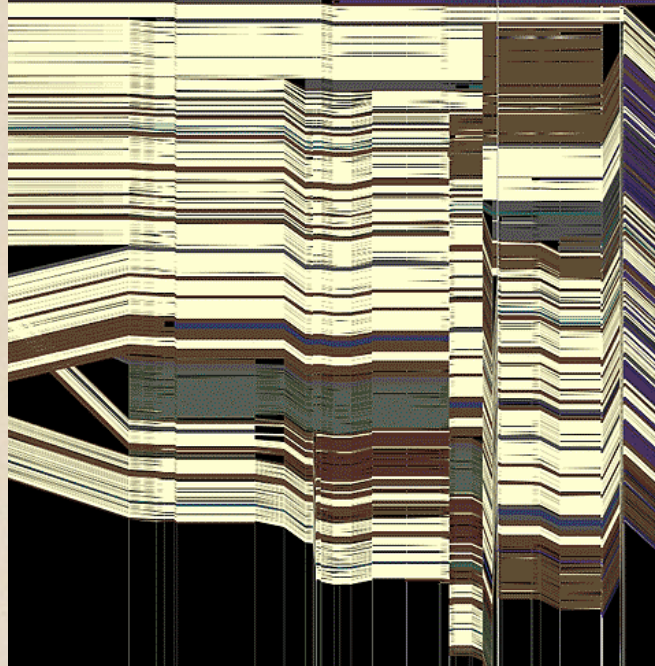
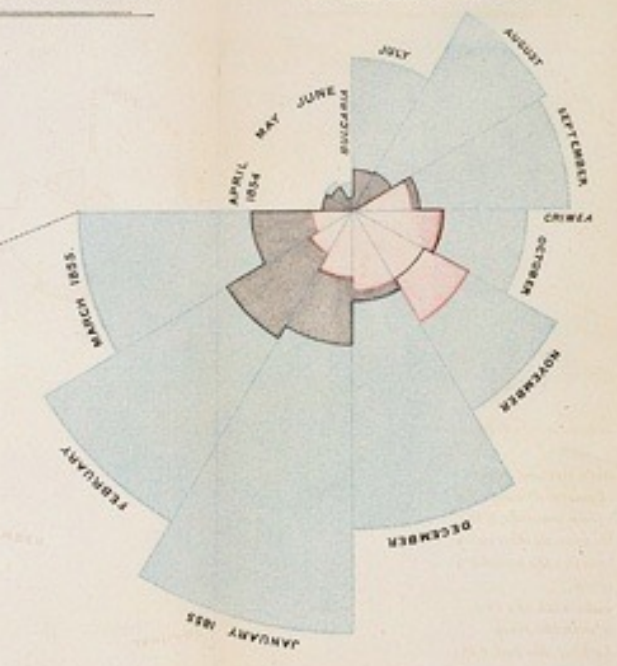


# CSE 442 - Data Visualization

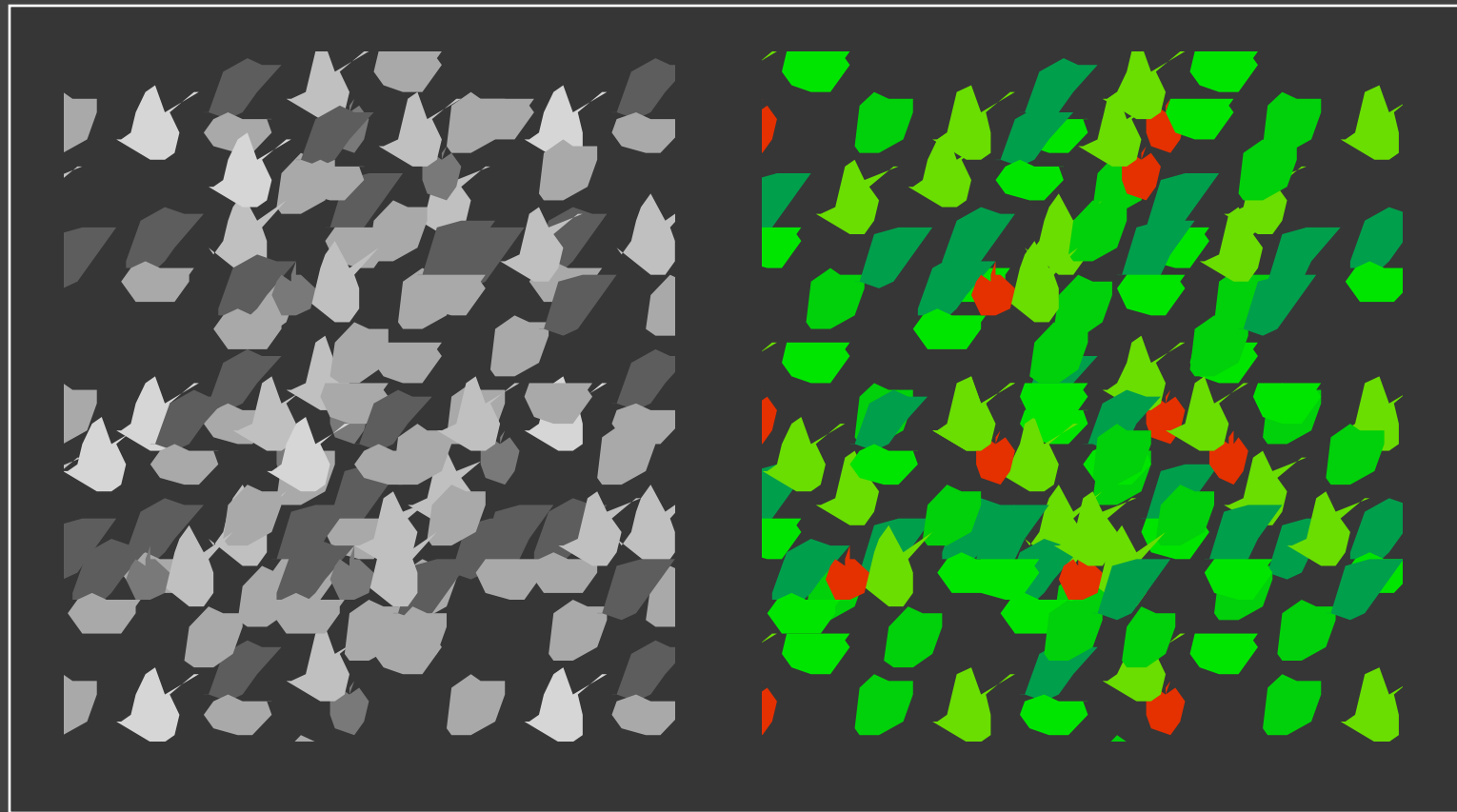
# Color



Jeffrey Heer University of Washington

# Color in Visualization

Identify, Group, Layer, Highlight



# Purpose of Color

To label

To measure

To represent and imitate

To enliven and decorate

*"Above all, do no harm."*

- Edward Tufte

# Topics

## **Perception of Color**

Light, Visual system, Mental models

## **Color in Information Visualization**

Nominal, Ordinal & Quantitative encoding

Guidelines for color palette design

# Perception of Color

What color is this?

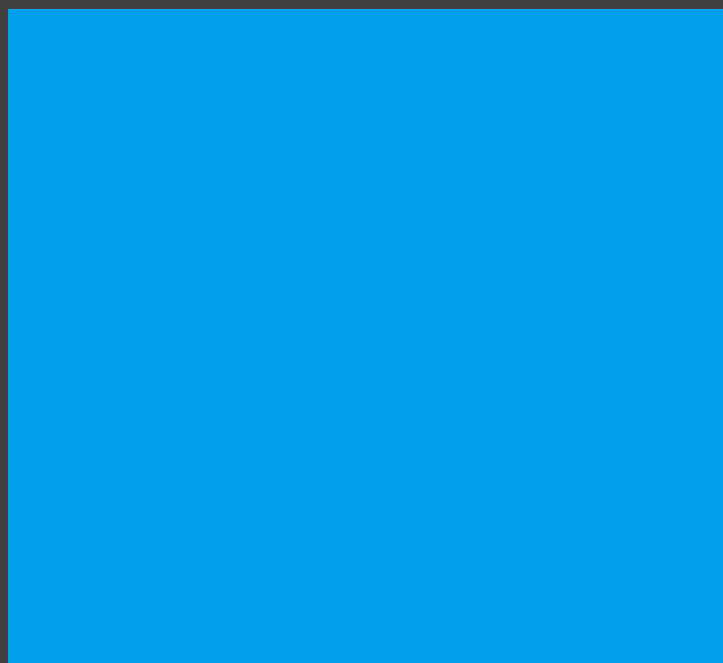


What color is this?



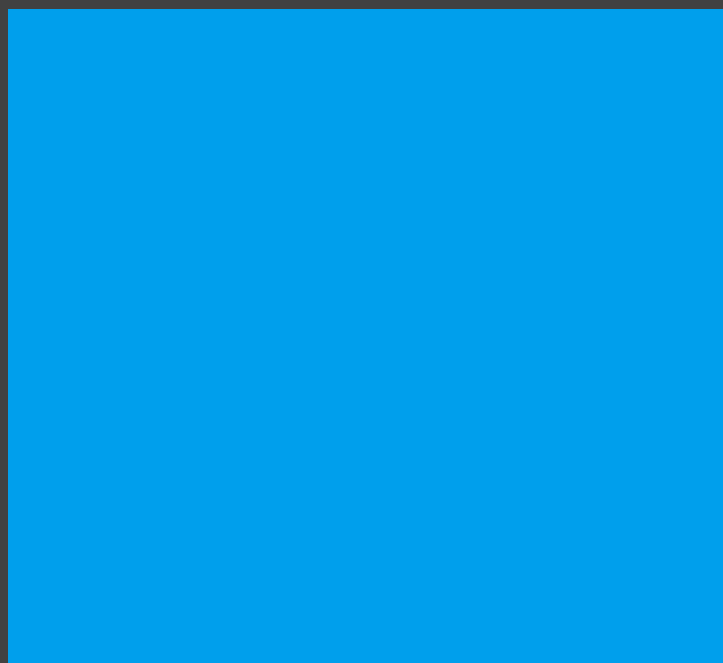
"Yellow"

What color is this?



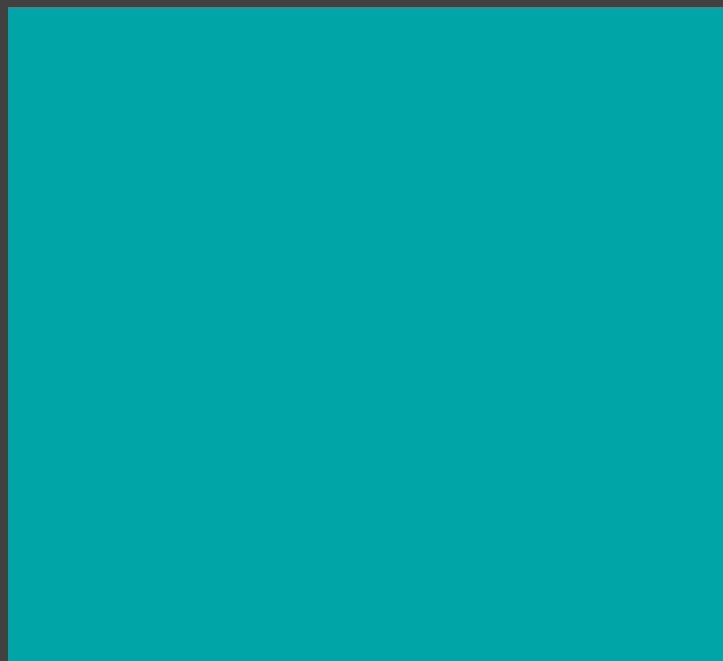


What color is this?



"Blue"

What color is this?

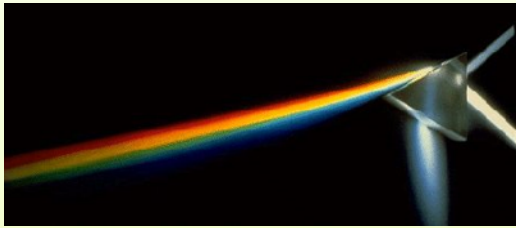


What color is this?

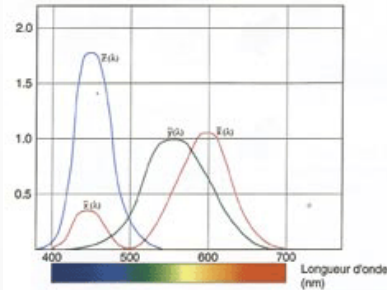


"Teal" ?

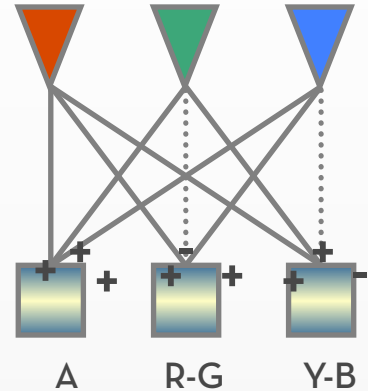
# Perception of Color



Light



Cone Response



Opponent Signals

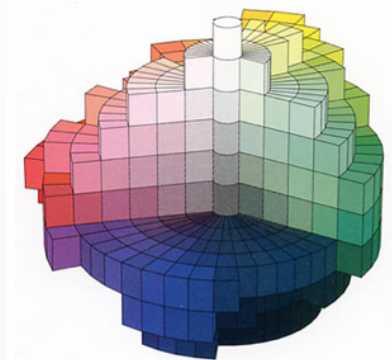
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



Color Perception

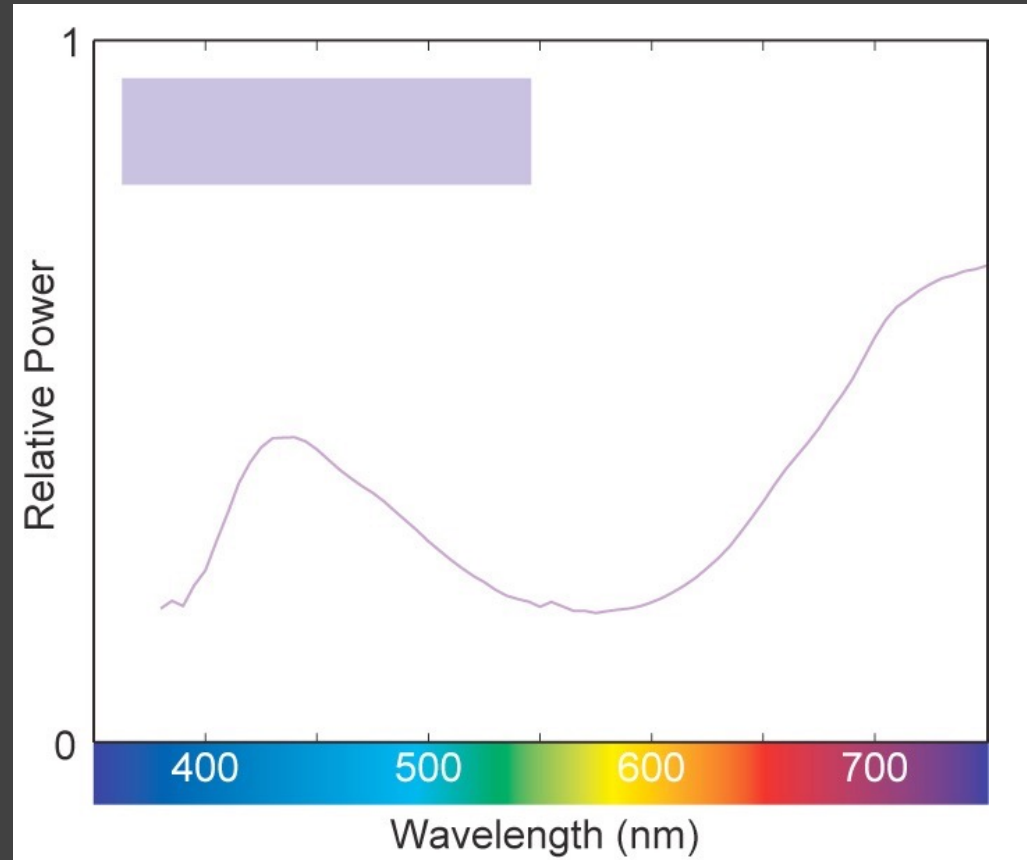
# Physicist's View

Light as electromagnetic wave

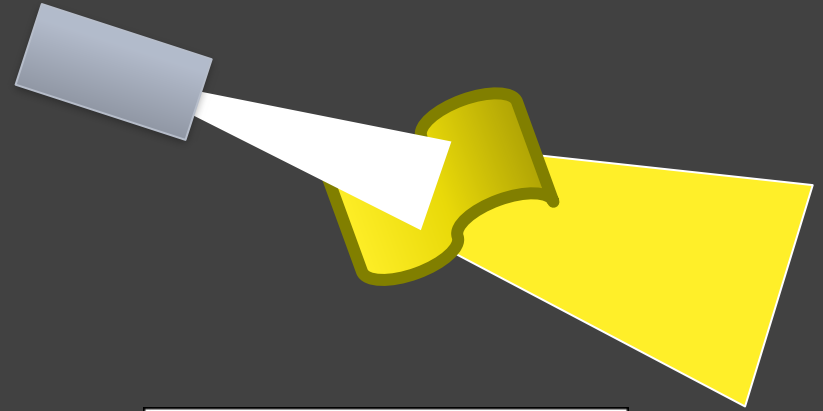
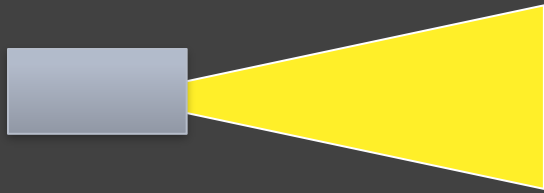
Wavelength

Energy or

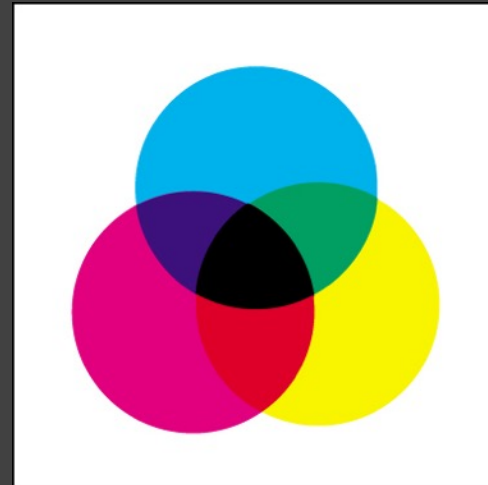
"Relative luminance"



# Emissive vs. Reflective Light

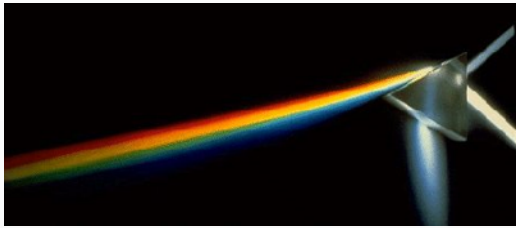


Additive  
(digital displays)

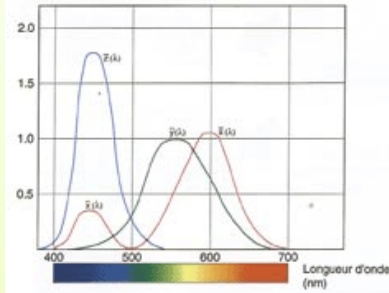


Subtractive  
(print, e-paper)

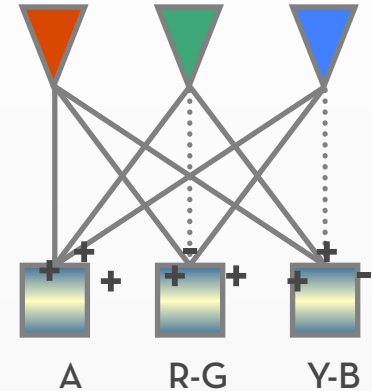
# Perception of Color



Light



Cone Response



Opponent Signals

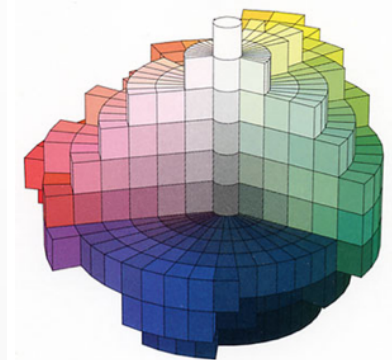
“Yellow”

Color Cognition



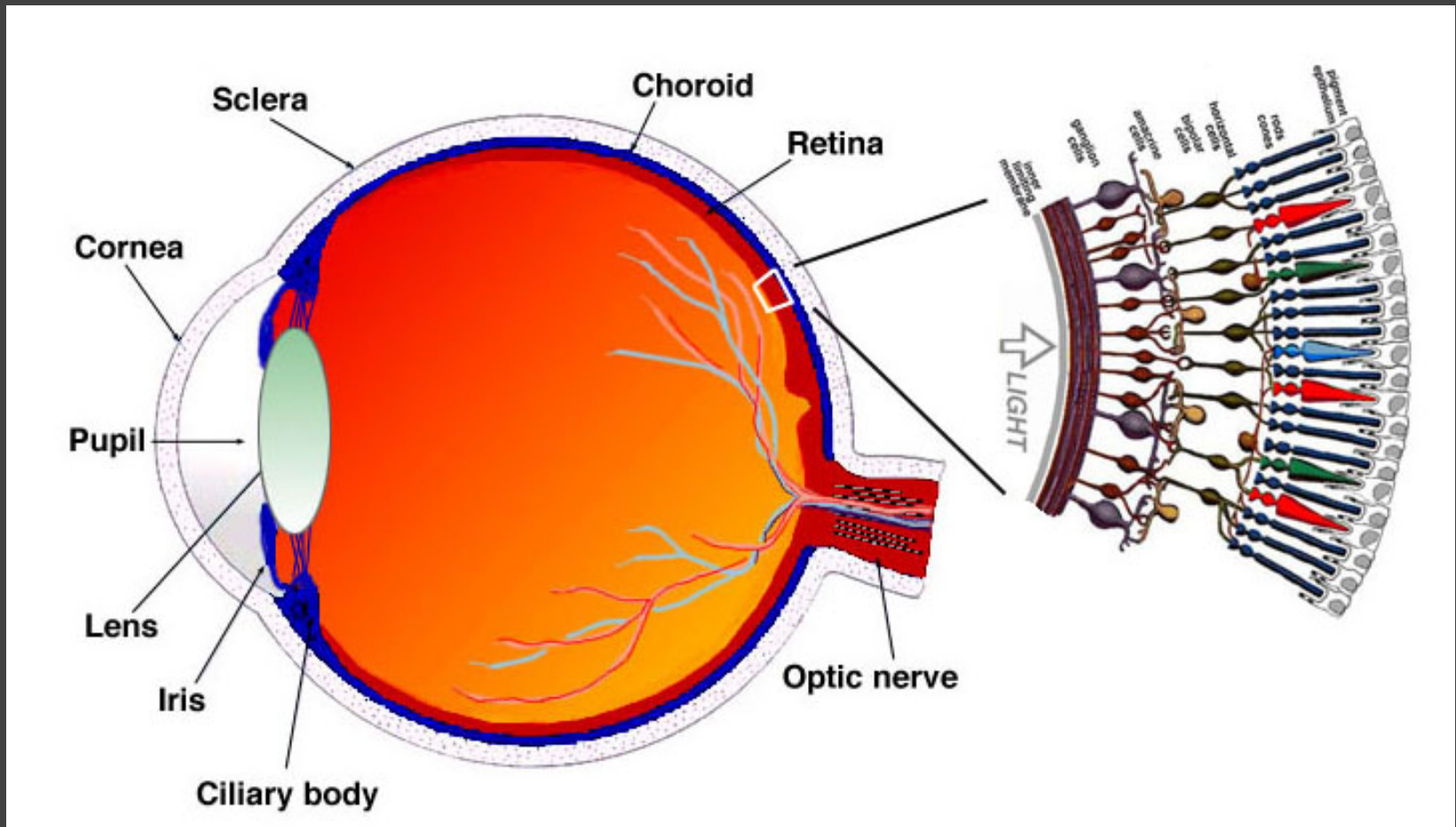
Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



Color Perception

# Retina



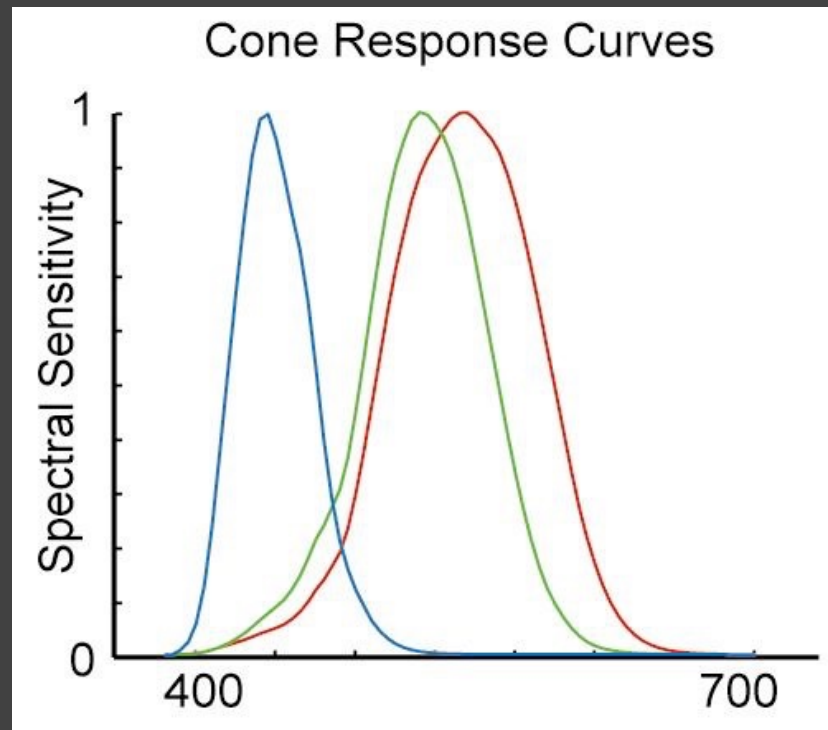
*Simple Anatomy of the Retina, Helga Kolb*



# As light enters our retina...

LMS (Long, Middle, Short) Cones

Sensitive to different wavelength

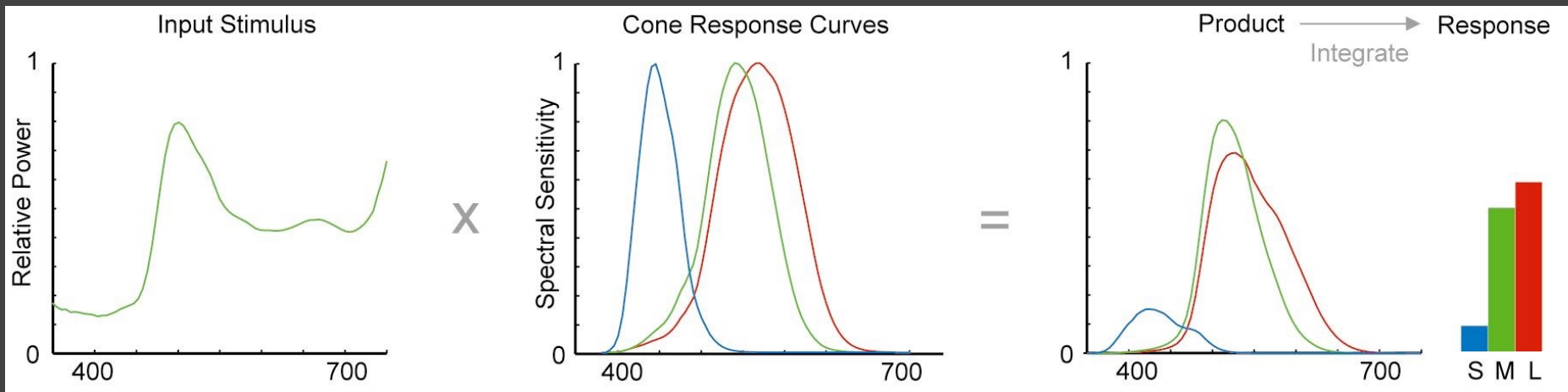


# As light enters our retina...

## LMS (Long, Middle, Short) Cones

Sensitive to different wavelength

Integration with input stimulus



# Effects of Retina Encoding

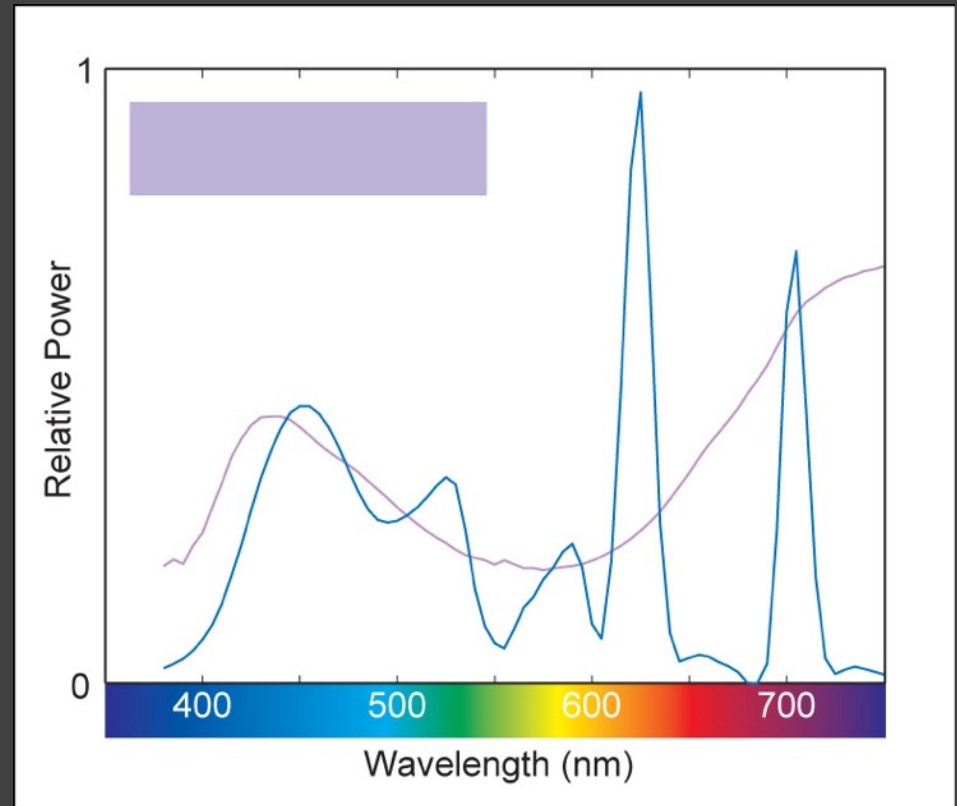
Spectra that stimulate the same LMS response are indistinguishable (a.k.a. "metamers").

