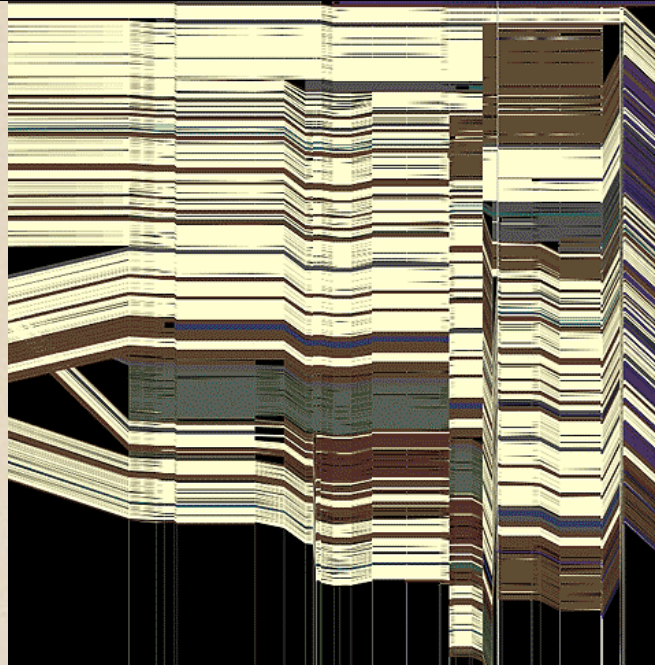
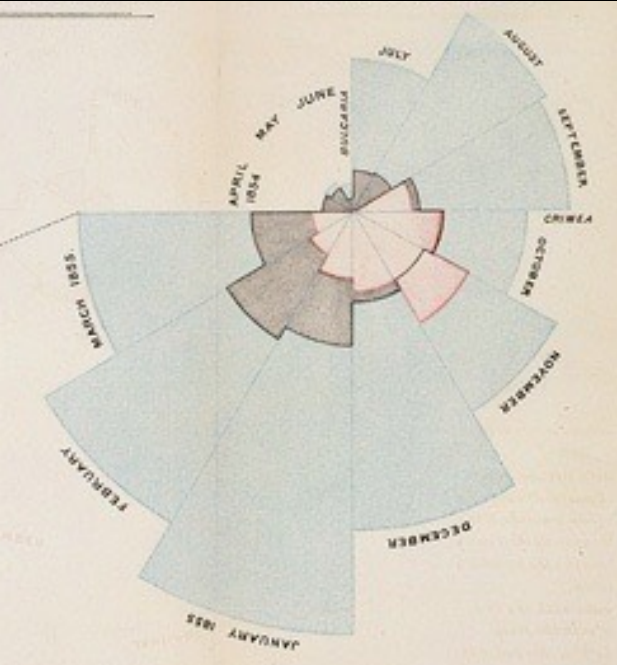


CSE 442 - Data Visualization

Exploratory Data Analysis



Jeffrey Heer University of Washington

What was the **first**
data visualization?

0 BC

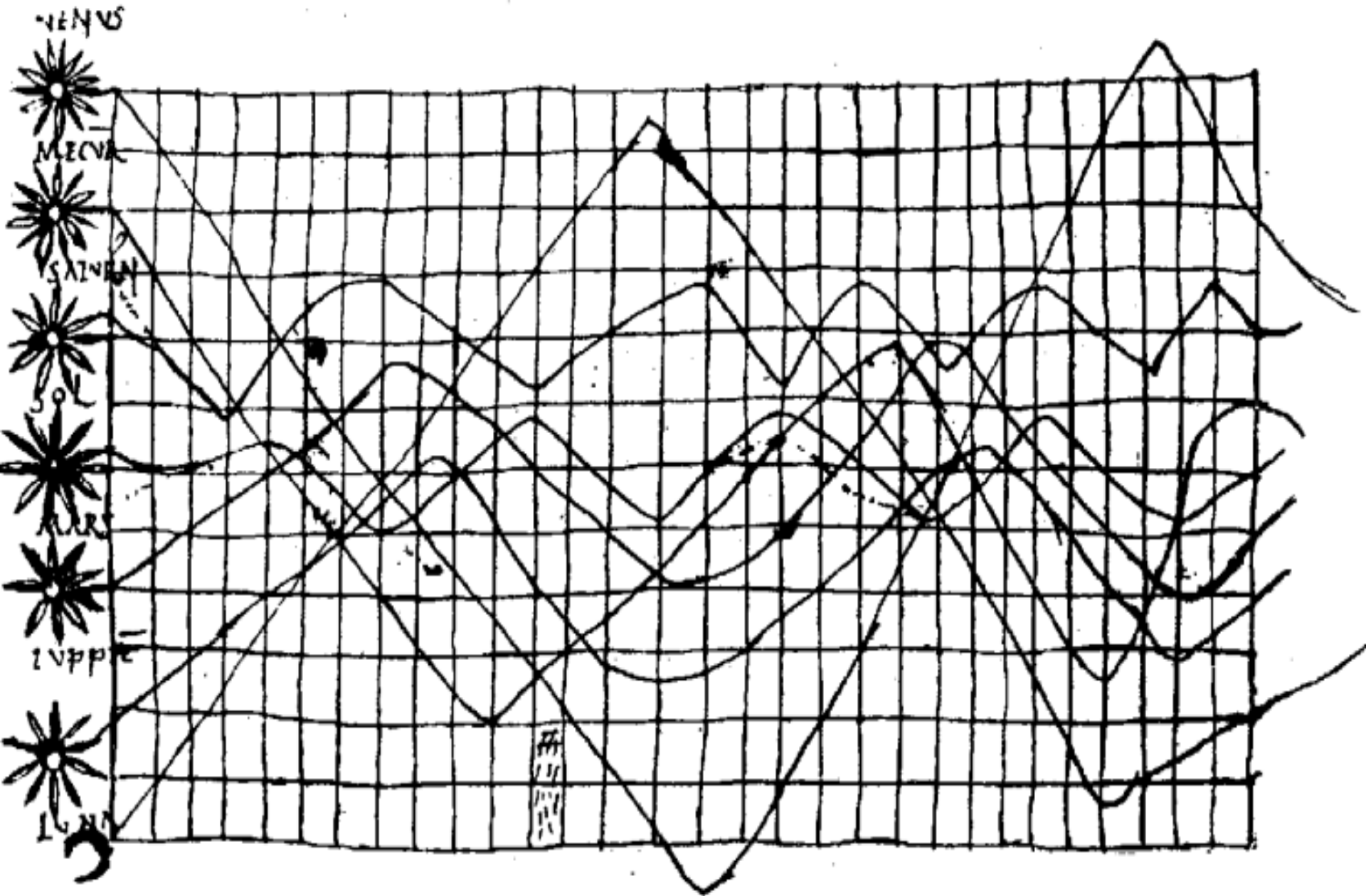




~6200 BC Town Map of Catal Hyuk, Konya Plain, Turkey

0 BC

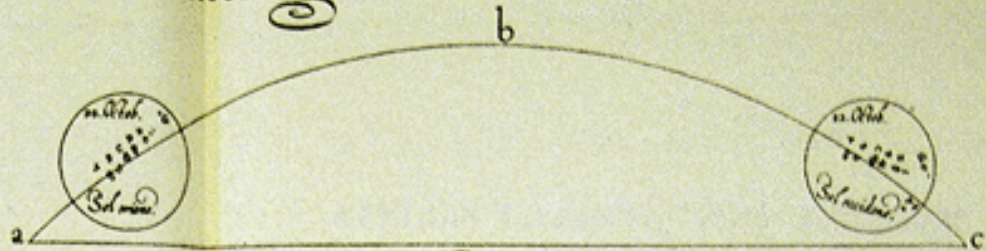




~950 AD Position of Sun, Moon and Planets



MACVLAE IN SOLE APPARENTES, OBSERVATAE
 anno 1611. ad latitudinem grad. 48. min. 40.



a c, horizon. a b c, arcus solis diurnus. Sol oriens ex parte a, maculas exhibet quas vides, occidens vero c, easdem ratione primj motus, non nihil inuertit. Et hanc matutinam vespertinamq; mutationem, omnes maculae quotidie subeunt. Quod semel exhibuisse et mouisse, sufficiat.



Macula M, est
 haec tenus usque
 maxima, nulliq;
 prima magnitudinis
 sideri fixo cedit.

Macula I fuit
 valde conspicua,
 propter notabi-
 lem pra reliquis
 magnitudinem.

