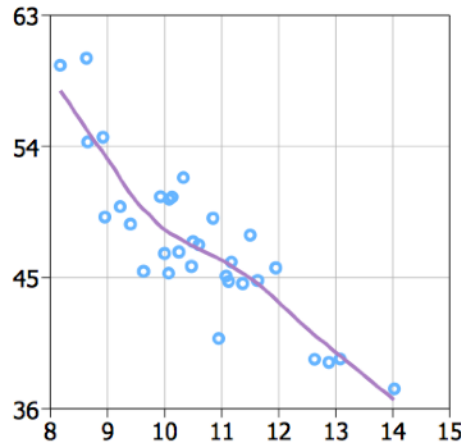
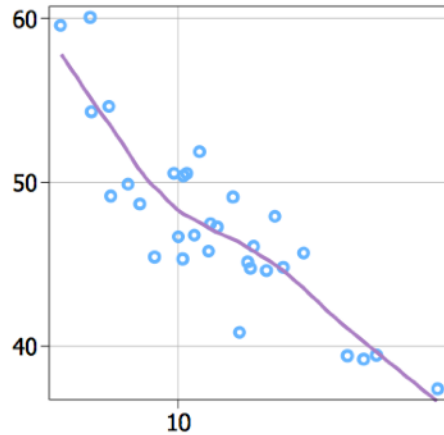
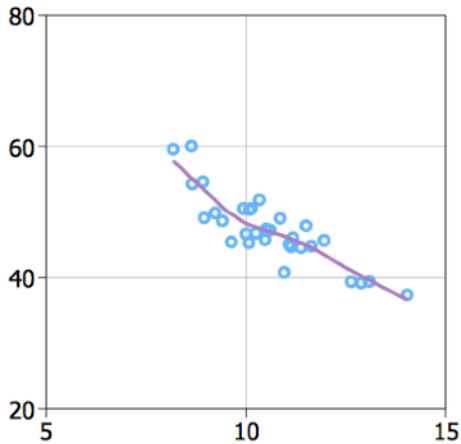
Compare Proportions (Q-Ratio)



Compare Relative Position (Q-Interval)

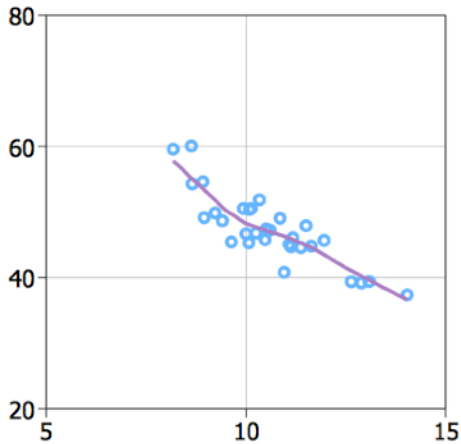


Axis Tick Mark Selection

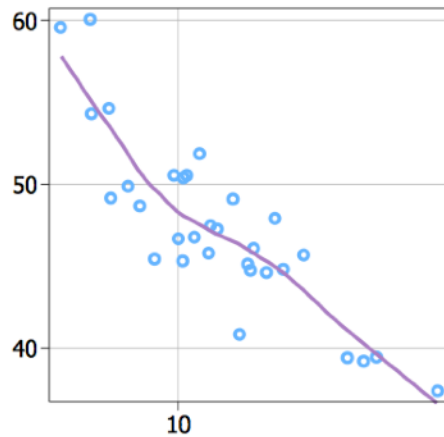


What are some properties of "good" tick marks?

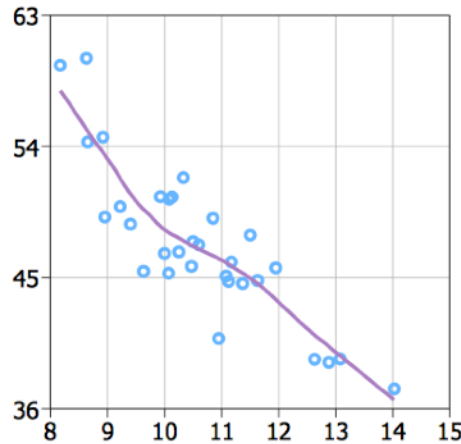
Axis Tick Mark Selection



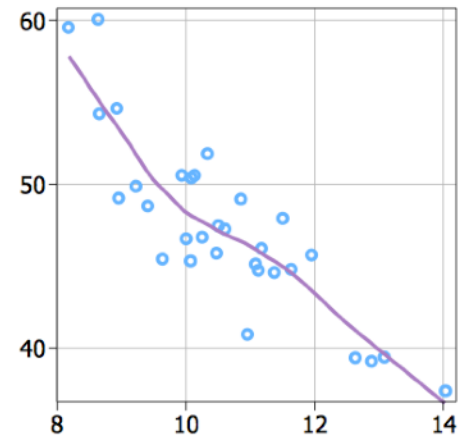
(a) Heckbert



(b) R's pretty



(c) Wilkinson



(d) Extended

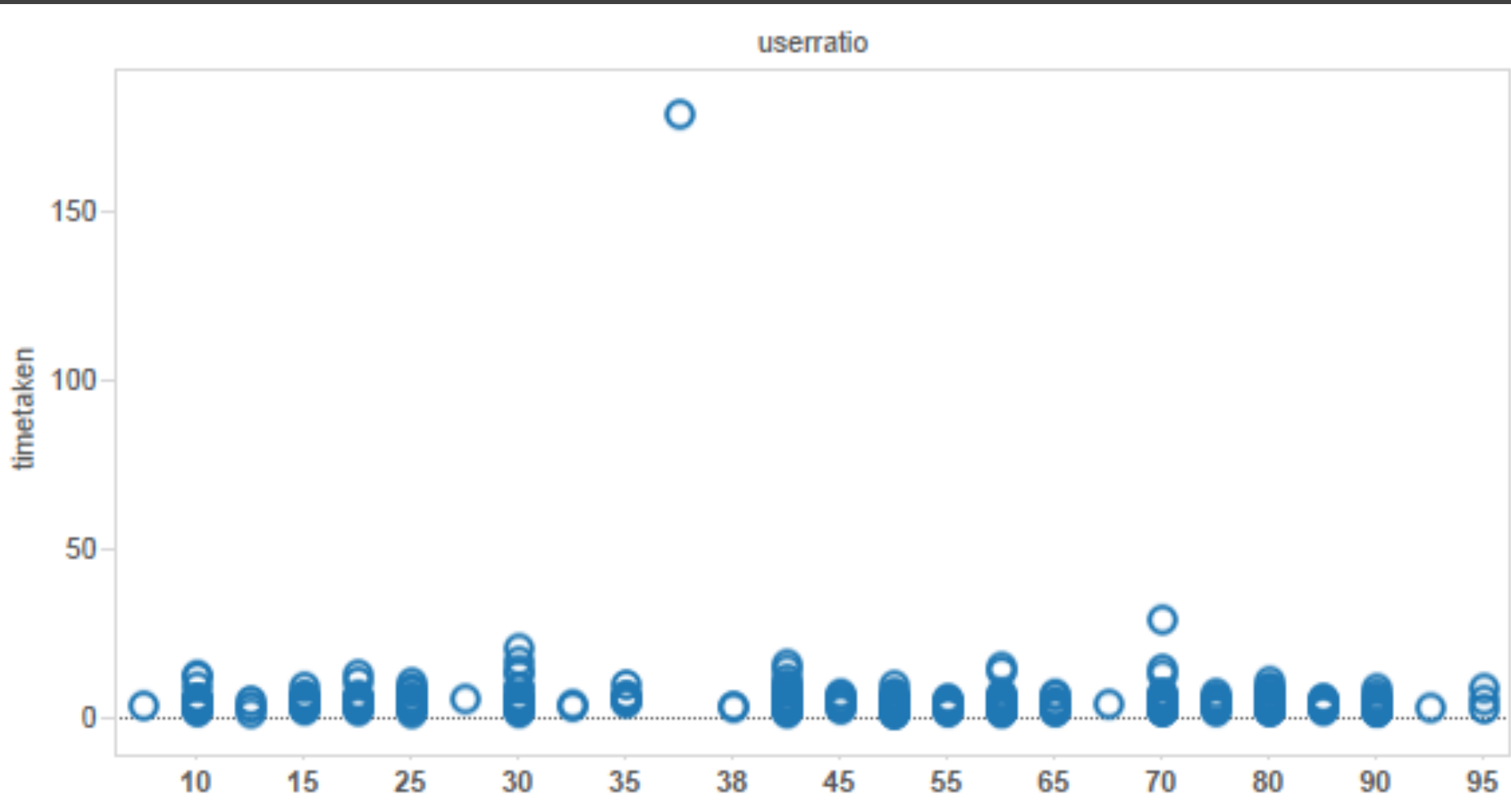
Simplicity - numbers are multiples of 10, 5, 2

Coverage - ticks near the ends of the data

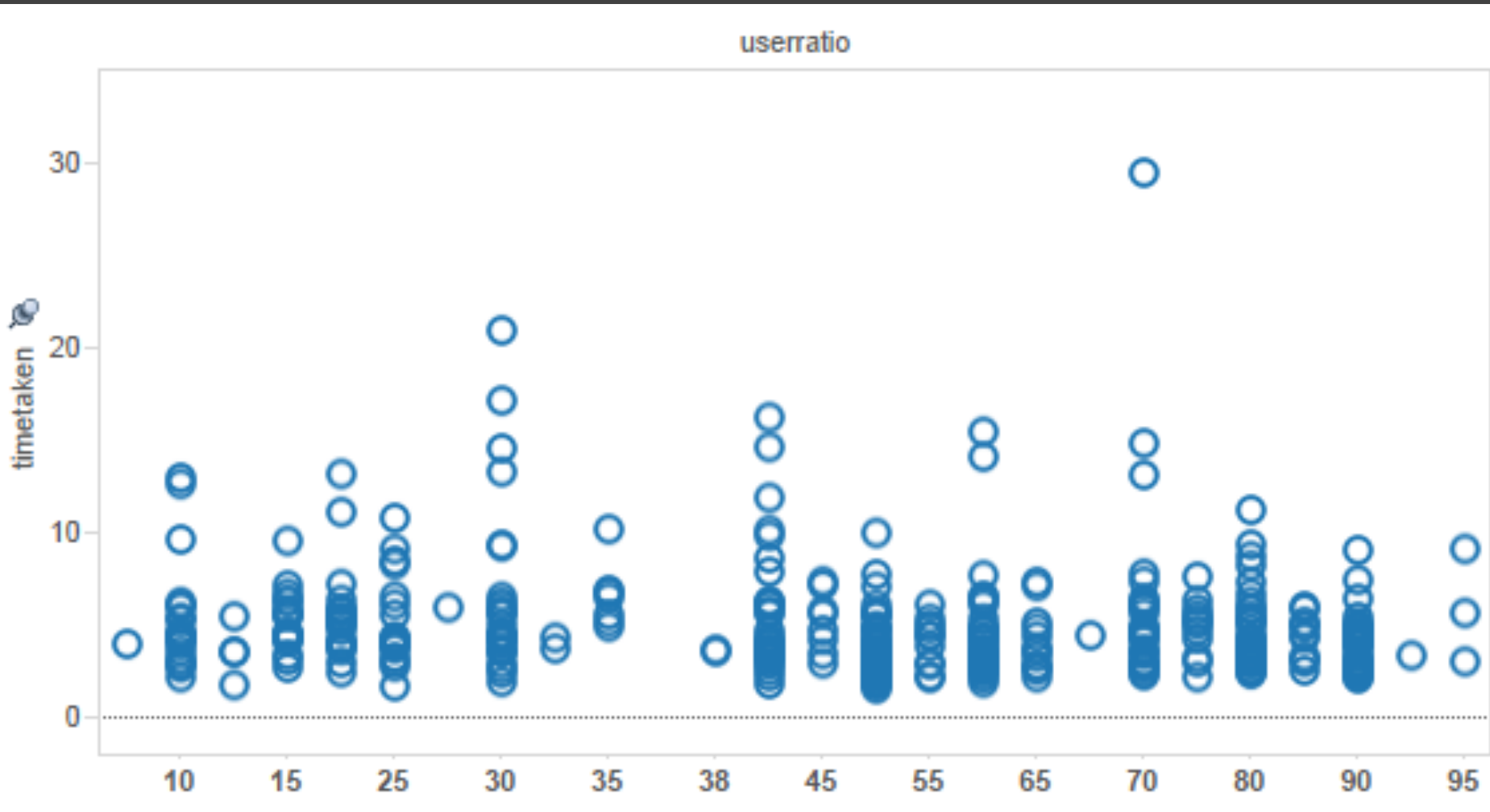
Density - not too many, nor too few

Legibility - whitespace, horizontal text, size

How to Scale the Axis?

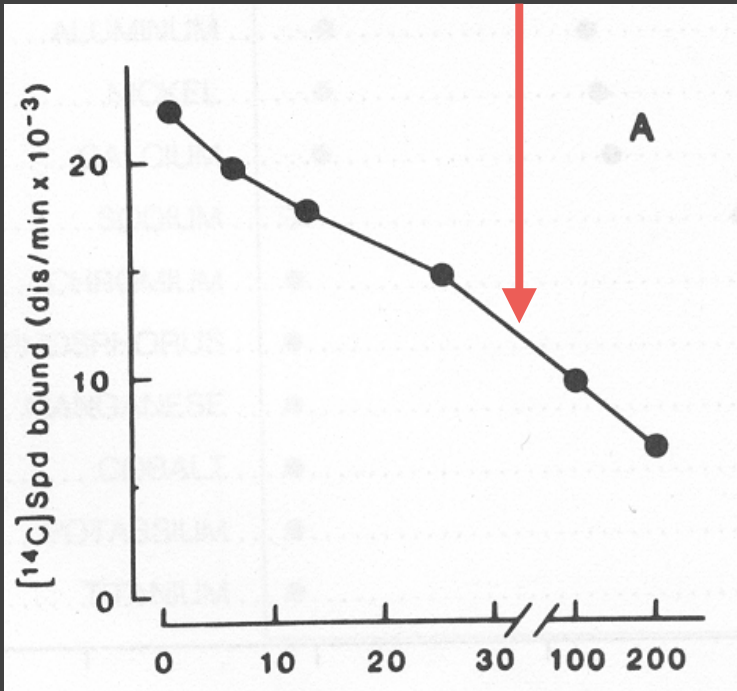


One Option: Clip Outliers

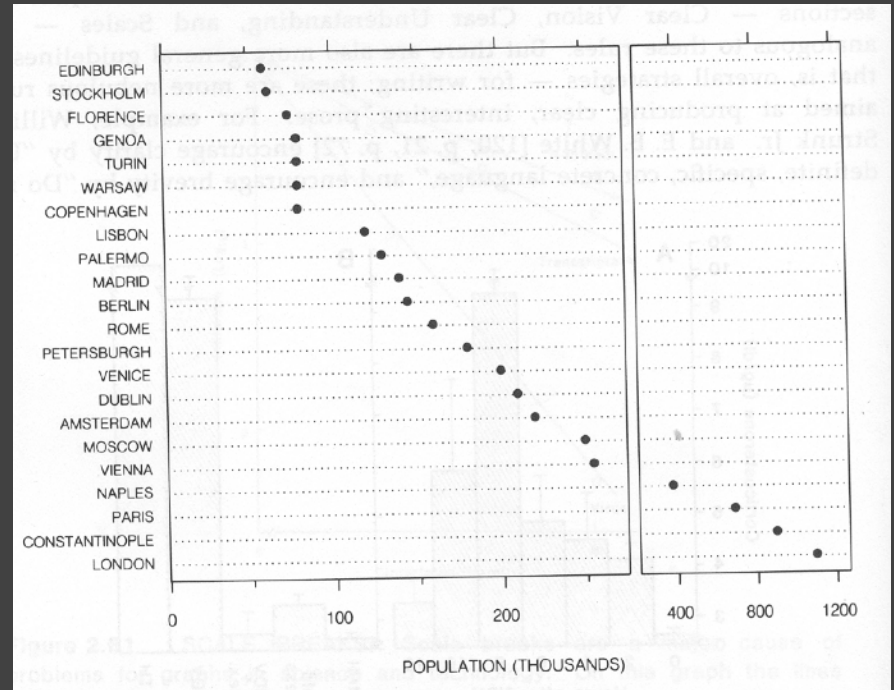


Clearly Mark Scale Breaks

Violates Expressiveness Principle!