## "Tri-stimulus"

Computer displays

Digital scanners

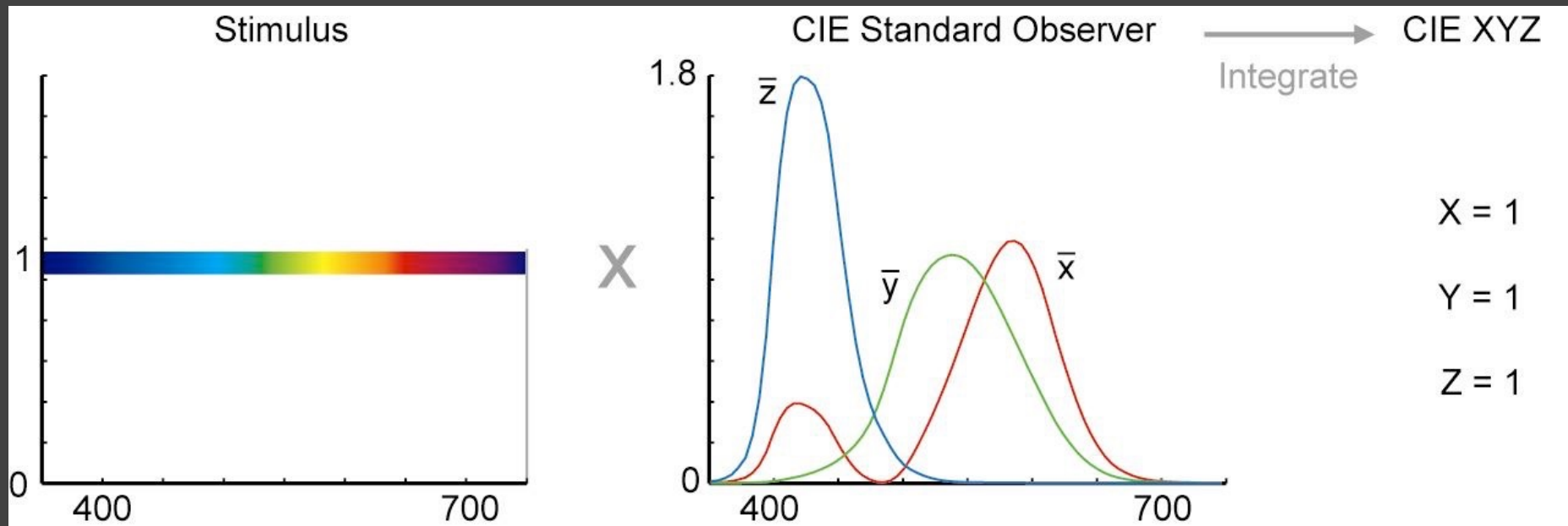
Digital cameras



# CIE XYZ Color Space

Standardized in 1931 to mathematically represent tri-stimulus response.

“Standard observer” response curves

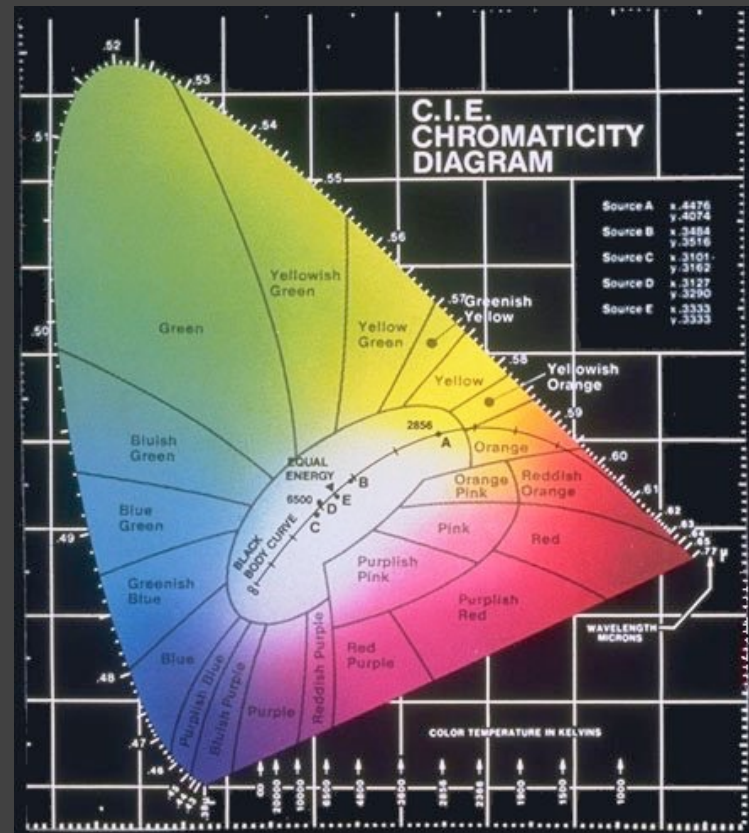


# CIE Chromaticity Diagram

Colorfulness vs. Brightness

$$x = X/(X+Y+Z)$$

$$y = Y/(X+Y+Z)$$

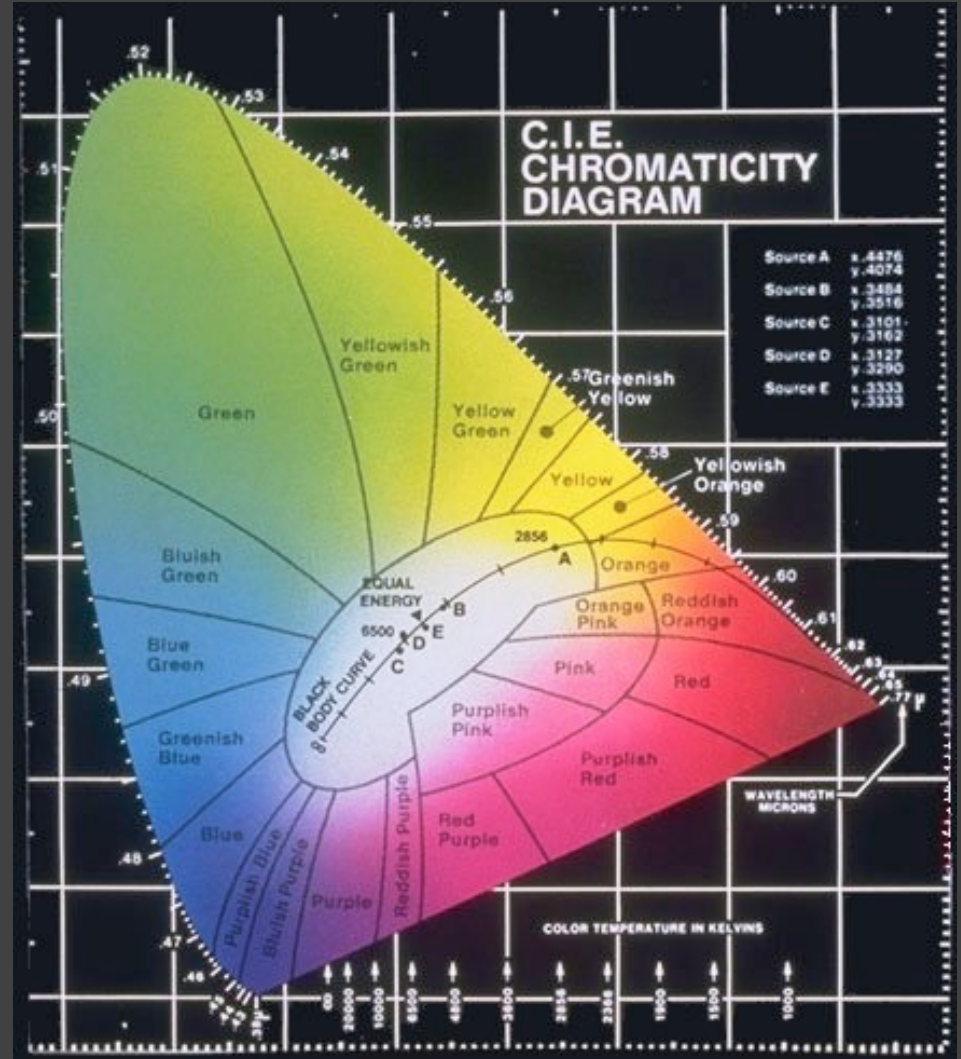


# CIE Chromaticity Diagram

Spectrum locus

Purple line

Mixture of two lights appears as a straight line.



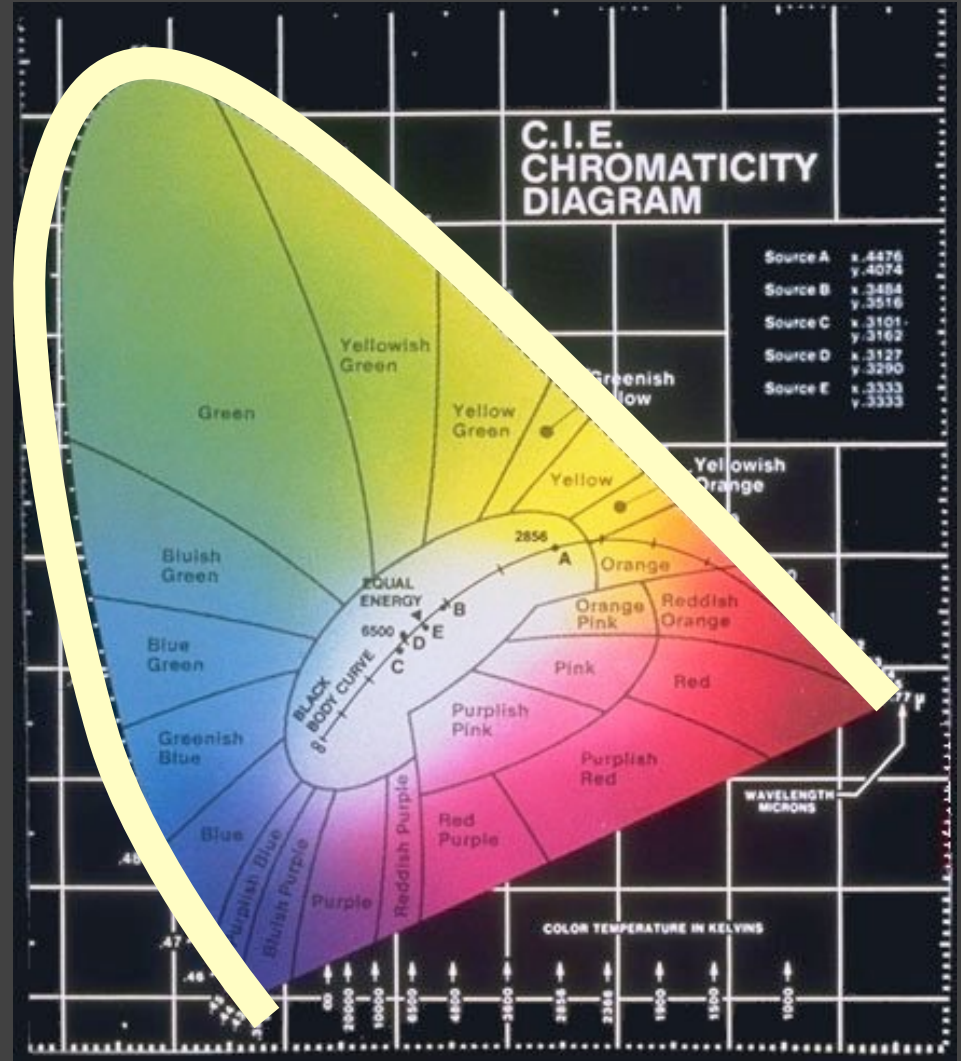


# CIE Chromaticity Diagram

Spectrum locus

Purple line

Mixture of two lights appears as a straight line.

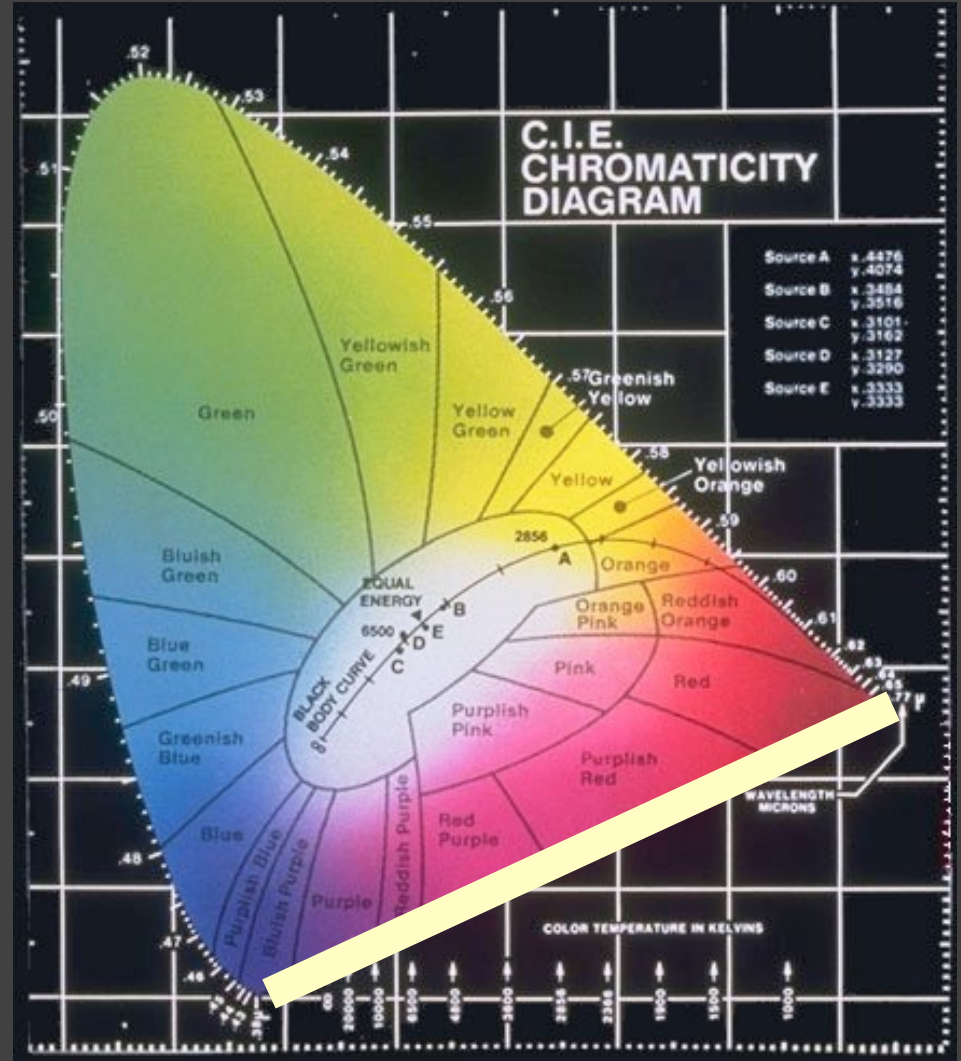


# CIE Chromaticity Diagram

Spectrum locus

Purple line

Mixture of two lights appears as a straight line.



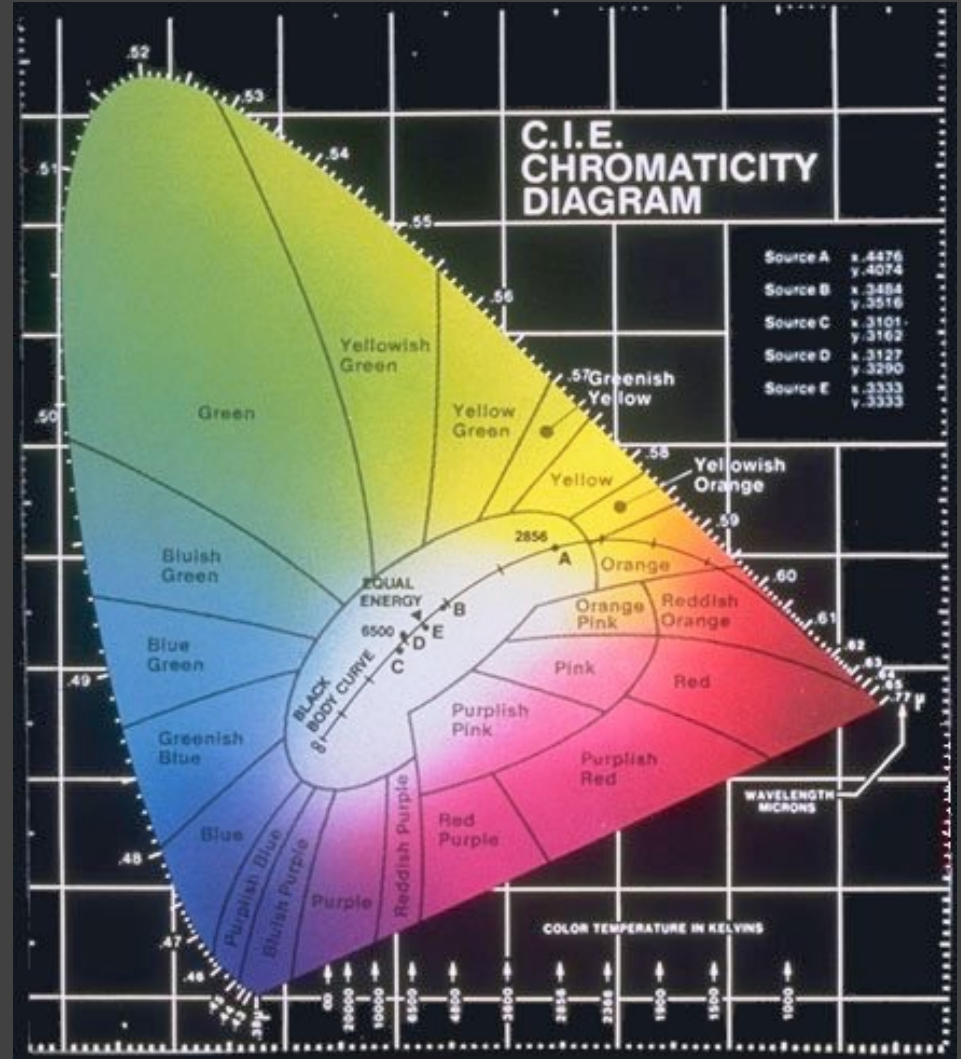


# CIE Chromaticity Diagram

Spectrum locus

Purple line

Mixture of two lights appears as a straight line.

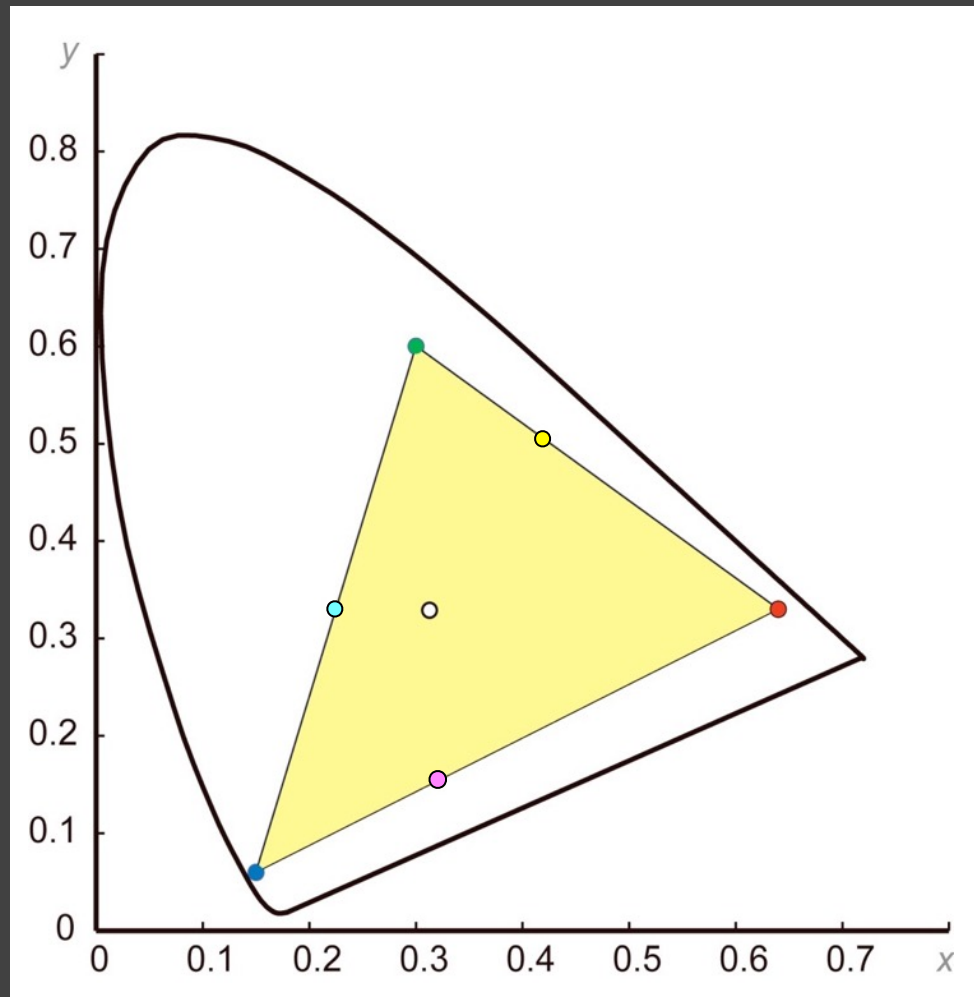


# Display Gamuts

Typically defined by:

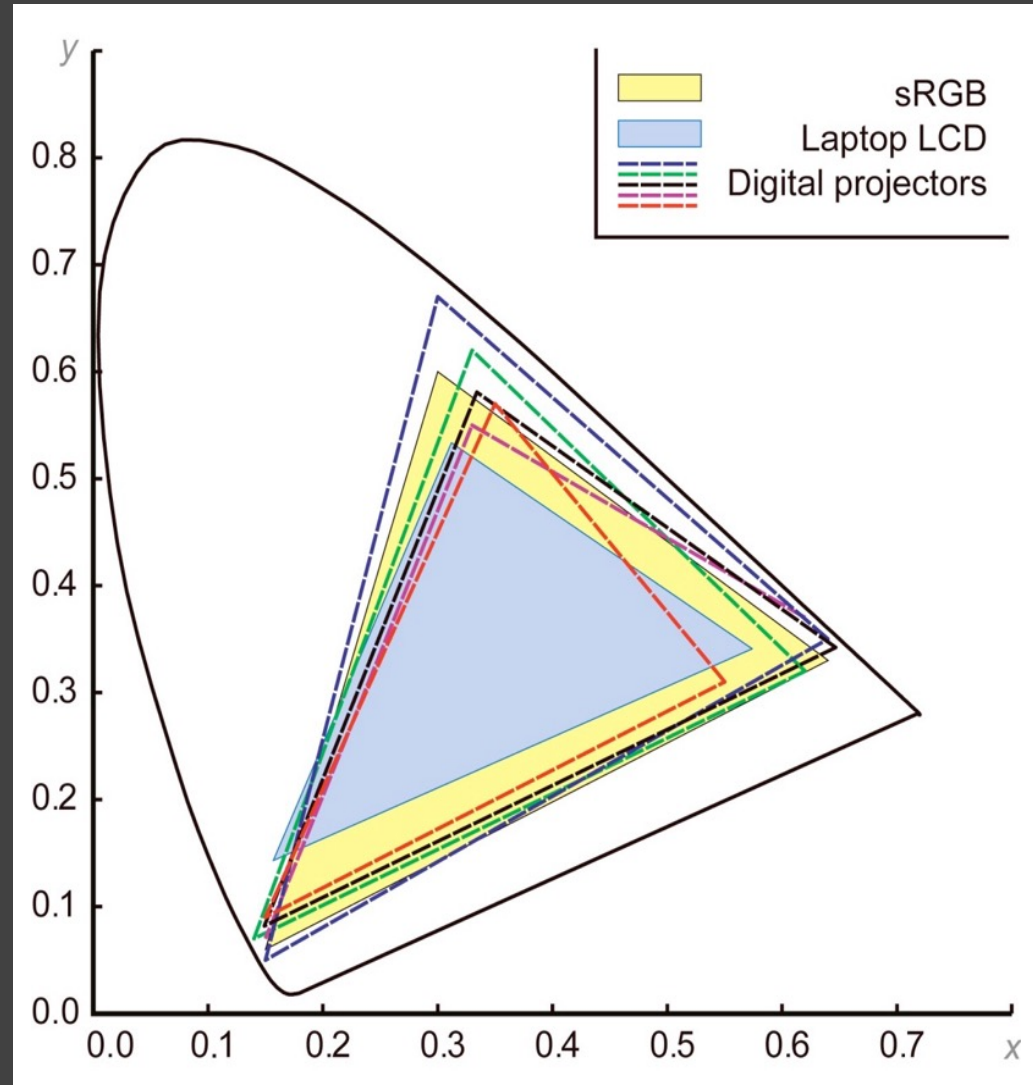
3 Colorants

Convex region



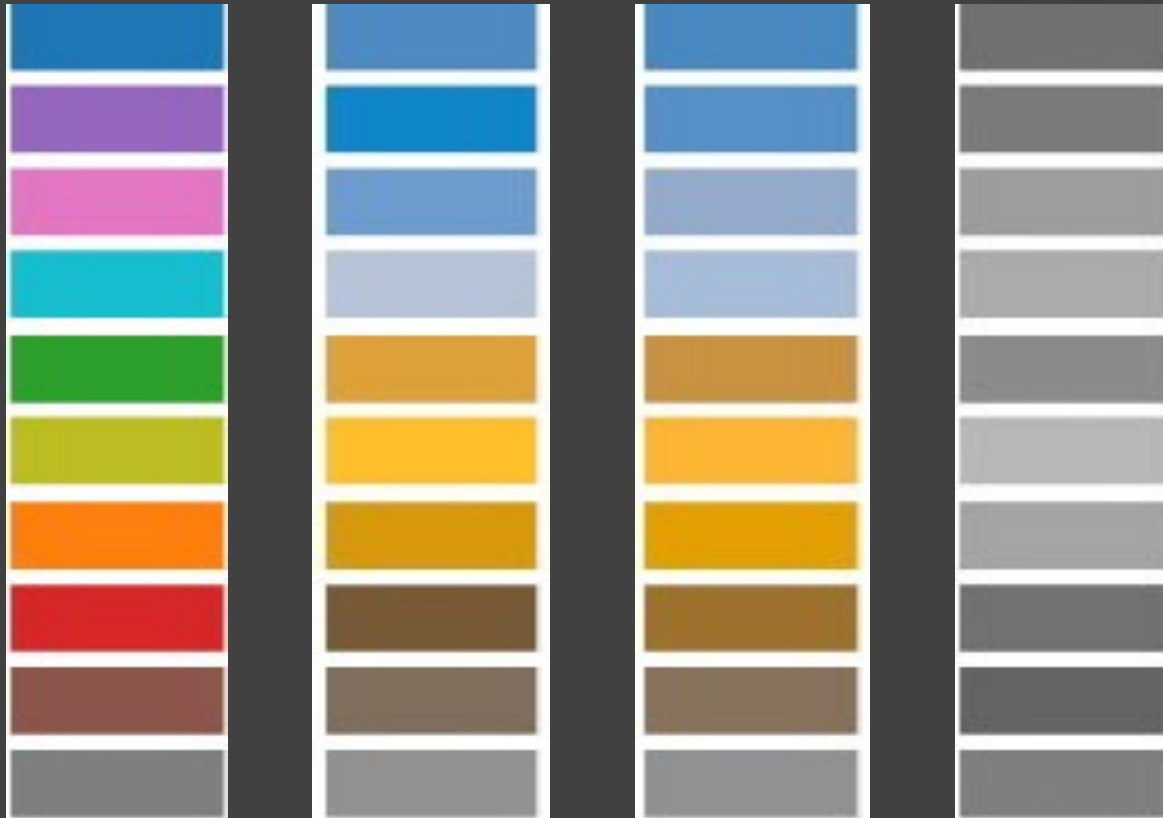
# Display Gamuts

Deviations from  
sRGB specification



# Color Blindness

Missing one or more cones or rods in retina.

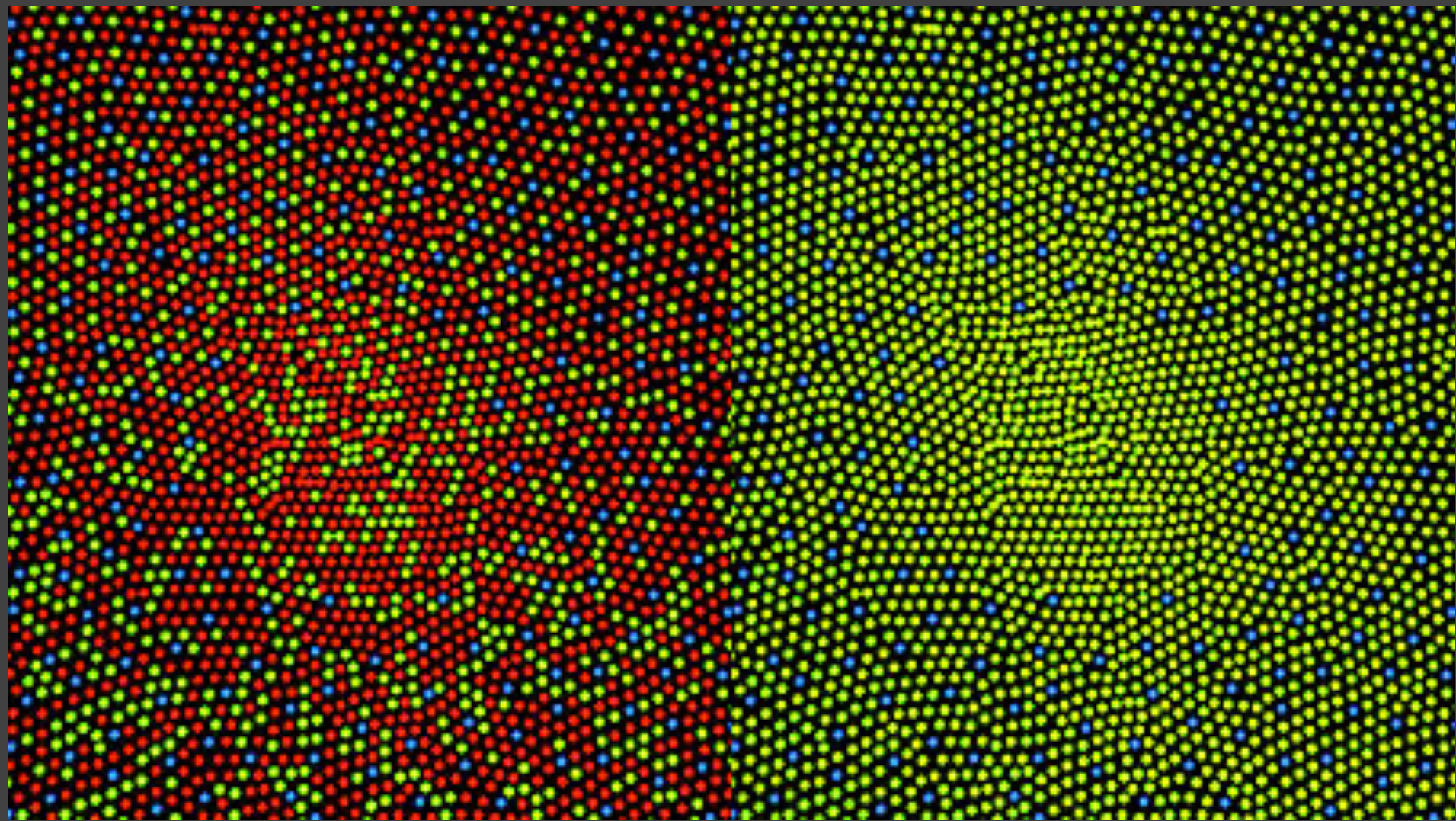


Protanope

Deuteranope

Luminance





Normal Retina

Protanopia



# Color Blindness Simulators

Simulate color vision deficiencies

Browser plug-ins (NoCoffee, SEE, ...)

Photoshop plug-ins, etc...



Deuteranope



Protanope

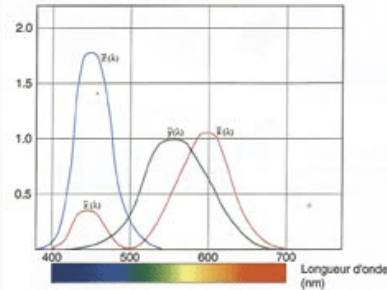


Tritanope

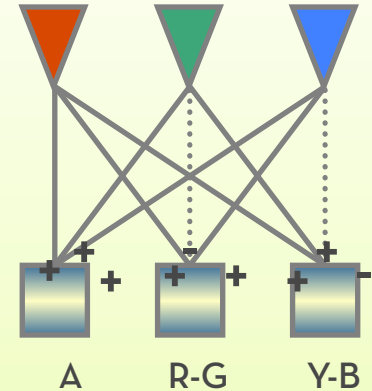
# Perception of Color



Light



Cone Response



Opponent Signals

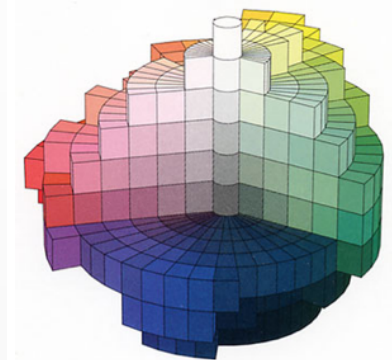
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



Color Perception

# Primary Colors

To paint "all colors":

Leonardo da Vinci, circa 1500 described in his notebooks a list of simple colors...

**Yellow**

**Blue**

**Green**

**Red**



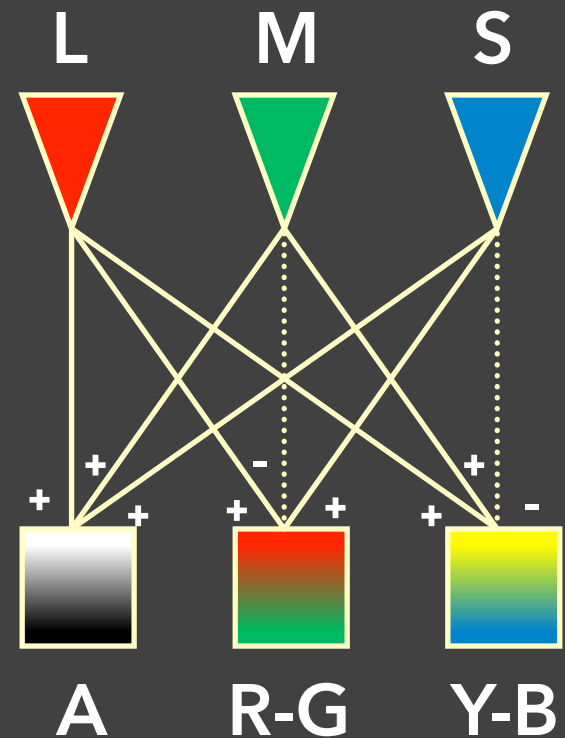
# Opponent Processing

LMS are combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



Fairchild

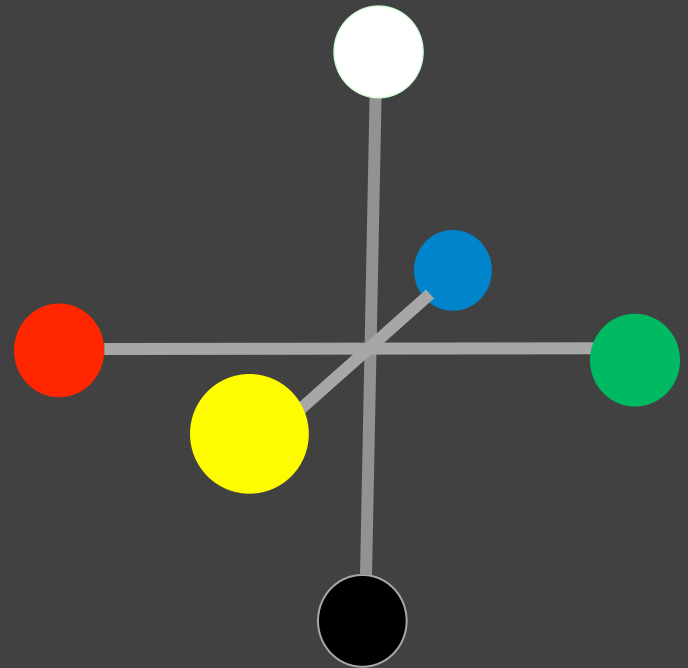
# Opponent Processing

LMS are combined to create:

Lightness

Red-green contrast

Yellow-blue contrast



# Opponent Processing

**LMS are combined to create:**

Lightness

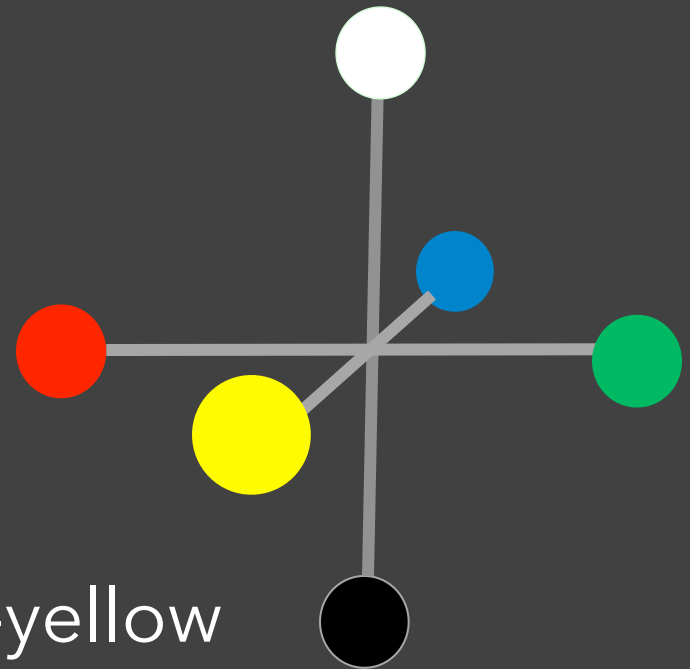
Red-green contrast

Yellow-blue contrast

**Experiments:**

No reddish-green, no blueish-yellow

Color after images



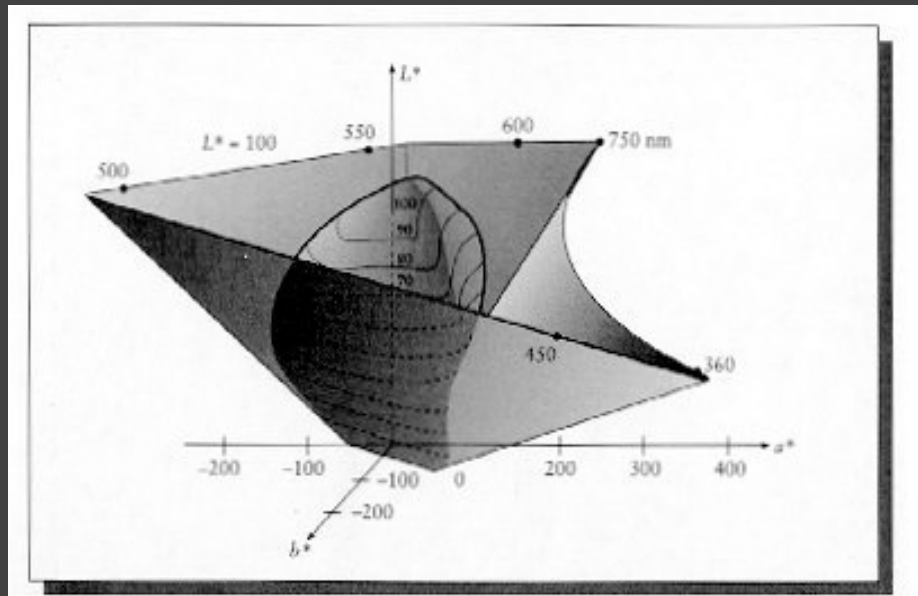
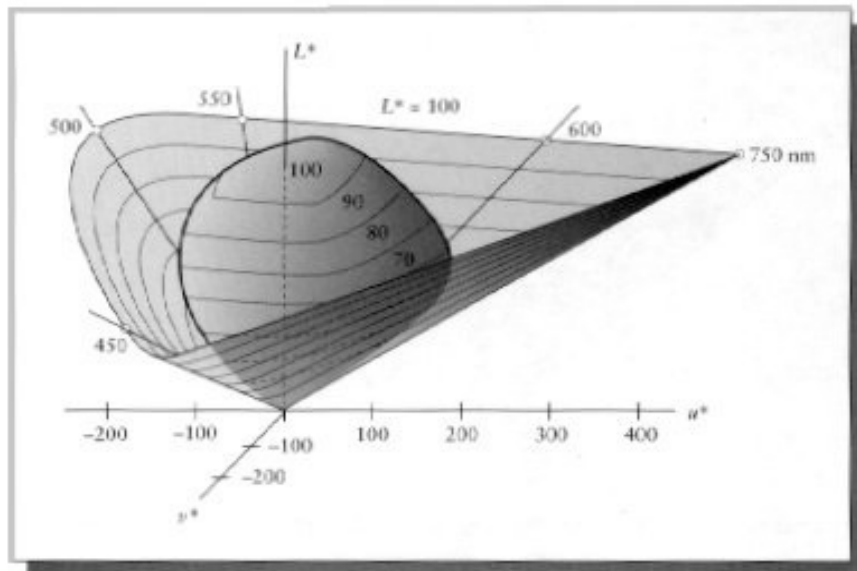




# CIE LAB and LUV Color Spaces

Standardized in 1976 to mathematically represent opponent processing theory.

Non-linear transformation of CIE XYZ



# CIE LAB Color Space

Axes correspond to opponent signals

$L^*$  = Luminance

$a^*$  = Red-green contrast

$b^*$  = Yellow-blue contrast

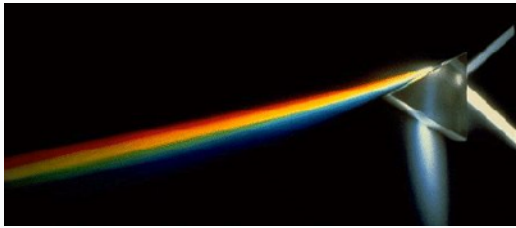
Much more perceptually uniform than sRGB!

Scaling of axes to represent "color distance"

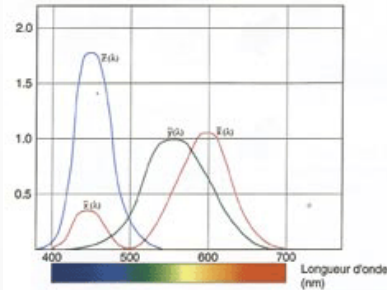
JND = Just noticeable difference (~2.3 units)

D3 includes LAB color space support!

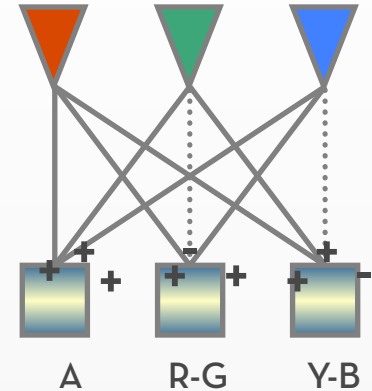
# Perception of Color



Light



Cone Response



Opponent Signals

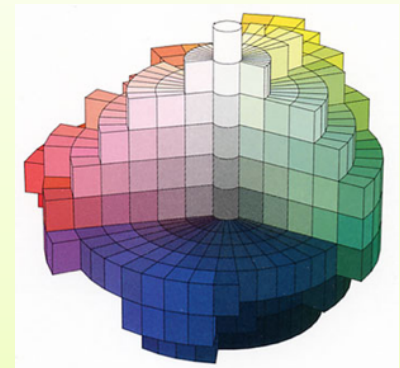
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance

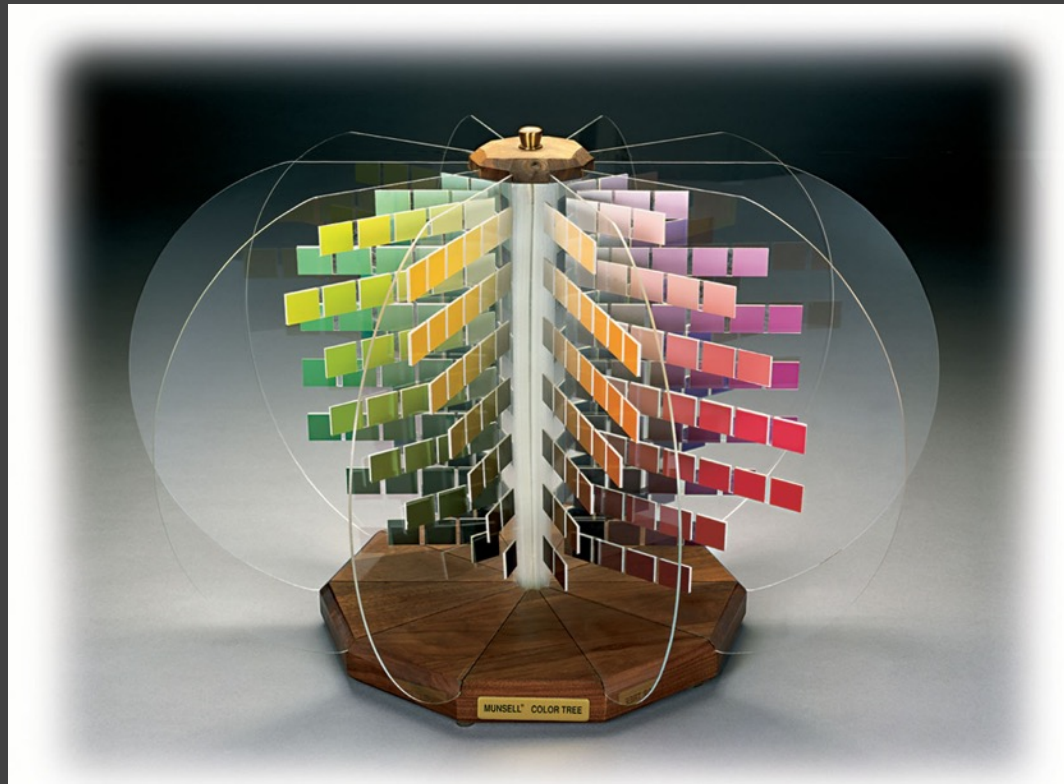


Color Perception

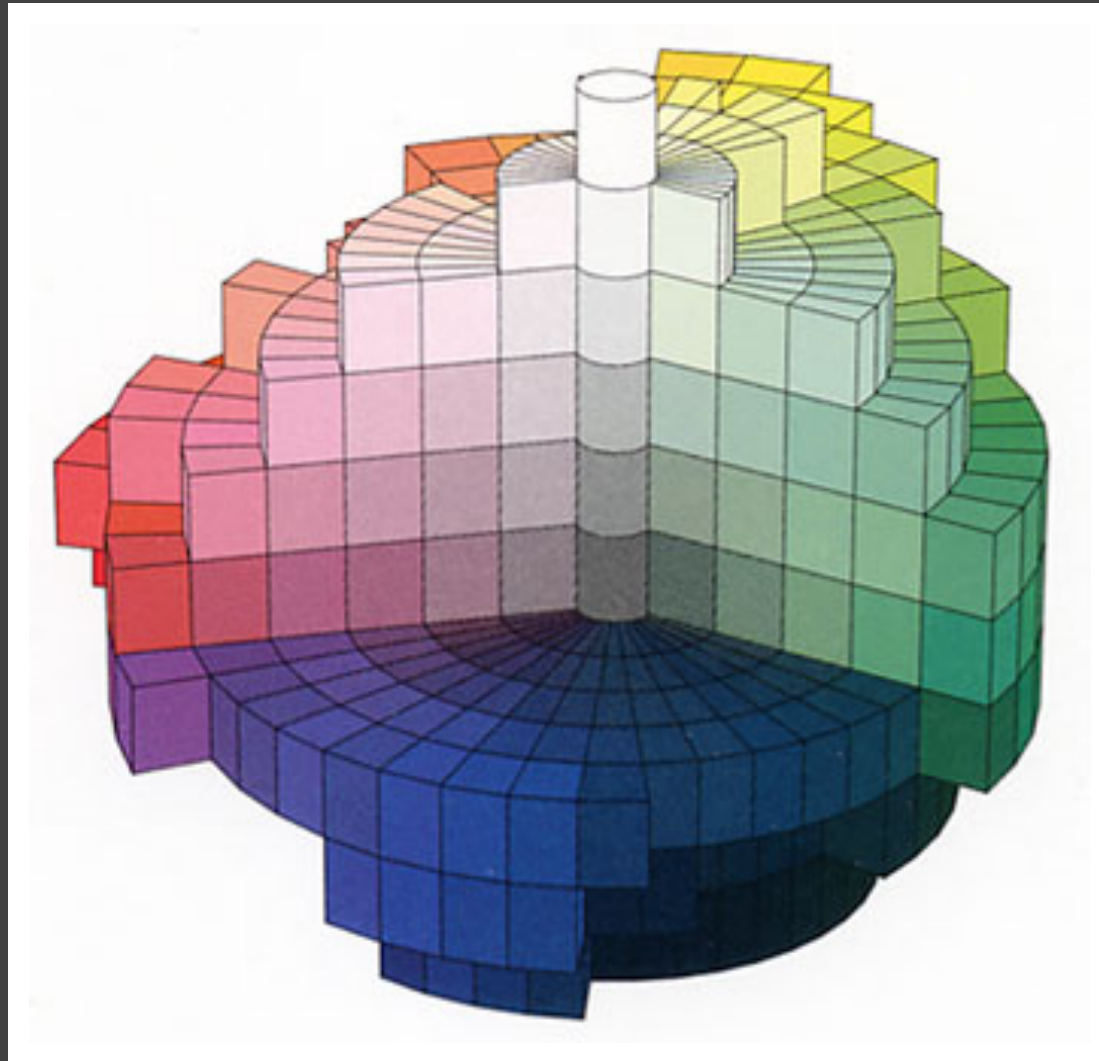


# Albert Munsell

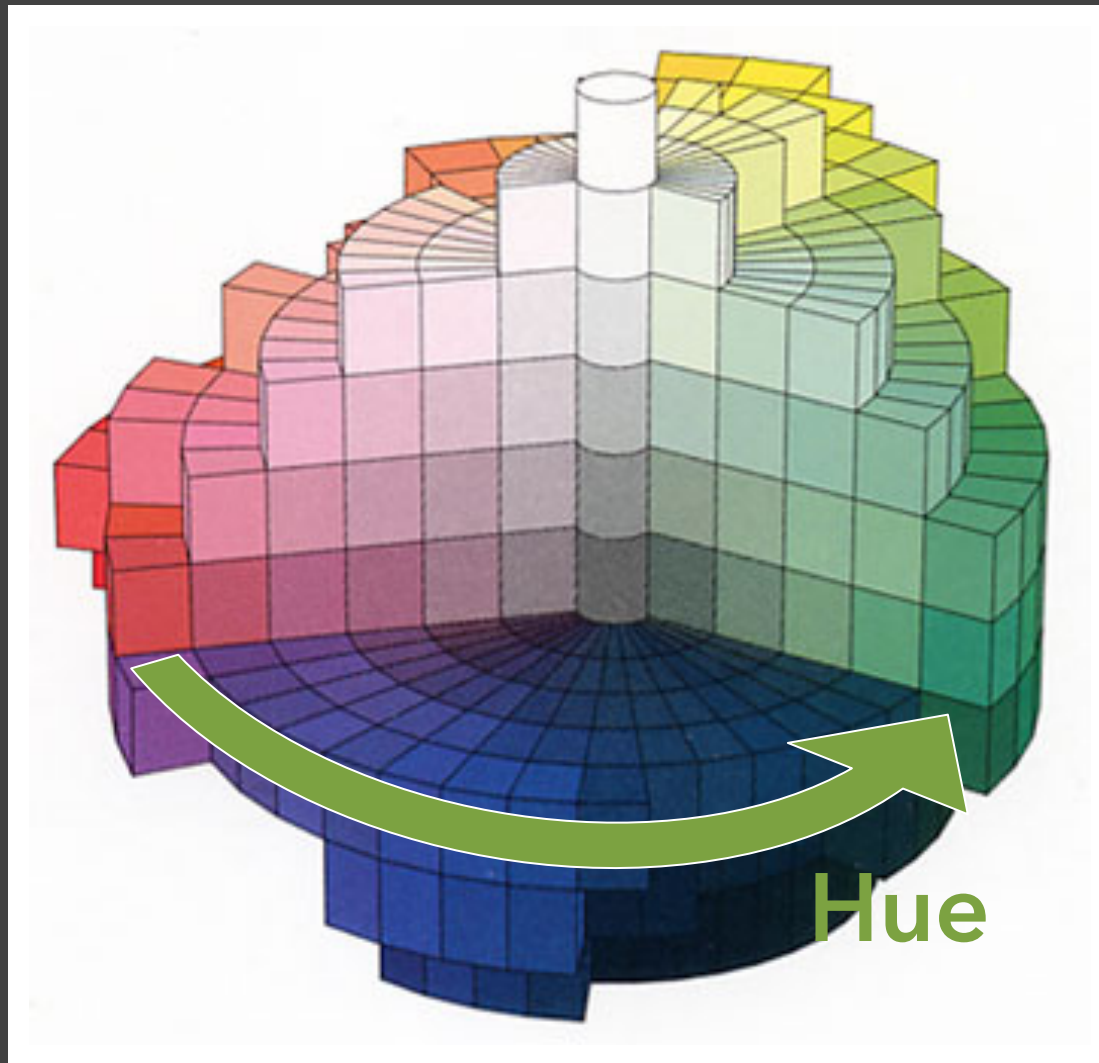
Developed the first perceptual color system based on his experience as an artist (1905).