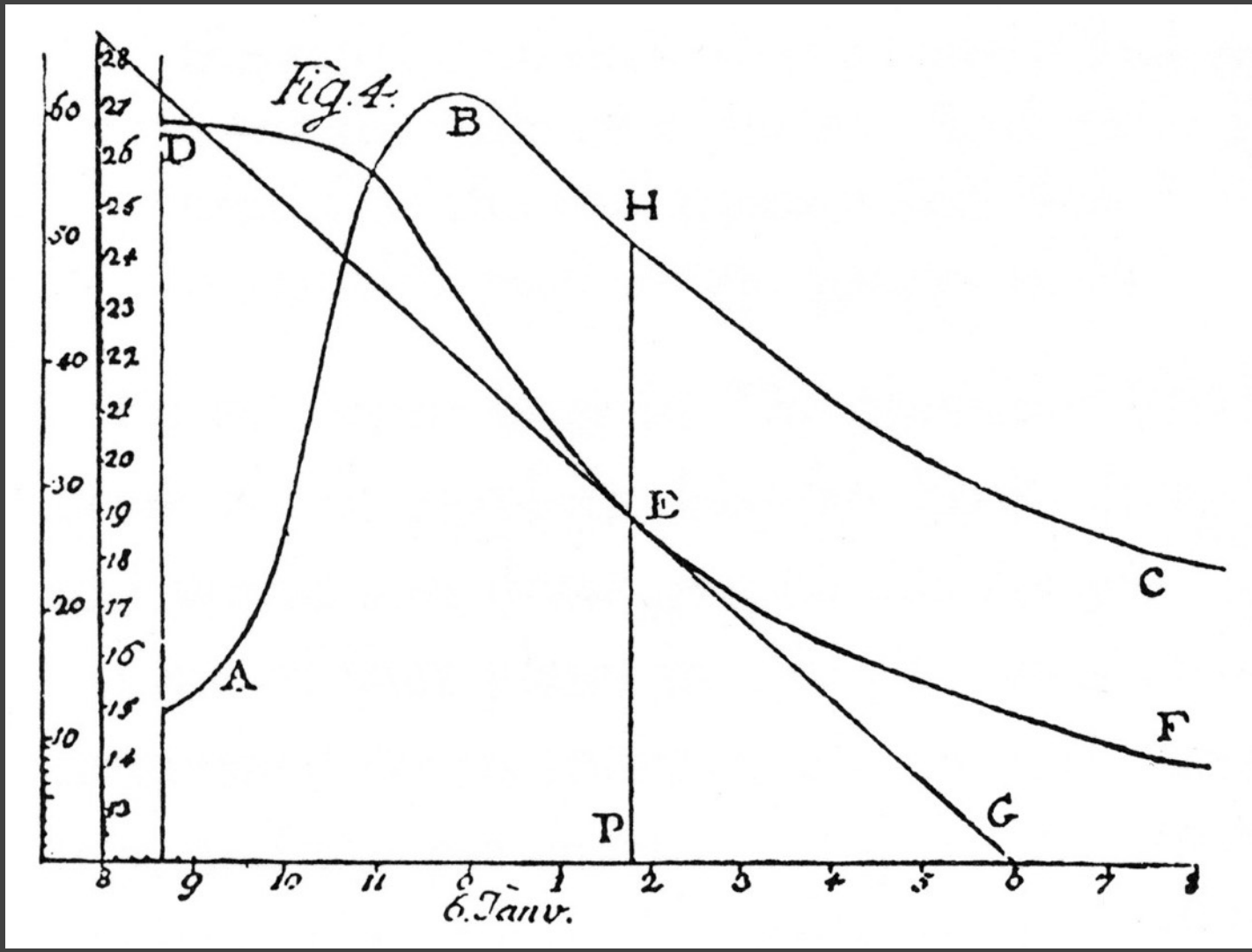
Figura qua
 habet annexum
 signum X, est
 Omittere.

TOLEDO.

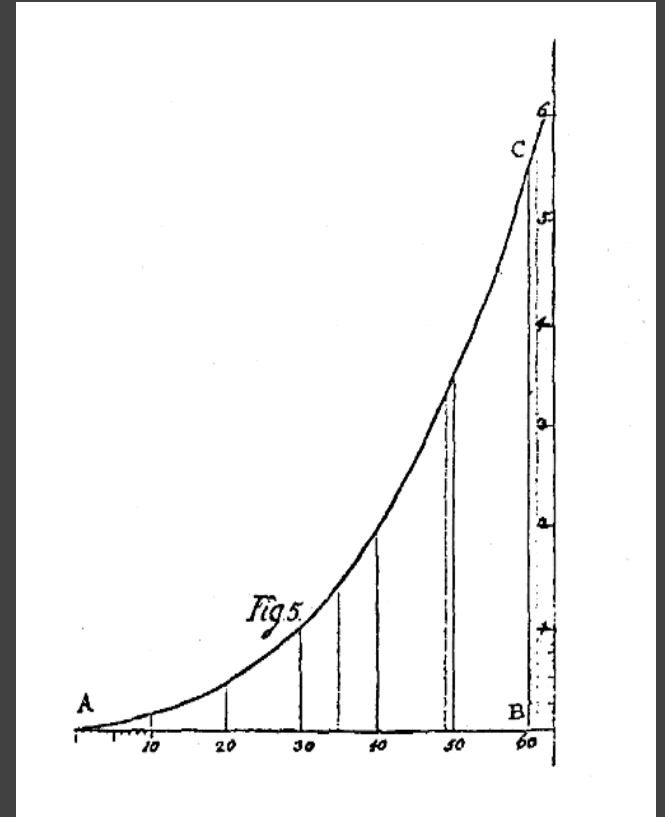
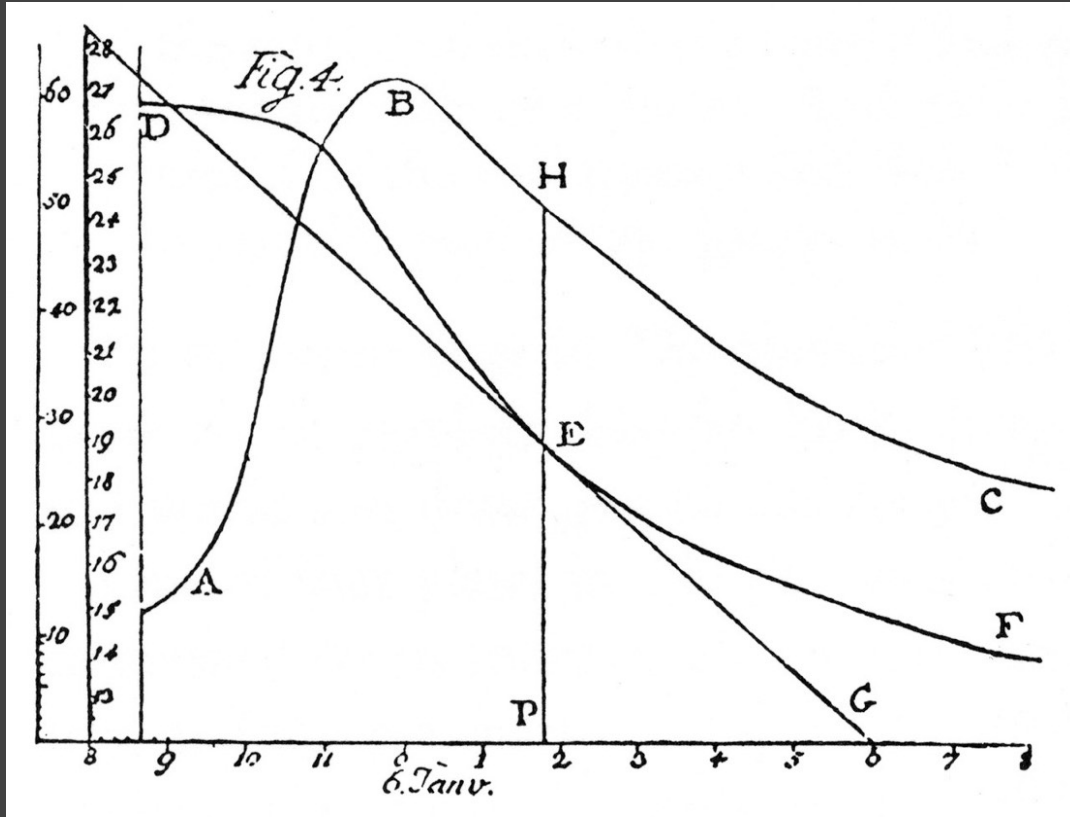
GRADOS DE LA LONGITUD.