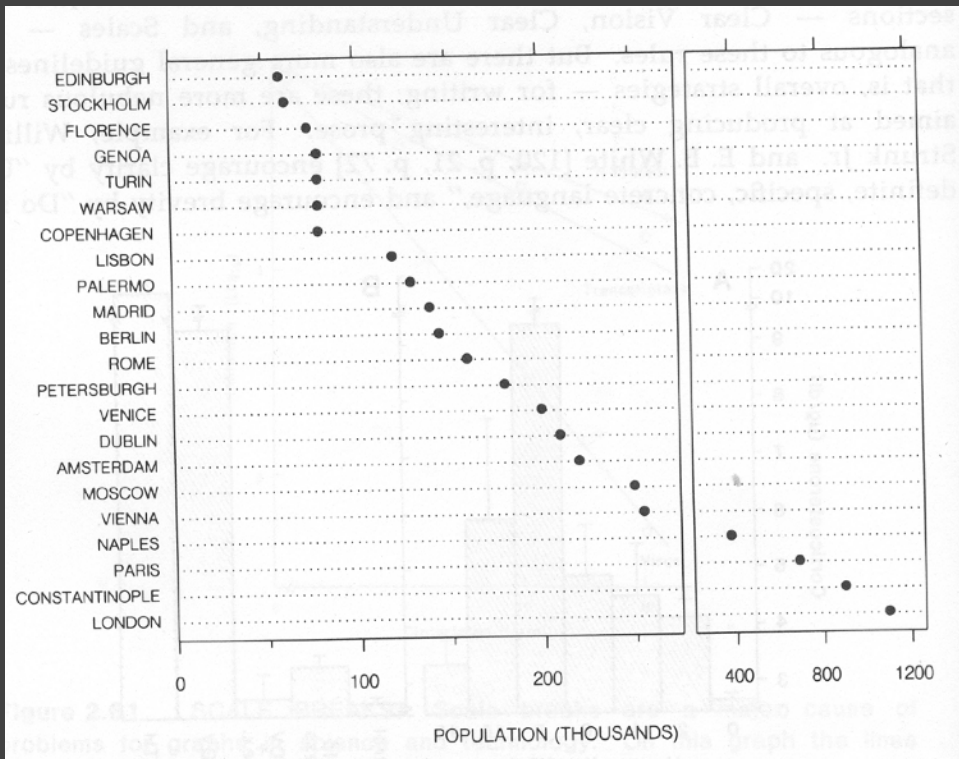


Poor scale break [Cleveland 85]

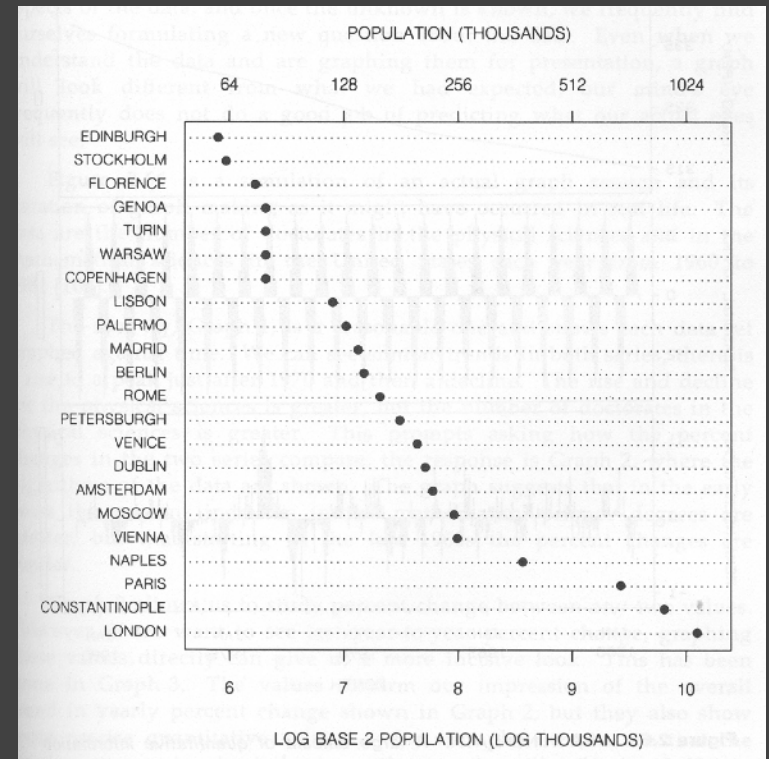


Well-marked scale break [Cleveland 85]

Scale Break vs. Log Scale

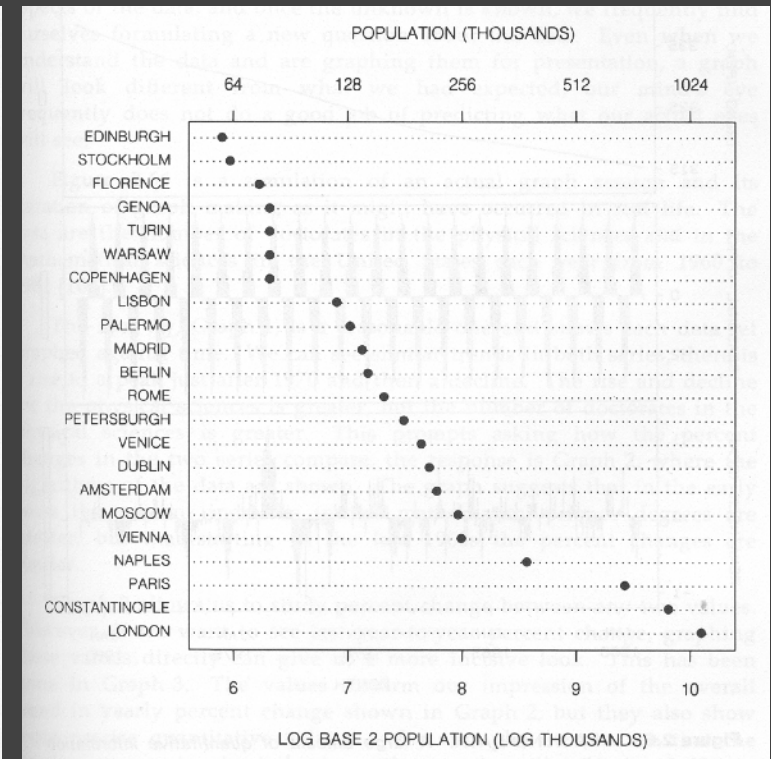
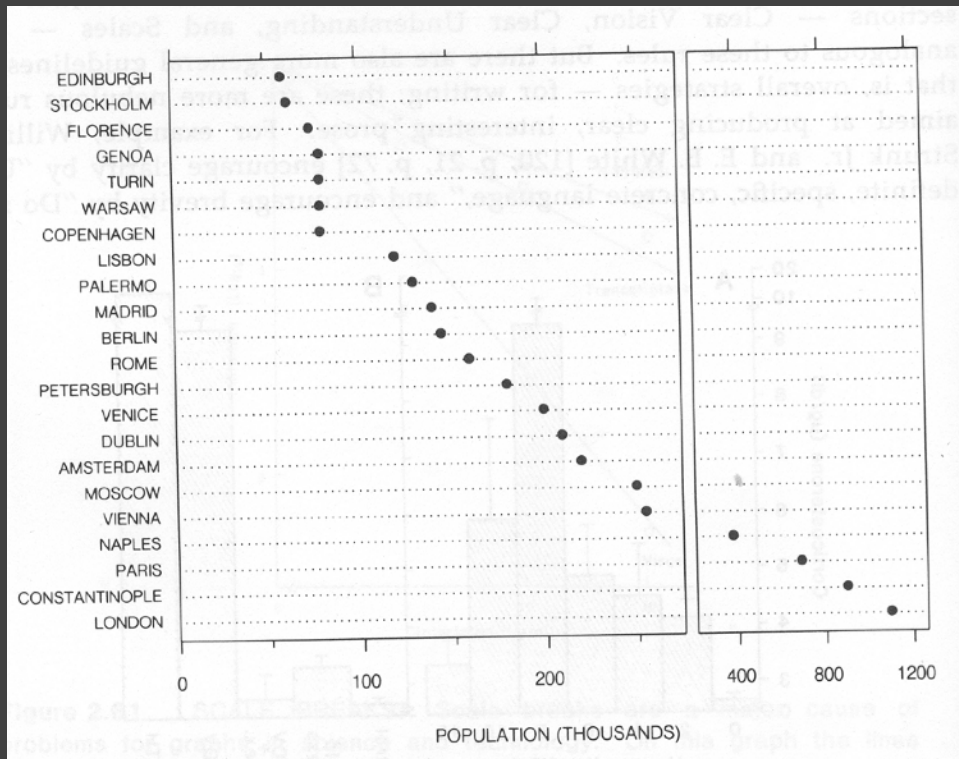


Scale Break



Log Scale

Scale Break vs. Log Scale



Both increase visual resolution

Scale break: difficult to compare (*cognitive* – not *perceptual* – work)

Log scale: direct comparison of all data

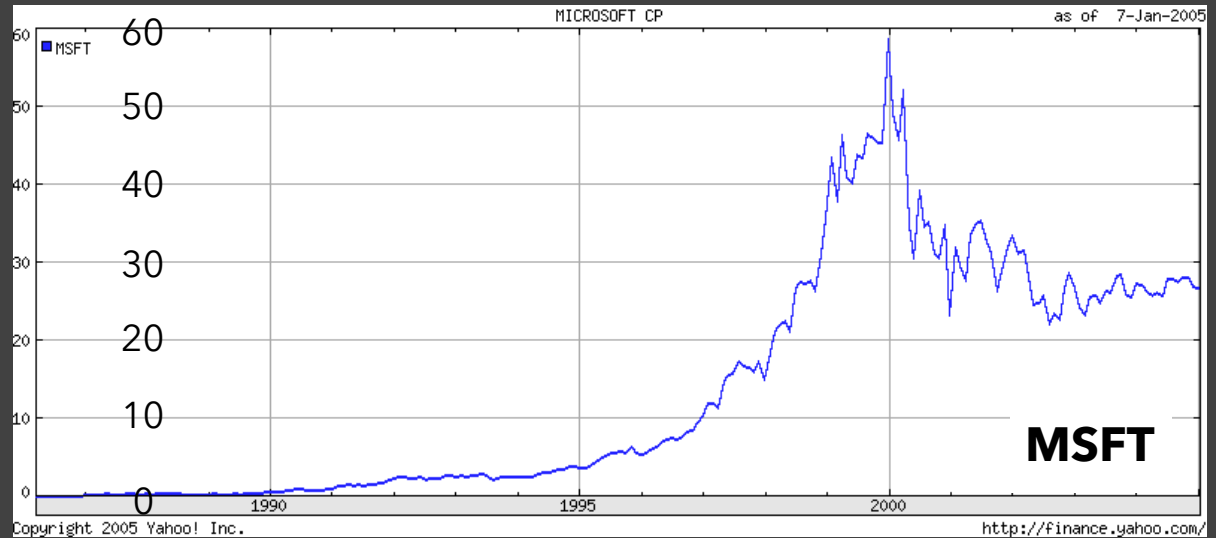
Logarithms turn *multiplication*
into *addition*.

$$\log(x y) = \log(x) + \log(y)$$

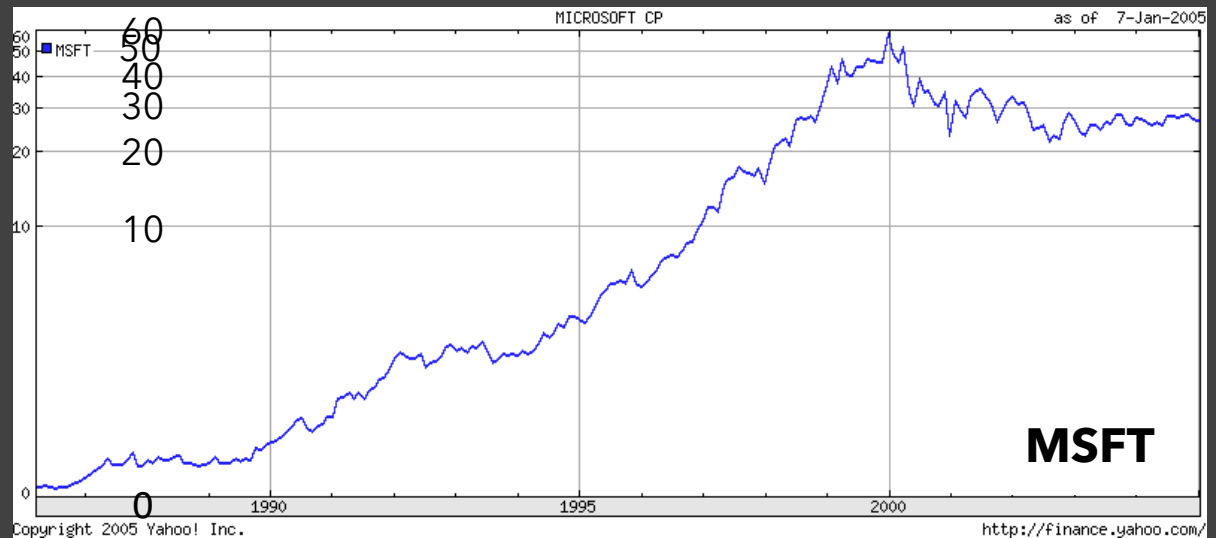
Equal steps on a log scale
correspond to equal changes to
a multiplicative scale factor.

Linear Scale vs. Log Scale

Linear Scale



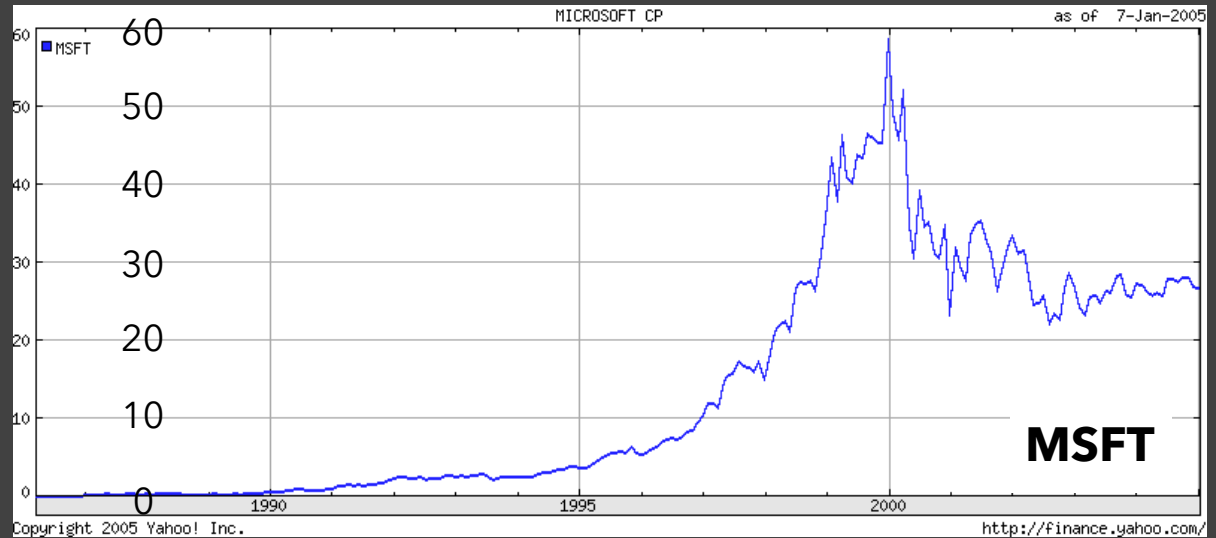
Log Scale



Linear Scale vs. Log Scale

Linear Scale

Absolute change

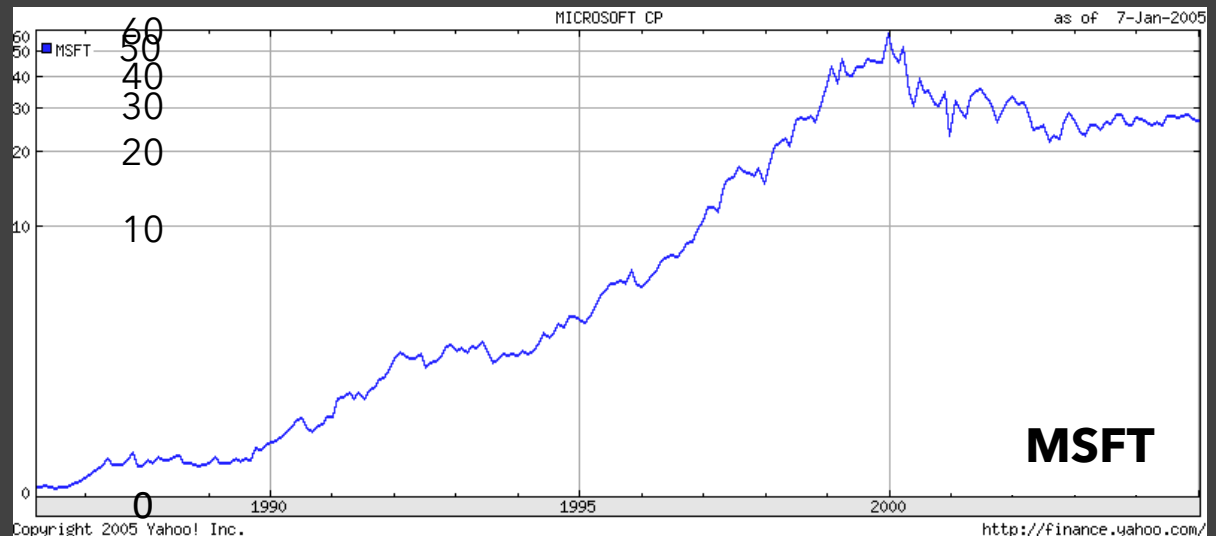


Log Scale

Small fluctuations

Percent change

$$d(10,30) > d(30,60)$$



When To Apply a Log Scale?