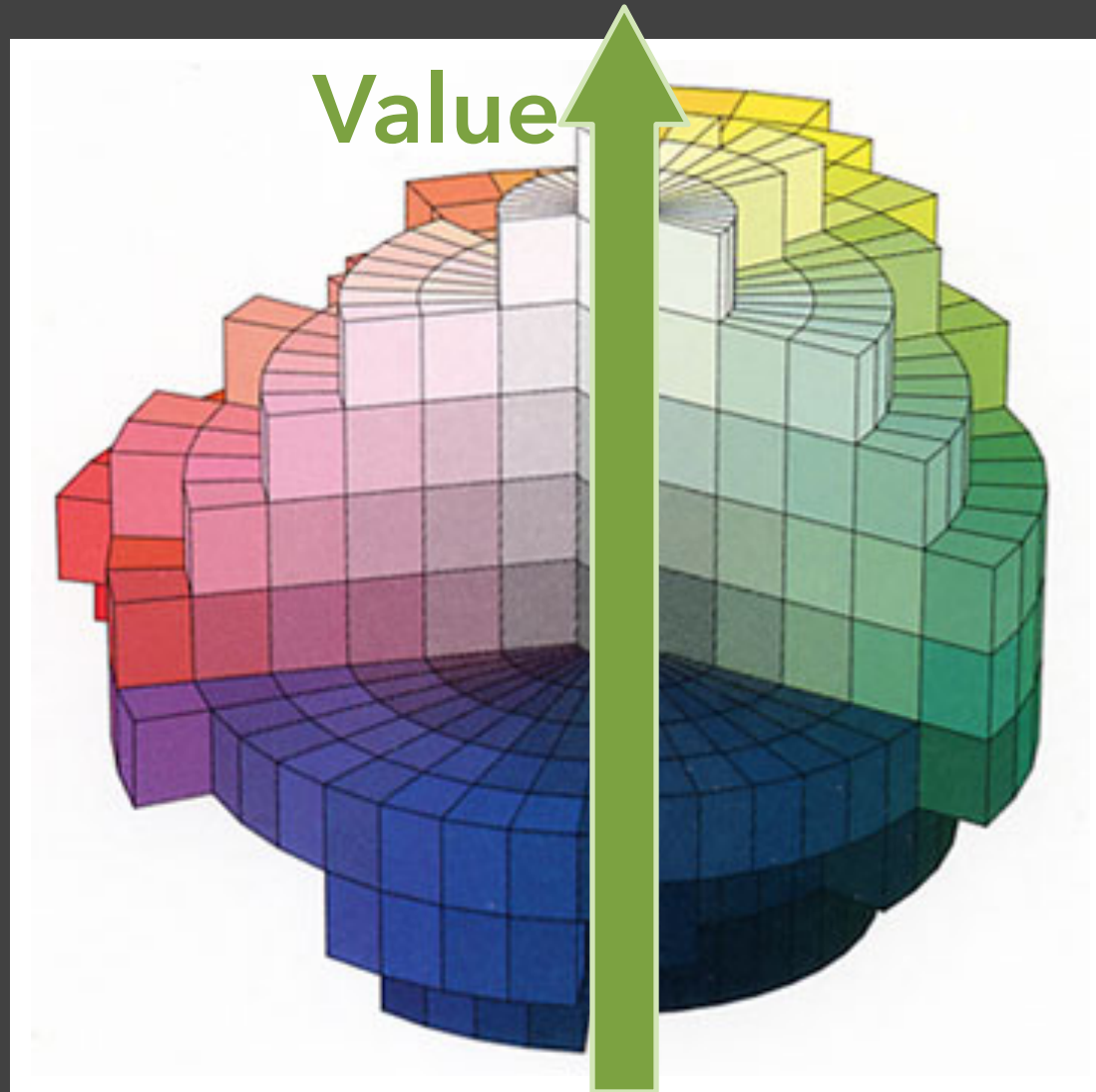
# Hue, Value and Chroma



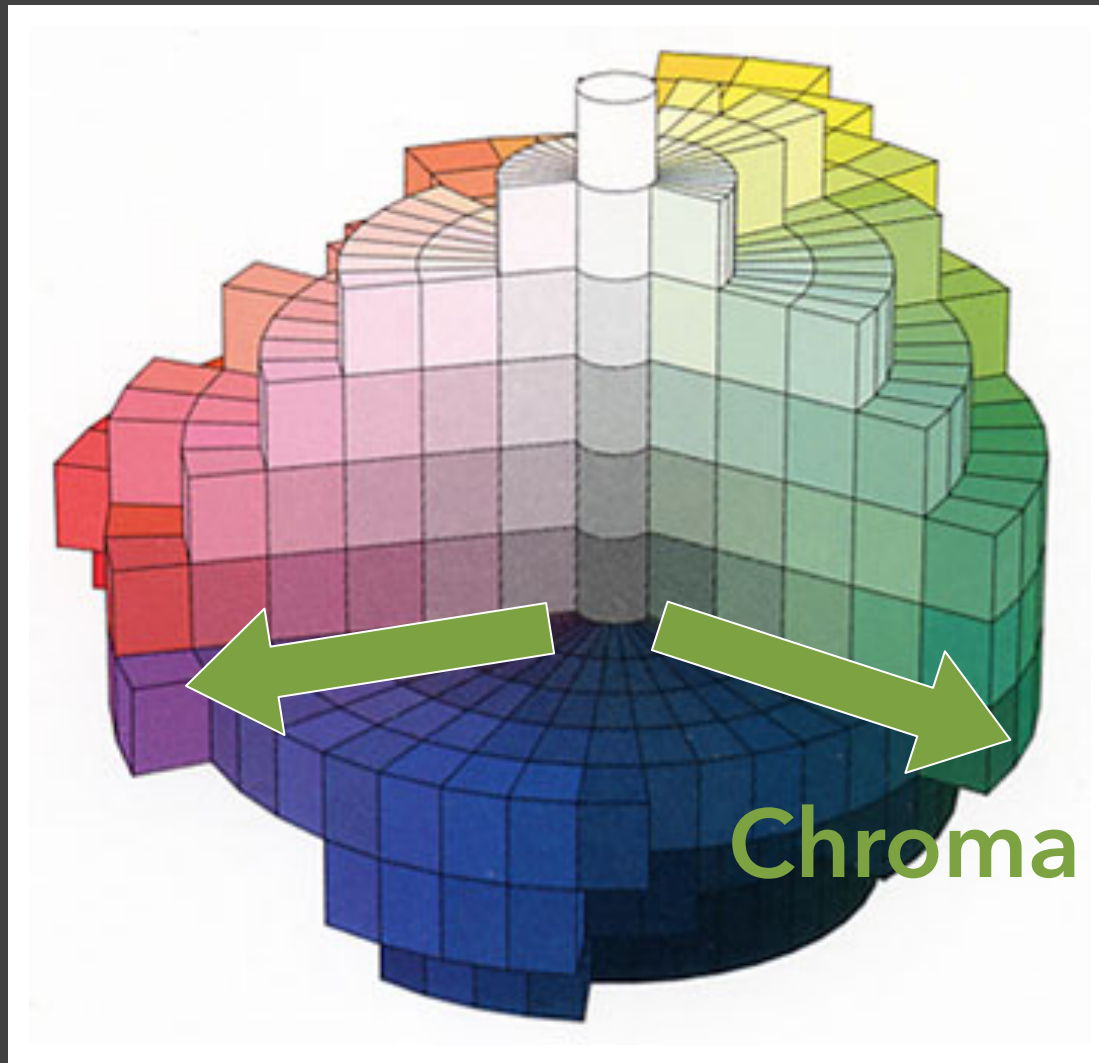
# Hue, Value and Chroma



# Hue, Value and Chroma



# Hue, Value and Chroma



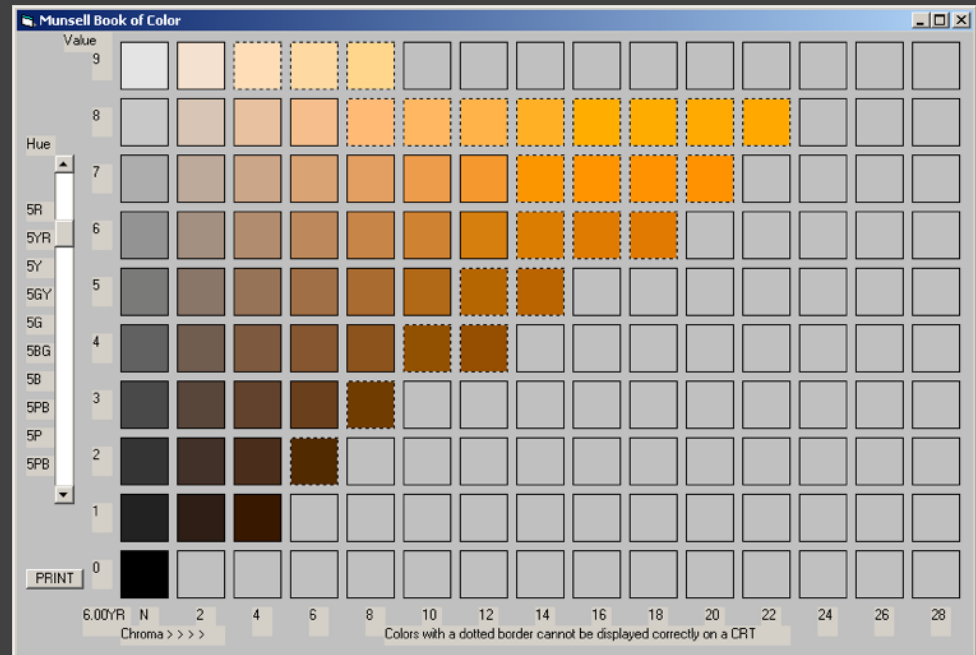
# Munsell Color System

Perceptually-based

Precisely reference a color

Intuitive dimensions

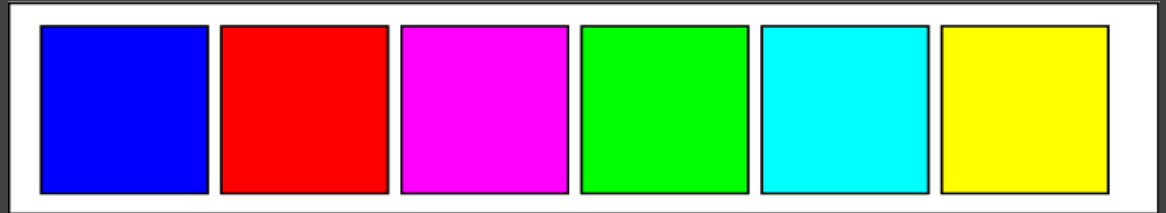
Look-up table (LUT)





# Perceptual Brightness

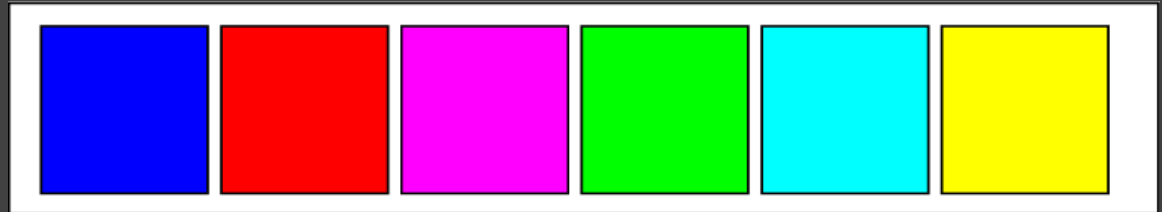
Color palette





# Perceptual Brightness

Color palette

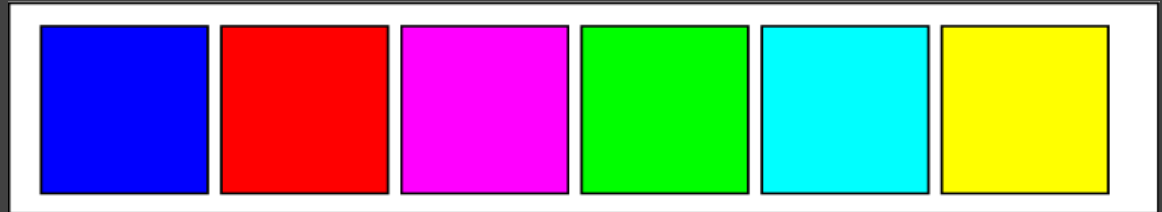


HSL Lightness  
*(Photoshop)*



# Perceptual Brightness

Color palette

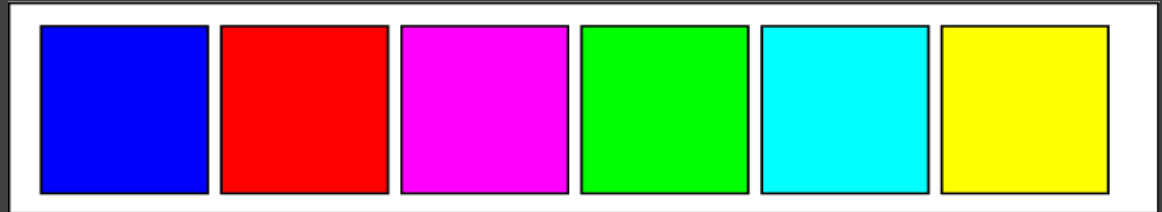


Luminance Y  
(*CIE XYZ*)



# Perceptual Brightness

Color palette

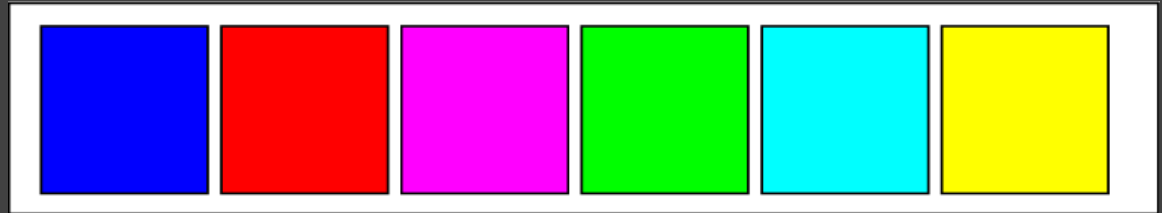


Munsell Value



# Perceptual Brightness

Color palette

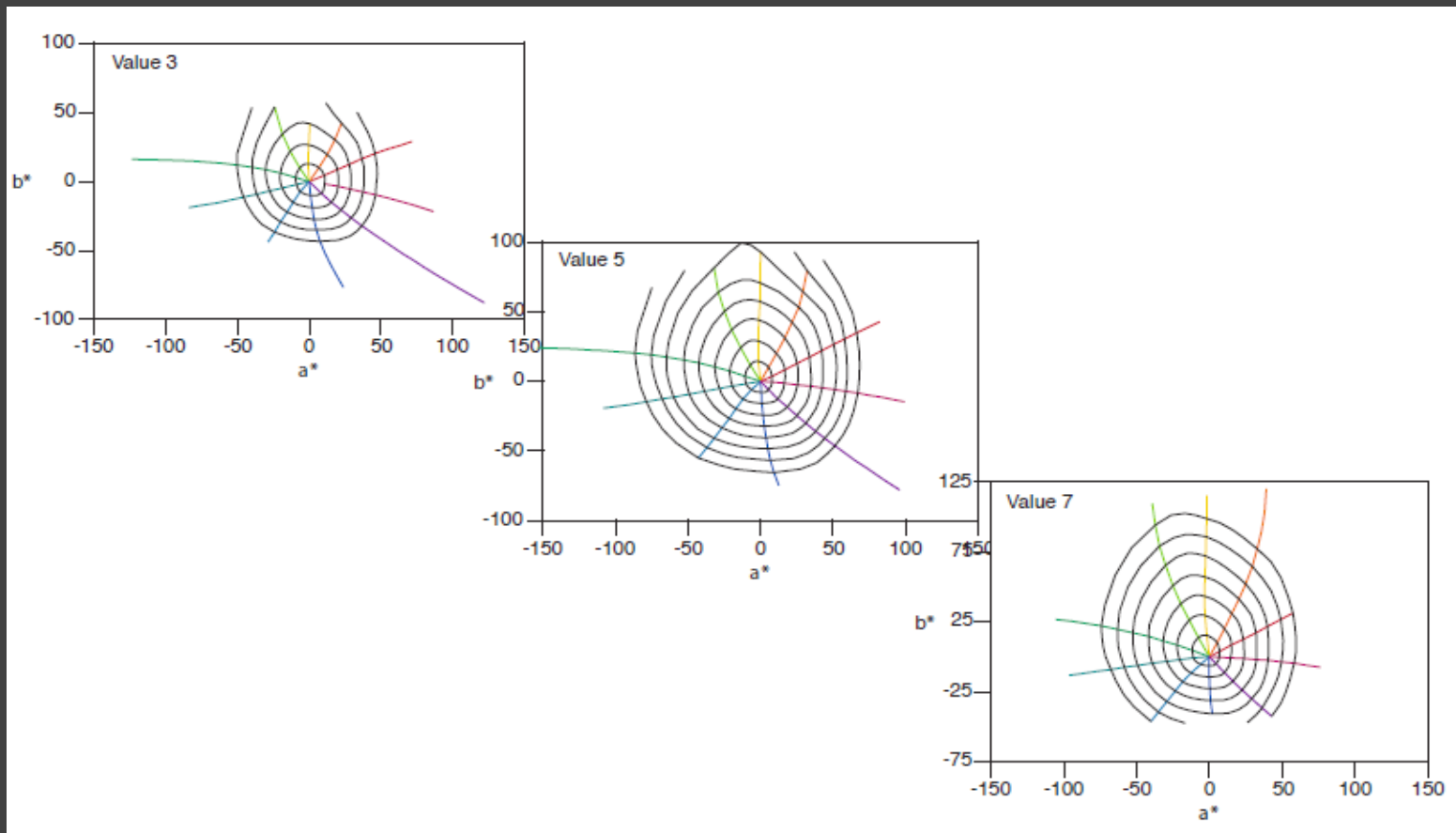


Munsell Value  
 $L^*$  (CIE LAB)

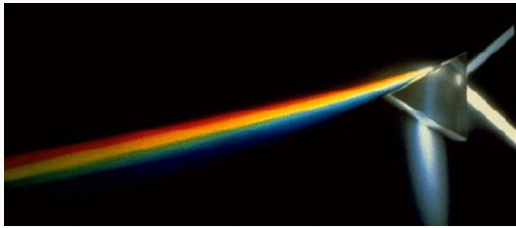


# Perceptually-Uniform Color Space

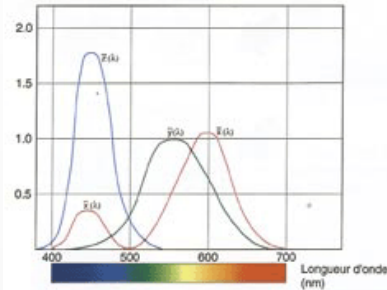
Munsell colors in CIE LAB coordinates



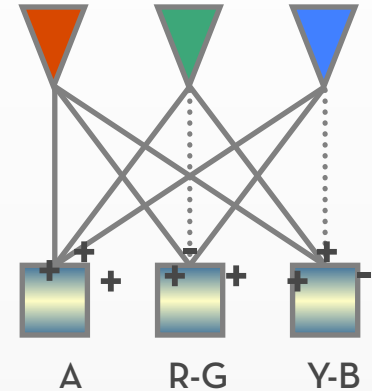
# Perception of Color



Light



Cone Response



Opponent Signals

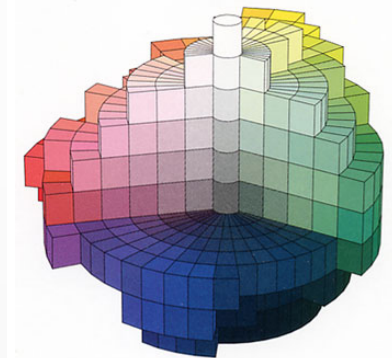
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



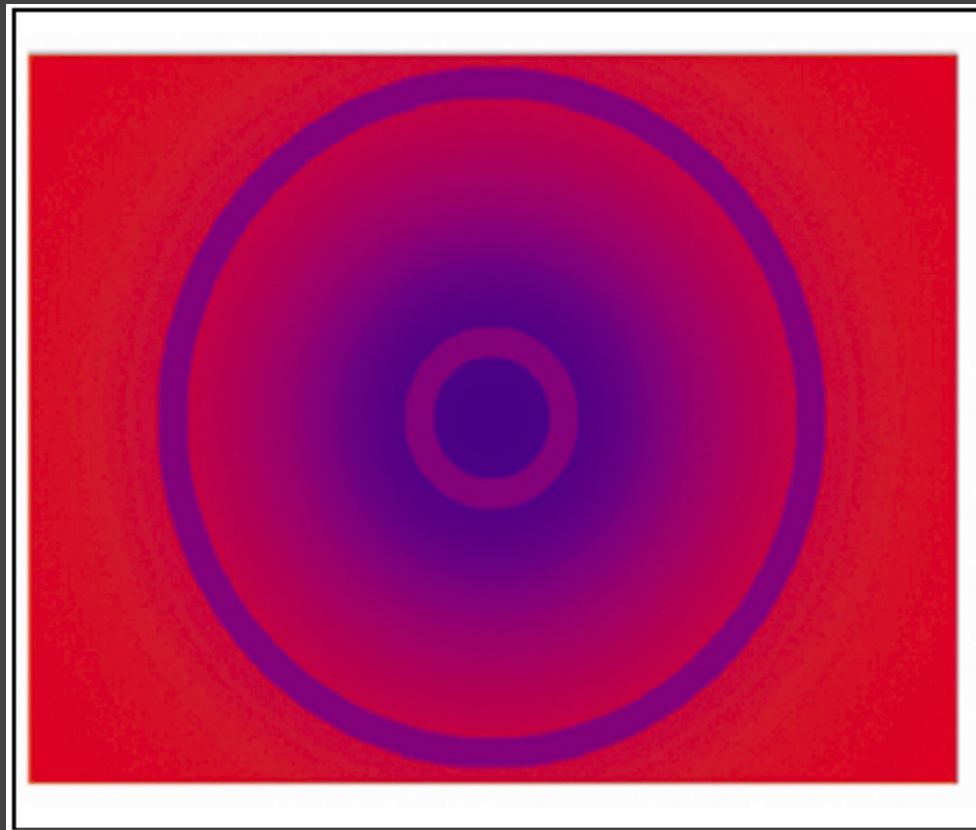
Color Perception

# Color Appearance

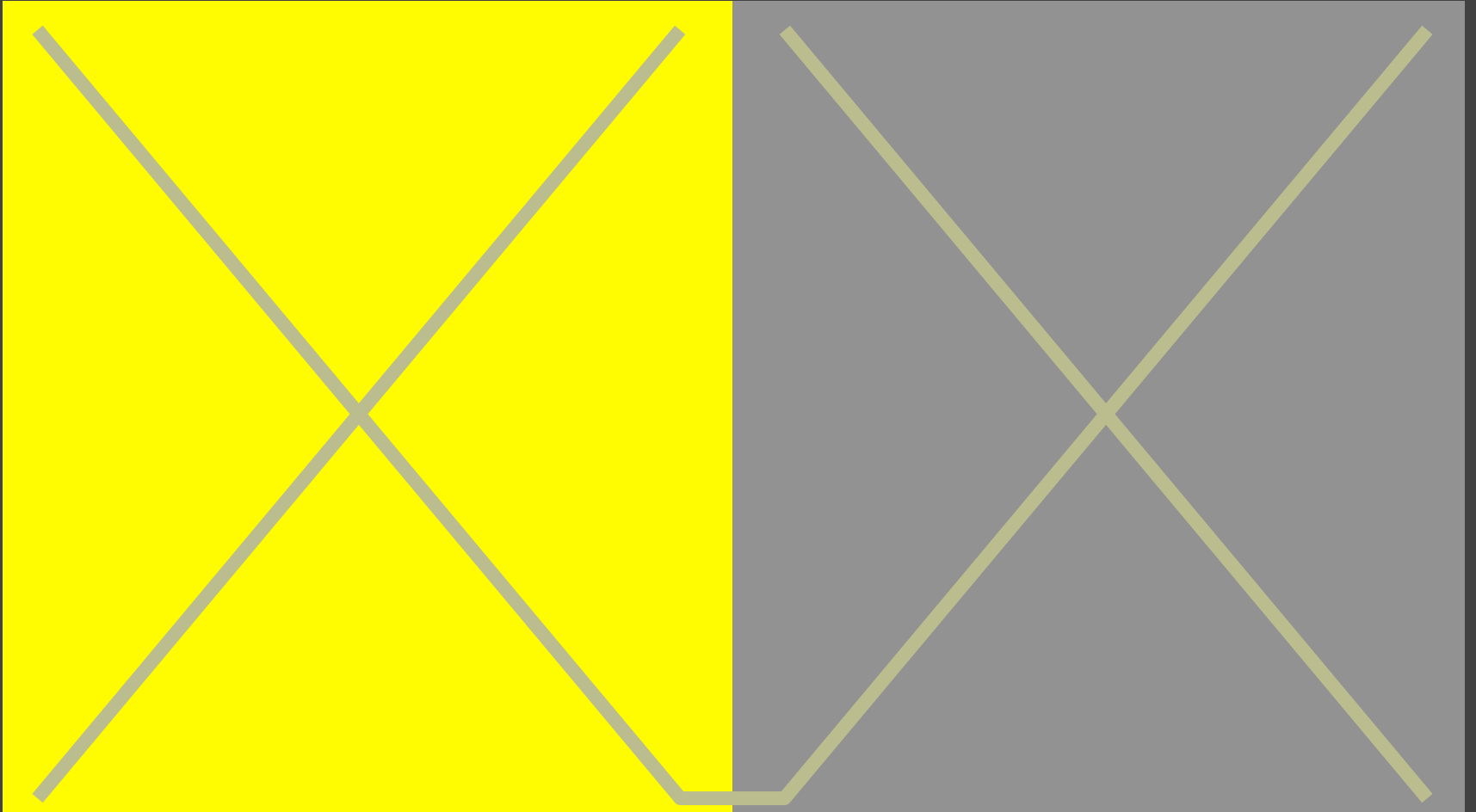
If we had a perceptually-uniform color space, can we predict how we perceive colors?