Longitudinal distance between Toledo and Rome, van Langren 1644



The Rate of Water Evaporation, Lambert 1765



The Rate of Water Evaporation, Lambert 1765

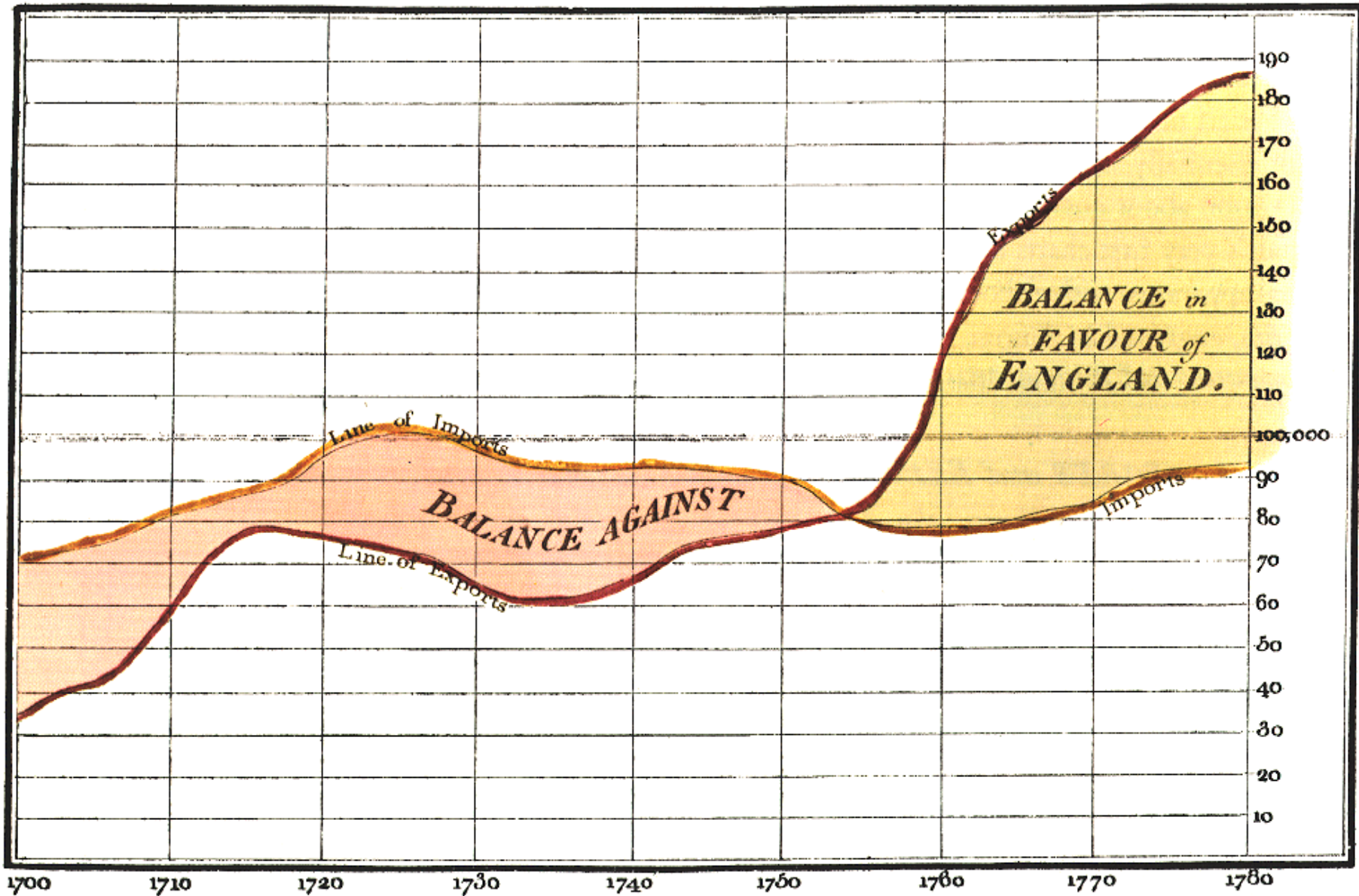


The **Golden Age** of Data Visualization

1786 1900

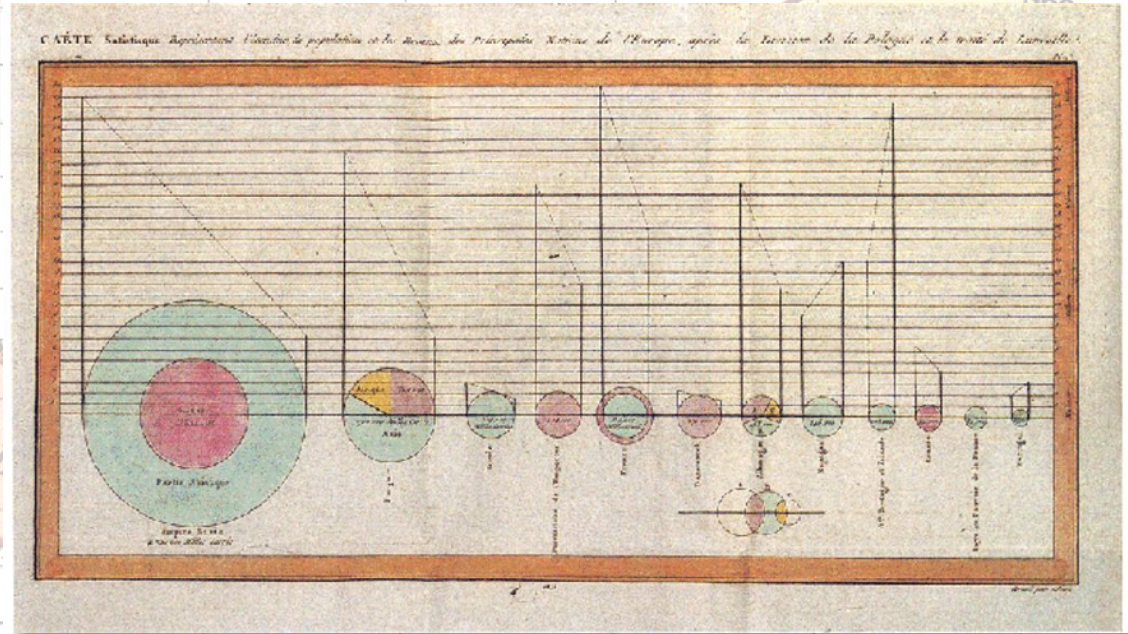
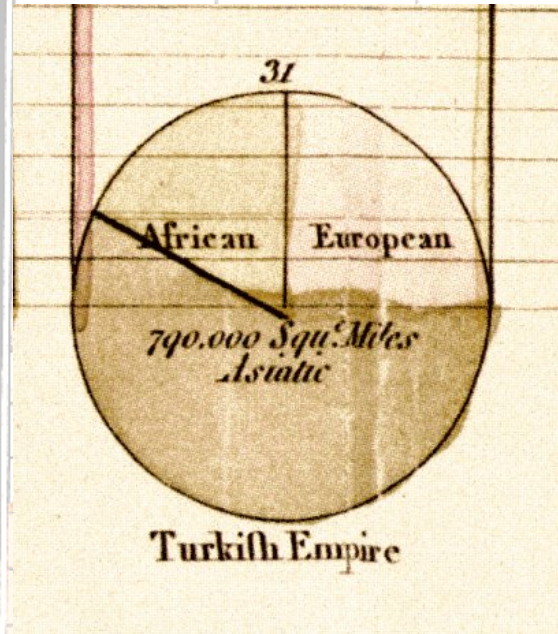
A horizontal white line at the bottom of the slide serves as a timeline. A small vertical tick mark is on the left. A red rectangular segment is positioned on the right side of the line, corresponding to the years 1786 and 1900.

Exports and Imports to and from DENMARK & NORWAY from 1700 to 1780.

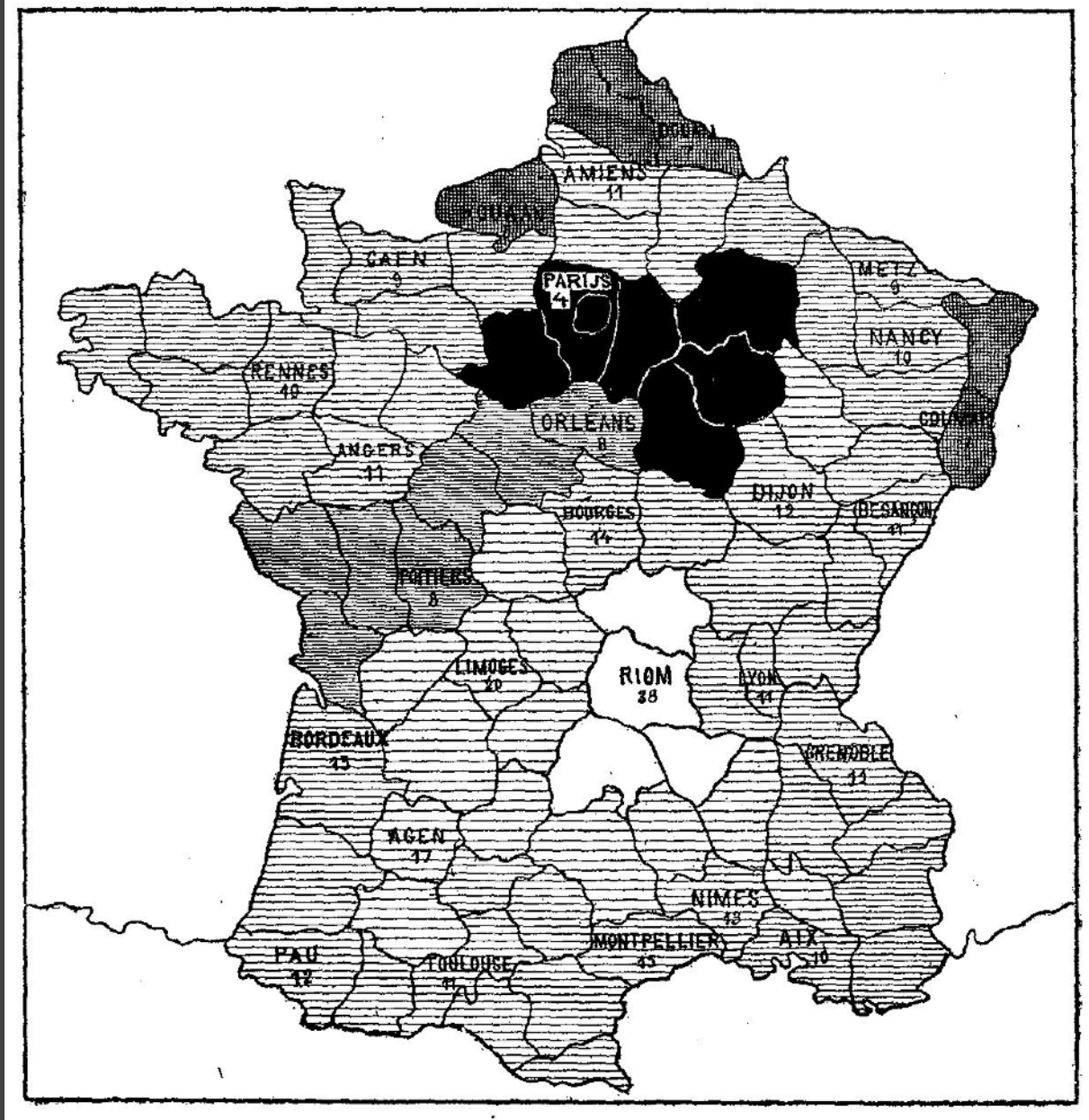


The Commercial and Political Atlas, William Playfair 1786

Exports and Imports to and from DENMARK & NORWAY from 1700 to 1780.



1700 1710 1720 1730 1740 1750 1760 1770 1780



1786 1826(?) Illiteracy in France, Pierre Charles Dupin

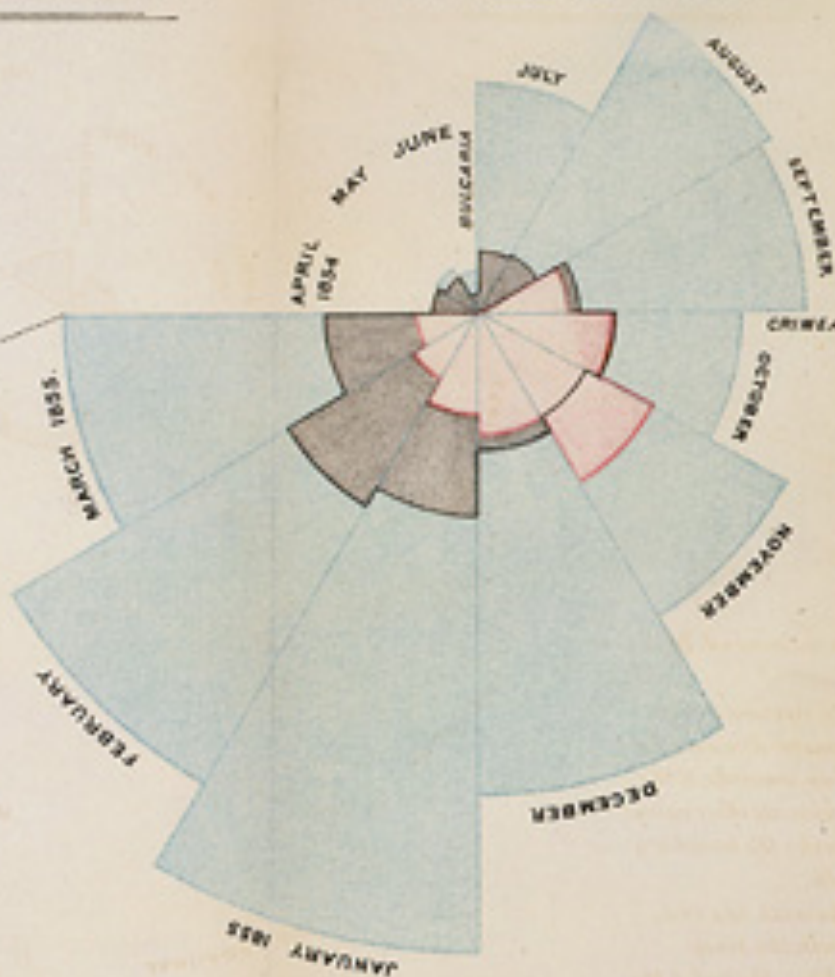


DIAGRAM OF THE CAUSES OF MORTALITY
IN THE ARMY IN THE EAST.