Address data skew (e.g., long tails, outliers)

Enables comparison within and across multiple orders of magnitude.

Focus on multiplicative factors (not additive)

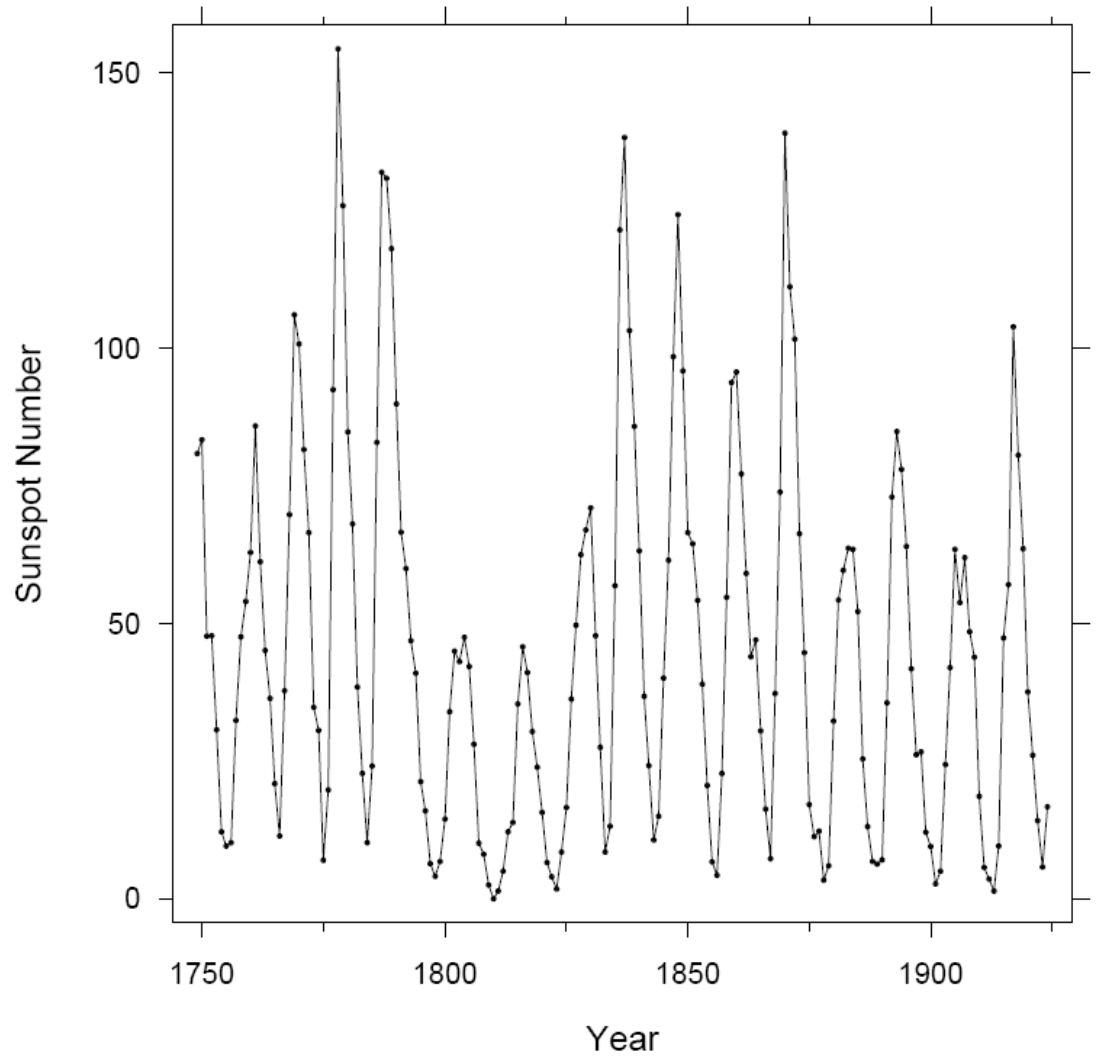
Recall that the logarithm transforms \times to $+$!

Percentage change, not linear difference.

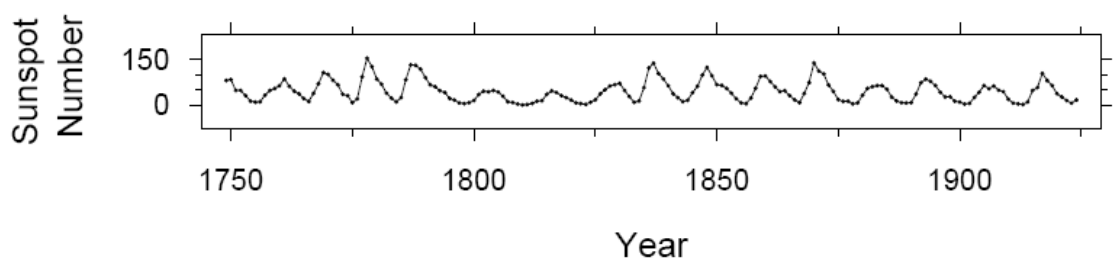
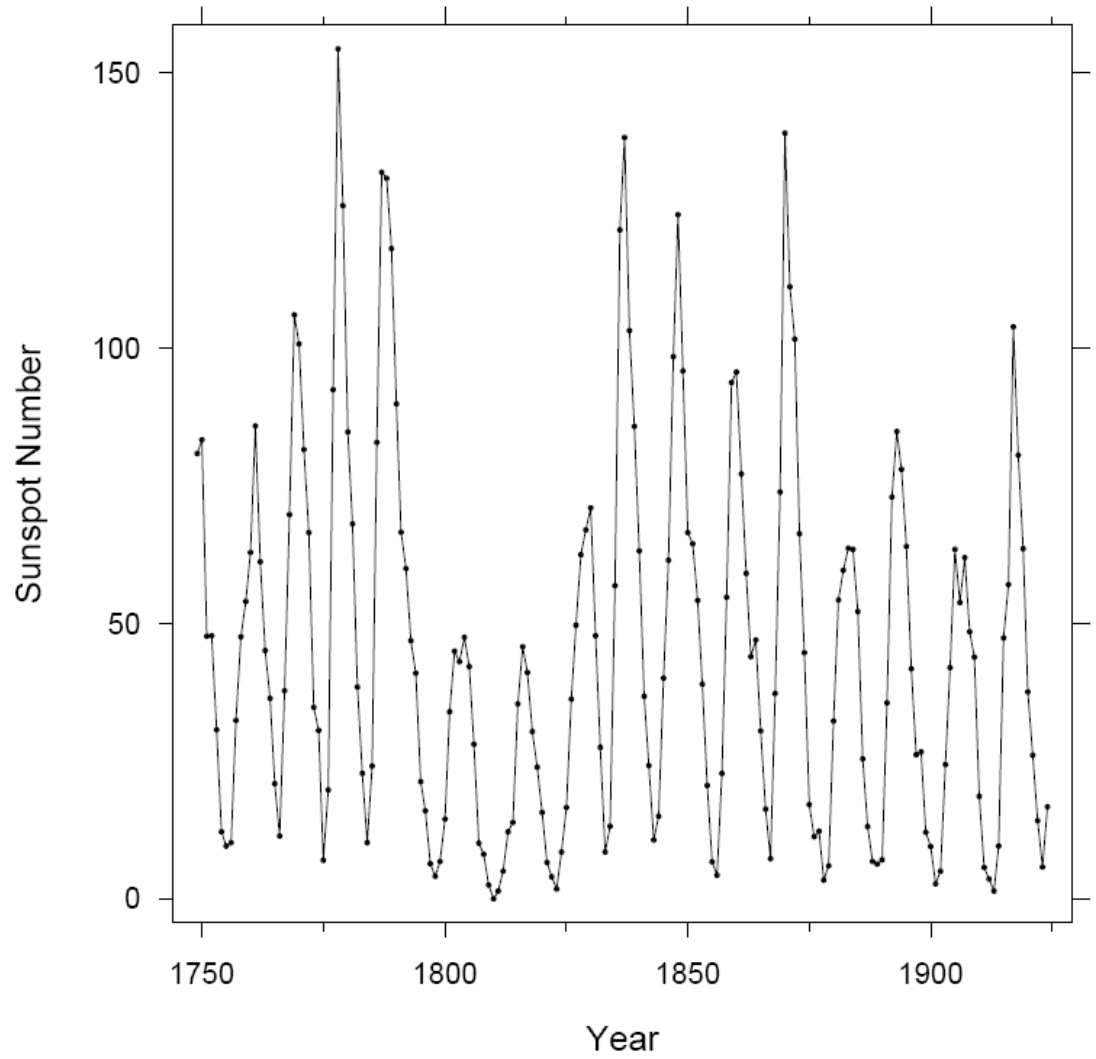
Constraint: **positive, non-zero values**

Constraint: **audience familiarity?**

Aspect Ratio
(width : height)



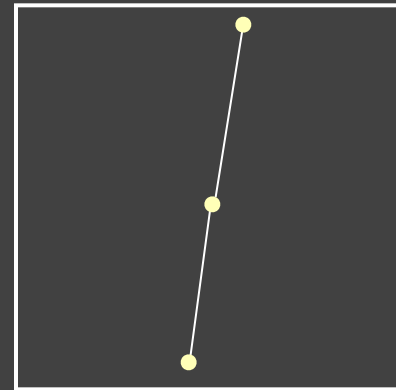
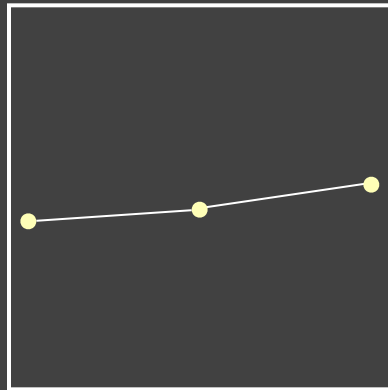
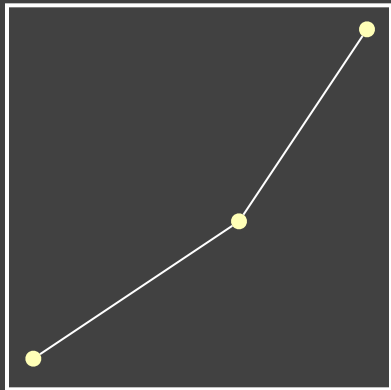
William S. Cleveland
*The Elements of
Graphing Data*



William S. Cleveland
*The Elements of
Graphing Data*

Banking to 45° [Cleveland]

To facilitate perception of trends, maximize the discriminability of line segment orientations

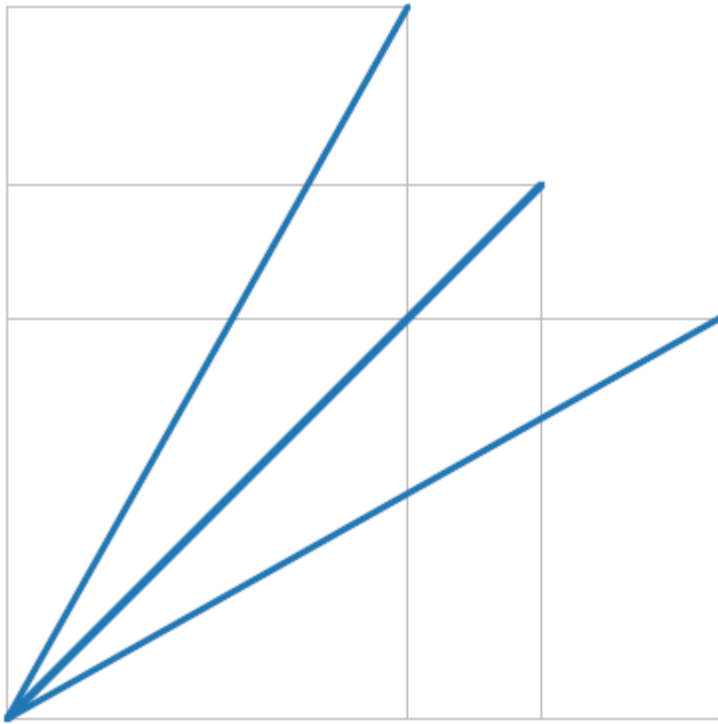


Two line segments are maximally discriminable when their average absolute angle is 45°

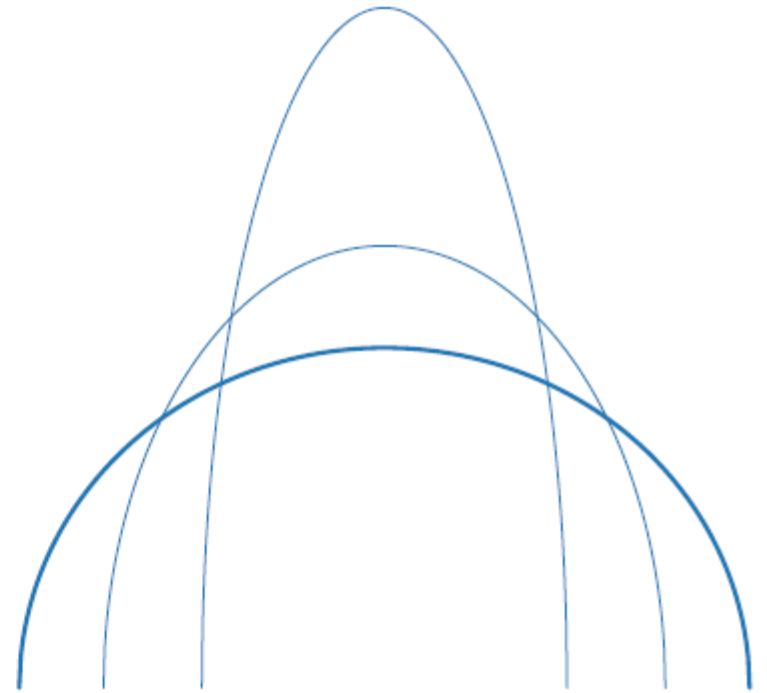
Method: optimize the aspect ratio such that the average absolute angle of all segments is 45°

Alternative: Minimize Arc Length

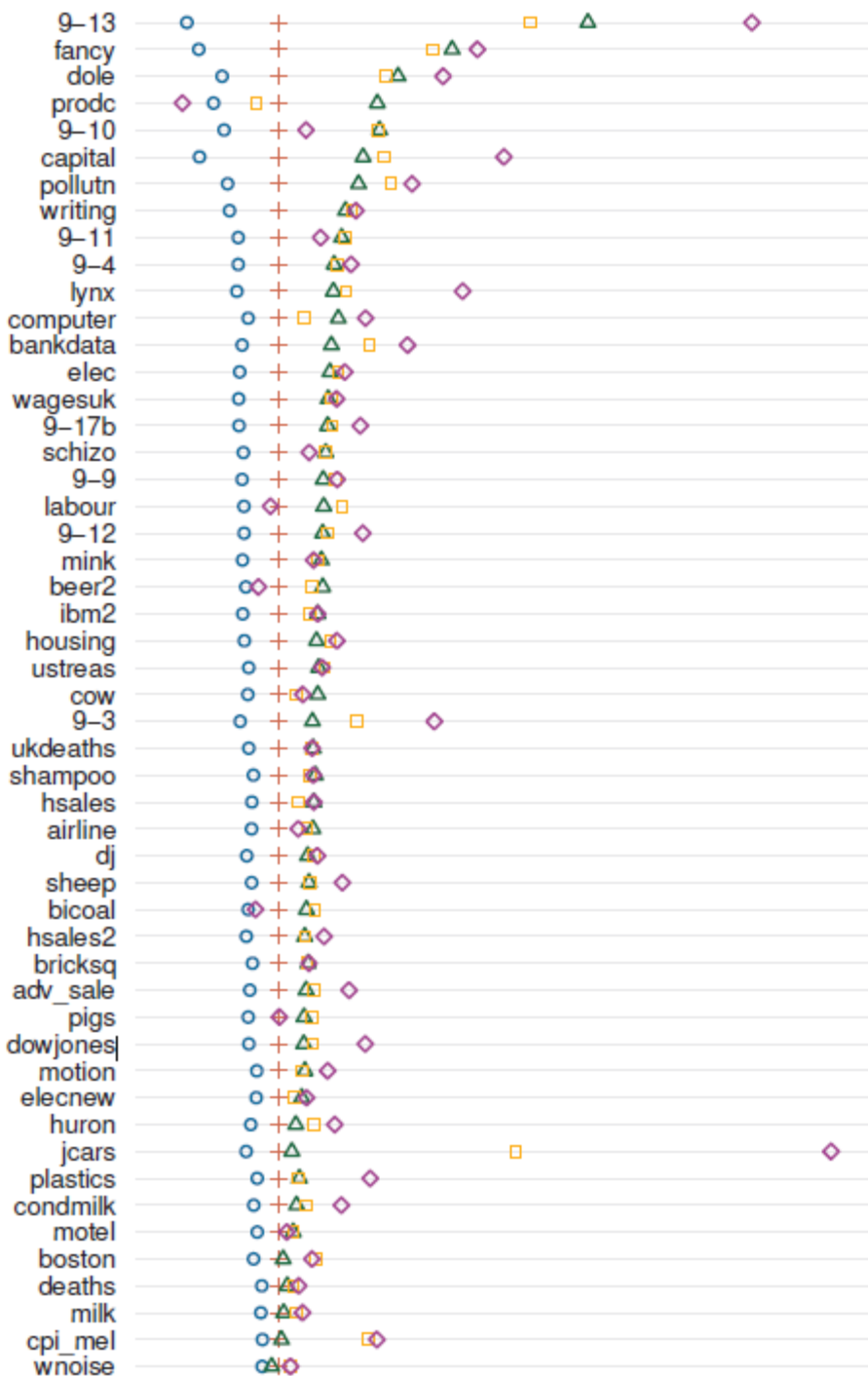
while holding area constant [Talbot et al. 2011]