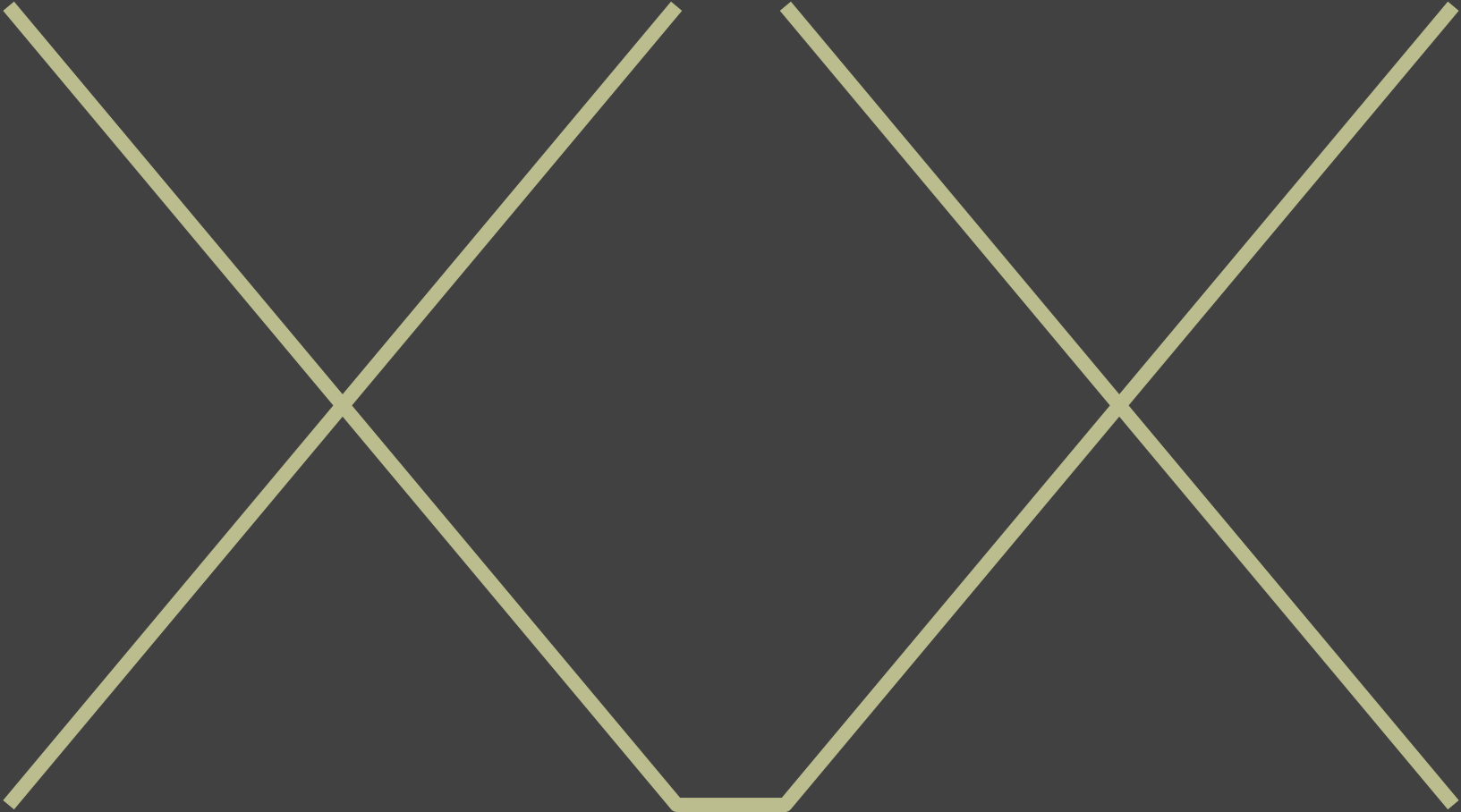
# Simultaneous Contrast

The inner and outer thin rings are in fact the same physical purple.

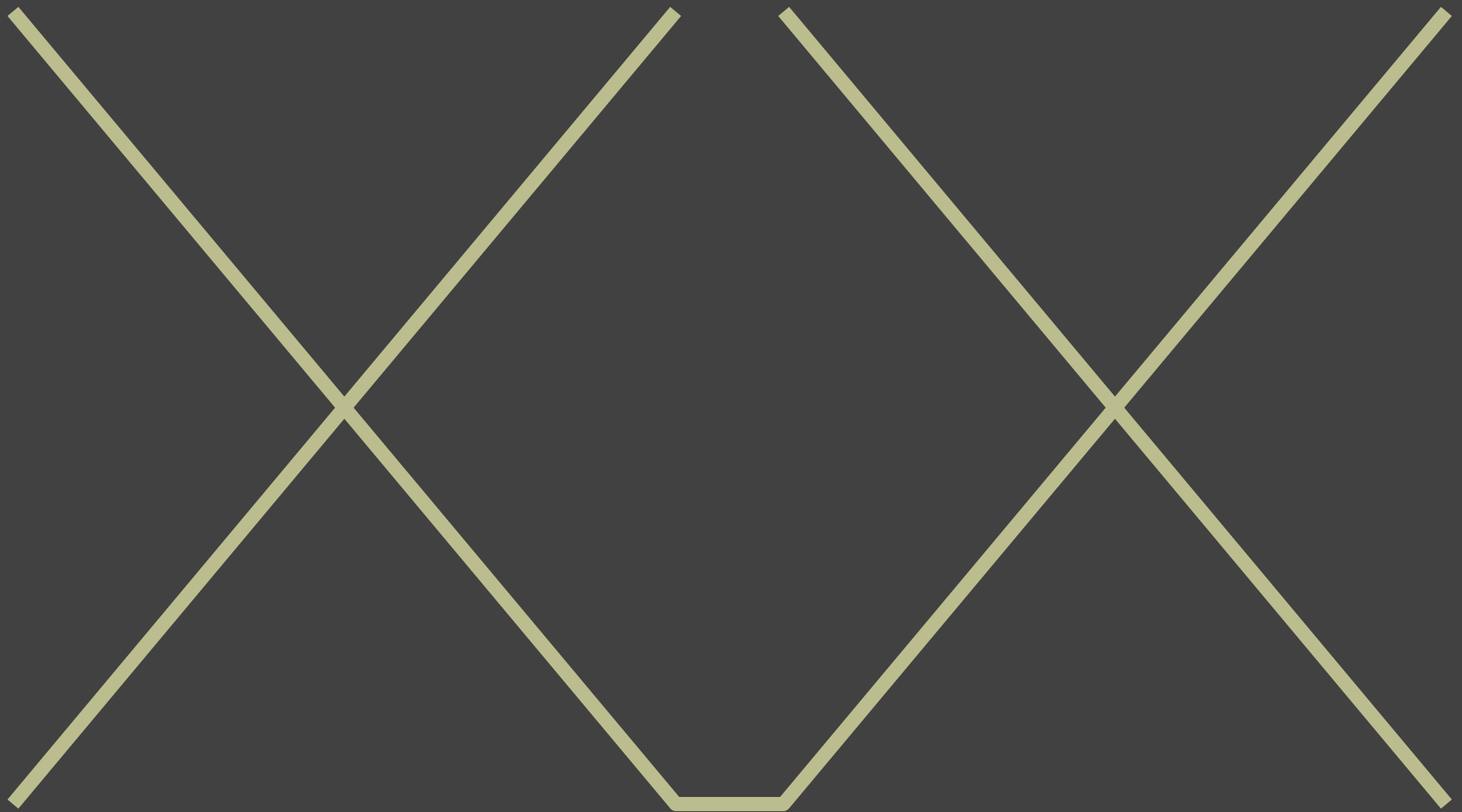






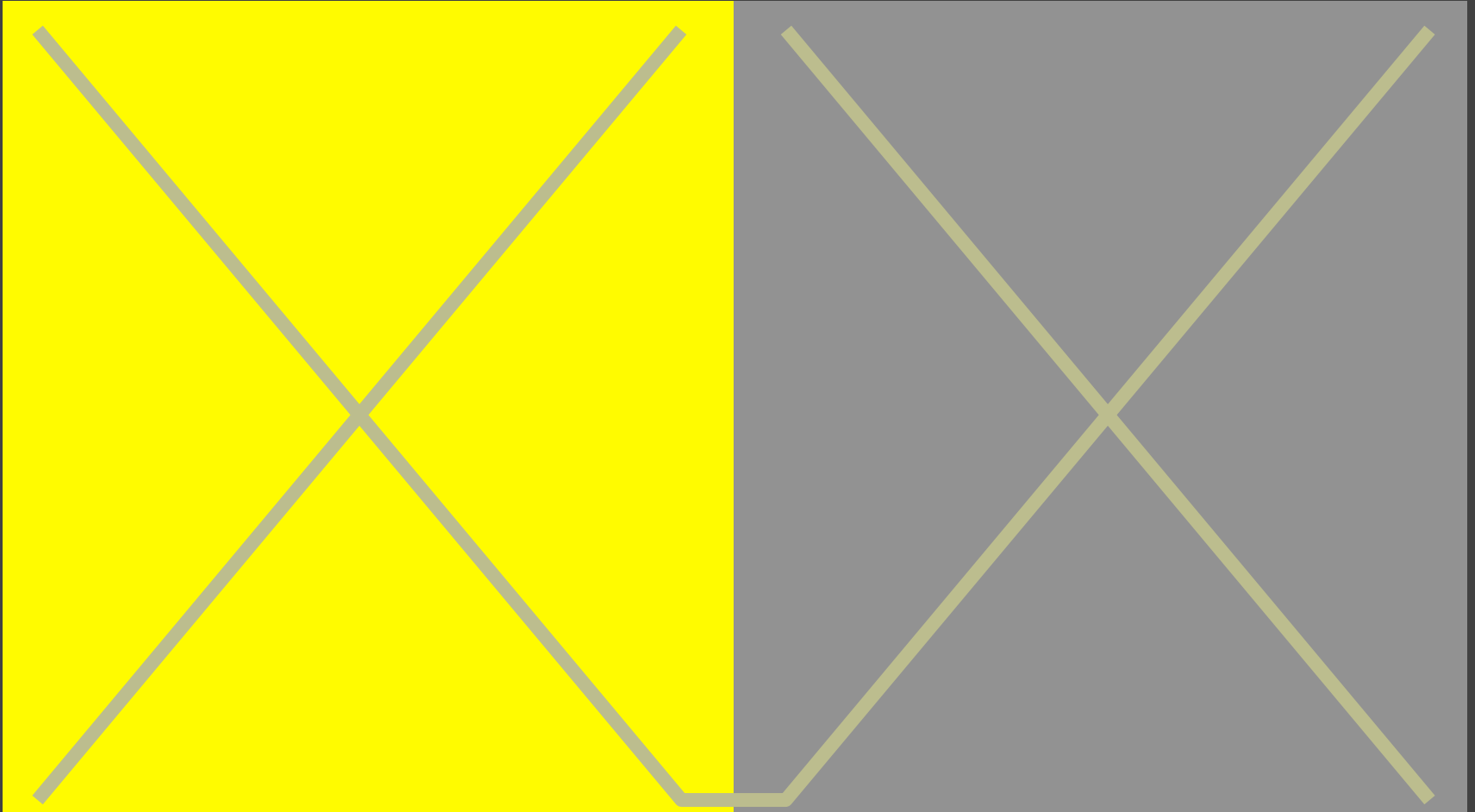


# Simultaneous Contrast



Josef Albers

# Simultaneous Contrast



Josef Albers

# Chromatic Adaptation



# Chromatic Adaptation



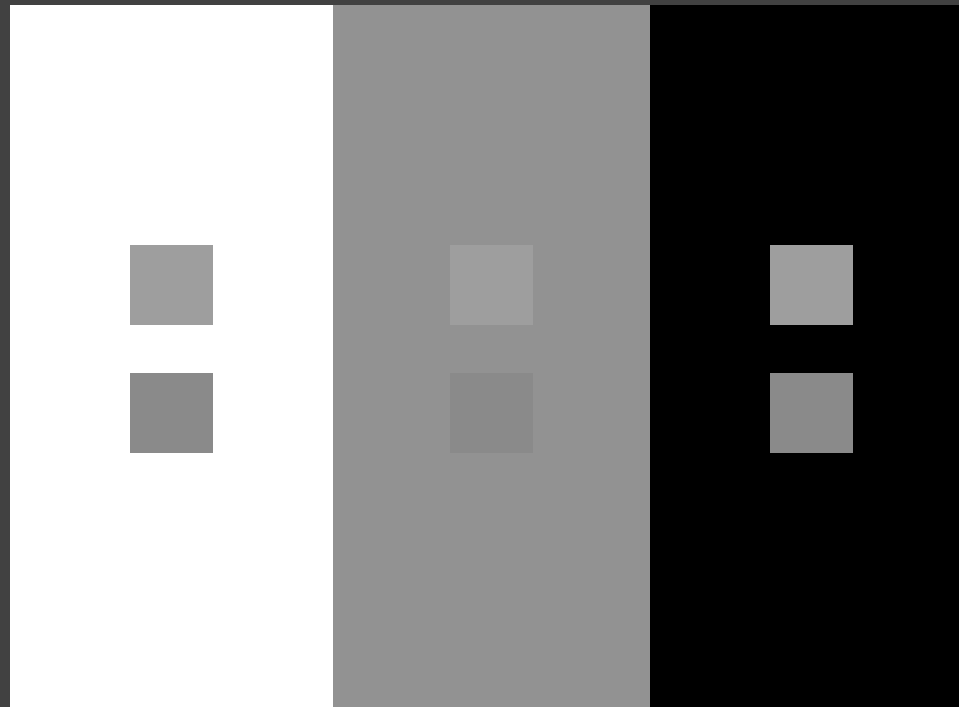
# Bezold Effect

Color appearance depends on adjacent colors



# Crispening

Perceived difference depends on background



*Color Appearance Models, Fairchild*



# Spreading

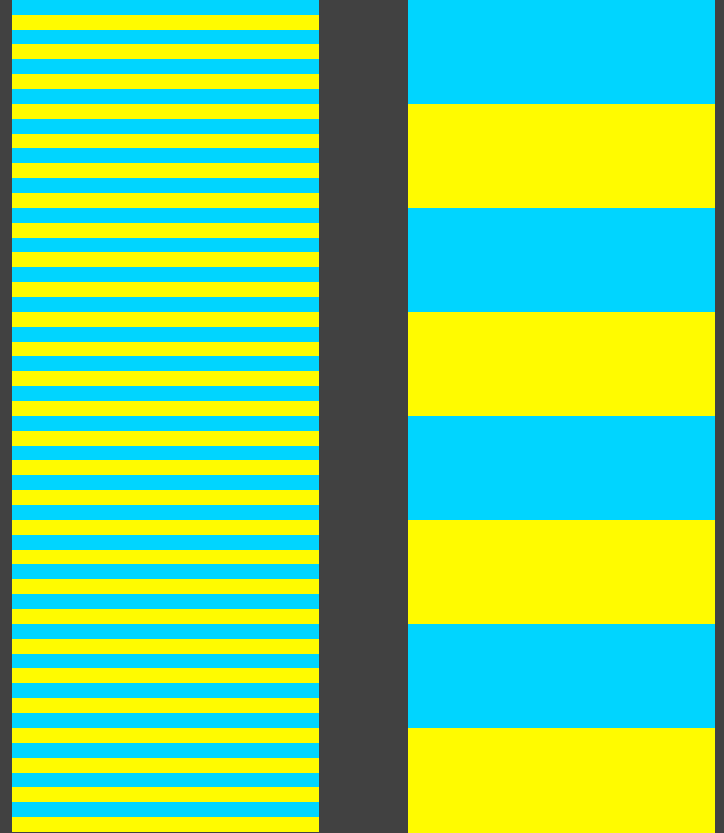
## Spatial frequency

The paint chip problem

Small text, lines, glyphs

Image colors

## Adjacent colors blend



*Foundations of Vision*, Brian Wandell

# Color Appearance

If we had a perceptually-uniform color space, can we predict how we perceive colors?

Chromatic adaptation

Luminance adaptation

Simultaneous contrast

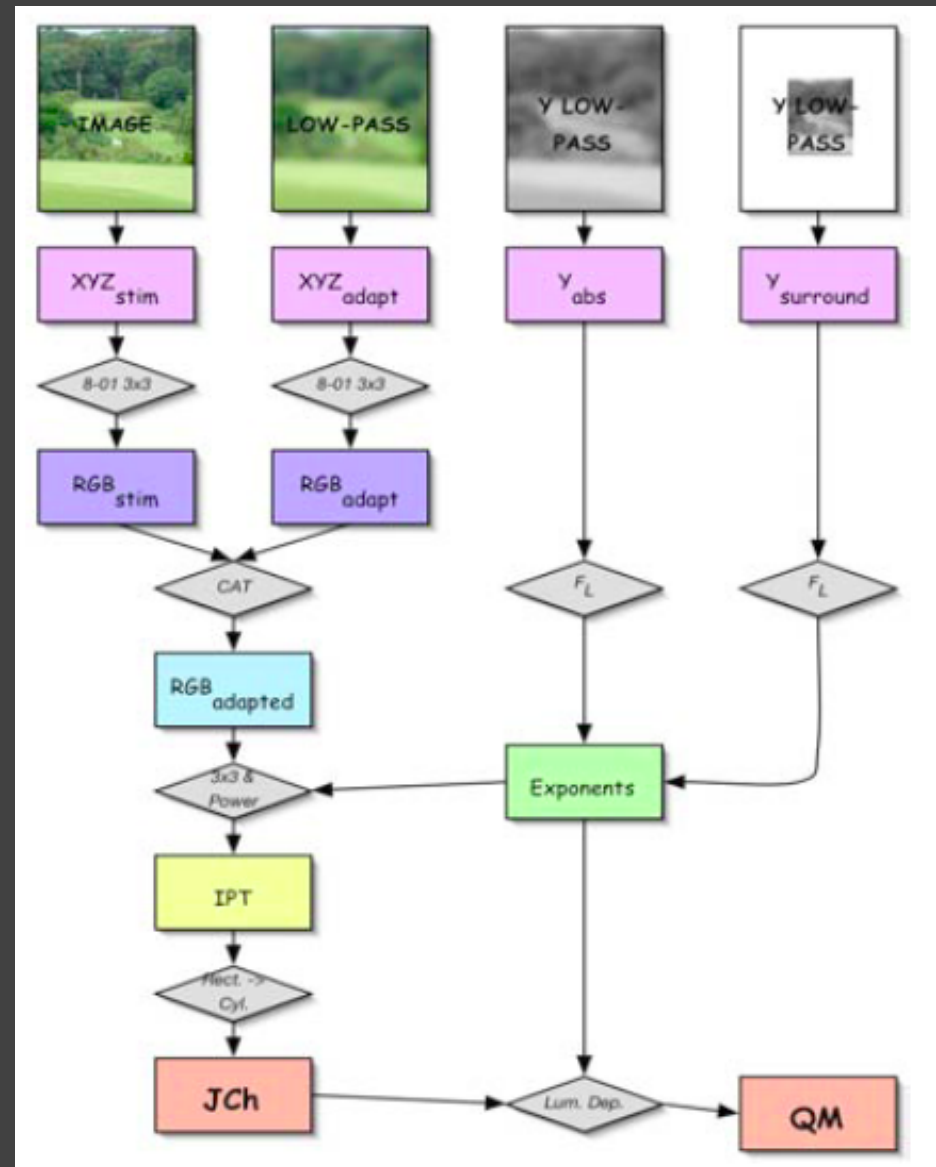
Spatial effects

Viewing angle

# iCAM

iCAM (2002) models:  
Chromatic adaptation  
Appearance scales  
Color difference  
Crispensing  
Spreading  
HDR tone mapping  
(see also **CIECAM02**)

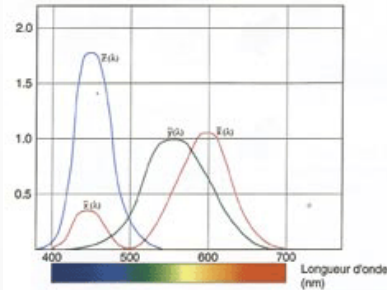
Mark Fairchild



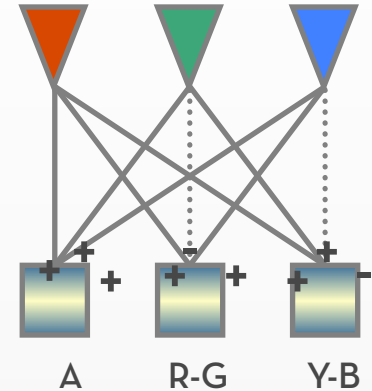
# Perception of Color



Light



Cone Response



Opponent Signals

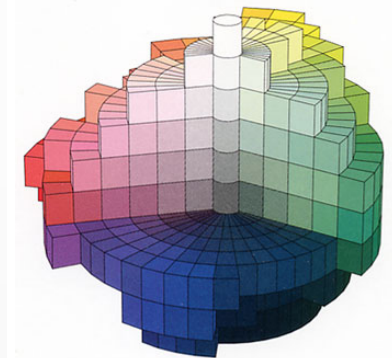
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



















Color Perception

# Colors according to XKCD...

Color names if  
you're a girl...

Color names if  
you're a guy...

Maraschino		Red
Cayenne		Purple
Maroon		
Plum		
Eggplant		
Grape		
Orchid		Pink
Lavender		
Carnation		
Strawberry		
Bubblegum		
Magenta		Orange
Salmon		
Tangerine		Yellow
Cantaloupe		
Banana		
Lemon		Green
Honeydew		
Lime		
Spring		
Clover		
Fern		
Moss		
Flora		
Sea Foam		Blue
Spindrift		
Teal		
Sky		
Turquoise		

Doghouse Diaries  
"We take no as an answer."

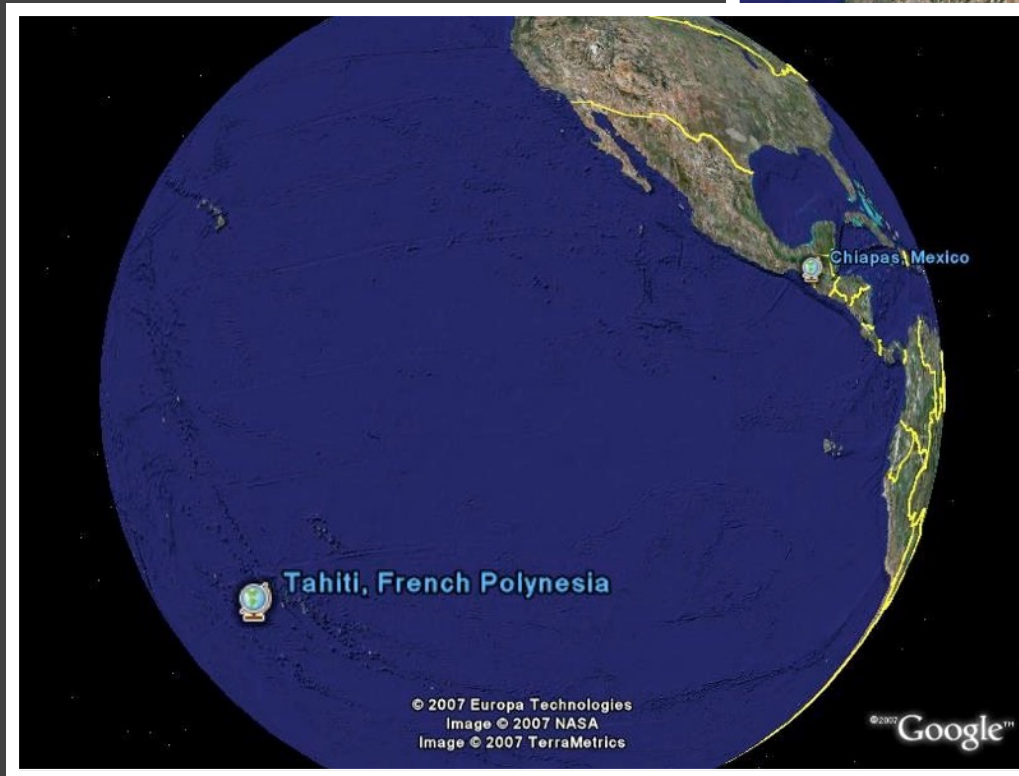
# Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay.



# Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay.