2.
APRIL 1855 TO MARCH 1856.



1.
APRIL 1854 TO MARCH 1855.



"to affect thro' the Eyes
what we fail to convey to
the public through their
word-proof ears"

1786

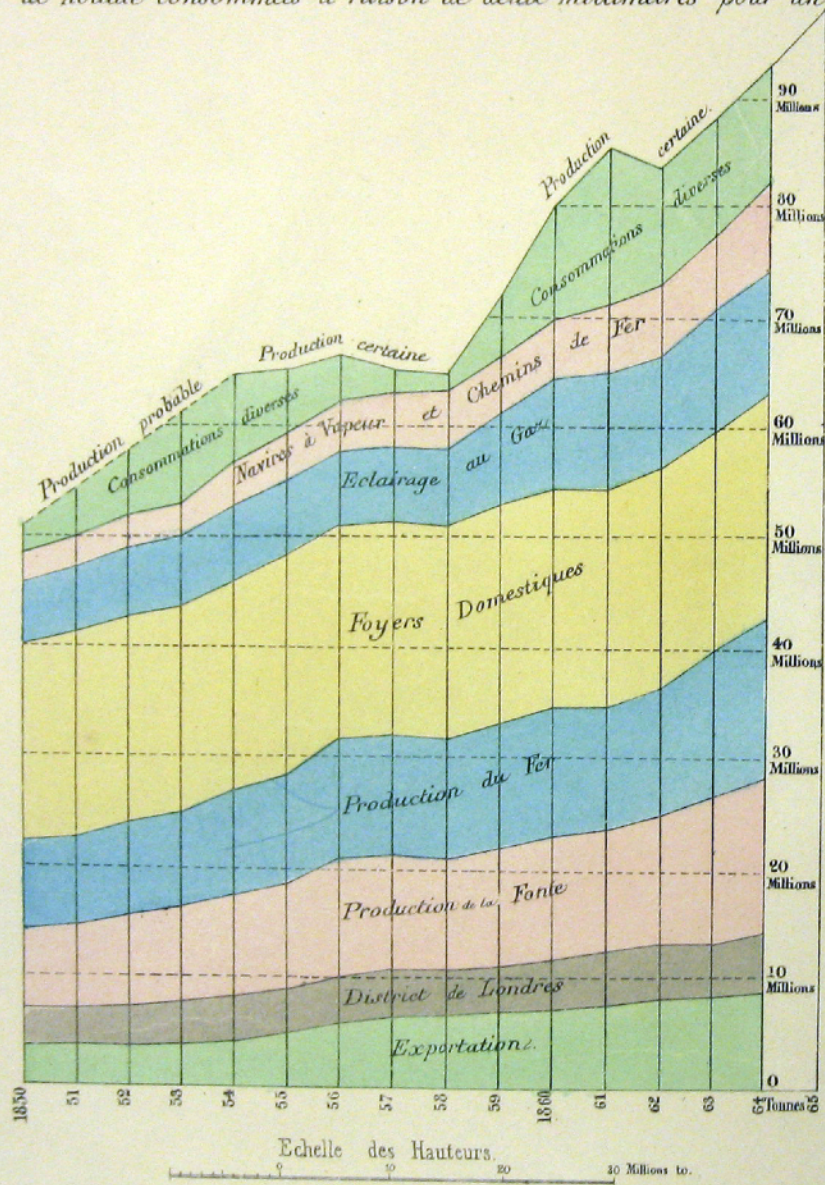
1856 "Coxcomb" of Crimean War Deaths, Florence Nightingale



Consommations approximatives de la Houille dans la Grande Bretagne de 1850 à 1864.

Les abscisses représentent les années et les ordonnées les quantités annuelles de houille consommée.

Les couleurs indiquent les espèces de consommations. Les longueurs d'ordonnées comprises dans une couleur sont les quantités de houille consommées à raison de deux millimètres pour un million de tonnes.



Données admises pour former le Tableau ci-contre.

Consommations. — Sources des Renseignements.

Exportations. — *Mineral statistics 1865 page 214 et Renseignements Parlementaires.*

District de Londres. — *id.* — page 213

Produits de la Fonte. — *id.* — page 215 et pour les années avant 1855 calculée à raison de 3^{tes} de houille pour 1^{re} de fonte, en admettant les quantités annuelles de fonte du Coal question page 192.

Production du fer — *Mineral statistics* — page 215 et pour les années avant 1855 — calculée à raison de 3^{tes} 35 de houille pour 1 tonne de fonte convertie en fer, et admettant $\frac{2}{10}$ de la fonte produite convertie en fer.

Foyers domestiques. — En y comprenant les petites manufactures.

On l'estimait en 1848 à 19 millions de tonnes, (A) qu'on peut réduire à 18 millions to. pour les foyers seuls, mais qu'on peut porter à 20 millions pour la population de 1864.

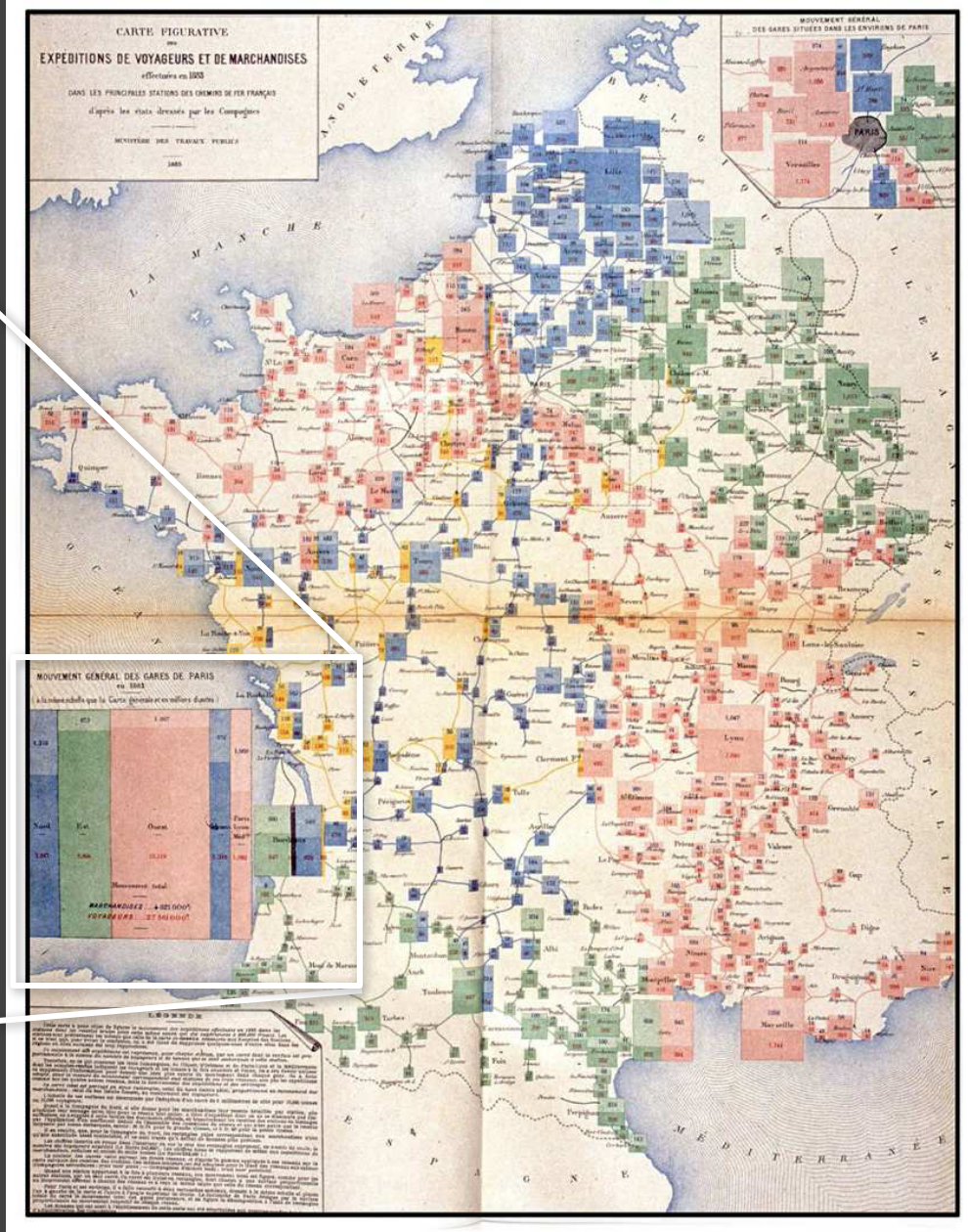
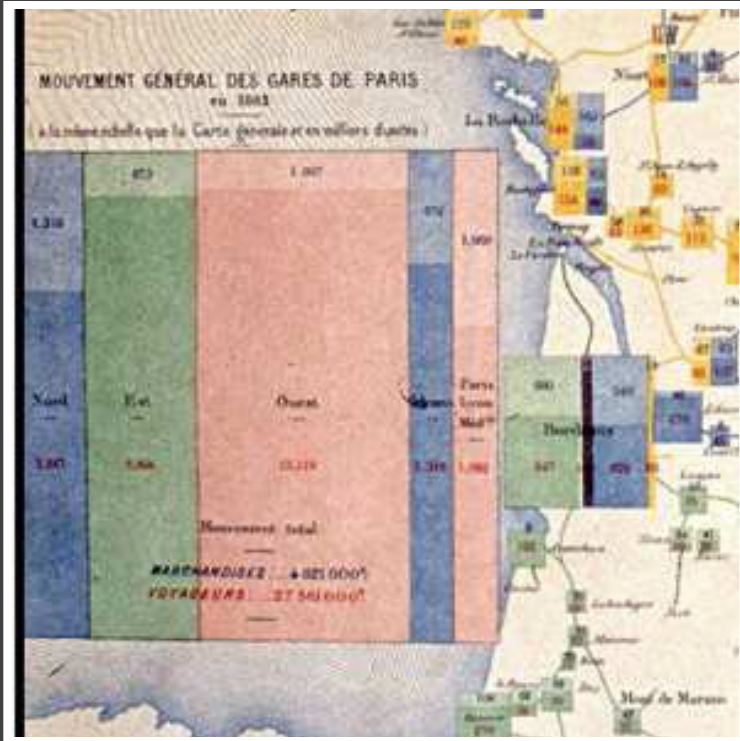
Eclairage au Gaz. — Consommation estimée généralement du $\frac{1}{3}$ au $\frac{1}{8}$ de la production totale.