Straight line $\rightarrow 45^\circ$

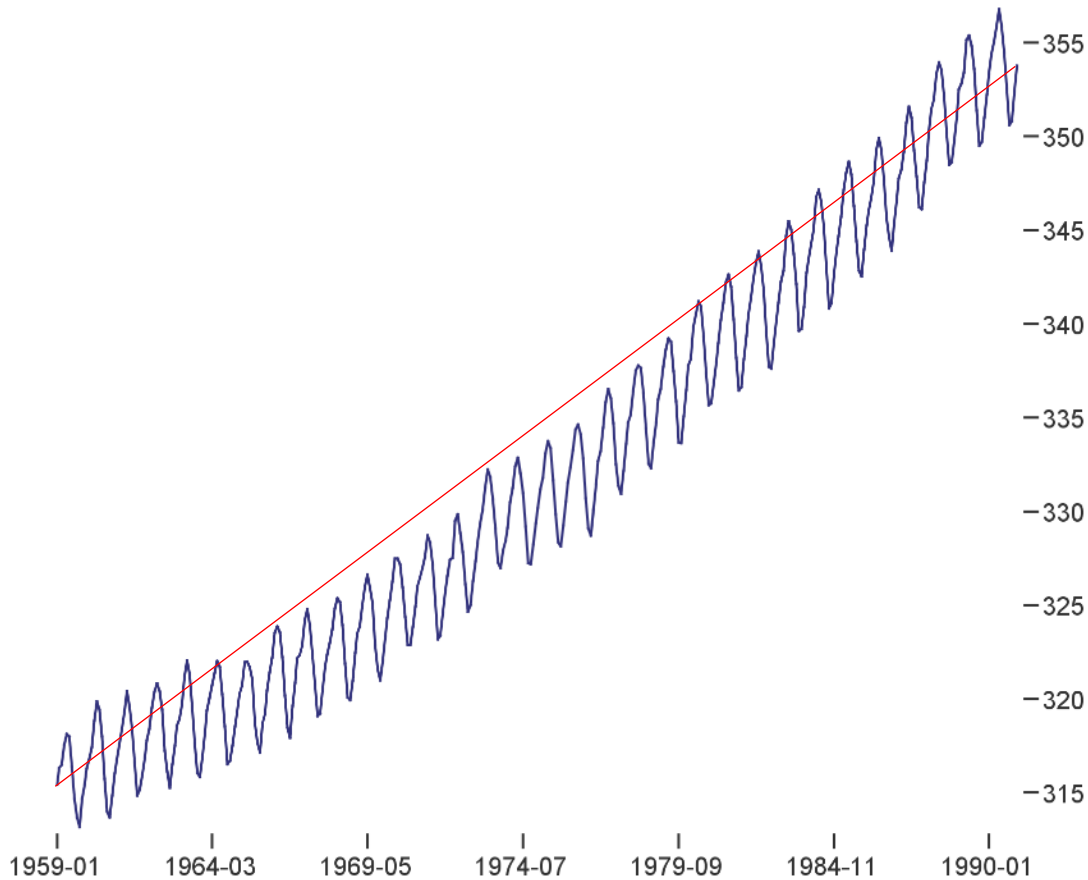


Ellipse \rightarrow Circle

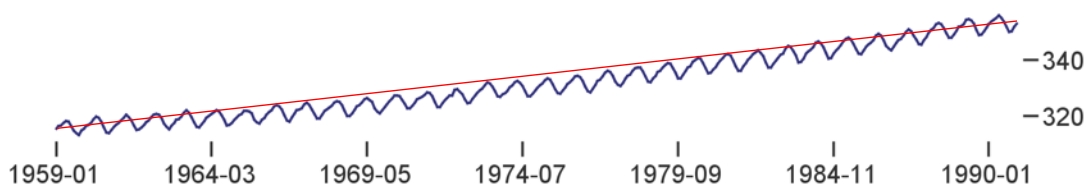


A Good Compromise

Arc-length banking produces aspect ratios in-between those produced by other methods.



Aspect Ratio = 1.17



Aspect Ratio = 7.87

Trends may occur at different scales!

Apply banking to the original data or to fitted trend lines.

[Heer & Agrawala '06]

CO₂ Measurements

William S. Cleveland

Visualizing Data

Administrivia

A2: Exploratory Data Analysis

Use visualization software to form & answer questions

First steps:

Step 1: Pick domain & data

Step 2: Pose questions

Step 3: Profile the data

Iterate as needed

Create visualizations

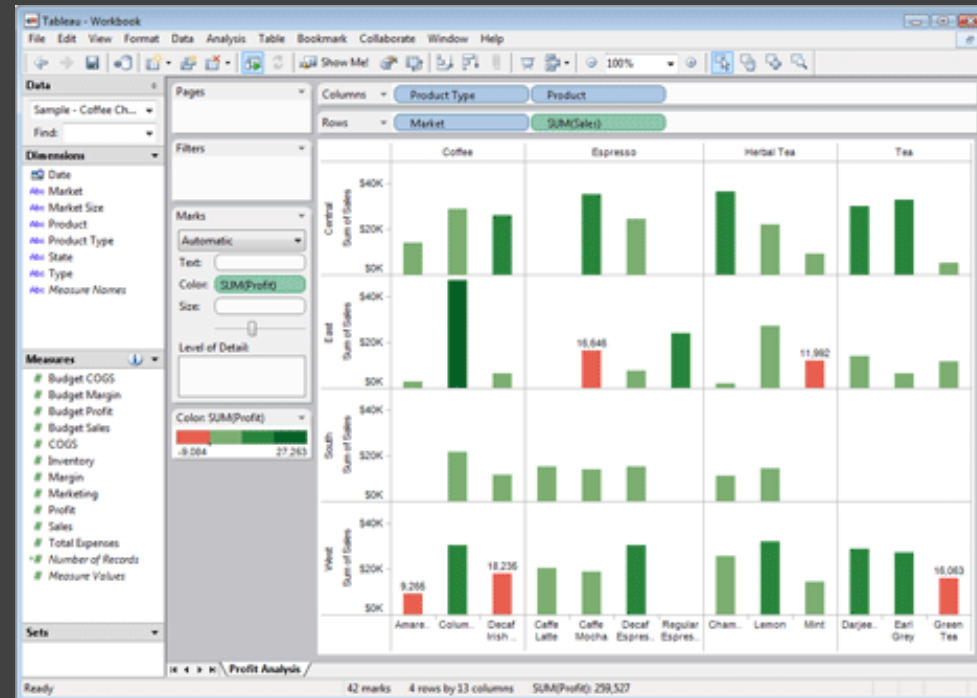
Interact with data

Refine your questions

Author a report notebook

Screenshots of most insightful views (8+)

Include titles and captions for each view



Due by 11:59pm

Monday, Oct 26

Tableau Tutorial (Optional)

Friday October 16, 1:30-3:00pm

Zoom link available on Canvas

Will also be recorded

Led by Kevin and Yang

Multidimensional Data

Visual Encoding Variables

Position (X)

Position (Y)

Size

Value

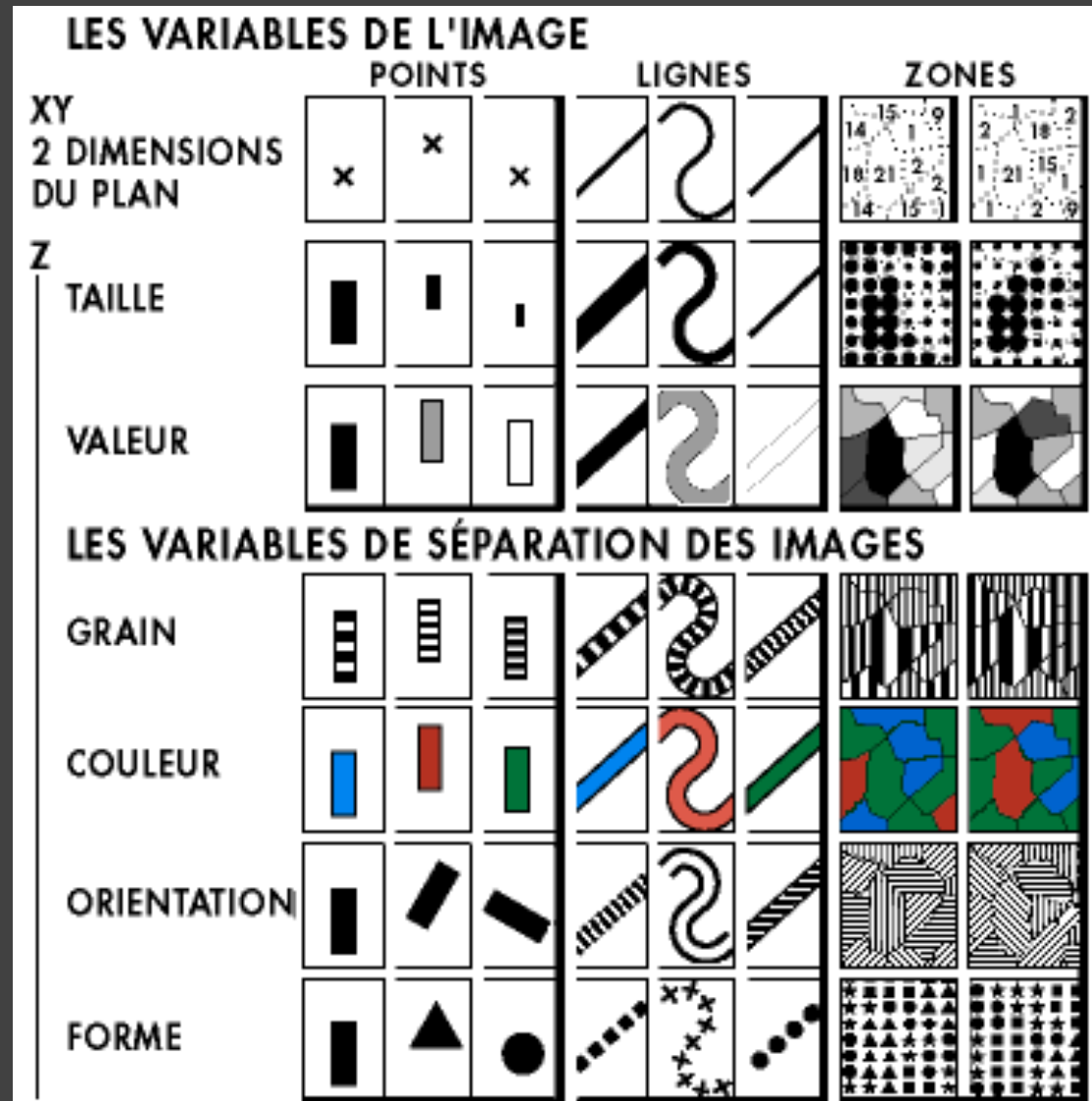
Texture

Color

Orientation

Shape

~8 dimensions?



Example: Coffee Sales

Sales figures for a fictional coffee chain

Sales	Q-Ratio
Profit	Q-Ratio
Marketing	Q-Ratio
Product Type	N {Coffee, Espresso, Herbal Tea, Tea}
Market	N {Central, East, South, West}