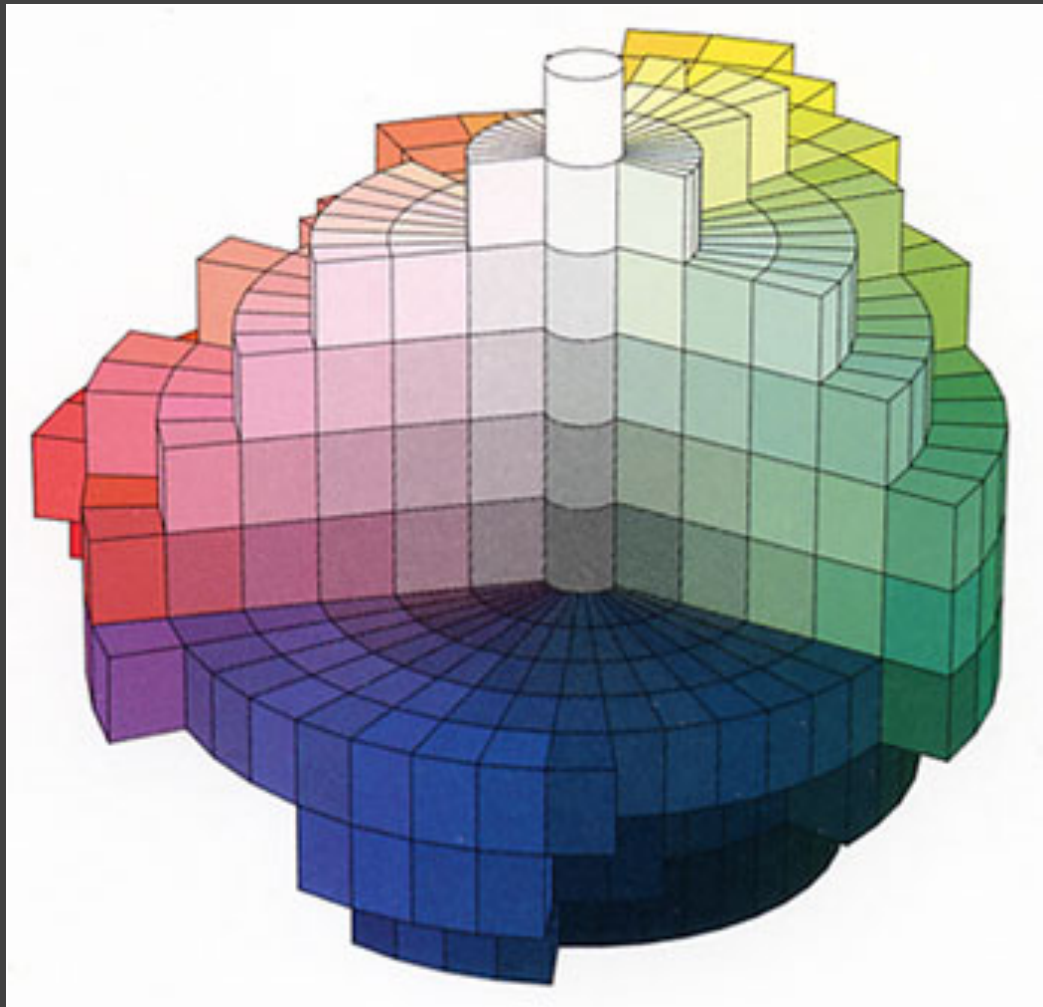
# Basic Color Terms

Chance discovery by Brent Berlin and Paul Kay.

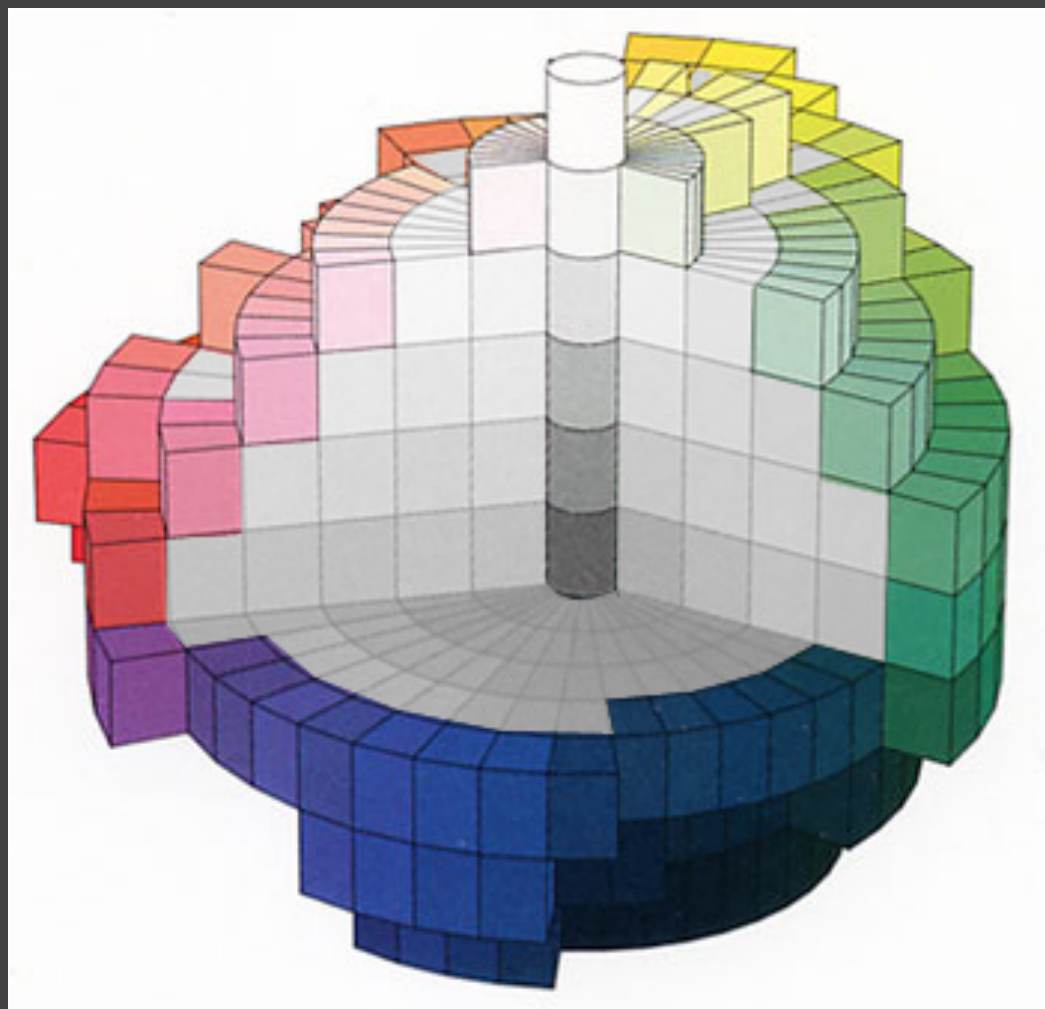
Initial study in 1969

- Surveyed speakers from 20 languages
- Literature from 69 languages

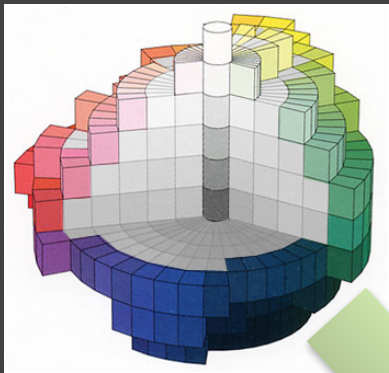
# World Color Survey



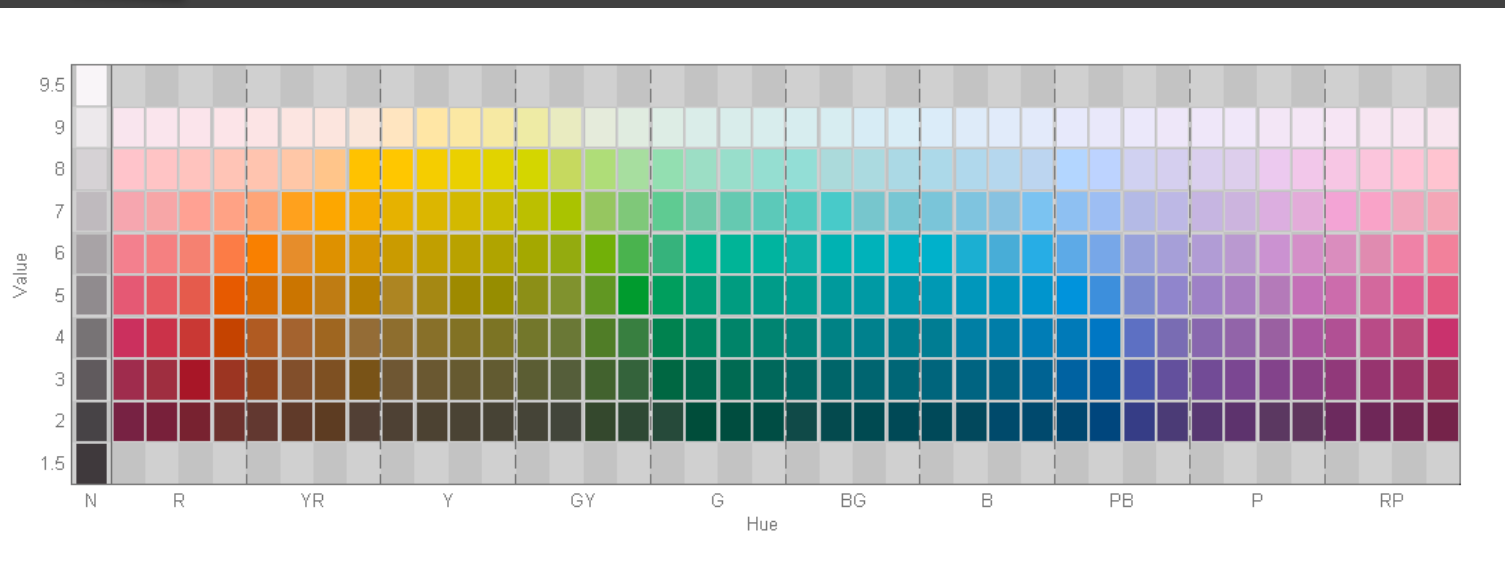
# World Color Survey



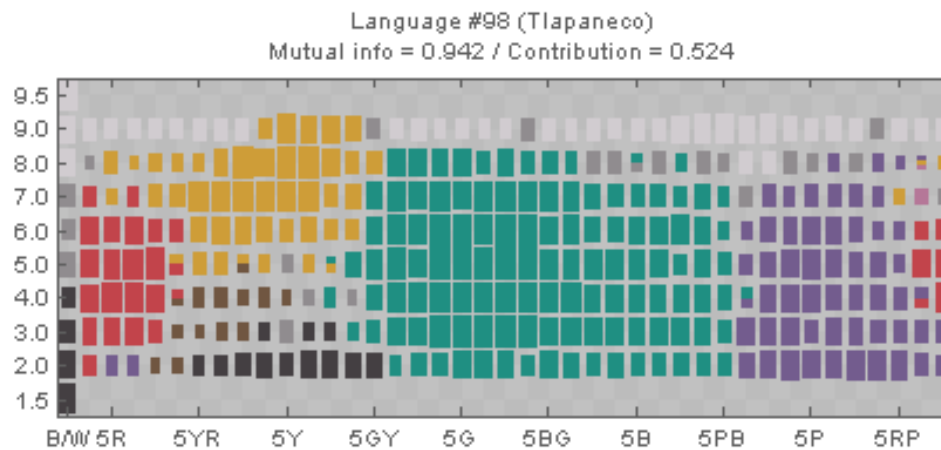
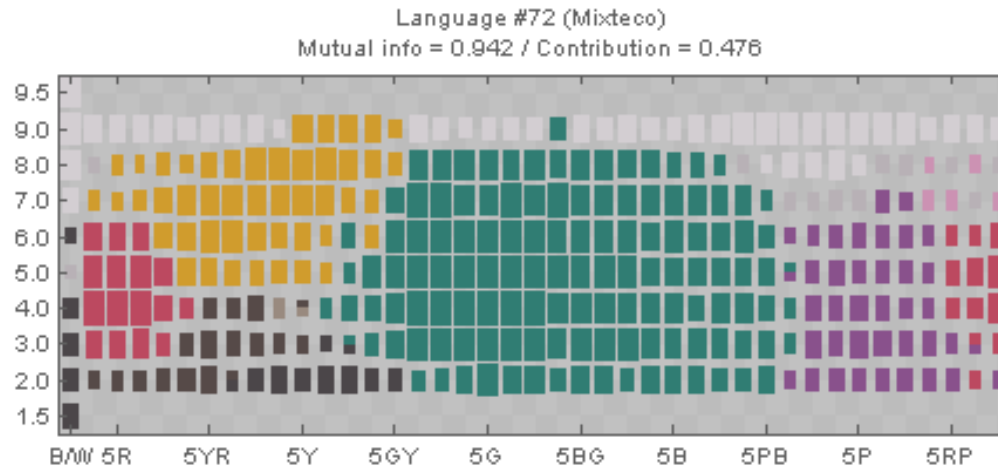
# World Color Survey



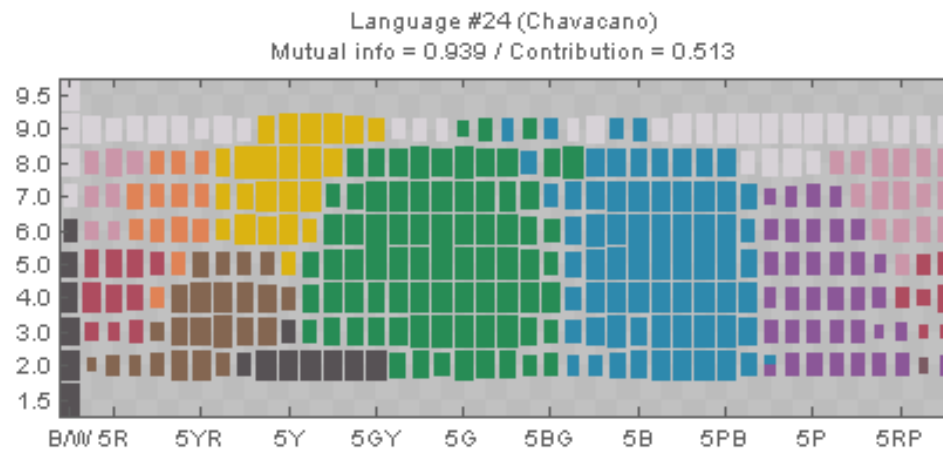
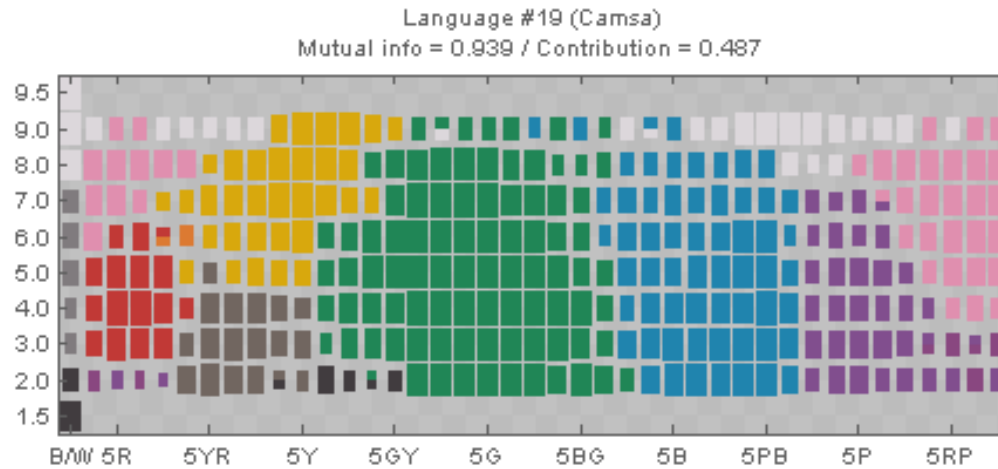
Naming information from 2616 speakers from 110 languages on 330 Munsell color chips



# Results from WCS



# Results from WCS



# Universal (?) Basic Color Terms

Basic color terms recur across languages.



White



Red



Pink



Grey



Yellow



Brown



Black



Green



Orange



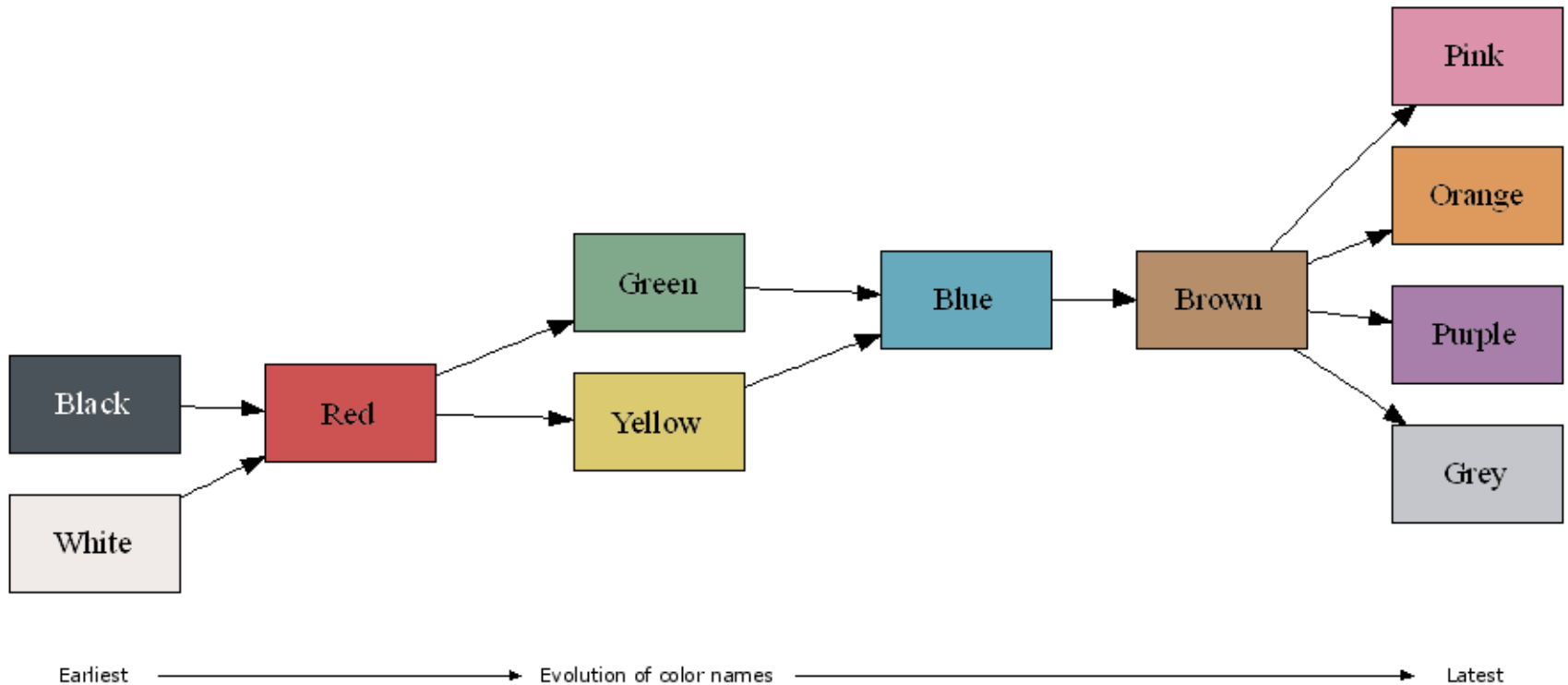
Blue



Purple

# Evolution of Basic Color Terms

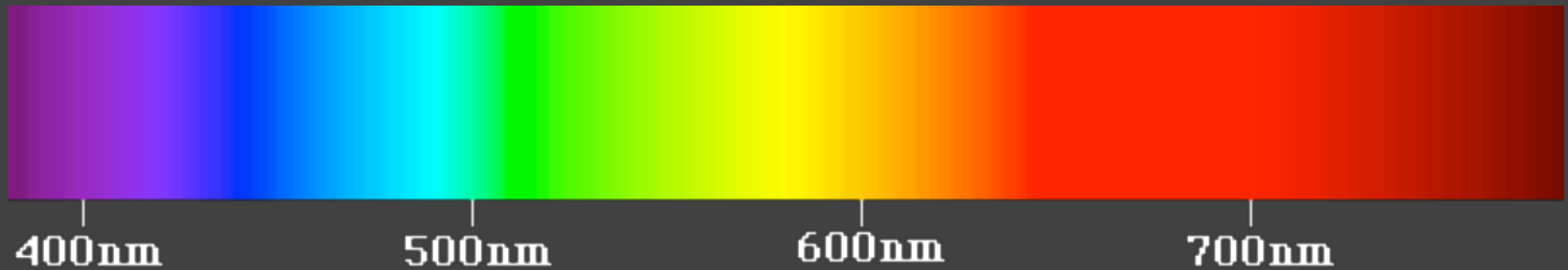
Proposed universal evolution across languages.





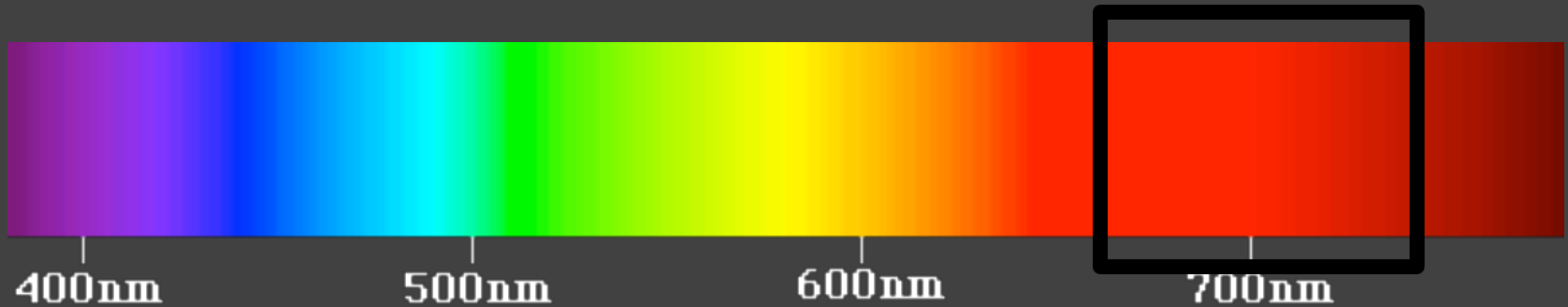
# Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



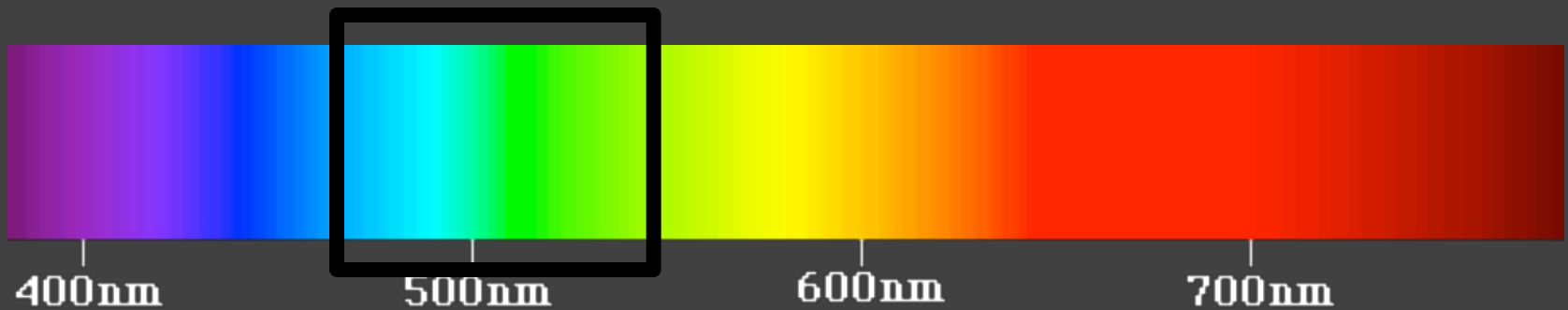
# Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



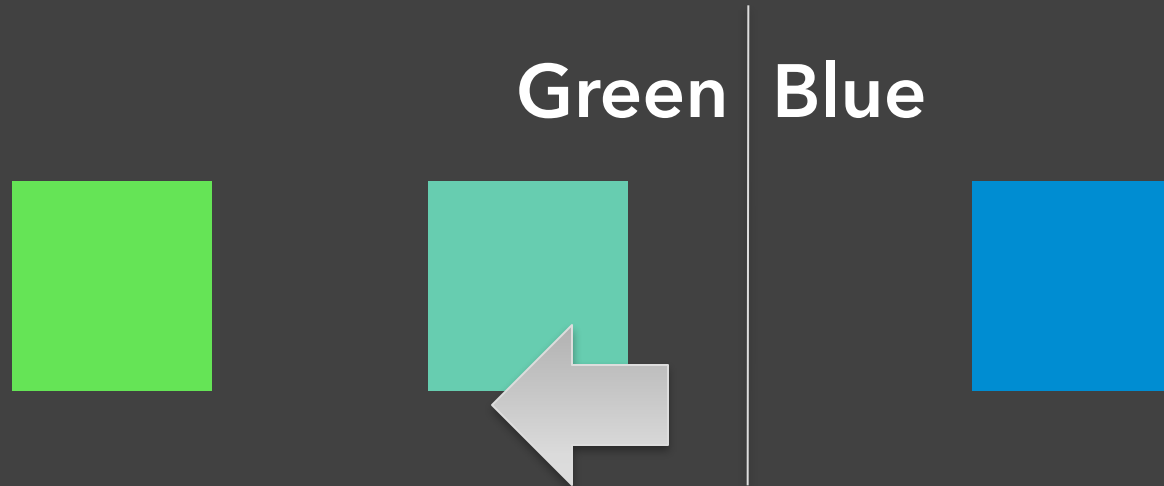
# Rainbow Color Map

We associate and group colors together, often using the name we assign to the colors.