Exploitation des Chemins de Fer. — En supposant pour consommation totale 10^{tes} par Kilomètre parcouru par les trains d'après les renseignements parlementaires.

Navigation à vapeur. — Calculée à raison de 5^{tes} houille par cheval vapeur et par heure, le nombre de chevaux étant celui du Steam Vessels pour 1864, et les steamers étant supposés marcher la moitié de l'année;

Avant 1864 j'ai supposé les consommations proportionnelles aux tonnages annuels des steamers du statistical abstract et du Board of trade.

(A) Voir l'excellent article houille de M.^r Lamé Fleury, Dictionnaire du Commerce Page III.



1786

1884 Rail Passengers and Freight from Paris

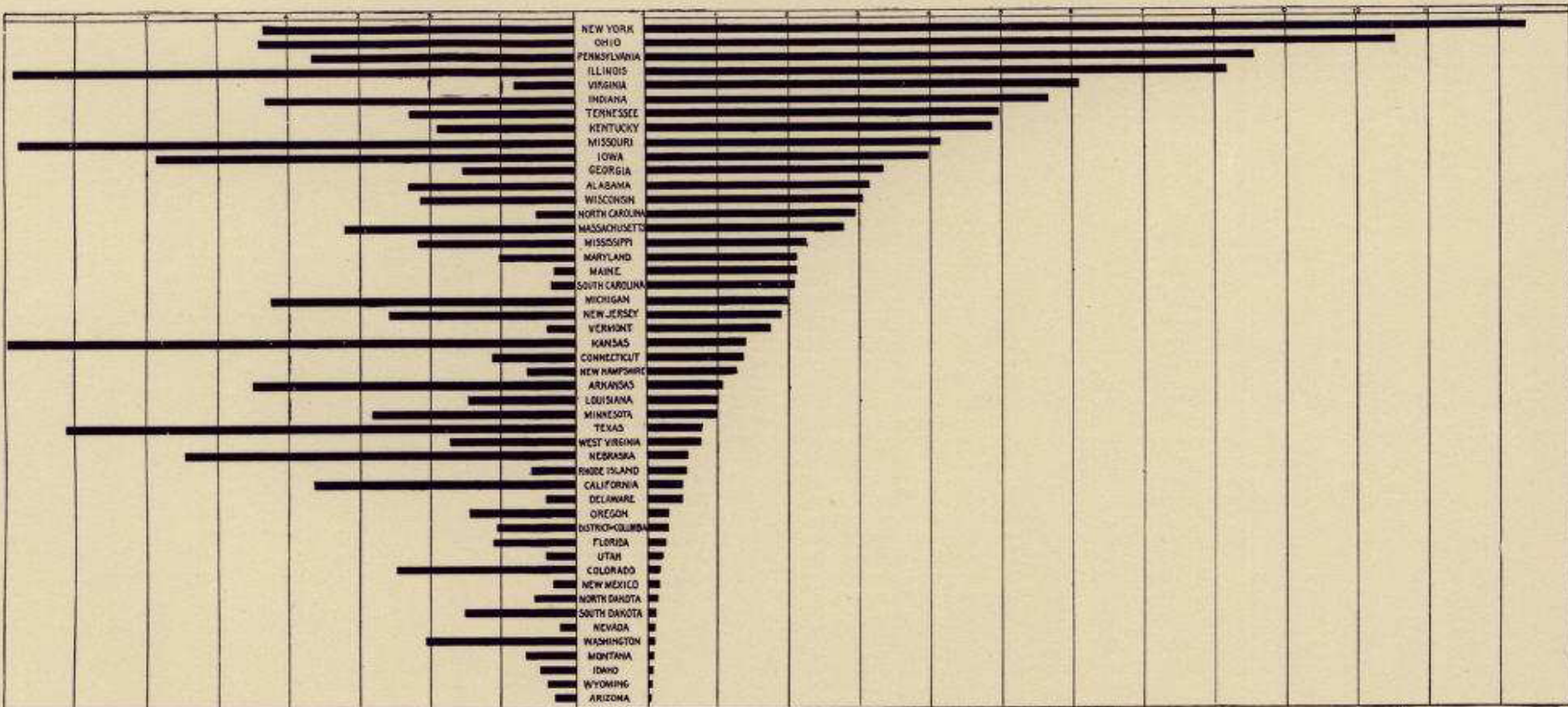


66. INTERSTATE MIGRATION—NUMBER OF NATIVE IMMIGRANTS AND NATIVE EMIGRANTS, BY STATES AND TERRITORIES: 1890.

Native immigrants.

[Hundreds of thousands.]

Native emigrants.



The Rise of Statistics

1786



1900



1950

Rise of **formal methods** in statistics and social science – Fisher, Pearson, ...

Little innovation in graphical methods

A period of **application and popularization**

Graphical methods enter textbooks, curricula, and **mainstream use**

1786

1900

1950





LIFE

1786

Data Analysis & Statistics, Tukey 1962





Four major influences act on data analysis today:

1. The formal theories of statistics.
2. Accelerating developments in computers and display devices.
3. The challenge, in many fields, of more and larger bodies of data.
4. The emphasis on quantification in a wider variety of disciplines.



The last few decades have seen the rise of formal theories of statistics, "legitimizing" variation by confining it by assumption to random sampling, often assumed to involve tightly specified distributions, and restoring the appearance of security by emphasizing narrowly optimized techniques and claiming to make statements with "known" probabilities of error.

LIFE



While some of the influences of statistical theory on data analysis have been helpful, others have not.

LIFE



Exposure, the effective laying open of the data to display the unanticipated, is to us a major portion of data analysis. Formal statistics has given almost no guidance to exposure; indeed, it is not clear how the **informality** and **flexibility** appropriate to the **exploratory character of exposure** can be fitted into any of the structures of formal statistics so far proposed.



Nothing - not the careful logic of mathematics, not statistical models and theories, not the awesome arithmetic power of modern computers - nothing can substitute here for the **flexibility of the informed human mind.**

Accordingly, both approaches and techniques need to be structured so as to **facilitate human involvement and intervention.**

Set A

| X | Y |
|----|-------|
| 10 | 8.04 |
| 8 | 6.95 |
| 13 | 7.58 |
| 9 | 8.81 |
| 11 | 8.33 |
| 14 | 9.96 |
| 6 | 7.24 |
| 4 | 4.26 |
| 12 | 10.84 |
| 7 | 4.82 |
| 5 | 5.68 |

Set B

| X | Y |
|----|------|
| 10 | 9.14 |
| 8 | 8.14 |
| 13 | 8.74 |
| 9 | 8.77 |
| 11 | 9.26 |
| 14 | 8.1 |
| 6 | 6.13 |
| 4 | 3.1 |
| 12 | 9.11 |
| 7 | 7.26 |
| 5 | 4.74 |

Set C

| X | Y |
|----|-------|
| 10 | 7.46 |
| 8 | 6.77 |
| 13 | 12.74 |
| 9 | 7.11 |
| 11 | 7.81 |
| 14 | 8.84 |
| 6 | 6.08 |
| 4 | 5.39 |
| 12 | 8.15 |
| 7 | 6.42 |
| 5 | 5.73 |

Set D

| X | Y |
|----|------|
| 8 | 6.58 |
| 8 | 5.76 |
| 8 | 7.71 |
| 8 | 8.84 |
| 8 | 8.47 |
| 8 | 7.04 |
| 8 | 5.25 |
| 19 | 12.5 |
| 8 | 5.56 |
| 8 | 7.91 |
| 8 | 6.89 |