Filters

YEAR(Date): 2010

Marks

x+ Automatic

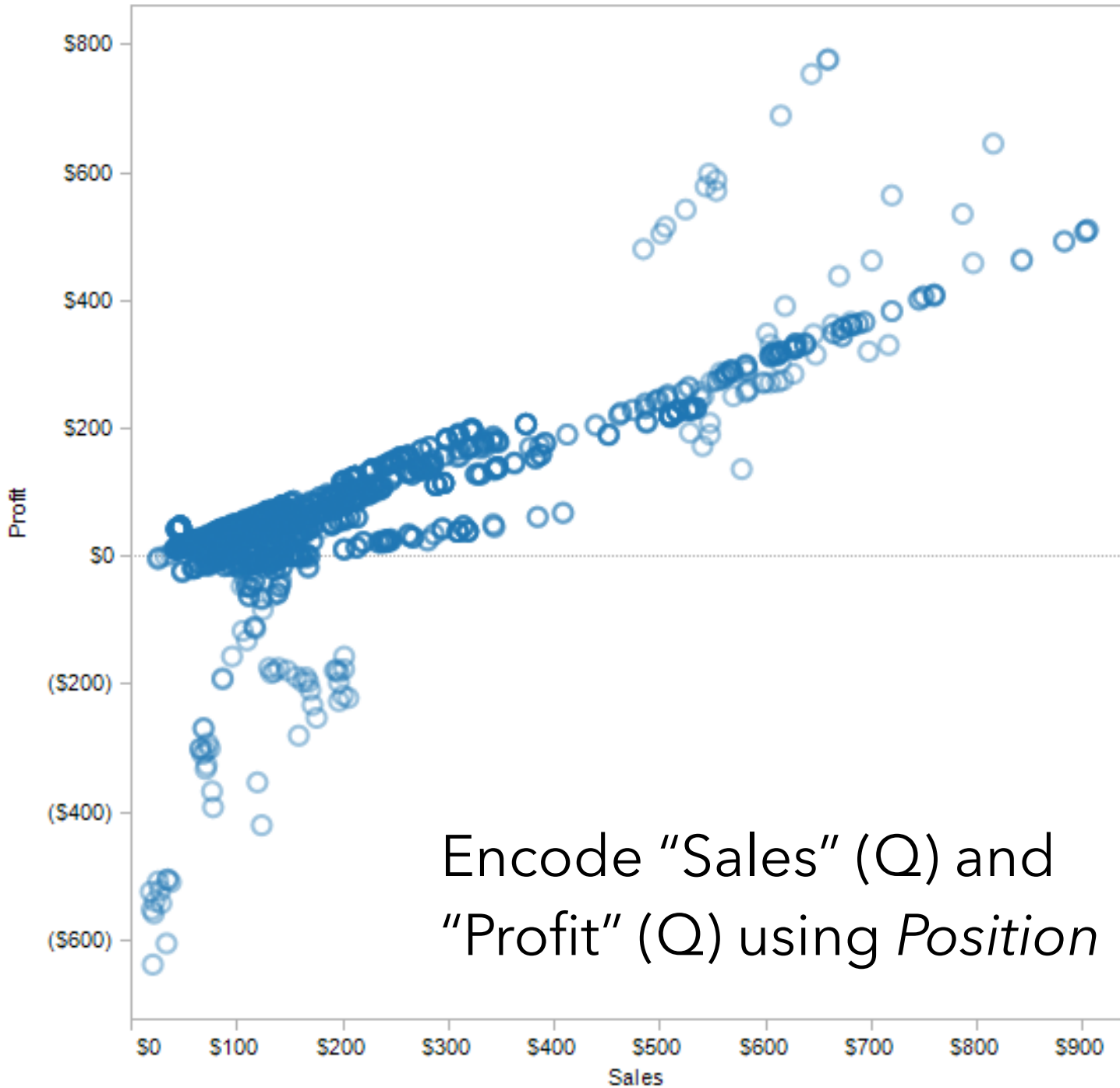
Shape Circle

Label

Color

Size

Level of Detail



Filters

YEAR(Date): 2010

Marks

x+ Automatic

Shape Circle

Label

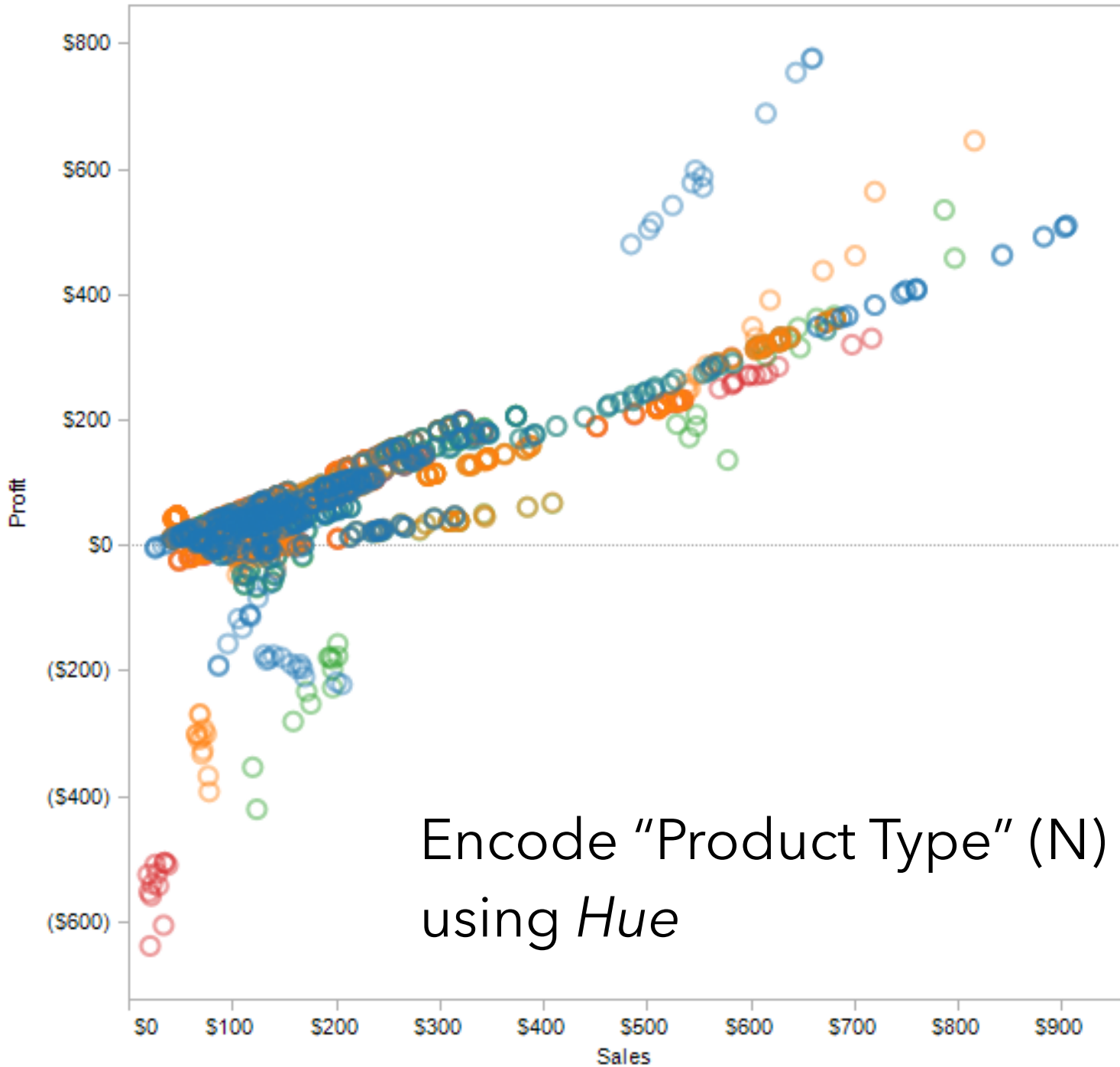
Color

Size

Level of Detail

Product Type

- Coffee
- Espresso
- Herbal Tea
- Tea



Filters

YEAR(Date): 2010

Marks

Automatic

Shape Market

Label Market

Color Product Type

Size

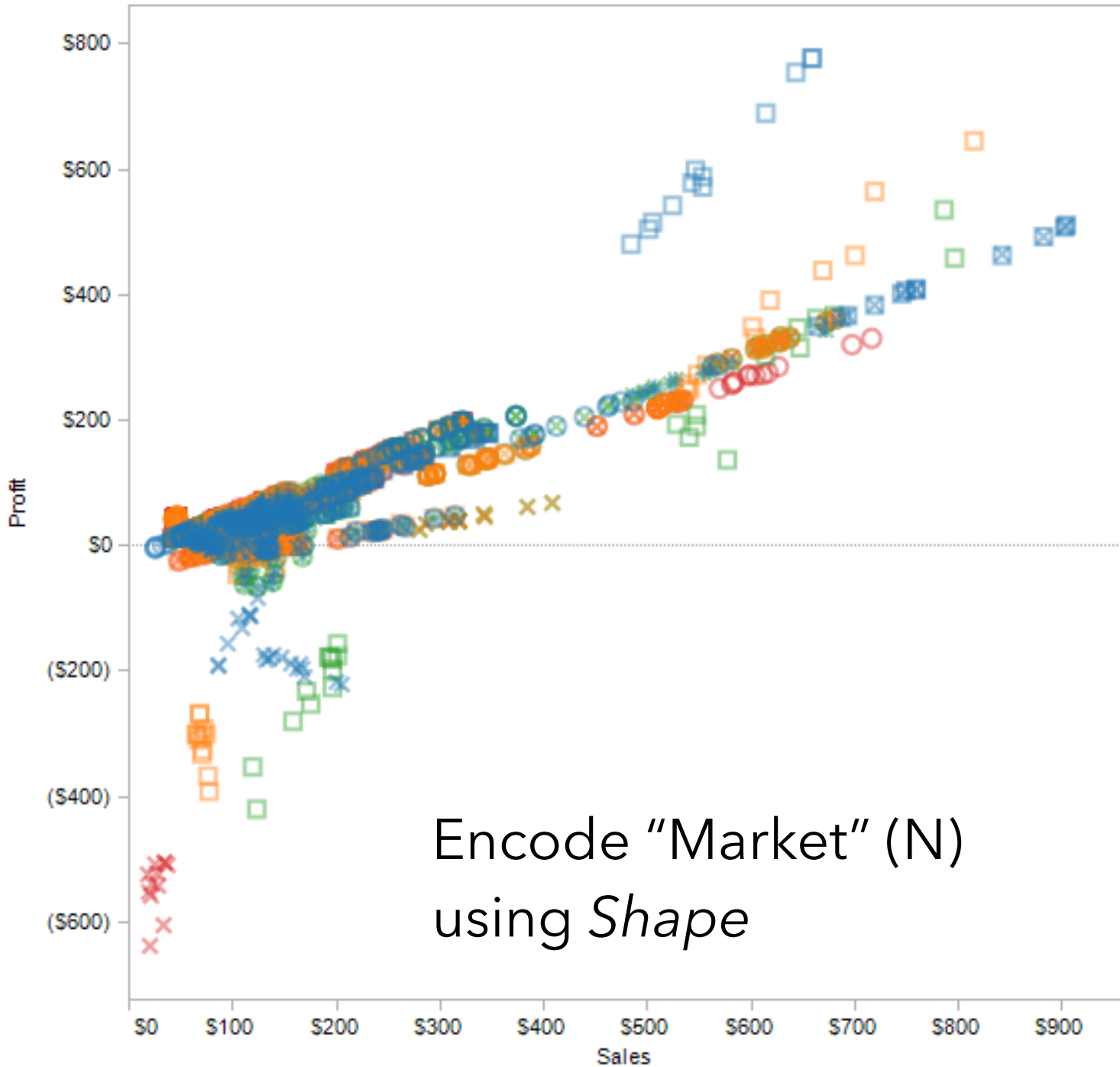
Level of Detail

Product Type

- Coffee
- Espresso
- Herbal Tea
- Tea

Market

- Central
- East
- South
- West



Filters

YEAR(Date): 2010

Marks

Automatic

Shape Market

Label

Color Product Type

Size Marketing

Marketing

Level of Detail

Product Type

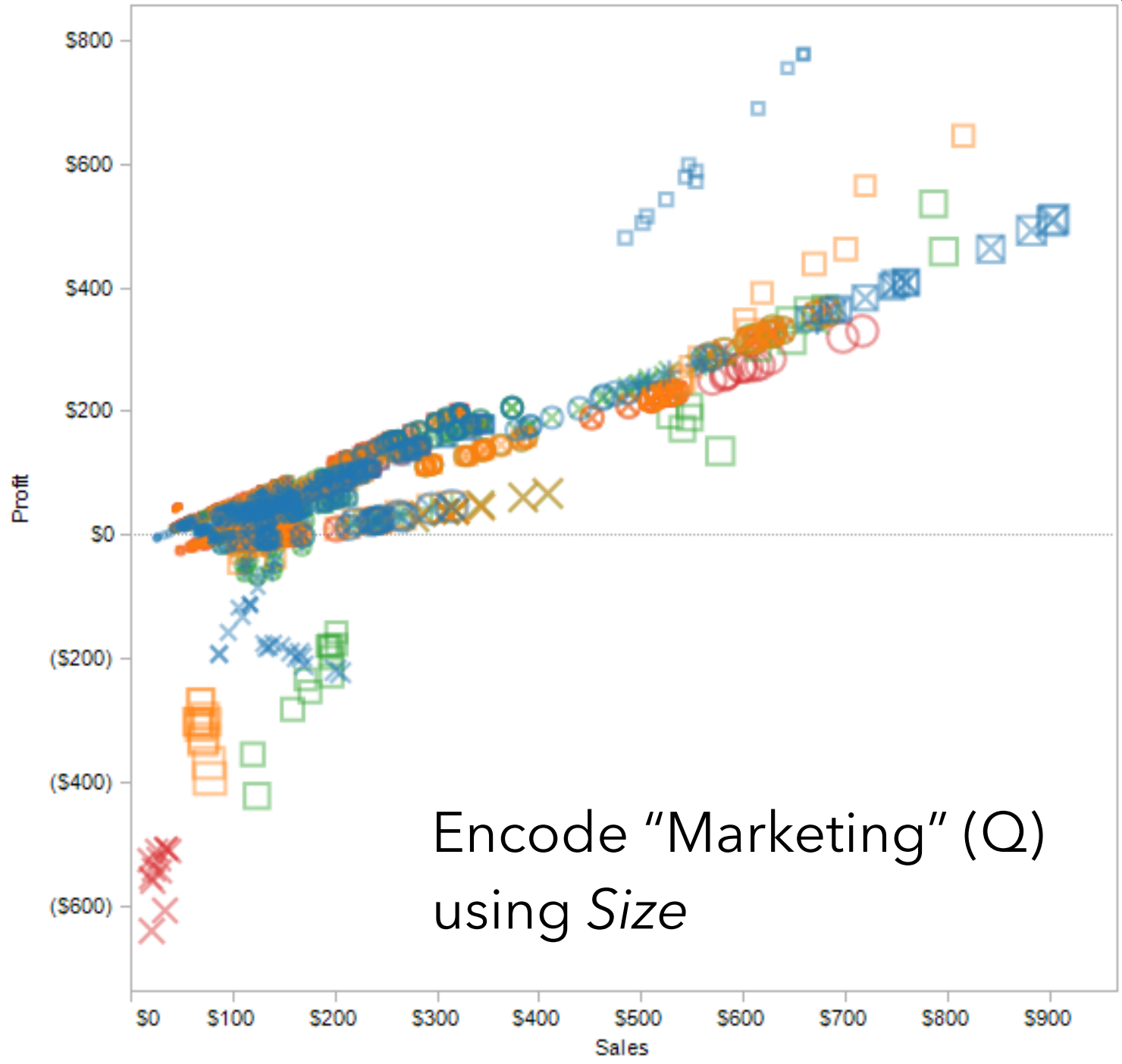
- Coffee
- Espresso
- Herbal Tea

Market

- Central
- East
- South

Marketing

- \$0
- \$50
- \$100



Encode "Marketing" (Q) using *Size*

Trellis Plots



A *trellis plot* subdivides space to enable comparison across multiple plots.

Typically nominal or ordinal variables are used as dimensions for subdivision.

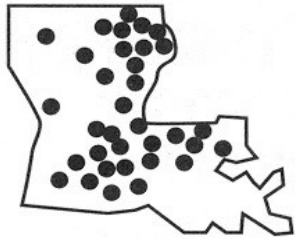
Small Multiples



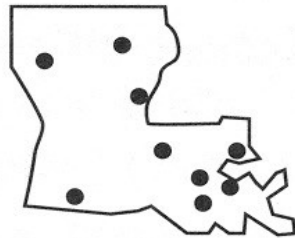
[MacEachren '95, Figure 2.11, p. 38]