# Naming Effects Color Perception

Color name boundaries



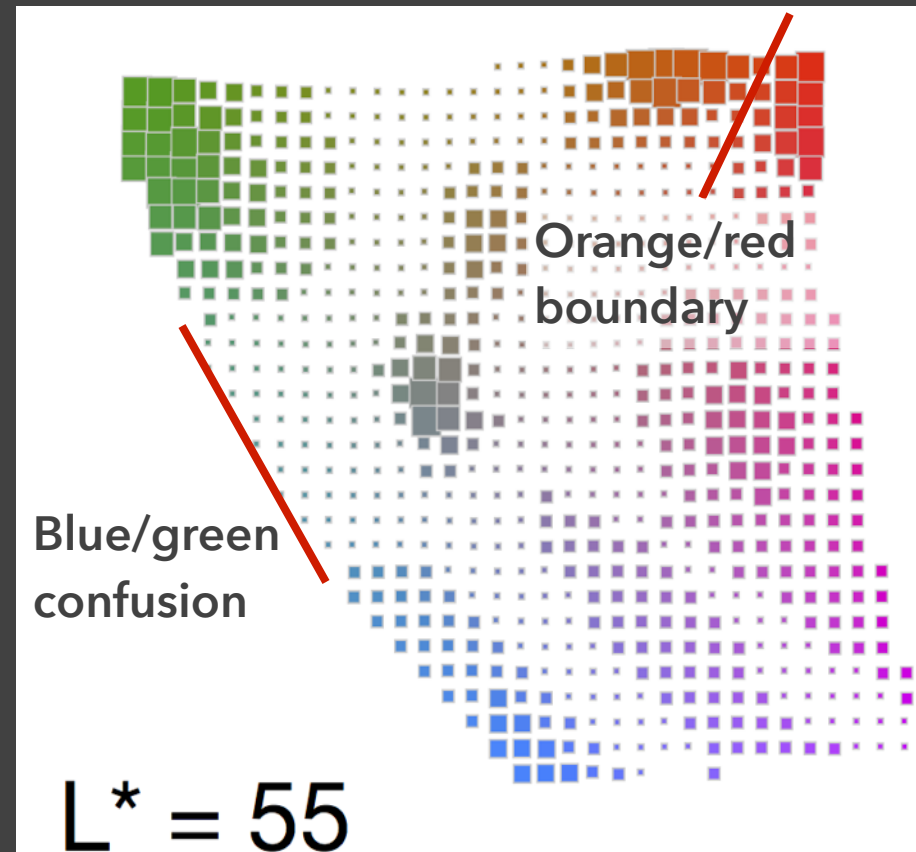
# Color Naming Models [Heer & Stone '12]

Model 3 million responses from XKCD survey

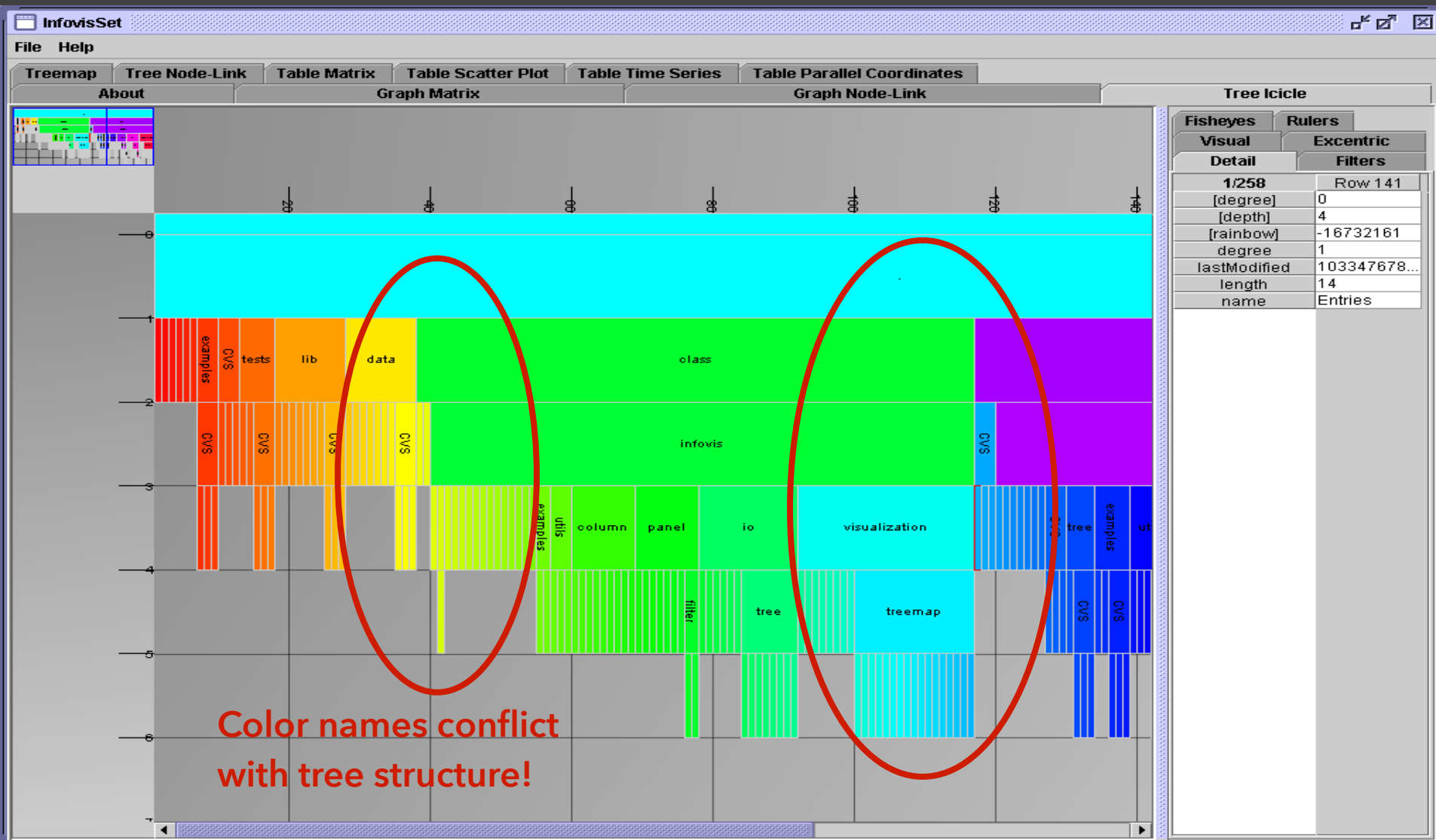
Bins in LAB space  
sized by *saliency*:

How much do people  
agree on color name?

Modeled by entropy  
of  $p(\text{name} \mid \text{color})$



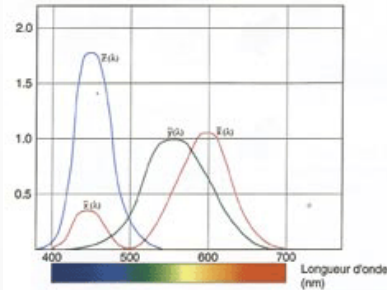
# Icicle Tree with Rainbow Coloring



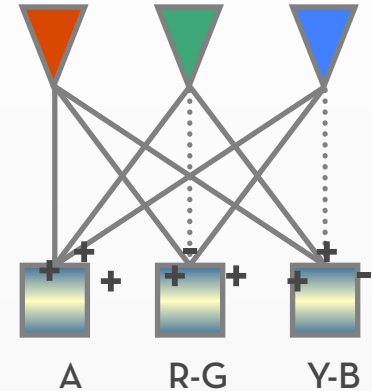
# Perception of Color



Light



Cone Response



Opponent Signals

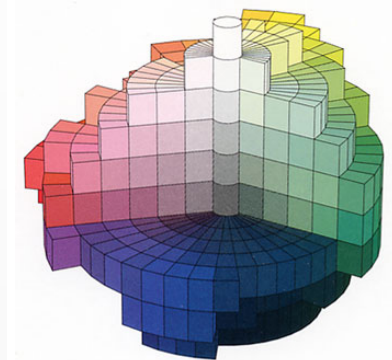
“Yellow”

Color Cognition



Mark D. Fairchild  
COLOR APPEARANCE  
MODELS

Color Appearance



Color Perception

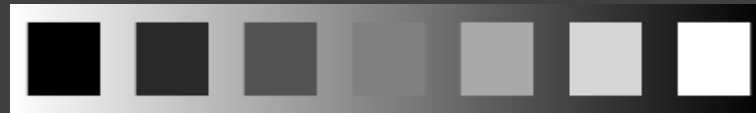
# Color Encodings



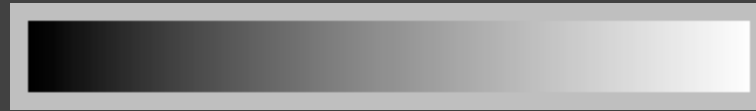
# Encoding Data with Color

Value is perceived as ordered

∴ Encode ordinal variables (O)



∴ Encode continuous variables (Q) [not as well]



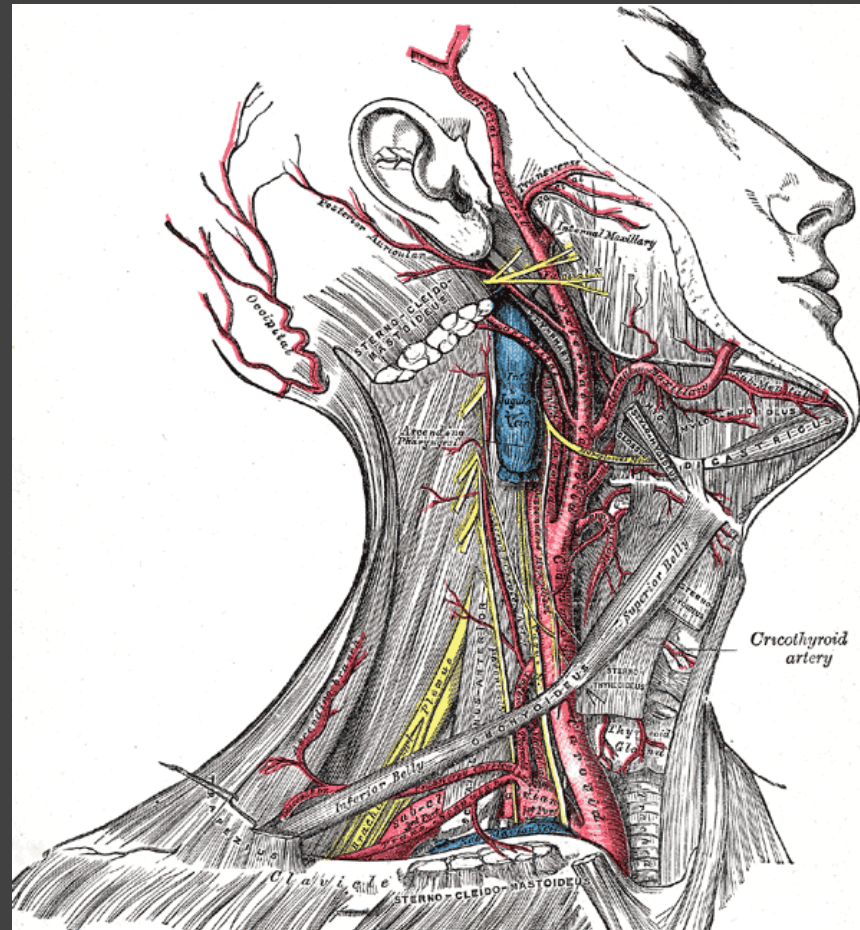
Hue is normally perceived as unordered

∴ Encode nominal variables (N) using color



# Categorical Color

# Gray's Anatomy



Superficial dissection of the right side of the neck, showing the carotid and subclavian arteries. (<http://www.bartleby.com/107/illus520.html>)

# Allocation of the Radio Spectrum

## UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

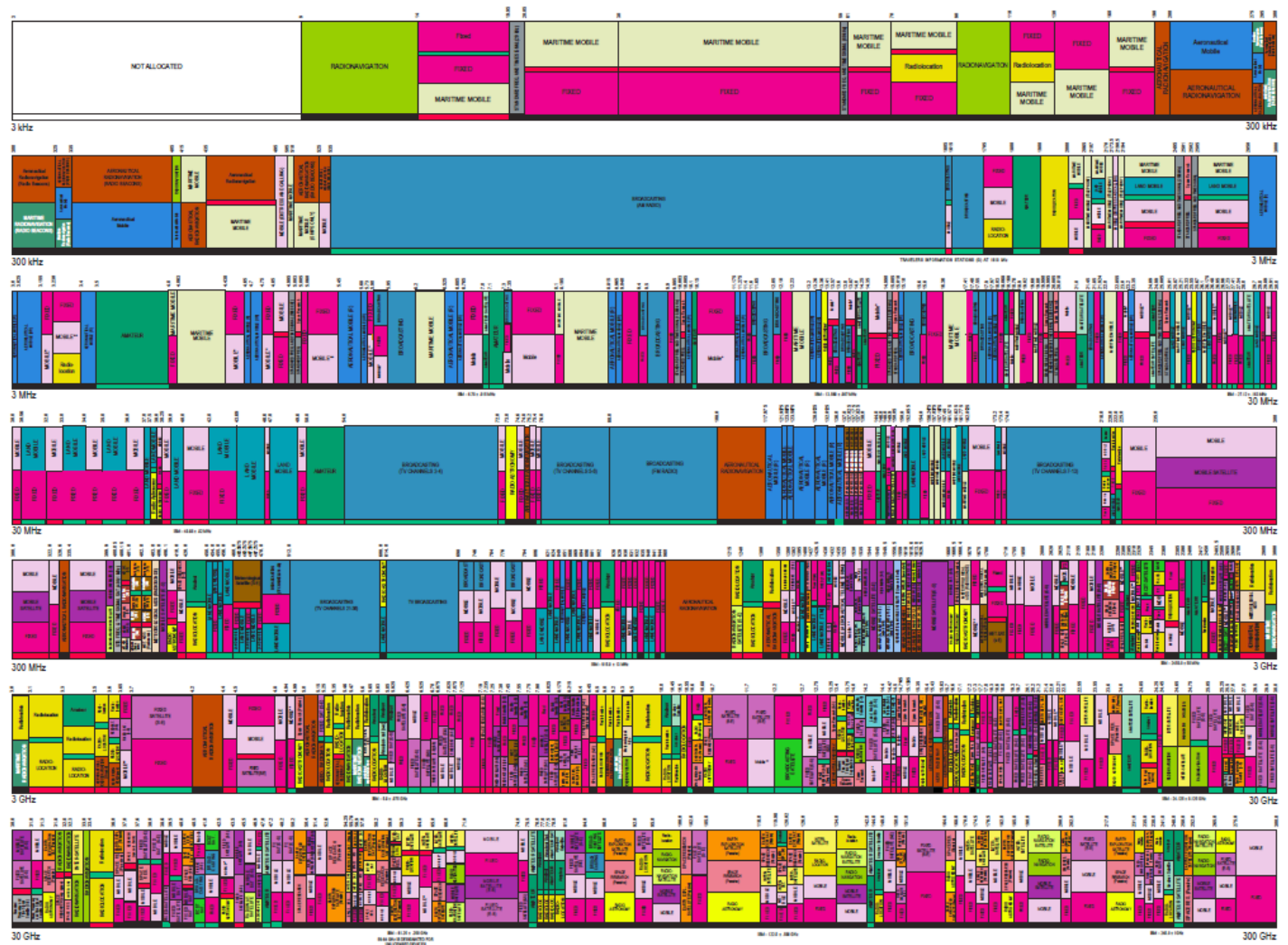
### RADIO SERVICES COLOR LEGEND

- |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|--|

- ### ACTIVITY CODE
- - 
  -

### ALLOCATION USAGE DESIGNATION

SERVICE	EXAMPLE	DESCRIPTION
Primary	F1ED	Capital Letters
Secondary	F1ED	Capital Letters



# Alloc

## UNITED STATES FREQUENCY ALLOCATION THE RADIO SPECTRUM

### RADIO SERVICES COLOR LEGEND

	AERONAUTICAL MOBILE		INTER-SATELLITE		RADIO ASTRONOMY
	AERONAUTICAL MOBILE SATELLITE		LAND MOBILE		RADIO DETERMINATION SATELLITE
	AERONAUTICAL RADIONAVIGATION		LAND MOBILE SATELLITE		RADIOLOCATION
	AMATEUR		MARITIME MOBILE		RADIOLOCATION SATELLITE
	AMATEUR SATELLITE		MARITIME MOBILE SATELLITE		RADIONAVIGATION
	BROADCASTING		MARITIME RADIONAVIGATION		RADIONAVIGATION SATELLITE
	BROADCASTING SATELLITE		METEOROLOGICAL AIDS		SPACE OPERATION
	EARTH EXPLORATION SATELLITE		METEOROLOGICAL SATELLITE		SPACE RESEARCH
	FIXED		MOBILE		STANDARD FREQUENCY AND TIME SIGNAL
	FIXED SATELLITE		MOBILE SATELLITE		STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

### ACTIVITY CODE

	GOVERNMENT EXCLUSIVE		GOVERNMENT-GOVERNMENT SHARED
	NON-GOVERNMENT EXCLUSIVE		

### ALLOCATION USAGE DESIGNATION

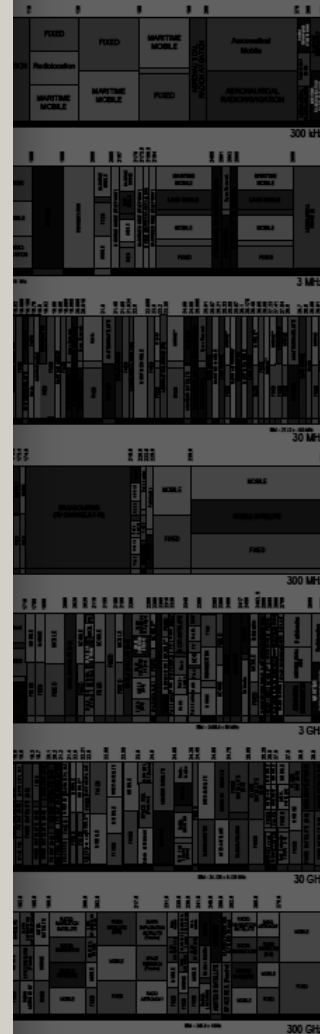
SERVICE	EXAMPLE	DESCRIPTION
Primary	FIXED	Capital Letters
Secondary	MOBILE	Capital Letters

## RADIO SERVICES COLOR LEGEND

	AERONAUTICAL MOBILE		INTER-SATELLITE		RADIO ASTRONOMY
	AERONAUTICAL MOBILE SATELLITE		LAND MOBILE		RADIO DETERMINATION SATELLITE
	AERONAUTICAL RADIONAVIGATION		LAND MOBILE SATELLITE		RADIOLOCATION
	AMATEUR		MARITIME MOBILE		RADIOLOCATION SATELLITE
	AMATEUR SATELLITE		MARITIME MOBILE SATELLITE		RADIONAVIGATION
	BROADCASTING		MARITIME RADIONAVIGATION		RADIONAVIGATION SATELLITE
	BROADCASTING SATELLITE		METEOROLOGICAL AIDS		SPACE OPERATION
	EARTH EXPLORATION SATELLITE		METEOROLOGICAL SATELLITE		SPACE RESEARCH
	FIXED		MOBILE		STANDARD FREQUENCY AND TIME SIGNAL
	FIXED SATELLITE		MOBILE SATELLITE		STANDARD FREQUENCY AND TIME SIGNAL SATELLITE

## ACTIVITY CODE

# rum













# Palette Design & Color Names

Minimize overlap and ambiguity of colors.

Color Name Distance

<b>0.00</b>	1.00	1.00	1.00	0.98	1.00	1.00	1.00	1.00	1.00	<b>0.20</b>
1.00	<b>0.00</b>	1.00	0.97	1.00	1.00	1.00	1.00	0.96	1.00	
1.00	1.00	<b>0.00</b>	1.00	1.00	1.00	1.00	1.00	0.90	0.99	
1.00	0.97	1.00	<b>0.00</b>	1.00	0.95	0.99	1.00	1.00	1.00	
0.98	1.00	1.00	1.00	<b>0.00</b>	0.96	0.91	0.97	1.00	0.99	
1.00	1.00	1.00	0.95	0.96	<b>0.00</b>	0.97	0.93	0.98	1.00	
1.00	1.00	1.00	0.99	0.91	0.97	<b>0.00</b>	1.00	1.00	1.00	
1.00	1.00	1.00	1.00	0.97	0.93	1.00	<b>0.00</b>	1.00	1.00	
1.00	0.96	0.90	1.00	1.00	0.98	1.00	1.00	<b>0.00</b>	1.00	
<b>0.20</b>	1.00	0.99	1.00	0.99	1.00	1.00	1.00	1.00	<b>0.00</b>	

Saliency

 .47
 .90
 .67
 .66
 .47
 .37
 .58
 .67
 .18
 .25

Name

<b>blue</b> 62.9%
<b>orange</b> 93.9%
<b>green</b> 79.8%
<b>red</b> 80.4%
<b>purple</b> 51.4%
<b>brown</b> 54.0%
<b>pink</b> 71.7%
<b>grey</b> 79.4%
<b>yellow</b> 31.2%
<b>blue</b> 25.4%

Tableau-10

Average 0.97

.52













# Palette Design & Color Names

Minimize overlap and ambiguity of colors.

Color Name Distance

<b>0.00</b>	1.00	1.00	0.89	<b>0.07</b>	1.00	<b>0.35</b>	0.99	1.00	0.89
1.00	<b>0.00</b>	0.99	1.00	1.00	0.92	1.00	<b>0.84</b>	0.98	0.99
1.00	0.99	<b>0.00</b>	1.00	0.98	1.00	1.00	1.00	<b>0.17</b>	1.00
0.89	1.00	1.00	<b>0.00</b>	0.98	1.00	<b>0.71</b>	0.93	1.00	<b>0.32</b>
<b>0.07</b>	1.00	0.98	0.98	<b>0.00</b>	1.00	<b>0.36</b>	1.00	0.97	0.95
1.00	0.92	1.00	1.00	1.00	<b>0.00</b>	1.00	0.97	0.99	1.00
<b>0.35</b>	1.00	1.00	<b>0.71</b>	<b>0.36</b>	1.00	<b>0.00</b>	0.95	0.92	<b>0.42</b>
0.99	<b>0.84</b>	1.00	0.93	1.00	0.97	0.95	<b>0.00</b>	0.98	<b>0.85</b>
1.00	0.98	<b>0.17</b>	1.00	0.97	0.99	0.92	0.98	<b>0.00</b>	0.97
0.89	0.99	1.00	<b>0.32</b>	0.95	1.00	<b>0.42</b>	<b>0.85</b>	0.97	<b>0.00</b>

Saliency

 .30
 .21
 .34
 .55
 .20
 .39
 .13
 .16
 .12
 .30

Name

<b>blue</b> 50.5%
<b>red</b> 27.8%
<b>green</b> 36.8%
<b>purple</b> 67.3%
<b>blue</b> 36.6%
<b>orange</b> 51.9%
<b>blue</b> 15.7%
<b>pink</b> 29.4%
<b>green</b> 21.7%
<b>purple</b> 23.9%

Excel-10

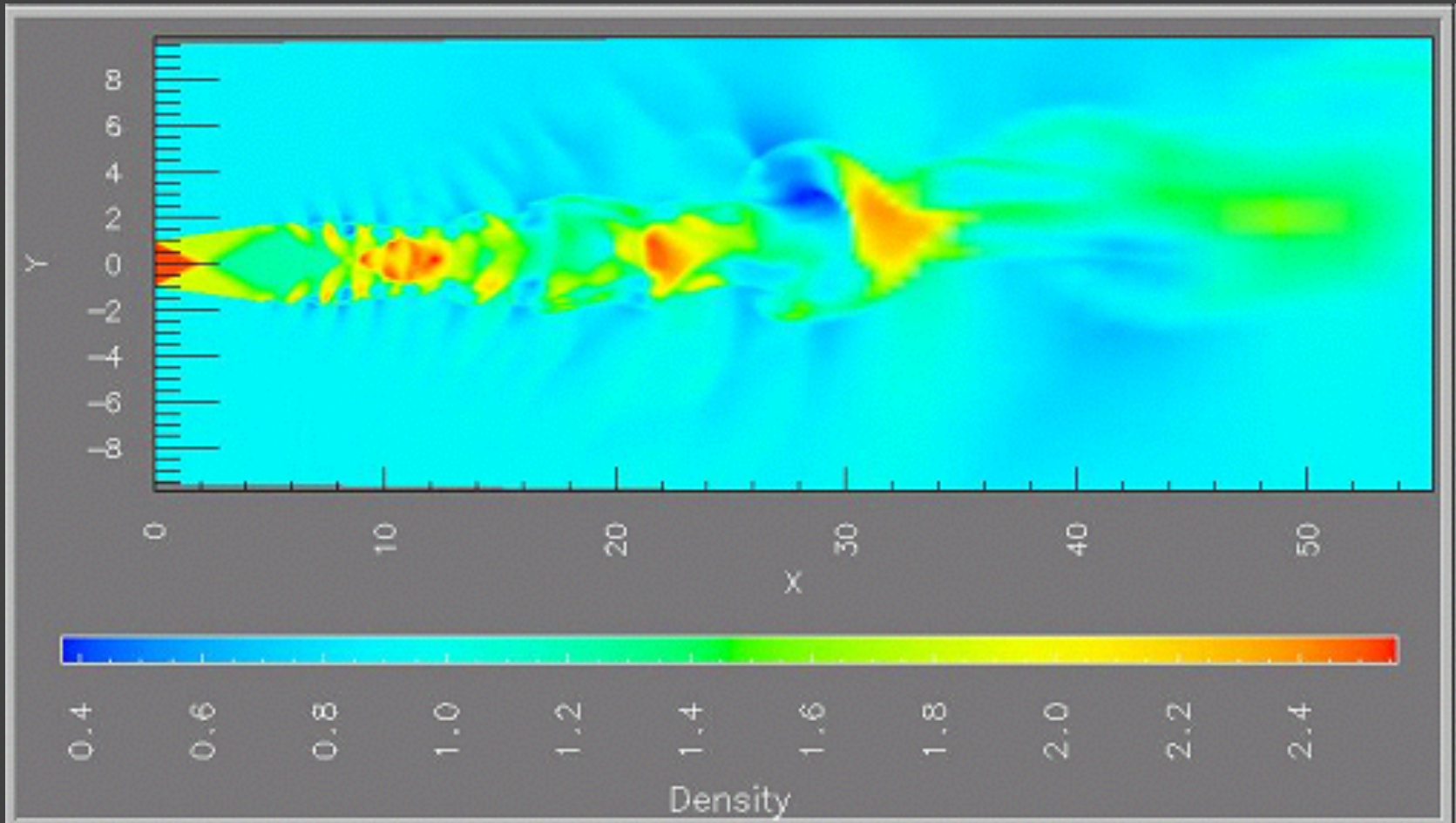
Average 0.87

.27

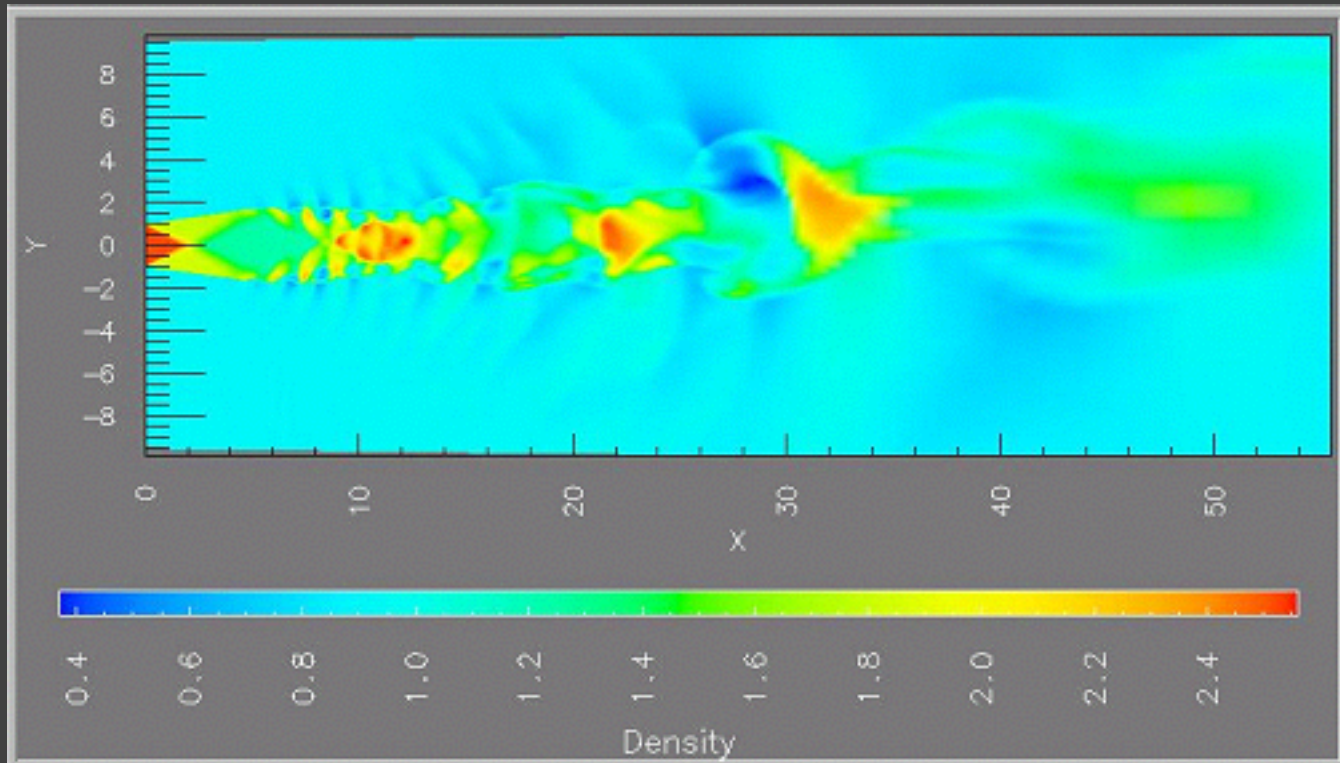
# Quantitative Color



# Rainbow Color Maps



# Be Wary of Rainbows!



1. People segment colors into classes
2. Hues are not naturally ordered
3. Different lightness emphasizes certain scalar values
4. Low luminance colors (blue) hide high frequencies