Summary Statistics

$$u_X = 9.0 \quad \sigma_X = 3.317$$

$$u_Y = 7.5 \quad \sigma_Y = 2.03$$

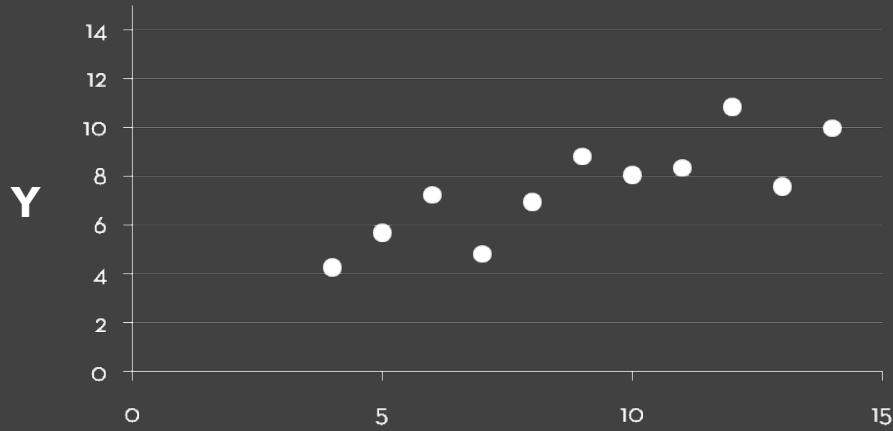
Linear Regression

$$Y = 3 + 0.5 X$$

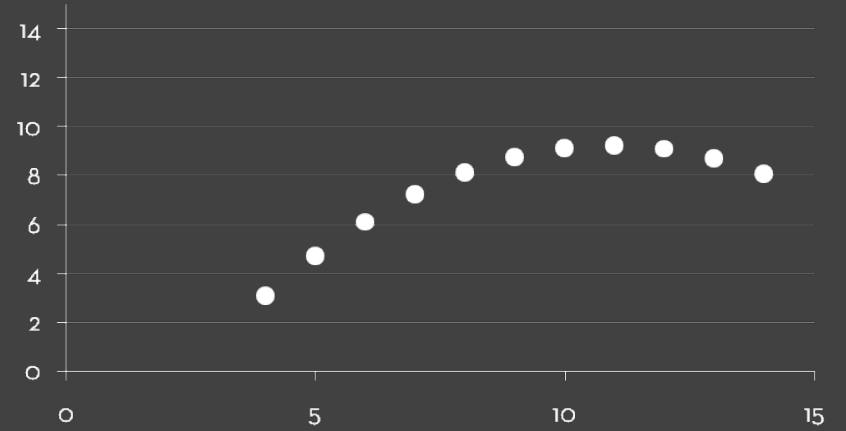
$$R^2 = 0.67$$

[Anscombe 1973]

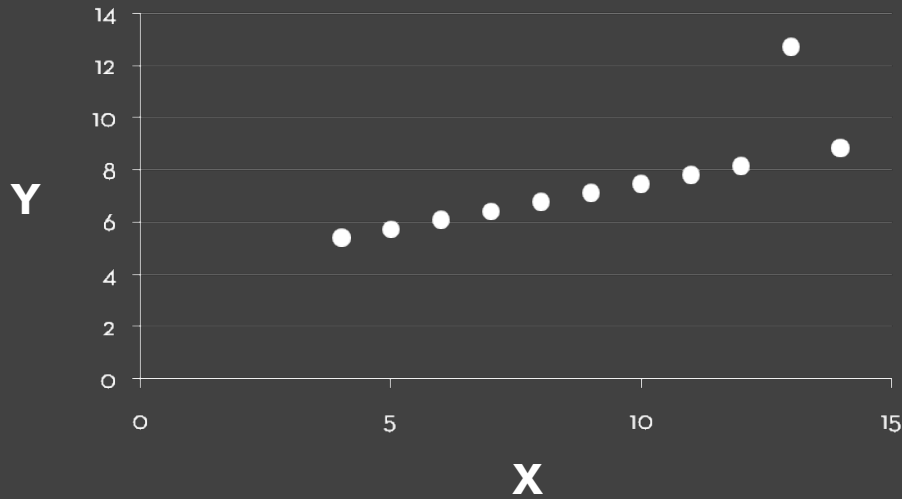
Set A



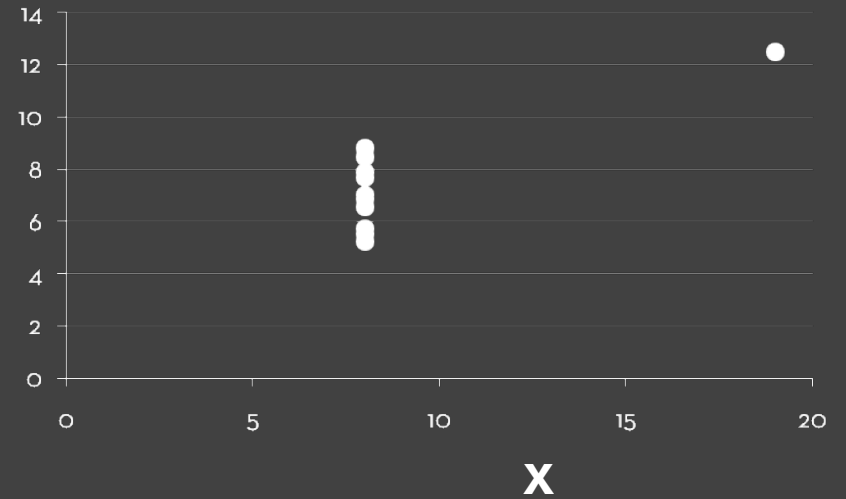
Set B



Set C



Set D



Topics

Exploratory Data Analysis

Data Wrangling

Exploratory Analysis Examples

Polaris / Tableau

Data Wrangling

I spend more than half of my time integrating, cleansing and transforming data without doing any actual analysis. Most of the time I'm lucky if I get to do any "analysis" at all.

Anonymous Data Scientist

[Kandel et al. '12]





**Big Data
Borat**

@BigDataBorat



Following

In Data Science, 80% of time spent prepare data, 20% of time spent complain about need for prepare data.



Reported crime in Alabama

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 4525375 | 4029.3 | 987 | 2732.4 | 309.9 |
| 2005 | 4548327 | 3900 | 955.8 | 2656 | 289 |
| 2006 | 4599030 | 3937 | 968.9 | 2645.1 | 322.9 |
| 2007 | 4627851 | 3974.9 | 980.2 | 2687 | 307.7 |
| 2008 | 4661900 | 4081.9 | 1080.7 | 2712.6 | 288.6 |

Reported crime in Alaska

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 657755 | 3370.9 | 573.6 | 2456.7 | 340.6 |
| 2005 | 663253 | 3615 | 622.8 | 2601 | 391 |
| 2006 | 670053 | 3582 | 615.2 | 2588.5 | 378.3 |
| 2007 | 683478 | 3373.9 | 538.9 | 2480 | 355.1 |
| 2008 | 686293 | 2928.3 | 470.9 | 2219.9 | 237.5 |

Reported crime in Arizona

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 5739879 | 5073.3 | 991 | 3118.7 | 963.5 |
| 2005 | 5953007 | 4827 | 946.2 | 2958 | 922 |
| 2006 | 6166318 | 4741.6 | 953 | 2874.1 | 914.4 |
| 2007 | 6338755 | 4502.6 | 935.4 | 2780.5 | 786.7 |
| 2008 | 6500180 | 4087.3 | 894.2 | 2605.3 | 587.8 |

Reported crime in Arkansas

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 2750000 | 4033.1 | 1096.4 | 2699.7 | 237 |
| 2005 | 2775708 | 4068 | 1085.1 | 2720 | 262 |
| 2006 | 2810872 | 4021.6 | 1154.4 | 2596.7 | 270.4 |
| 2007 | 2834797 | 3945.5 | 1124.4 | 2574.6 | 246.5 |
| 2008 | 2855390 | 3843.7 | 1182.7 | 2433.4 | 227.6 |

Reported crime in California

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 35842038 | 3423.9 | 686.1 | 2033.1 | 704.8 |
| 2005 | 36154147 | 3321 | 692.9 | 1915 | 712 |
| 2006 | 36457549 | 3175.2 | 676.9 | 1831.5 | 666.8 |
| 2007 | 36553215 | 3032.6 | 648.4 | 1784.1 | 600.2 |
| 2008 | 36756666 | 2940.3 | 646.8 | 1769.8 | 523.8 |

Reported crime in Colorado

| Year | Population | Property crime rate | Burglary rate | Larceny-theft rate | Motor vehicle theft rate |
|------|------------|---------------------|---------------|--------------------|--------------------------|
| 2004 | 4601821 | 3918.5 | 717.3 | 2679.5 | 521.6 |

DataWrangler

The screenshot displays the DataWrangler interface. On the left, there are two panels: 'Suggestions' and 'Script'. The 'Suggestions' panel lists four actions: 'Delete rows 8,10', 'Delete empty rows', 'Delete rows where Property_crime_rate is null', and 'Delete rows where Year is null'. The 'Script' panel has an 'Export' button and two script suggestions: 'Split data repeatedly on newline into rows' and 'Split data repeatedly on ',''. On the right, a data table is shown with 408 rows. The table has two columns: '# Year' and '# Property_crime_rate'. The data is as follows:

| # | Year | # | Property_crime_rate |
|----|---------------------------|---|---------------------|
| 1 | Reported crime in Alabama | | |
| 2 | | | |
| 3 | 2004 | | 4029.3 |
| 4 | 2005 | | 3900 |
| 5 | 2006 | | 3937 |
| 6 | 2007 | | 3974.9 |
| 7 | 2008 | | 4081.9 |
| 8 | | | |
| 9 | Reported crime in Alaska | | |
| 10 | | | |
| 11 | 2004 | | 3370.9 |
| 12 | 2005 | | 3615 |
| 13 | 2006 | | 3582 |
| 14 | 2007 | | 3373.9 |

Wrangler: Interactive Visual Specification of Data Transformation Scripts

Sean Kandel et al. *CHI'11*

| CAND_ID | CAND_NAME | CAND_PARTY_AFFILIATION | CAND_ELECTION_YEAR | CAND_OFFICE_STATE | CAND_OFFICE |
|-----------|------------------------------|------------------------|--------------------|-------------------|-------------|
| H0AK00097 | COX, JOHN R. | REP | 2014 | AK | H |
| H0AL02087 | ROBY, MARTHA | REP | 2016 | AL | H |
| H0AL02095 | JOHN, ROBERT E JR | IND | 2016 | AL | H |
| H0AL05049 | CRAMER, ROBERT E "BUD" JR | DEM | 2008 | AL | H |
| H0AL05163 | BROOKS, MO | REP | 2016 | AL | H |
| H0AL06088 | COOKE, STANLEY KYLE | REP | 2010 | AL | H |
| H0AL07086 | SEWELL, TERRI A. | DEM | 2016 | AL | H |
| H0AL07094 | HILLIARD, EARL FREDERICK JR | DEM | 2010 | AL | H |
| H0AL07177 | CHAMBERLAIN, DON | REP | 2012 | AL | H |
| H0AR01083 | CRAWFORD, ERIC ALAN RICK | REP | 2016 | AR | H |
| H0AR01091 | GREGORY, JAMES CHRISTOPHER | DEM | 2010 | AR | H |
| H0AR01109 | CAUSEY, CHAD | DEM | 2010 | AR | H |
| H0AR01125 | SMITH, PRINCELLA D | REP | 2010 | AR | H |
| H0AR02107 | GRIFFIN, JOHN TIMOTHY | REP | 2014 | AR | H |
| H0AR02131 | ELLIOTT, JOYCE ANN | DEM | 2010 | AR | H |
| H0AR03022 | SKOCH, BERNARD KURT "BERNIE" | REP | 2010 | AR | H |
| H0AR03030 | WHITAKER, DAVID JEFFREY | DEM | 2010 | AR | H |
| H0AR03055 | WOMACK, STEVE | REP | 2016 | AR | H |
| H0AS00018 | FALEOMAVAEGA, ENI | DEM | 2014 | AS | H |
| H0AZ01184 | FLAKE, JEFF MR. | REP | 2012 | AZ | H |
| H0AZ01259 | GOSAR, PAUL ANTHONY | REP | 2016 | AZ | H |
| H0AZ01283 | MEHTA, STEVE | REP | 2010 | AZ | H |
| H0AZ01325 | TOBIN, ANDY HON. | REP | 2014 | AZ | H |
| H0AZ01333 | GRESSLEY, FORREST DAYL | REP | 2010 | AZ | H |
| H0AZ03321 | PARKER, VERNON | REP | 2014 | AZ | H |