Small Multiples

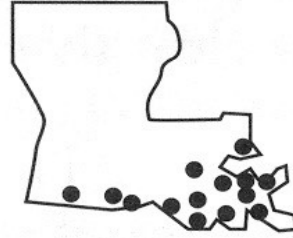
alfisol



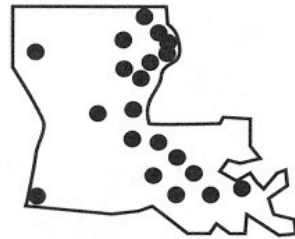
entisol



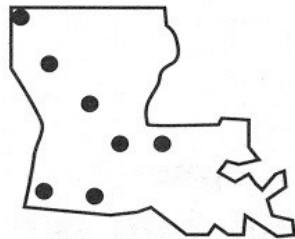
histosol



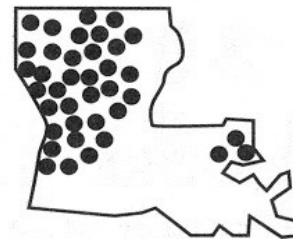
inceptisol



mollisol

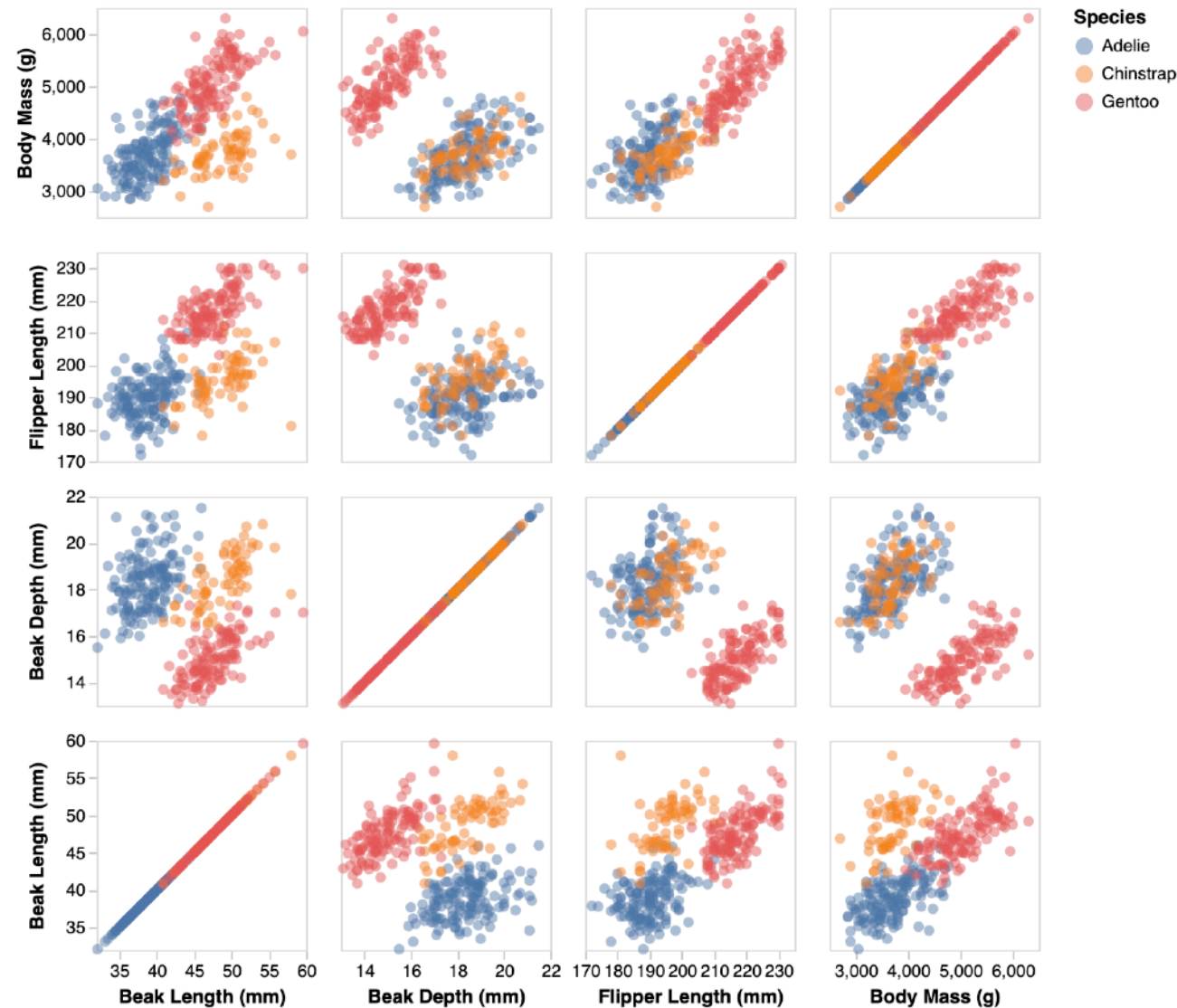


ultisol



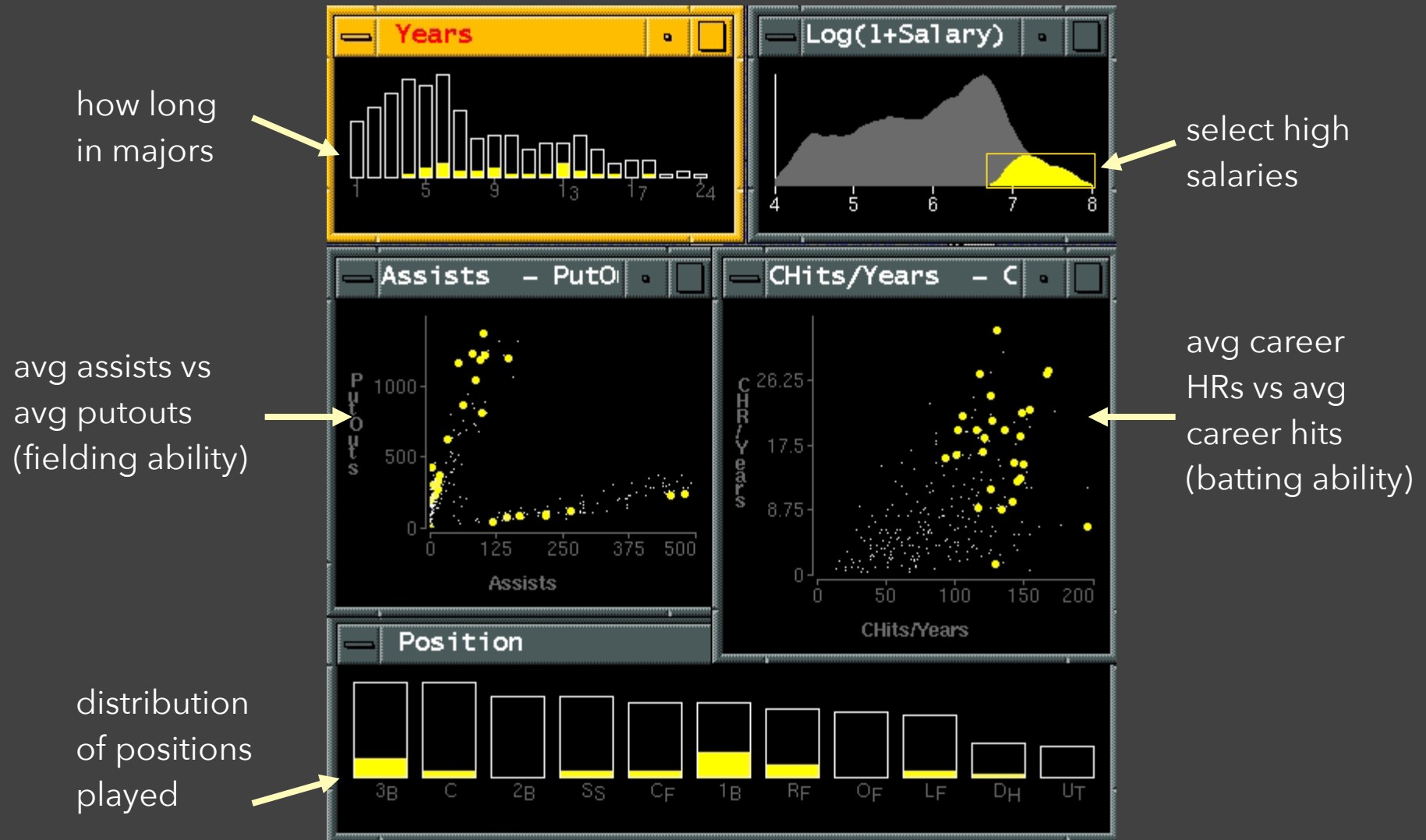
[MacEachren '95, Figure 2.11, p. 38]

Scatterplot Matrix (SPLOM)



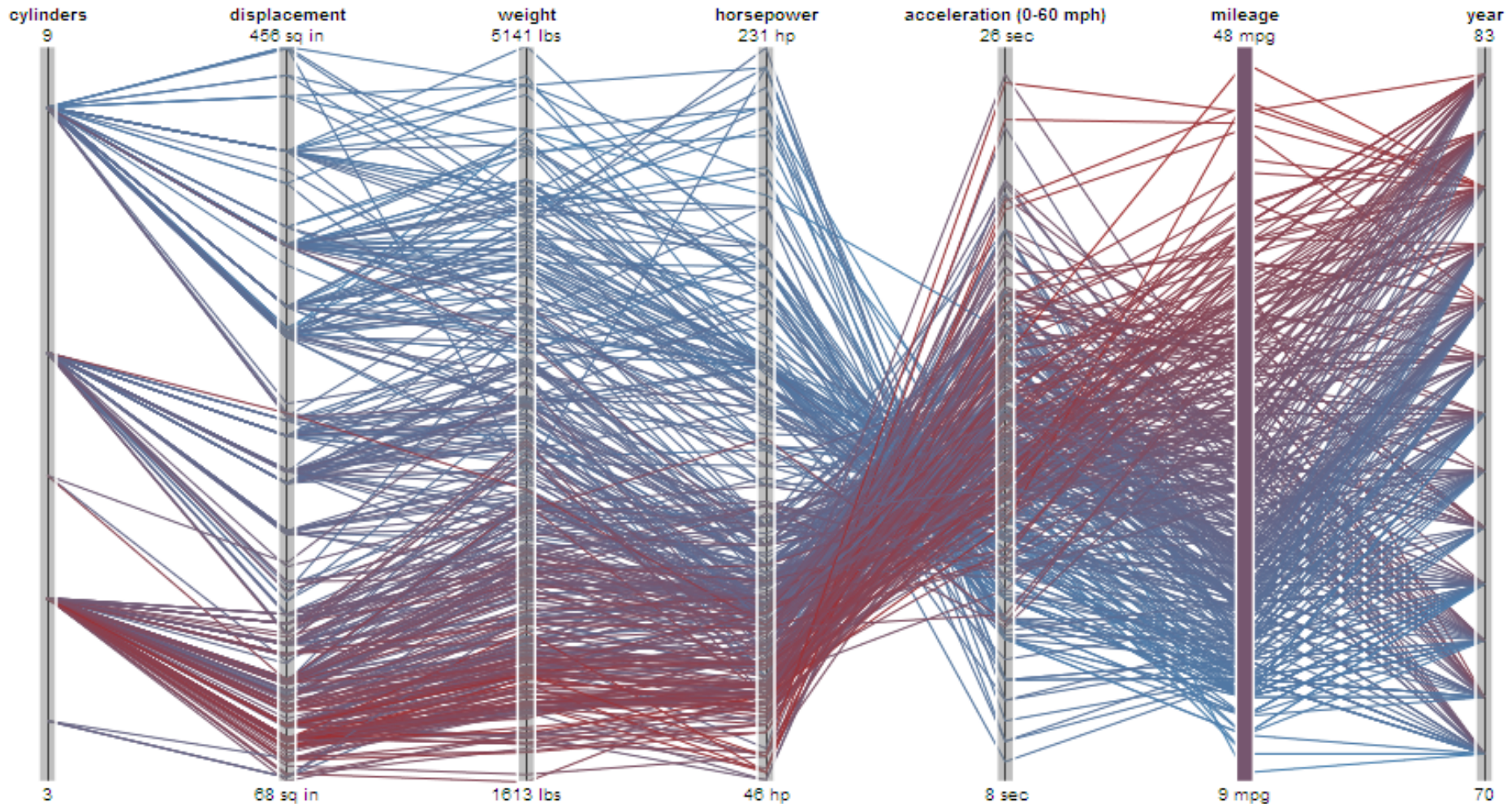
Scatter plots for pairwise comparison of each data dimension.

Multiple Coordinated Views



Parallel Coordinates

Parallel Coordinates [Inselberg]



Parallel Coordinates [Inselberg]

Visualize up to ~two dozen dimensions at once

1. Draw parallel axes for each variable
2. For each tuple, connect points on each axis

Between adjacent axes: line crossings imply neg. correlation, shared slopes imply pos. correlation.

Full plot can be cluttered. **Interactive selection** can be used to assess multivariate relationships.

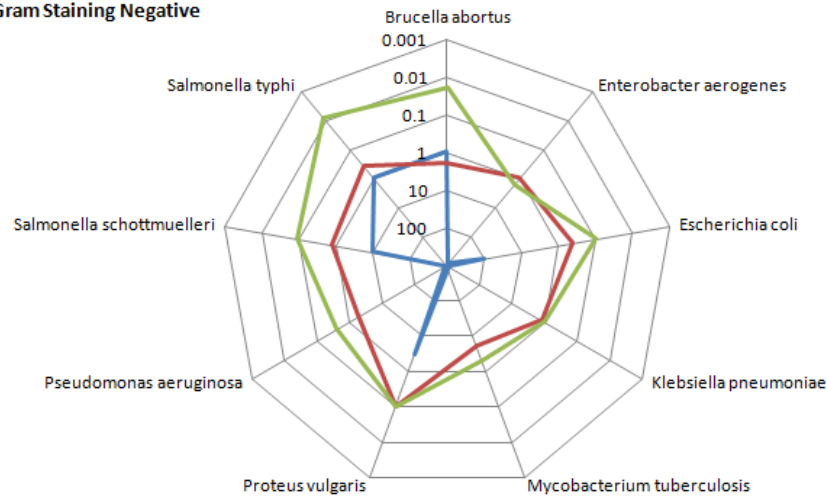
Highly sensitive to axis **scale** and **ordering**.

Expertise required to use effectively!

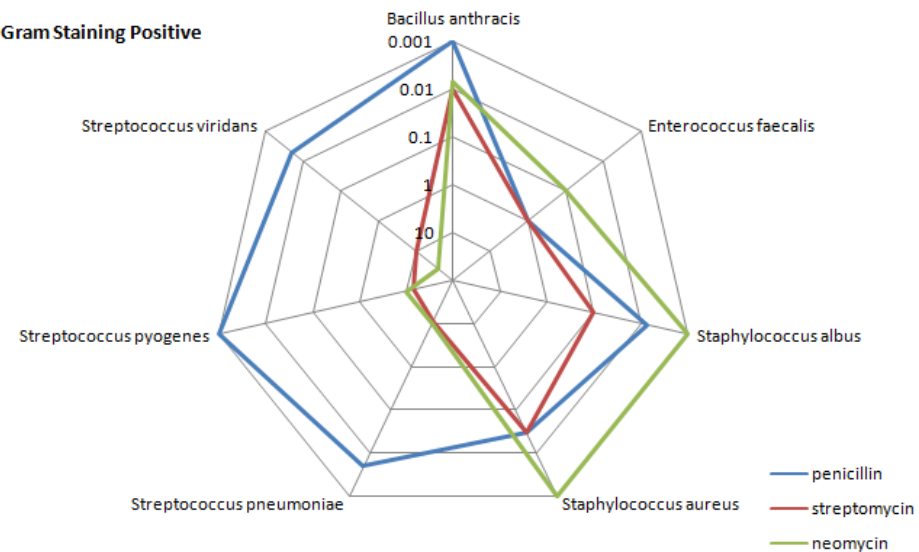
Radar Plot / Star Graph

Antibiotics MIC Concentrations

Gram Staining Negative



Gram Staining Positive



“Parallel” dimensions in polar coordinate space
Best if same units apply to each axis

Dimensionality Reduction

Dimensionality Reduction (DR)

Project nD data to 2D or 3D for viewing. Often used to interpret and sanity check high-dimensional representations fit by machine learning methods.

Different DR methods make different trade-offs: for example to **preserve global structure** (e.g., PCA) or **emphasize local structure** (e.g., nearest-neighbor approaches, including t-SNE and UMAP).

Reduction Techniques

Principal Components Analysis (PCA)

Linear transformation of basis vectors, ordered by amount of data variance they explain.

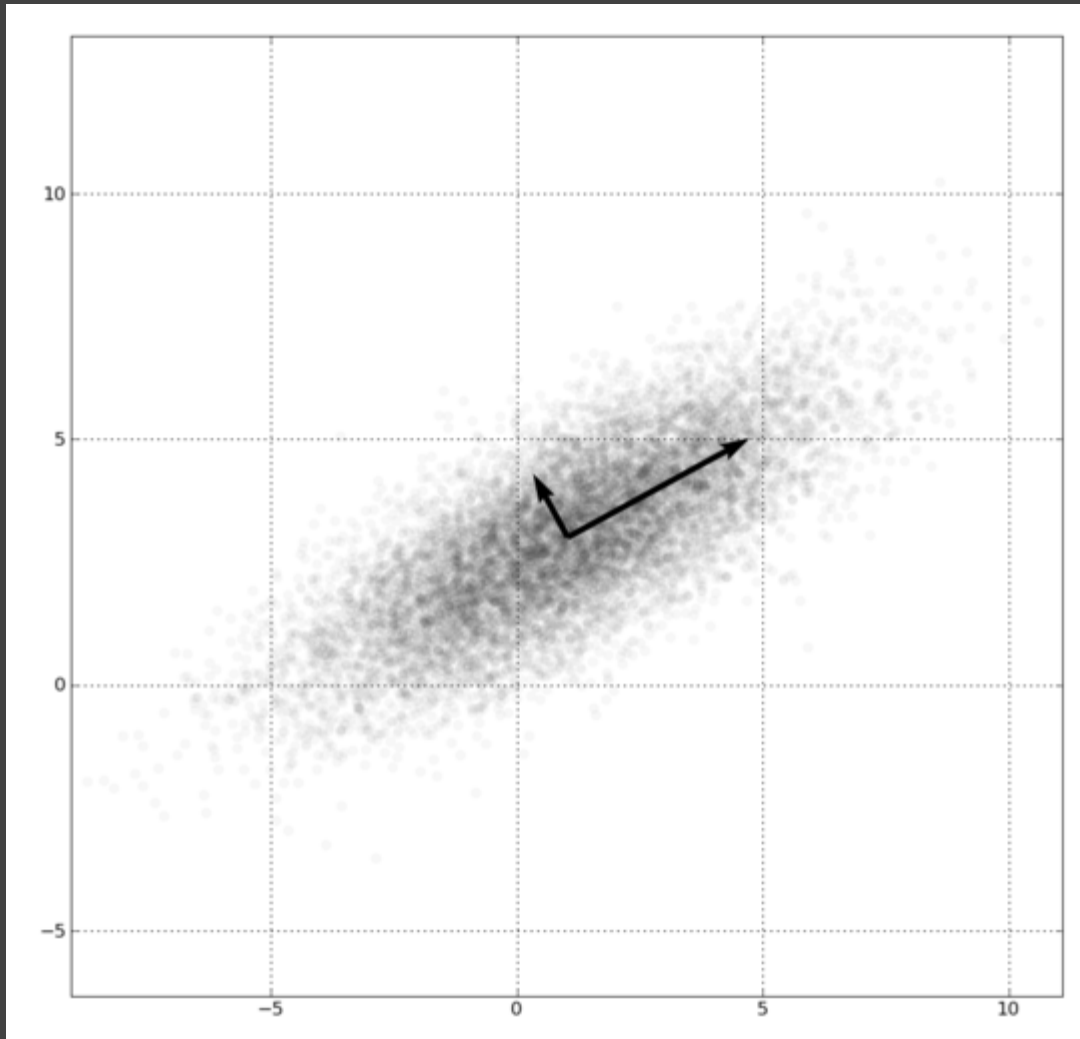
t-Dist. Stochastic Neighbor Embedding (t-SNE)

Probabilistically model distance, optimize positions.

Uniform Manifold Approx. & Projection (UMAP)

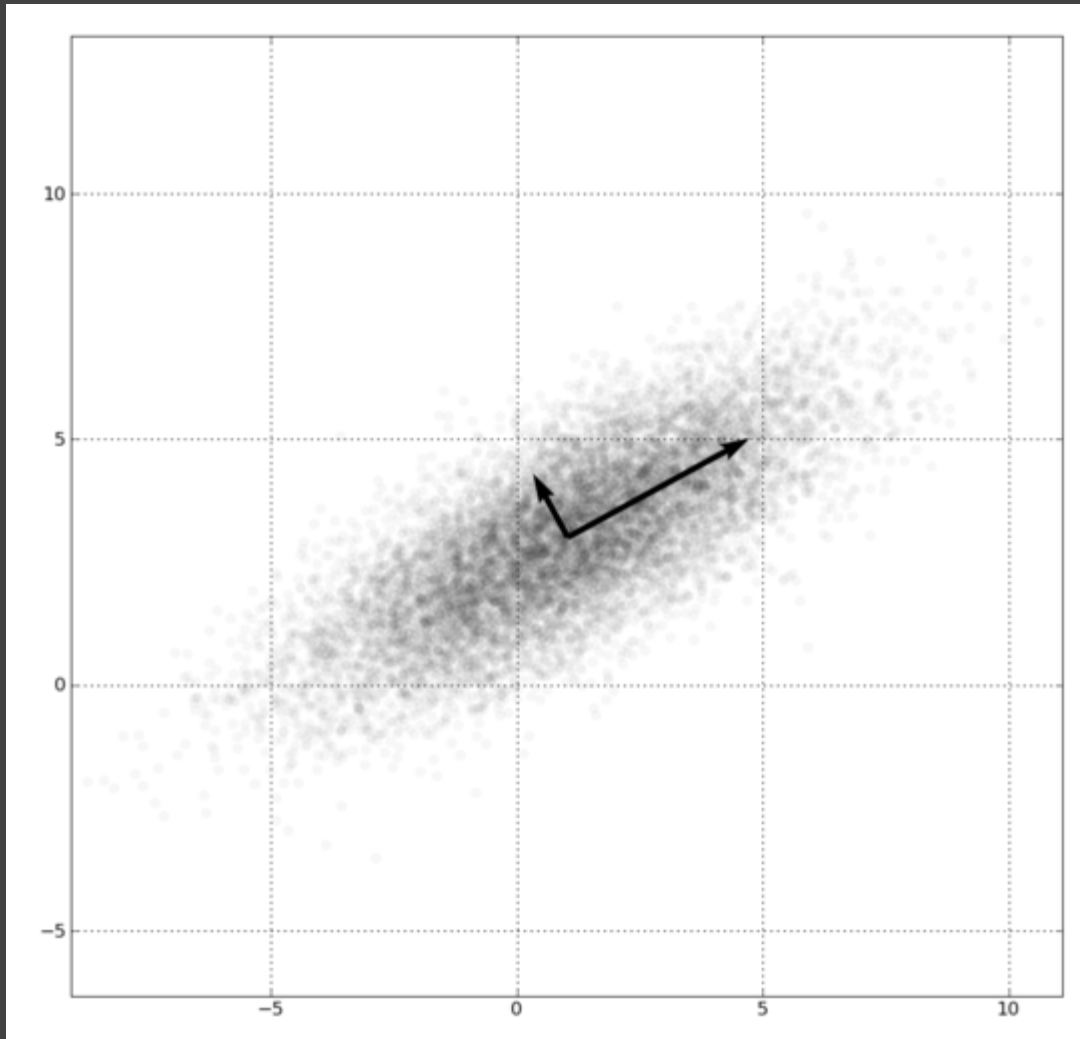
Identify local manifolds, then stitch them together.