# Color Brewer: Palettes for Maps

number of data classes on your map

3 [learn more >](#)

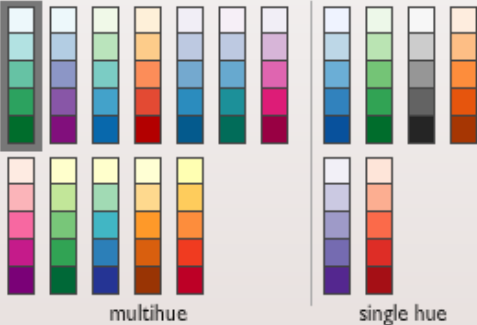
[how to use](#) | [updates](#) | [credits](#)

**COLORBREWER** 2.0  
color advice for cartography

the nature of your data

sequential [learn more >](#)

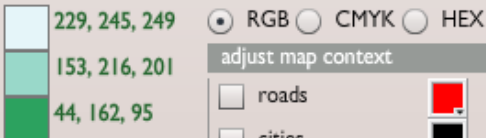
pick a color scheme: BuGn



(optional) only show schemes that are:

- colorblind safe
- print friendly
- photocopy-able [learn more >](#)

pick a color system

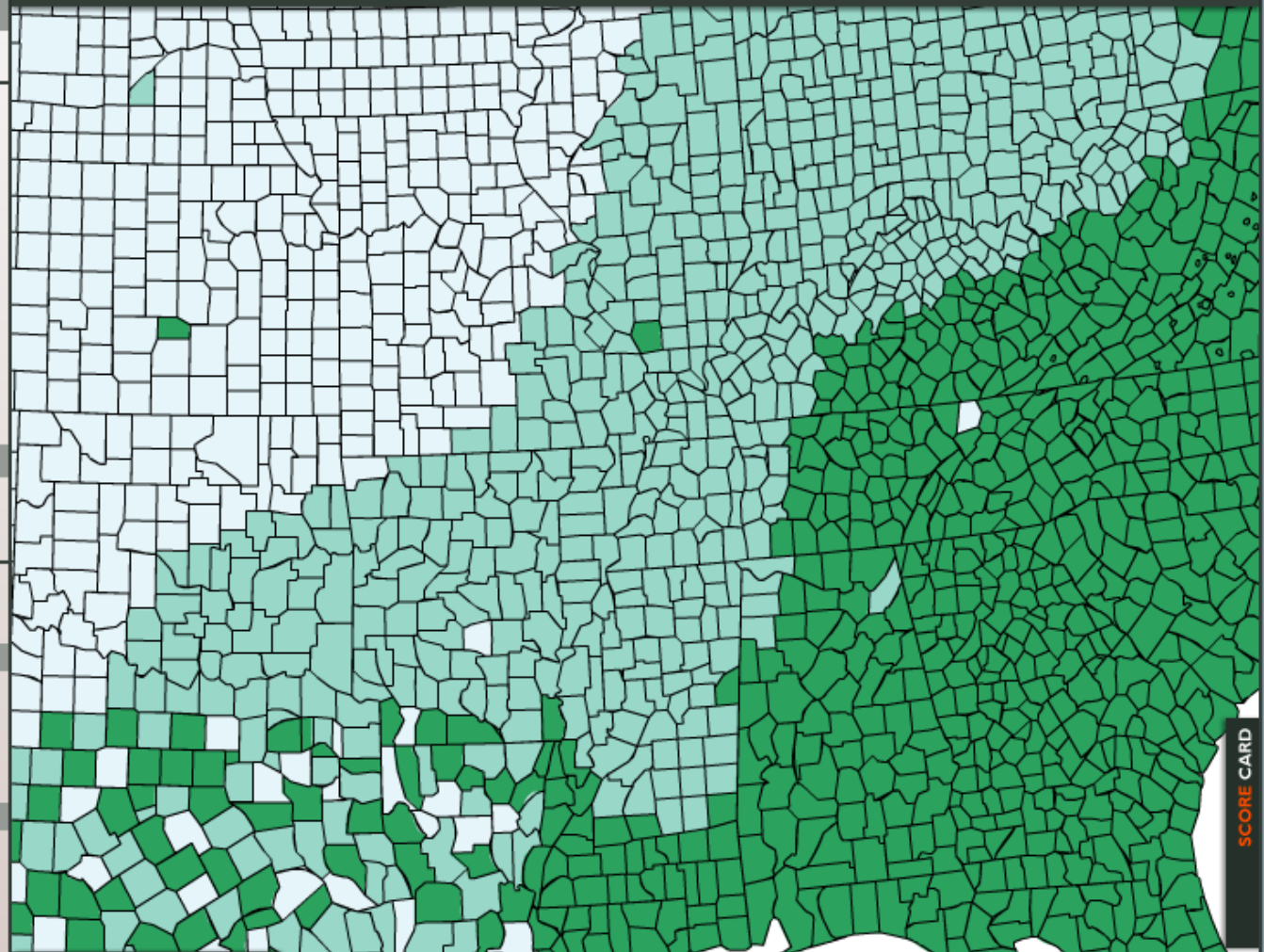


adjust map context

- roads
- cities
- borders

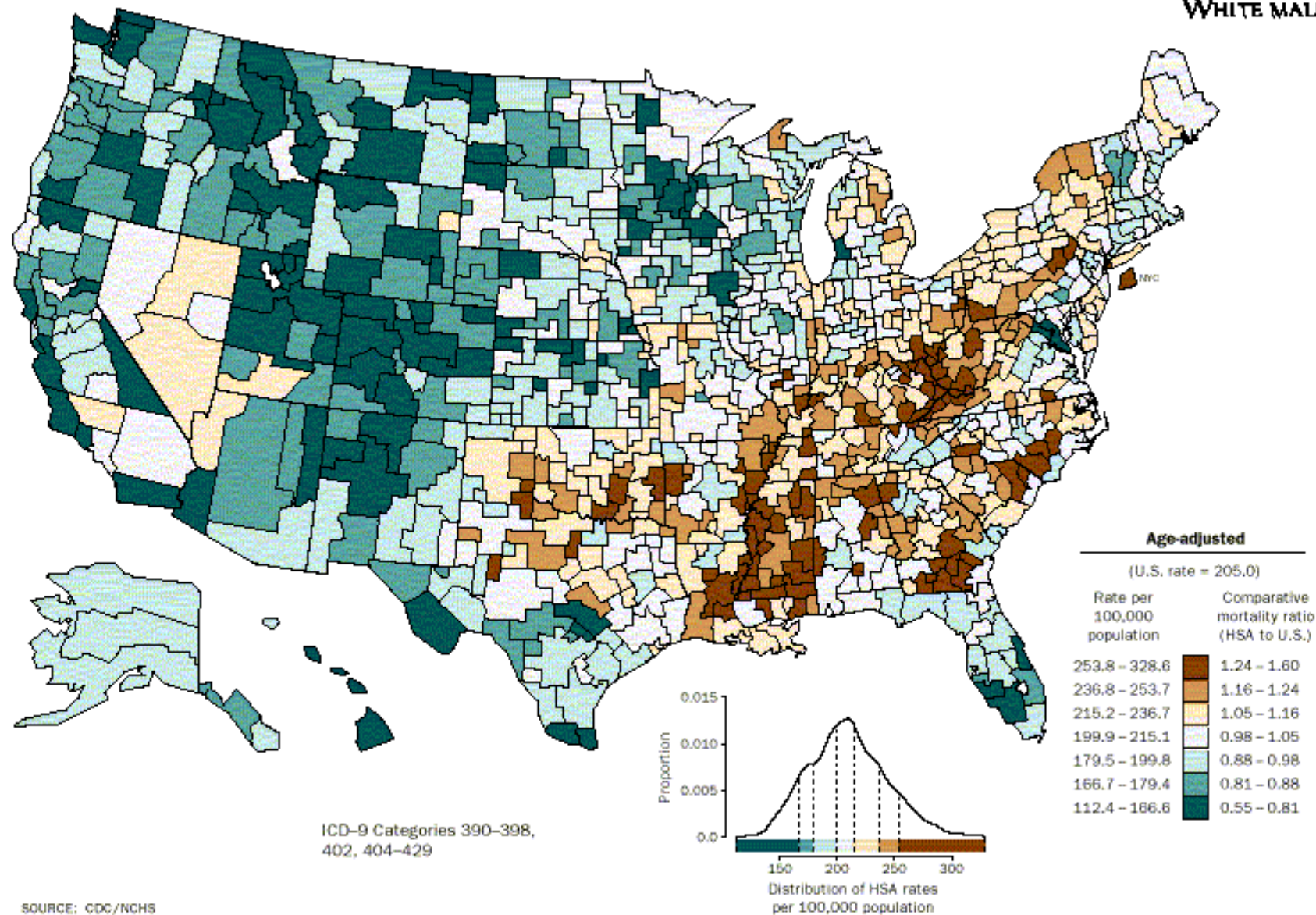
select a background

- solid color
- terrain



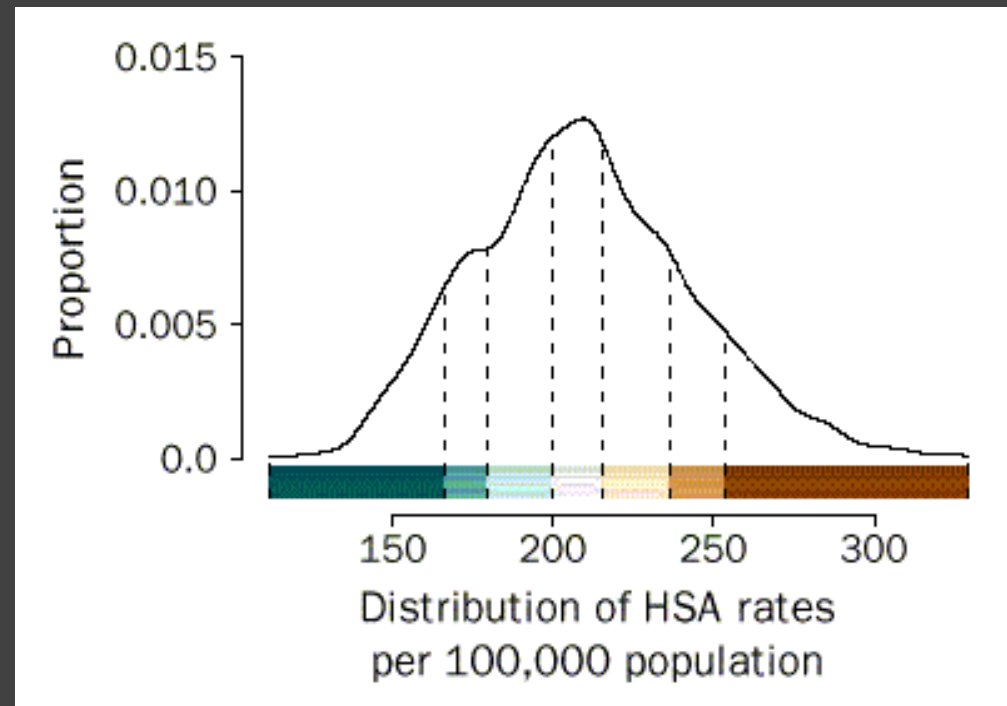
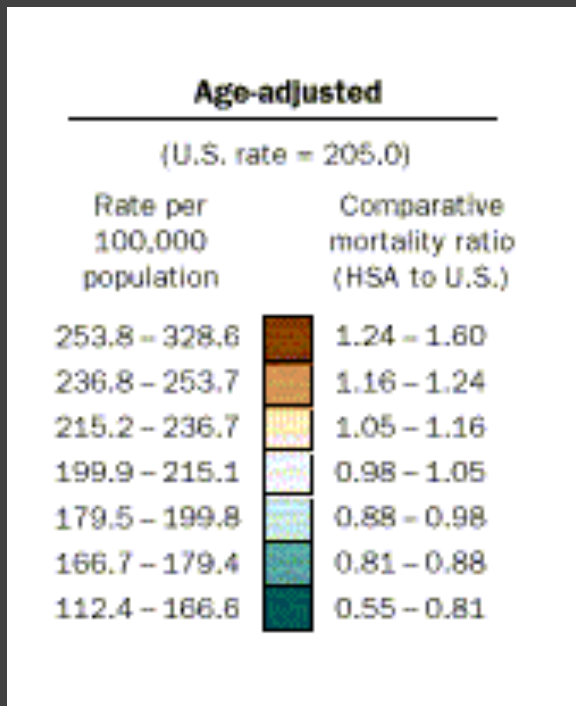


## AGE-ADJUSTED DEATH RATES BY HSA, 1988-92

HEART DISEASE  
WHITE MALE

SOURCE: CDC/NCHS

# Classing Quantitative Data



Age-adjusted mortality rates for the United States.  
Common option: break into 5 or 7 quantiles.

# Classing Quantitative Data

1. Equal interval (arithmetic progression)
2. Quantiles (*recommended*)
3. Standard deviations
4. Clustering (Jenks' natural breaks / 1D K-Means)  
Minimize within group variance  
Maximize between group variance

# Quantitative Color Encoding

## Sequential color scale

Constrain hue, vary luminance/saturation

Map higher values to darker colors



# Quantitative Color Encoding

## Sequential color scale

Constrain hue, vary luminance/saturation  
Map higher values to darker colors



## Diverging color scale

Useful when data has meaningful "midpoint"  
Use neutral color (e.g., grey) for midpoint  
Use saturated colors for endpoints

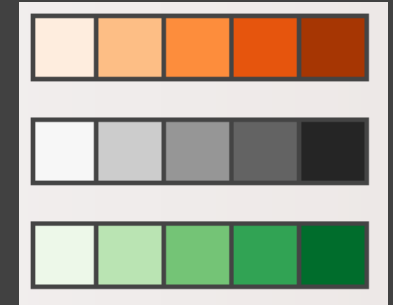




# Quantitative Color Encoding

## Sequential color scale

Constrain hue, vary luminance/saturation  
Map higher values to darker colors



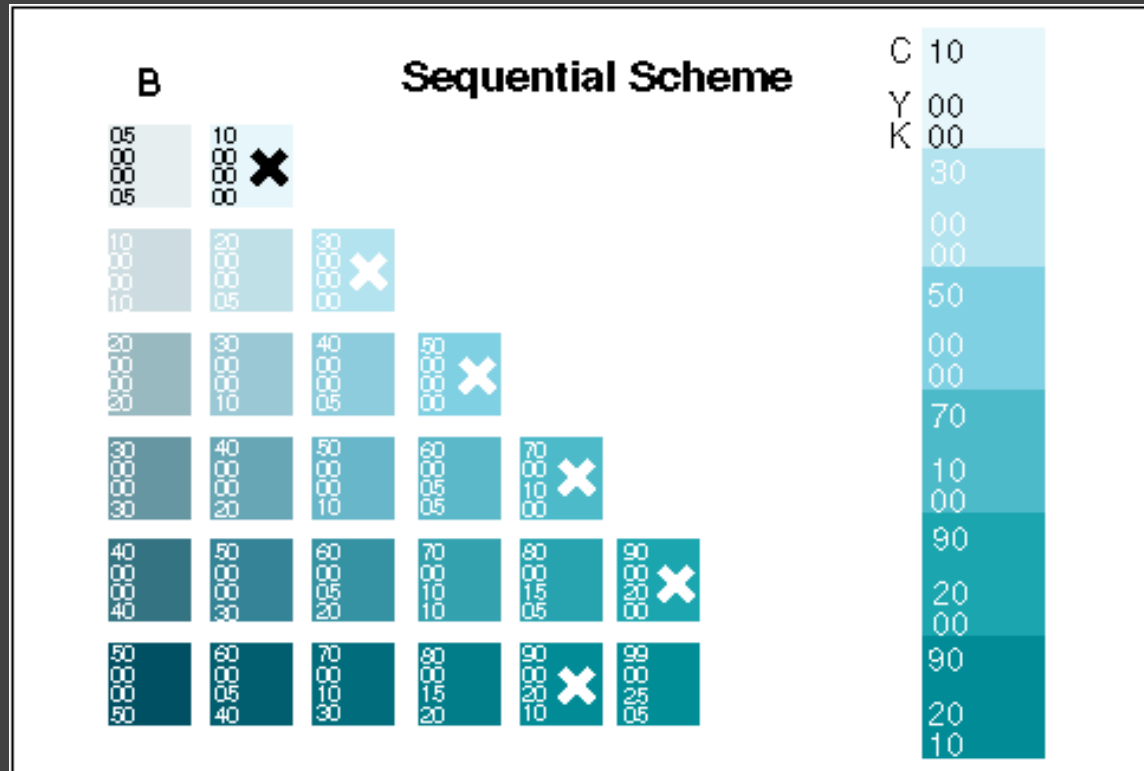
## Diverging color scale

Useful when data has meaningful "midpoint"  
Use neutral color (e.g., grey) for midpoint  
Use saturated colors for endpoints



**Limit number of steps in color to 3-9**

# Designing Sequential Scales



# Designing Sequential Scales

## **Hue-Lightness** (*Recommended*)

Higher values mapped to darker colors

ColorBrewer schemes have 3-9 steps

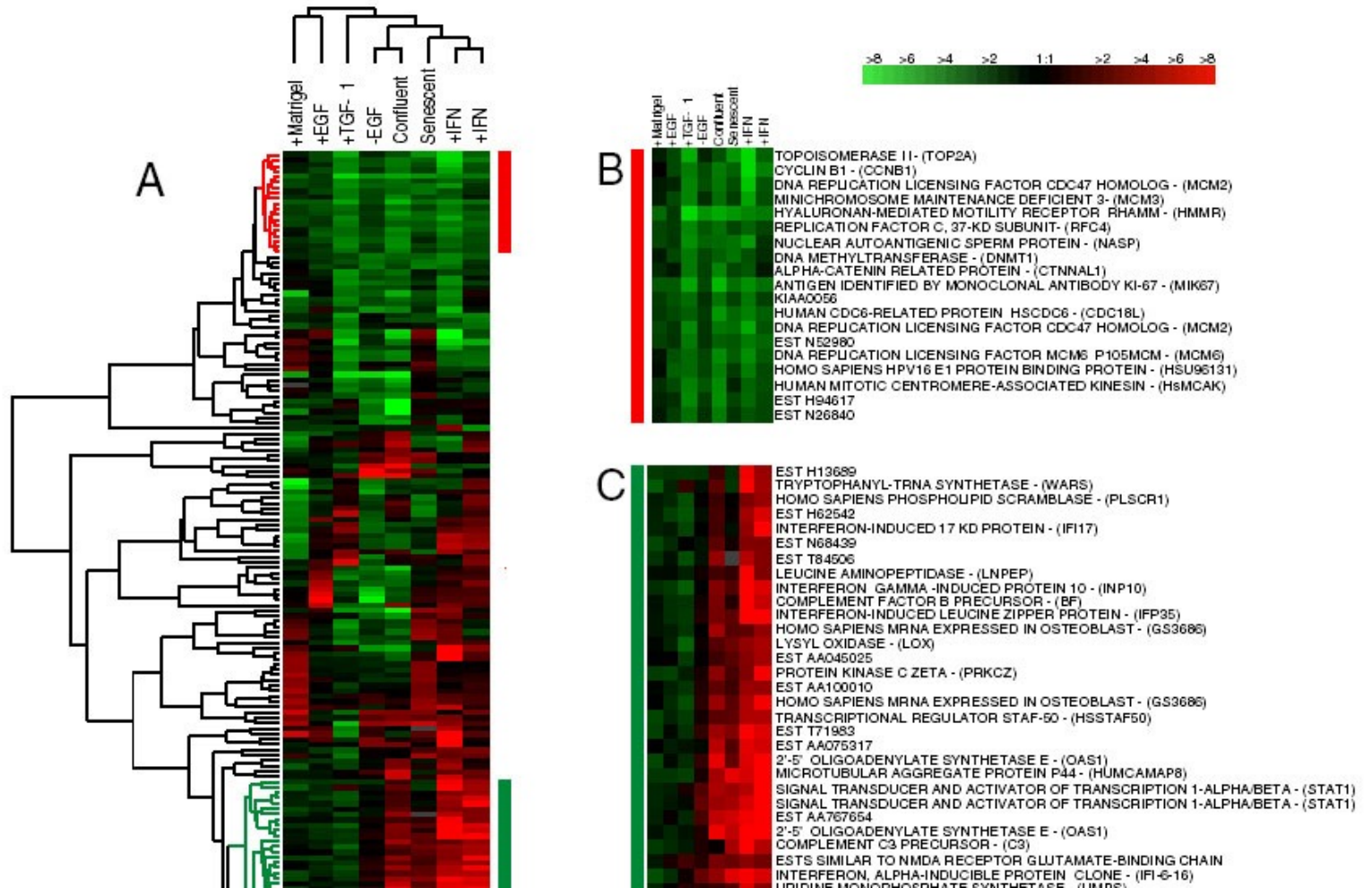
## **Hue Transition**

Two hues

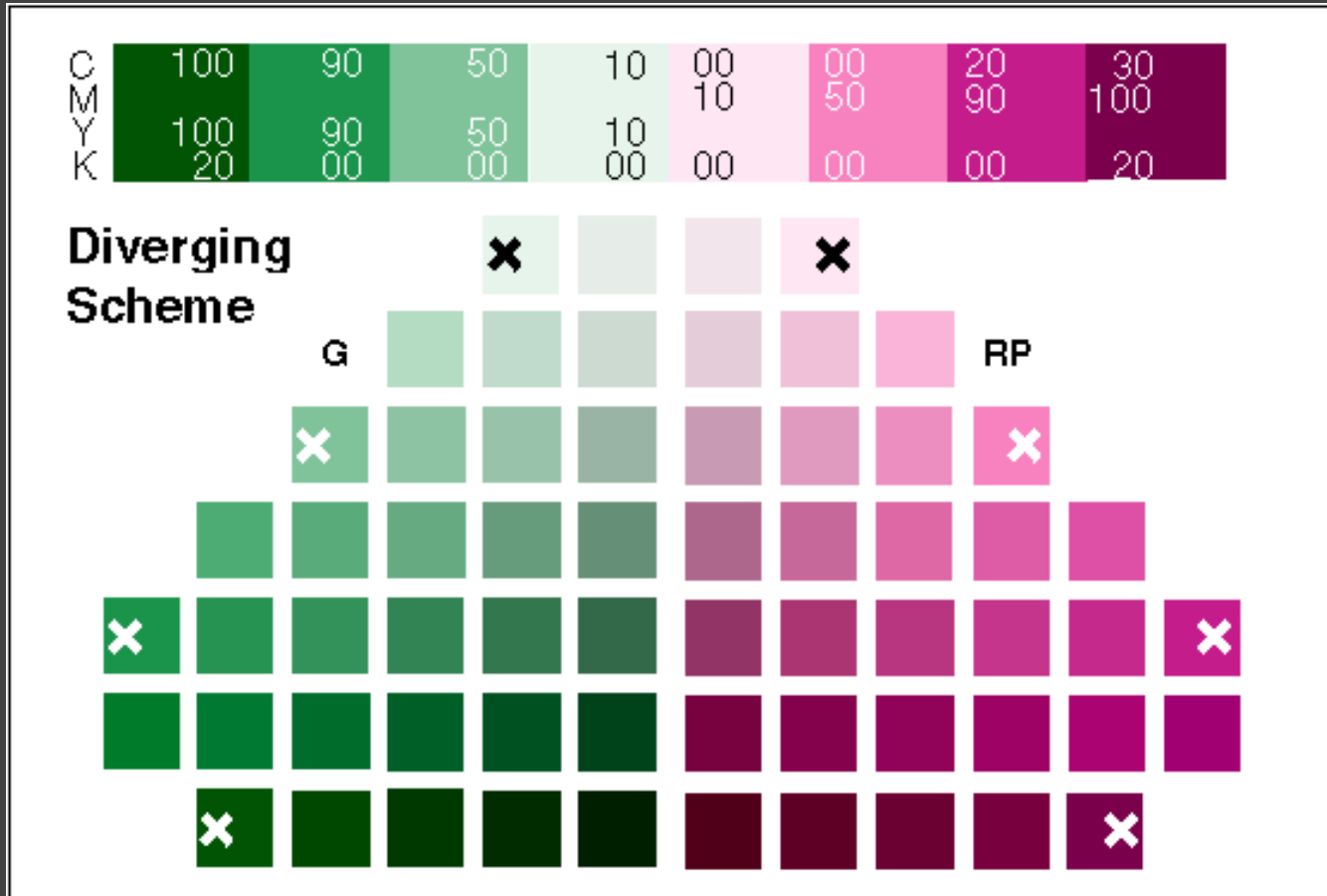
Neighboring hues interpolate better

Couple with change in lightness

# Diverging Color Scheme



# Designing Diverging Scales



# Designing Diverging Scales

## Hue Transition

### Carefully Handle Midpoint

Choose classes of values

Low, Average, High - Average should be gray

### Critical Breakpoint

Defining value e.g., 0

Positive & negative should use different hues

**Extremes saturated, middle desaturated**

# Hints for the Colorist

# Hints for the Colorist

Use **only a few** colors (~6 ideal)



# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

Use **cultural conventions**; appreciate symbolism

# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

Use **cultural conventions**; appreciate symbolism

Get it right in **black and white**

# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

Use **cultural conventions**; appreciate symbolism

Get it right in **black and white**

Respect the **color blind**

# Hints for the Colorist

Use **only a few** colors (~6 ideal)

Colors should be **distinctive** and **named**

Strive for color **harmony** (natural colors?)

Use **cultural conventions**; appreciate symbolism

Get it right in **black and white**

Respect the **color blind**

Take advantage of **perceptual color spaces**