New Step [Switch to editor](#) Cancel [Add to Recipe](#)

Choose a transformation

| ABC | CAND_ID | Source | to be dropped | Preview | ABC | CAND_NAME | ABC | CAND_NAME1 | ABC | CAND_NAME2 | ABC | CAND_PARTY_AFFILIATION | ABC | CAND_ELECTION_YEAR | ABC | |
|-----|-----------|------------------------------|---------------|---------|-----|------------------|-----|------------------|-----|-----------------------|-----|------------------------|-----|--------------------|-----|---------|
| | | 4,864 Categories | | | | 4,760 Categories | | 3,416 Categories | | 3,677 Categories | | 76 Categories | | 1986 - 2052 | | 57 Cate |
| | H0AK00097 | COX, JOHN R. | | | | COX | | COX | | JOHN R. | | REP | | 2014 | | AK |
| | H0AL02087 | ROBY, MARTHA | | | | ROBY | | ROBY | | MARTHA | | REP | | 2016 | | AL |
| | H0AL02095 | JOHN, ROBERT E JR | | | | JOHN | | JOHN | | ROBERT E JR | | IND | | 2016 | | AL |
| | H0AL05049 | CRAMER, ROBERT E "BUD" JR | | | | CRAMER | | CRAMER | | ROBERT E "BUD" JR | | DEM | | 2008 | | AL |
| | H0AL05163 | BROOKS, MO | | | | BROOKS | | BROOKS | | MO | | REP | | 2016 | | AL |
| | H0AL06088 | COOKE, STANLEY KYLE | | | | COOKE | | COOKE | | STANLEY KYLE | | REP | | 2010 | | AL |
| | H0AL07086 | SEWELL, TERRI A. | | | | SEWELL | | SEWELL | | TERRI A. | | DEM | | 2016 | | AL |
| | H0AL07094 | HILLIARD, EARL FREDERICK JR | | | | HILLIARD | | HILLIARD | | EARL FREDERICK JR | | DEM | | 2010 | | AL |
| | H0AL07177 | CHAMBERLAIN, DON | | | | CHAMBERLAIN | | CHAMBERLAIN | | DON | | REP | | 2012 | | AL |
| | H0AR01083 | CRAWFORD, ERIC ALAN RICK | | | | CRAWFORD | | CRAWFORD | | ERIC ALAN RICK | | REP | | 2016 | | AR |
| | H0AR01091 | GREGORY, JAMES CHRISTOPHER | | | | GREGORY | | GREGORY | | JAMES CHRISTOPHER | | DEM | | 2010 | | AR |
| | H0AR01109 | CAUSEY, CHAD | | | | CAUSEY | | CAUSEY | | CHAD | | DEM | | 2010 | | AR |
| | H0AR01125 | SMITH, PRINCELLA D | | | | SMITH | | SMITH | | PRINCELLA D | | REP | | 2010 | | AR |
| | H0AR02107 | GRIFFIN, JOHN TIMOTHY | | | | GRIFFIN | | GRIFFIN | | JOHN TIMOTHY | | REP | | 2014 | | AR |
| | H0AR02131 | ELLIOTT, JOYCE ANN | | | | ELLIOTT | | ELLIOTT | | JOYCE ANN | | DEM | | 2010 | | AR |
| | H0AR03022 | SKOCH, BERNARD KURT "BERNIE" | | | | SKOCH | | SKOCH | | BERNARD KURT "BERNIE" | | REP | | 2010 | | AR |
| | H0AR03030 | WHITAKER, DAVID JEFFREY | | | | WHITAKER | | WHITAKER | | DAVID JEFFREY | | DEM | | 2010 | | AR |
| | H0AR03055 | WOMACK, STEVE | | | | WOMACK | | WOMACK | | STEVE | | REP | | 2016 | | AR |
| | H0AS00018 | FALEOMAVAEGA, ENI | | | | FALEOMAVAEGA | | FALEOMAVAEGA | | ENI | | DEM | | 2014 | | AS |
| | H0AZ01184 | FLAKE, JEFF MR. | | | | FLAKE | | FLAKE | | JEFF MR. | | REP | | 2012 | | AZ |
| | H0AZ01259 | GOSAR, PAUL ANTHONY | | | | GOSAR | | GOSAR | | PAUL ANTHONY | | REP | | 2016 | | AZ |

SUGGESTIONS

Split CAND_NAME into 2 columns on '{delim-ws}'

| ABC | CAND_NAME | ABC | CAND_NAME1 | ABC | CAND_NAME2 |
|-----|-------------------|-----|------------|-----|-------------|
| | COX, JOHN R. | | COX | | JOHN R. |
| | ROBY, MARTHA | | ROBY | | MARTHA |
| | JOHN, ROBERT E JR | | JOHN | | ROBERT E JR |

Affects 1 column, 4859 rows Creates 2 columns

Extract '{delim-ws}' from CAND_NAME

| ABC | CAND_NAME | ABC | CAND_NAME1 |
|-----|-------------------|-----|------------|
| | COX, JOHN R. | | , |
| | ROBY, MARTHA | | , |
| | JOHN, ROBERT E JR | | , |

Affects 1 column, 4859 rows Creates 1 column

Count occurrences of '{delim-ws}'

| ABC | CAND_NAME |
|-----|-------------------|
| | COX, JOHN R. |
| | ROBY, MARTHA |
| | JOHN, ROBERT E JR |

Affects 1 column, 4859 rows

| CAND_ID | CAND_NAME | CAND_PARTY_AFFILIATION | CAND_ELECTION_YEAR | CAND_OFFICE_STATE | CAND_OFFICE |
|-----------|------------------------------|------------------------|--------------------|-------------------|-------------|
| H0AK00097 | COX, JOHN R. | REP | 2014 | AK | H |
| H0AL02087 | ROBY, MARTHA | REP | 2016 | AL | H |
| H0AL02095 | JOHN, ROBERT E JR | IND | 2016 | AL | H |
| H0AL05049 | CRAMER, ROBERT E "BUD" JR | DEM | 2008 | AL | H |
| H0AL05163 | BROOKS, MO | REP | 2016 | AL | H |
| H0AL06088 | COOKE, STANLEY KYLE | REP | 2010 | AL | H |
| H0AL07086 | SEWELL, TERRI A. | DEM | 2016 | AL | H |
| H0AL07094 | HILLIARD, EARL FREDERICK JR | DEM | 2010 | AL | H |
| H0AL07177 | CHAMBERLAIN, DON | REP | 2012 | AL | H |
| H0AR01083 | CRAWFORD, ERIC ALAN RICK | REP | 2016 | AR | H |
| H0AR01091 | GREGORY, JAMES CHRISTOPHER | DEM | 2010 | AR | H |
| H0AR01109 | CAUSEY, CHAD | DEM | 2010 | AR | H |
| H0AR01125 | SMITH, PRINCELLA D | REP | 2010 | AR | H |
| H0AR02107 | GRIFFIN, JOHN TIMOTHY | REP | 2014 | AR | H |
| H0AR02131 | ELLIOTT, JOYCE ANN | DEM | 2010 | AR | H |
| H0AR03022 | SKOCH, BERNARD KURT "BERNIE" | REP | 2010 | AR | H |
| H0AR03030 | WHITAKER, DAVID JEFFREY | DEM | 2010 | AR | H |
| H0AR03055 | WOMACK, STEVE | REP | 2016 | AR | H |
| H0AS00018 | FALEOMAVAEGA, ENI | DEM | 2014 | AS | H |
| H0AZ01184 | FLAKE, JEFF MR. | REP | 2012 | AZ | H |
| H0AZ01259 | GOSAR, PAUL ANTHONY | REP | 2016 | AZ | H |
| H0AZ01283 | MEHTA, STEVE | REP | 2010 | AZ | H |
| H0AZ01325 | TOBIN, ANDY HON. | REP | 2014 | AZ | H |
| H0AZ01333 | GRESSLEY, FORREST DAYL | REP | 2010 | AZ | H |
| H0AZ03321 | PARKER, VERNON | REP | 2014 | AZ | H |

New Step [Switch to editor](#) Cancel [Add to Recipe](#)