Principal Components Analysis



1. Mean-center the data.
2. Find \perp basis vectors that maximize the data variance.
3. Plot the data using the top vectors.

Principal Components Analysis

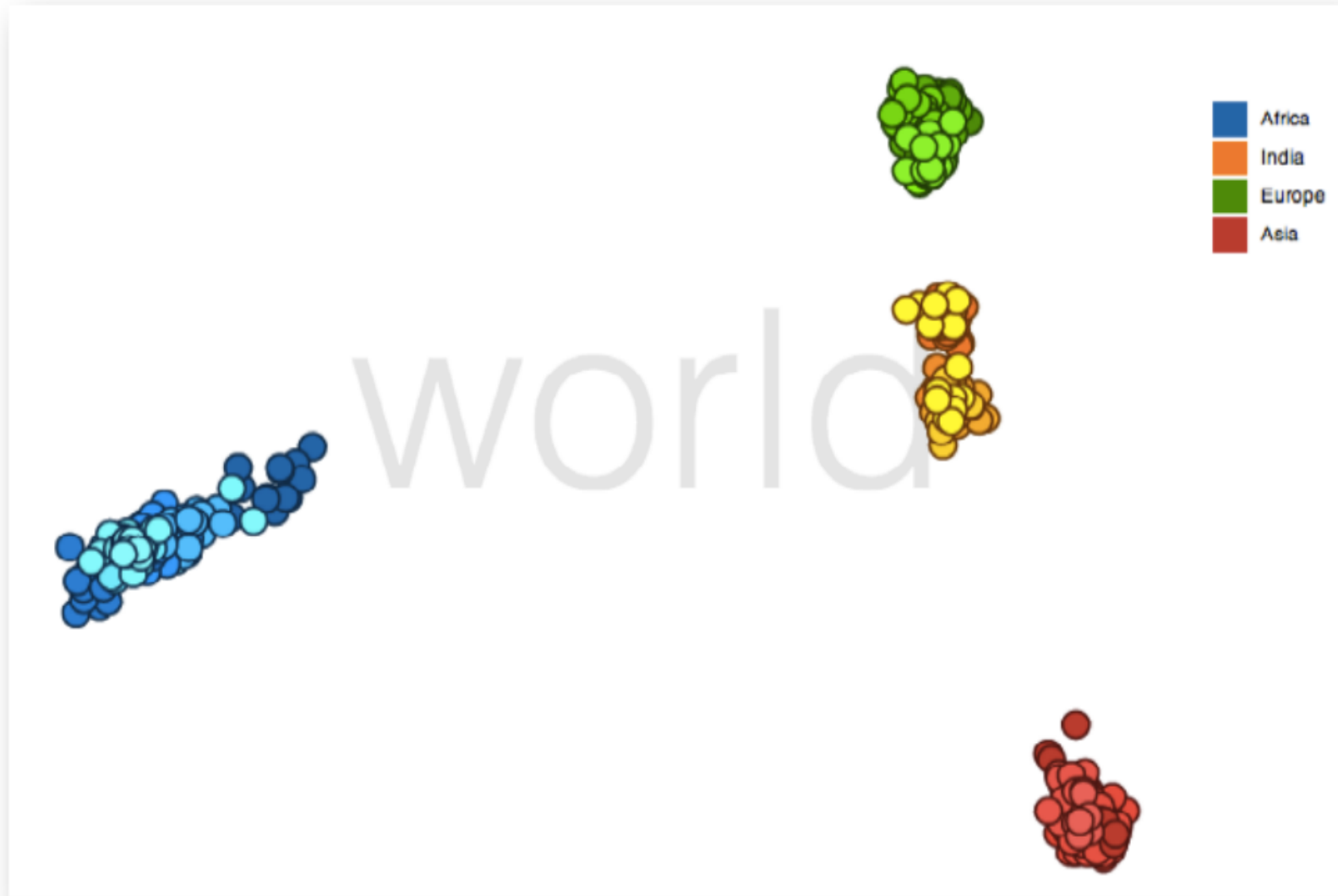


Linear transform:
scale and rotate
original space.

Lines (vectors)
project to lines.

Preserves global
distances.

PCA of Genomes [Demiralp et al. '13]



Non-Linear Techniques

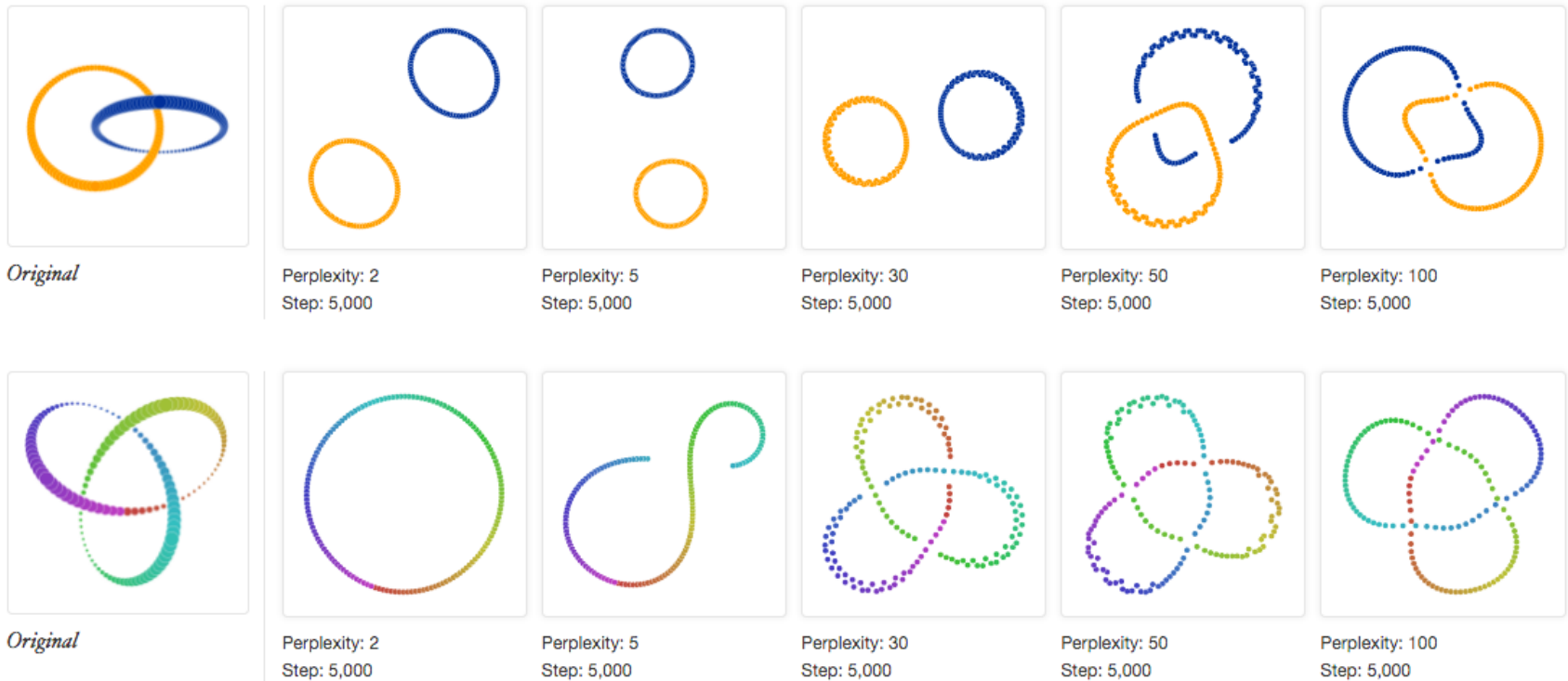
Distort the space, trade-off preservation of global structure to emphasize local neighborhoods. Use topological (nearest neighbor) analysis.

Two popular contemporary methods:

t-SNE - probabilistic interpretation of distance

UMAP - tries to balance local/global trade-off

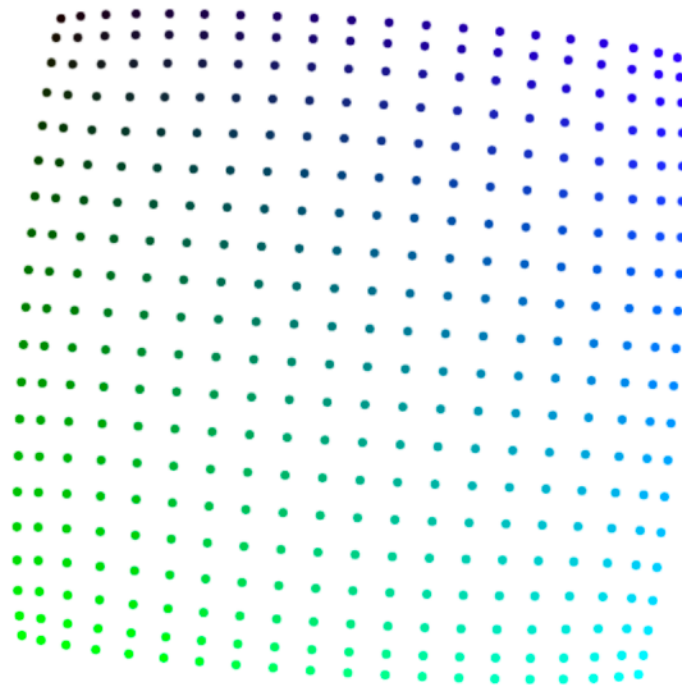
Visualizing t-SNE [Wattenberg et al. '16]



Results can be highly sensitive to the algorithm parameters!

How to Use t-SNE Effectively

Although extremely useful for visualizing high-dimensional data, t-SNE plots can sometimes be mysterious or misleading. By exploring how it behaves in simple cases, we can learn to use it more effectively.



⏸ ↻ Step 1,910
 Points Per Side 20
 Perplexity 10
 Epsilon 5

A square grid with equal spacing between points. Try convergence at different sizes.

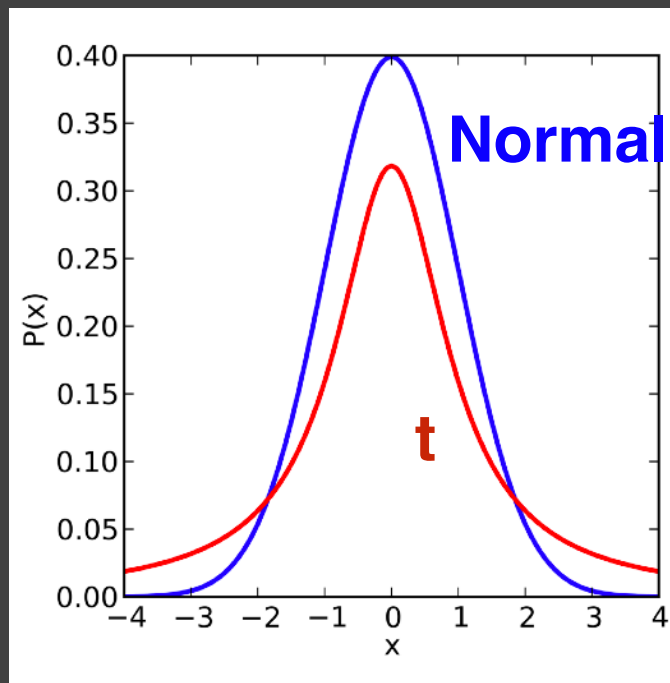
distill.pub

t-SNE [Maaten & Hinton 2008]

1. Model probability \mathbf{P} of one point “choosing” another as its neighbor in the original space, using a Gaussian distribution defined using the distance between points. Nearer points have higher probability than distant ones.

t-SNE [Maaten & Hinton 2008]

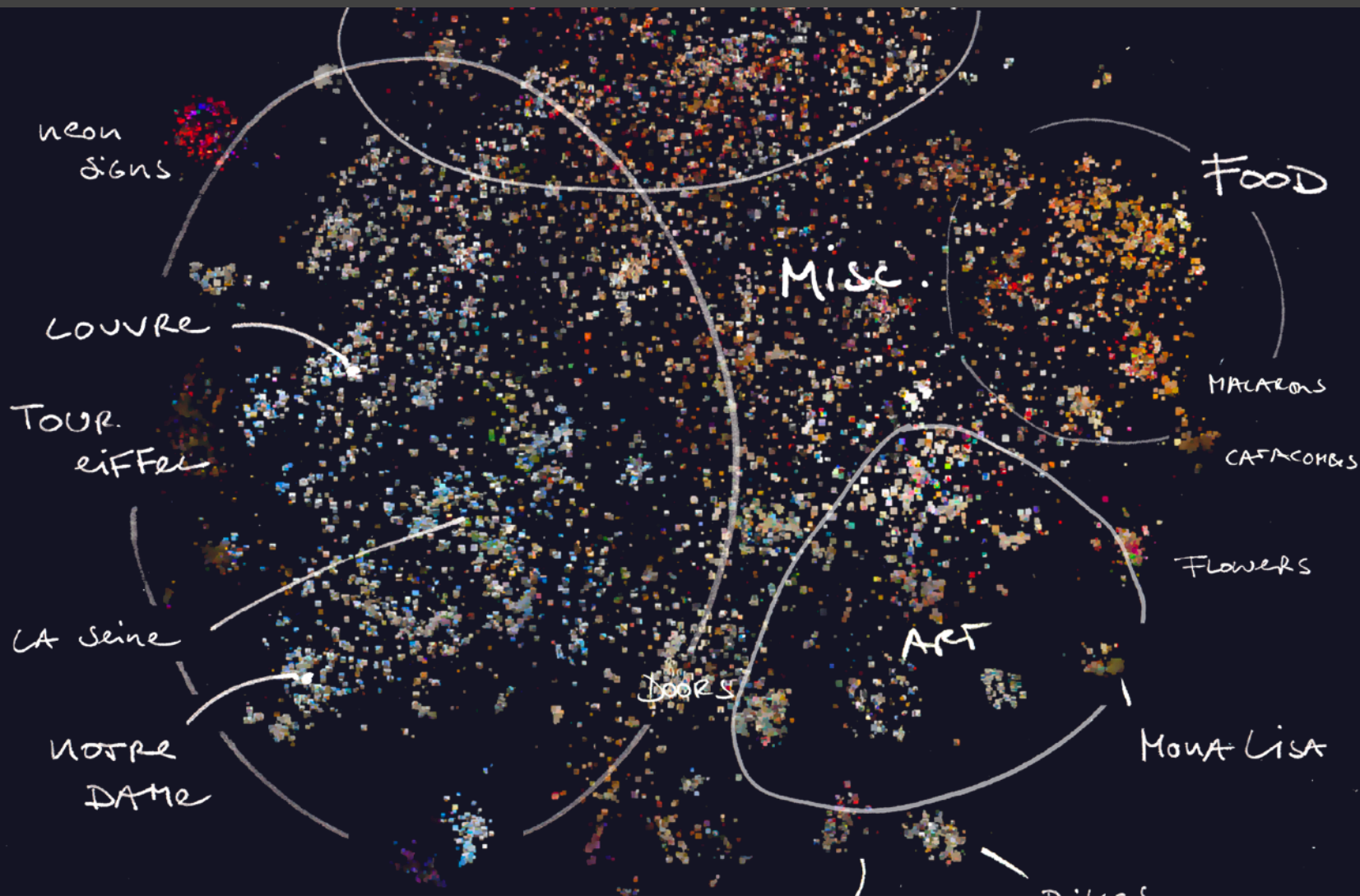
2. Define a similar probability Q in the low-dimensional (2D or 3D) embedding space, using a Student's t distribution (hence the "t-" in "t-SNE"!). The t -distribution is heavy-tailed, allowing distant points to be even further apart.



t-SNE [Maaten & Hinton 2008]

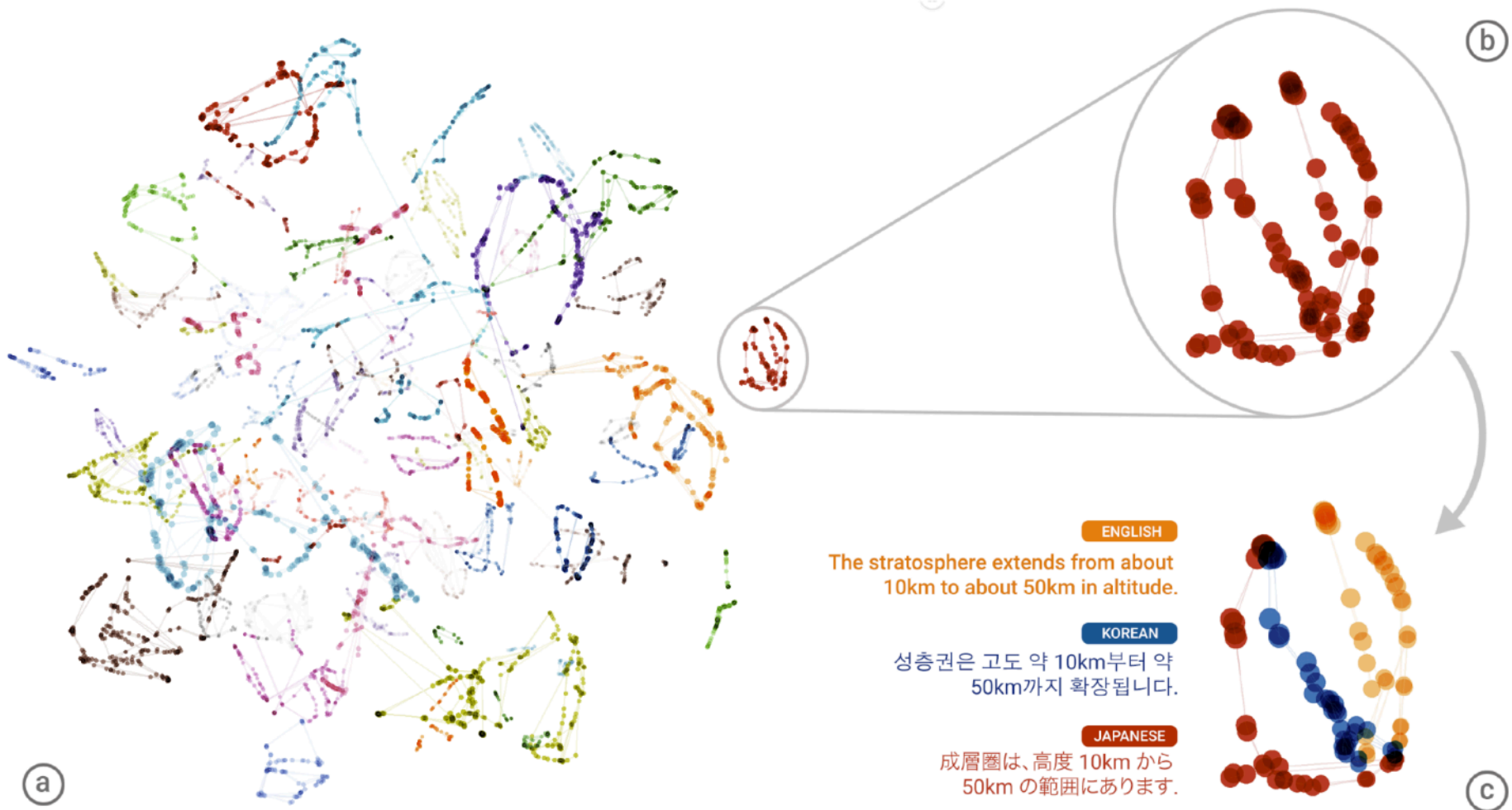
1. Model probability \mathbf{P} of one point “choosing” another as its neighbor in the original space, using a Gaussian distribution defined using the distance between points. Nearer points have higher probability than distant ones.
2. Define a similar probability \mathbf{Q} in the low-dimensional (2D or 3D) embedding space, using a Student’s t distribution (*hence the “t-” in “t-SNE”!*). The t -distribution is heavy-tailed, allowing distant points to be even further apart.
3. Optimize to find the positions in the embedding space that minimize the Kullback-Leibler divergence between the \mathbf{P} and \mathbf{Q} distributions: $KL(P \parallel Q)$

Multiplicity [Stefaner 2018]



t-SNE projection of photos taken in Paris, France

MT Embedding [Johnson et al. 2018]



t-SNE projection of latent space of language translation model.

UMAP [McInnes et al. 2018]

Form weighted nearest neighbor graph, then layout the graph in a manner that balances embedding of local and global structure.

“Our algorithm is competitive with t-SNE for visualization quality and arguably preserves more of the global structure with superior run time performance.” - McInnes et al. 2018

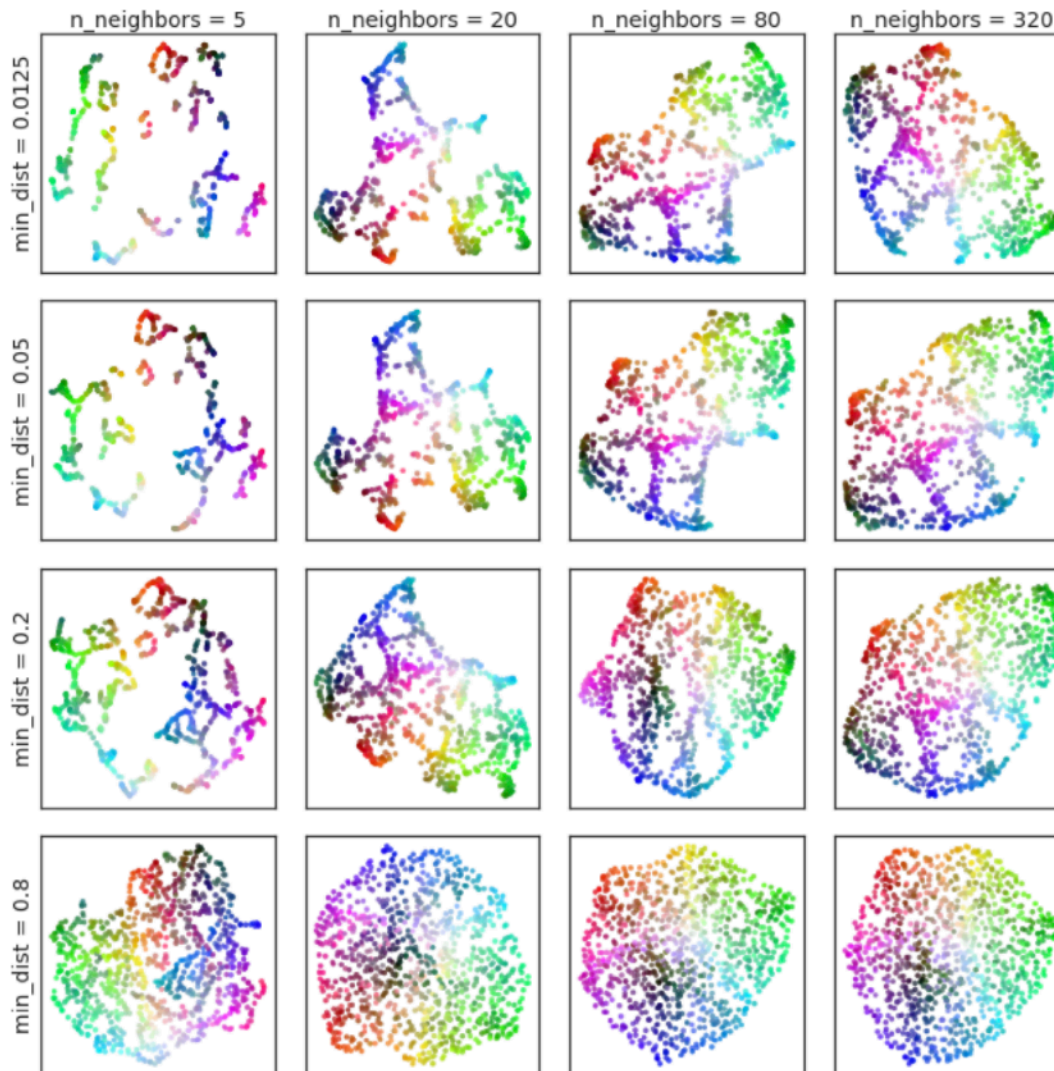
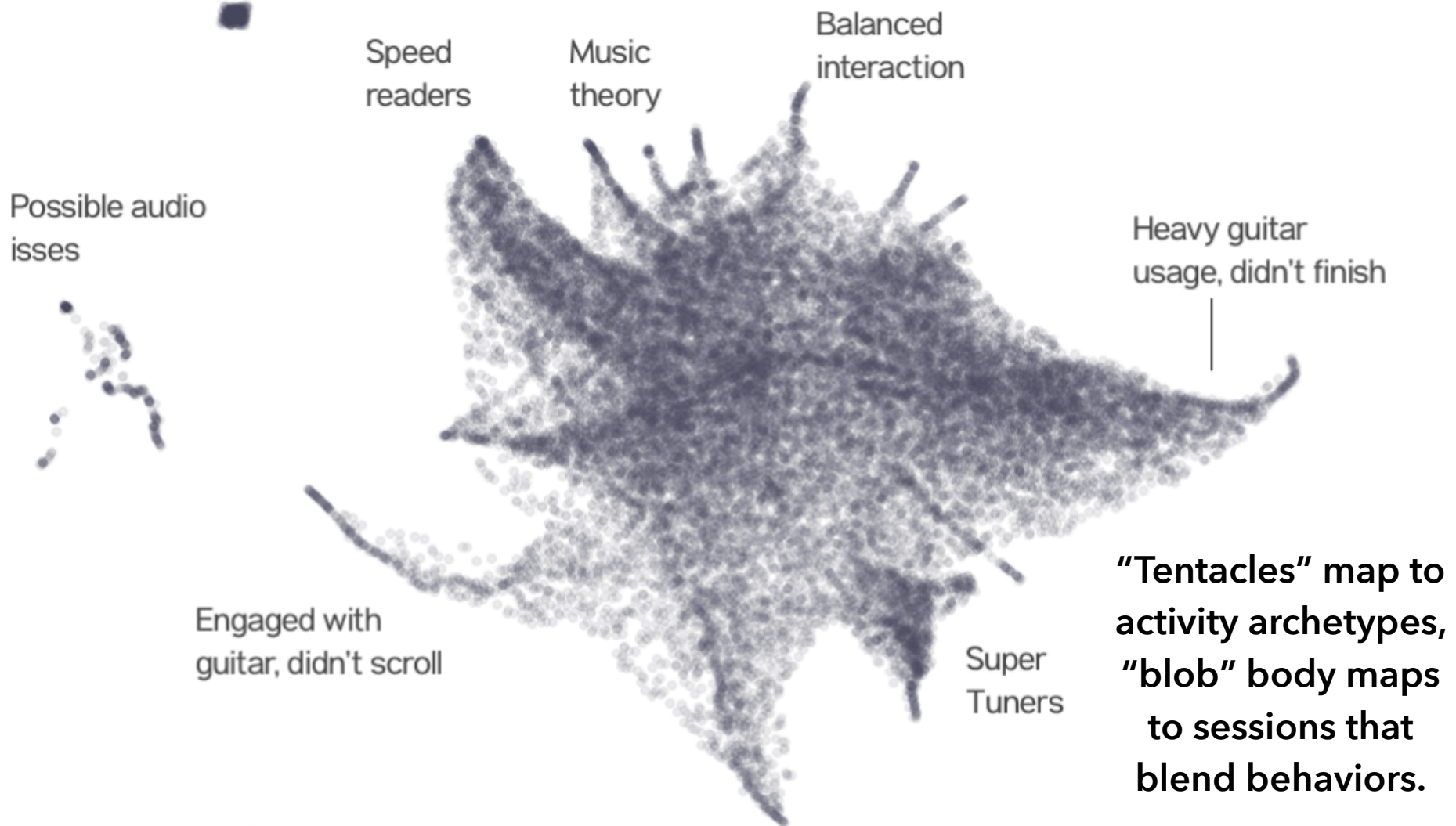


Figure 1: Variation of UMAP hyperparameters n and min_dist result in different embeddings. The data is uniform random samples from a 3-dimensional color-cube, allowing for easy visualization of the original 3-dimensional coordinates in the embedding space by using the corresponding RGB colour. Low values of n spuriously interpret structure from the random sampling noise – see Section 6 for further discussion of this phenomena.

Reader Behavior [Conlen et al. 2019]



UMAP projection of reader activity for an interactive article.

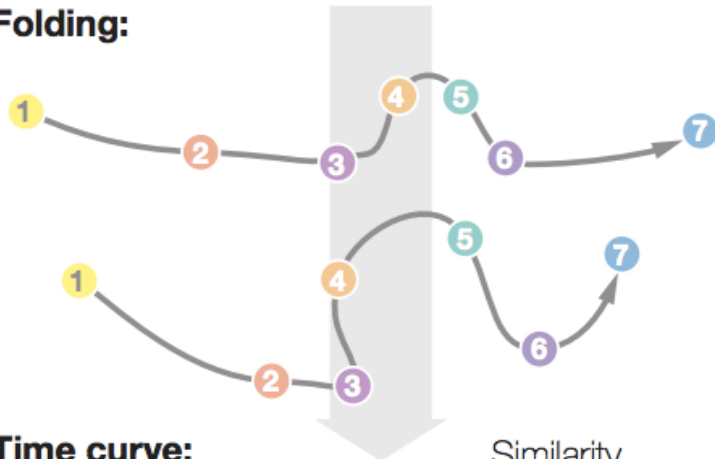
Time Curves [Bach et al. '16]

Timeline:



Circles are data cases with a time stamp.
Similar colors indicate similar data cases.

Folding:

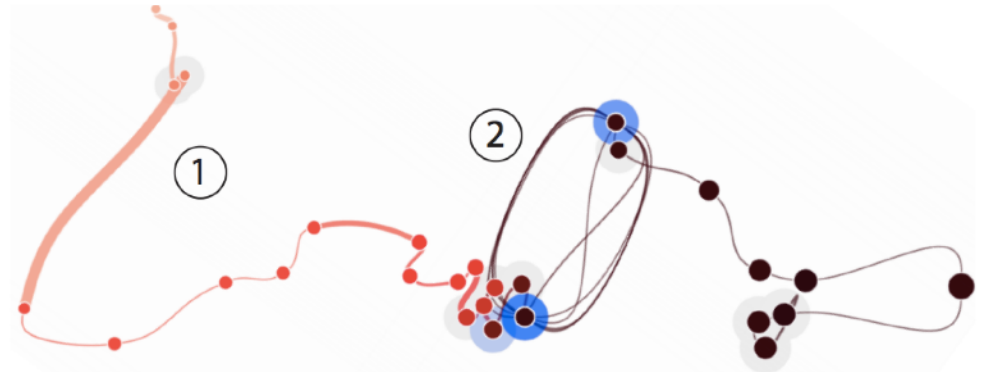


Time curve:

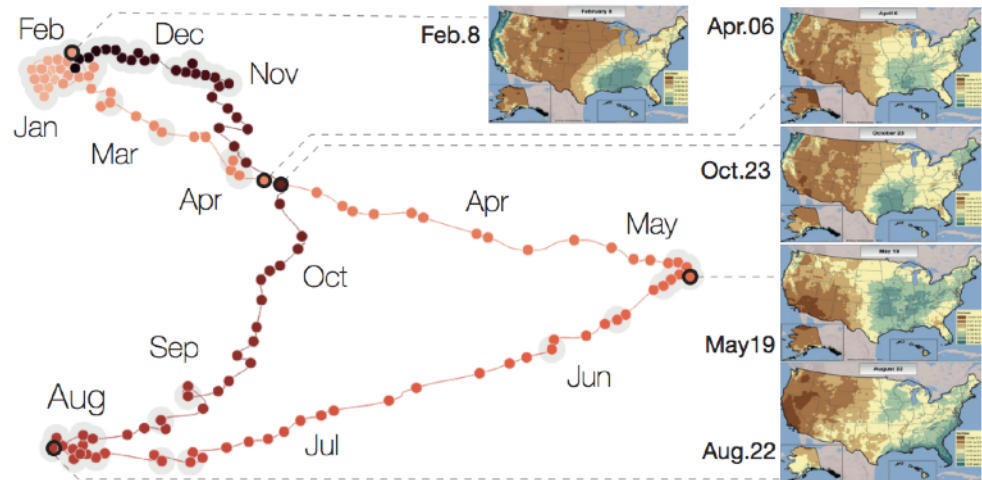


The temporal ordering of data cases is preserved.
Spatial proximity now indicates similarity.

(a) Folding time



Wikipedia "Chocolate" Article



U.S. Precipitation over 1 Year

Visual Encoding Design

Use **expressive** and **effective** encodings

Reduce the problem space

Avoid **over-encoding**

Use **space** and **small multiples** intelligently

Use **interaction** to generate *relevant* views

Rarely does a single visualization answer all questions. Instead, the ability to generate appropriate visualizations quickly is critical!

About the design process...

Visualization draws upon both science and art!

Principles like expressiveness & effectiveness are not hard-and-fast rules, but can assist us to guide the process and articulate alternatives.

They can lead us to think more deeply about our design rationale and prompt us to reflect.

It helps to know “the rules” in order to wisely bend (*or break*) them at the right times!