Choose a transformation

| ABC | CAND_ID | ABC | CAND_NAME | ABC | CAND_PARTY_AFFILIATION | CAND_ELECTION_YEAR | ABC | CAND_OFFICE_STATE | ABC | CAND_OFFICE |
|------------------|------------------|-----|--------------------------|-----|------------------------|--------------------|-----|-------------------|-----|--------------|
| 4,864 Categories | 4,760 Categories | | | | | 1986 - 2052 | | 57 Categories | | 3 Categories |
| H0AK00097 | | | COX, JOHN R. | | | 2014 | | AK | | H |
| H0AL02087 | | | ROBY, MARTHA | | | 2016 | | AL | | H |
| H0AL02095 | | | JOHN, ROBERT E JR | | | 2016 | | AL | | H |
| H0AL05049 | | | CRAMER, ROBERT E "BUD" J | | | 2008 | | AL | | H |
| H0AL05163 | | | BROOKS, MO | | | 2016 | | AL | | H |
| H0AL06088 | | | COOKE, STANLEY KYLE | | | 2010 | | AL | | H |
| H0AL07086 | | | SEWELL, TERRI A. | | | 2016 | | AL | | H |
| H0AL07094 | | | HILLIARD, EARL FREDERICK | | | 2010 | | AL | | H |
| H0AL07177 | | | CHAMBERLAIN, DON | | | 2012 | | AL | | H |
| H0AR01083 | | | CRAWFORD, ERIC ALAN RICK | | | 2016 | | AR | | H |
| H0AR01091 | | | GREGORY, JAMES CHRISTOPH | | | 2010 | | AR | | H |
| H0AR01109 | | | CAUSEY, CHAD | | | 2010 | | AR | | H |
| H0AR01125 | | | SMITH, PRINCELLA D | | | 2010 | | AR | | H |
| H0AR02107 | | | GRIFFIN, JOHN TIMOTHY | | | 2014 | | AR | | H |
| H0AR02131 | | | ELLIOTT, JOYCE ANN | | | 2010 | | AR | | H |
| H0AR03022 | | | SKOCH, BERNARD KURT 'BER | | | 2010 | | AR | | H |
| H0AR03030 | | | WHITAKER, DAVID JEFFREY | | | 2010 | | AR | | H |
| H0AR03055 | | | WOMACK, STEVE | | REP | 2016 | | AR | | H |
| H0AS00018 | | | FALEOMAVAEGA, ENI | | DEM | 2014 | | AS | | H |
| H0AZ01184 | | | FLAKE, JEFF MR. | | REP | 2012 | | AZ | | H |
| H0AZ01259 | | | GOSAR, PAUL ANTHONY | | REP | 2016 | | AZ | | H |
| H0AZ01283 | | | MEHTA, STEVE | | REP | 2010 | | AZ | | H |
| H0AZ01325 | | | TOBIN, ANDY HON. | | REP | 2014 | | AZ | | H |
| H0AZ01333 | | | GRESSLEY, FORREST DAYL | | REP | 2010 | | AZ | | H |
| H0AZ03321 | | | PARKER, VERNON | | REP | 2014 | | AZ | | H |

- Rename
- Change type >
- Edit column >
- Column Details
- Find >
- Format >
- Filter >
- Clean >
- Formula >
- Aggregate >
- Restructure >
- Lookup...
- Drop

New Step [Switch to editor](#)

Cancel [Add to Recipe](#)

Choose a transformation

Choose transformation

ABC CAND_NAME

SUMMARY

| | | |
|------------|-------|--------|
| Valid | 4,863 | 100.0% |
| Unique | 4,760 | 97.9% |
| Outliers | 18 | 0.4% |
| Mismatched | 0 | 0.0% |
| Missing | 1 | 0.0% |

STRING LENGTH STATISTICS

| | |
|--------------------|-------|
| Minimum | 4.00 |
| Lower Quartile | 14.00 |
| Median | 18.00 |
| Upper Quartile | 21.00 |
| Maximum | 70.00 |
| Average | 18.14 |
| Standard Deviation | 4.99 |

TOP VALUES

| | |
|------------------------------|---|
| KALEMKARIAN, TIMOTHY CHARLES | 3 |
| MARTIN, ANDY | 3 |
| AGBEDE, AKINYEMI | 2 |
| AKIN, W TODD | 2 |
| ARMSTRONG, BRANDON CHRISTINA | 2 |
| BACHMANN, MITCHELE | 2 |
| BALDWIN, TAMMY | 2 |
| BARR, BOB | 2 |
| BATES, DON JR | 2 |
| BELLIS, JOSEPH K III | 2 |
| BICKELMEYER, MICHAEL | 2 |
| BLASS, PIOTR DR | 2 |
| BLUNT, ROY | 2 |
| BOSS, JEFF | 2 |

MISMATCHED VALUES

None

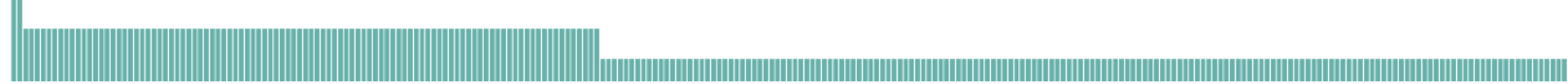
STRING LENGTH OUTLIERS

| | |
|---------------------------------------|---|
| AAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAAA | 1 |
| AKA THE PROPHET AKA EARL, TRIP... | 1 |
| CLARKSON, JEREMY CHARLES ROBER... | 1 |
| CONNOLLY, MATTHEW DONALD (MATT... | 1 |
| DE BUONAPARTE, HRM CAESAR ST A... | 1 |
| EASTON, EARNEST LEE PROFESSOR | 1 |

STRING LENGTH



FREQUENT VALUES



New Step [Switch to editor](#) Cancel [Add to Recipe](#)

Choose a transformation

Data Wrangling

One often needs to manipulate data prior to analysis. Tasks include reformatting, cleaning, quality assessment, and integration.

Approaches include:

Manual manipulation in spreadsheets

Custom code (e.g., dplyr in R, Pandas in Python)

Trifacta Wrangler <http://www.trifacta.com/products/wrangler/>

Open Refine <http://openrefine.org/>

Data Quality

"The first sign that a visualization is good is that it shows you a problem in your data...

...every successful visualization that I've been involved with has had this stage where you realize, "Oh my God, this data is not what I thought it would be!" So already, you've discovered something."

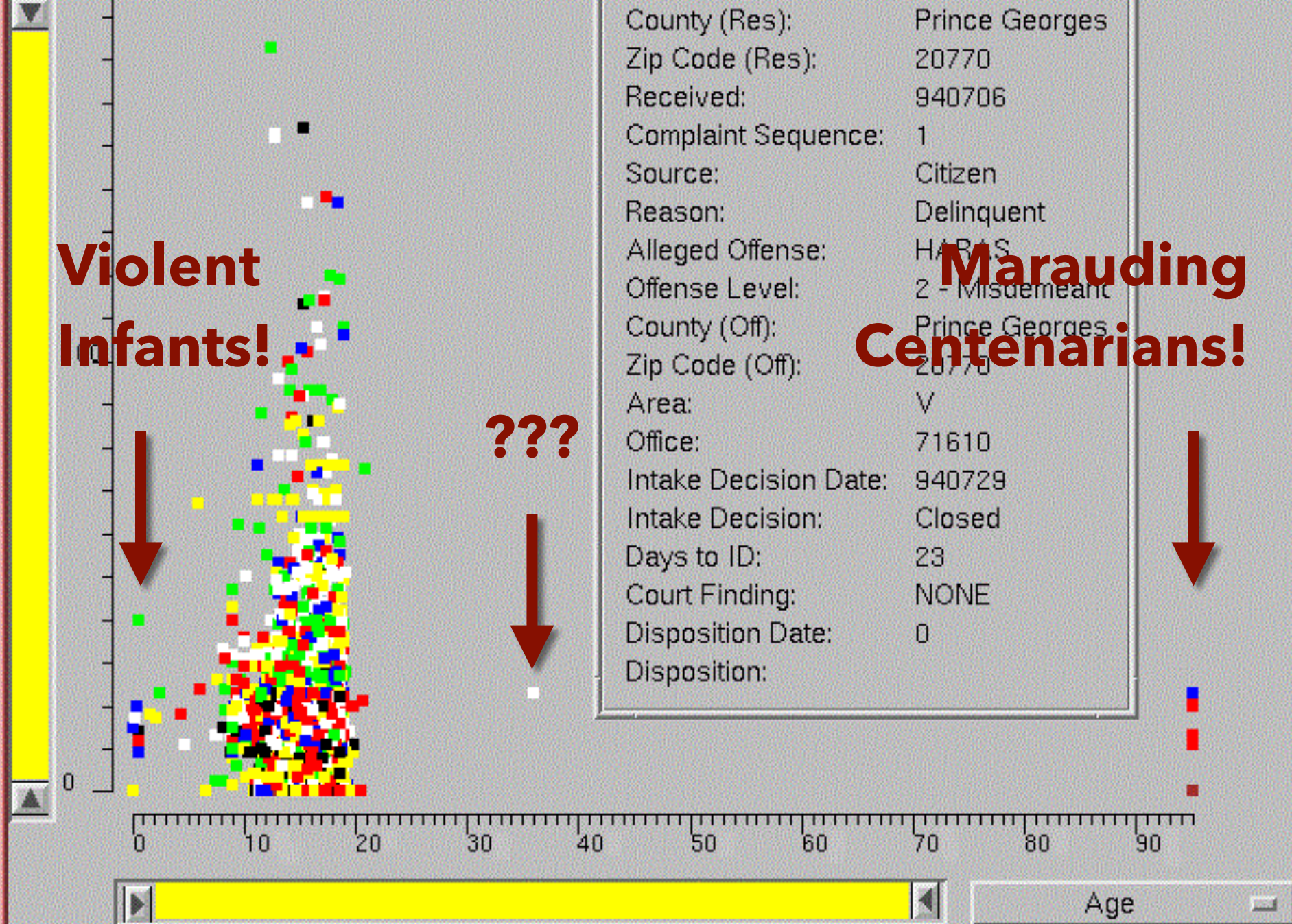
Martin Wattenberg

| | |
|-----------------------|-----------------|
| County (Res): | Prince Georges |
| Zip Code (Res): | 20770 |
| Received: | 940706 |
| Complaint Sequence: | 1 |
| Source: | Citizen |
| Reason: | Delinquent |
| Alleged Offense: | HARASS |
| Offense Level: | 2 - Misdemeanor |
| County (Off): | Prince Georges |
| Zip Code (Off): | 20770 |
| Area: | V |
| Office: | 71610 |
| Intake Decision Date: | 940729 |
| Intake Decision: | Closed |
| Days to ID: | 23 |
| Court Finding: | NONE |
| Disposition Date: | 0 |
| Disposition: | |

**Violent
Infants!**

**Marauding
Centenarians!**

???



Query Result: 4792 out of 4792 (100%)

Graph Viewer

Roll-up by:

All

Visualization:

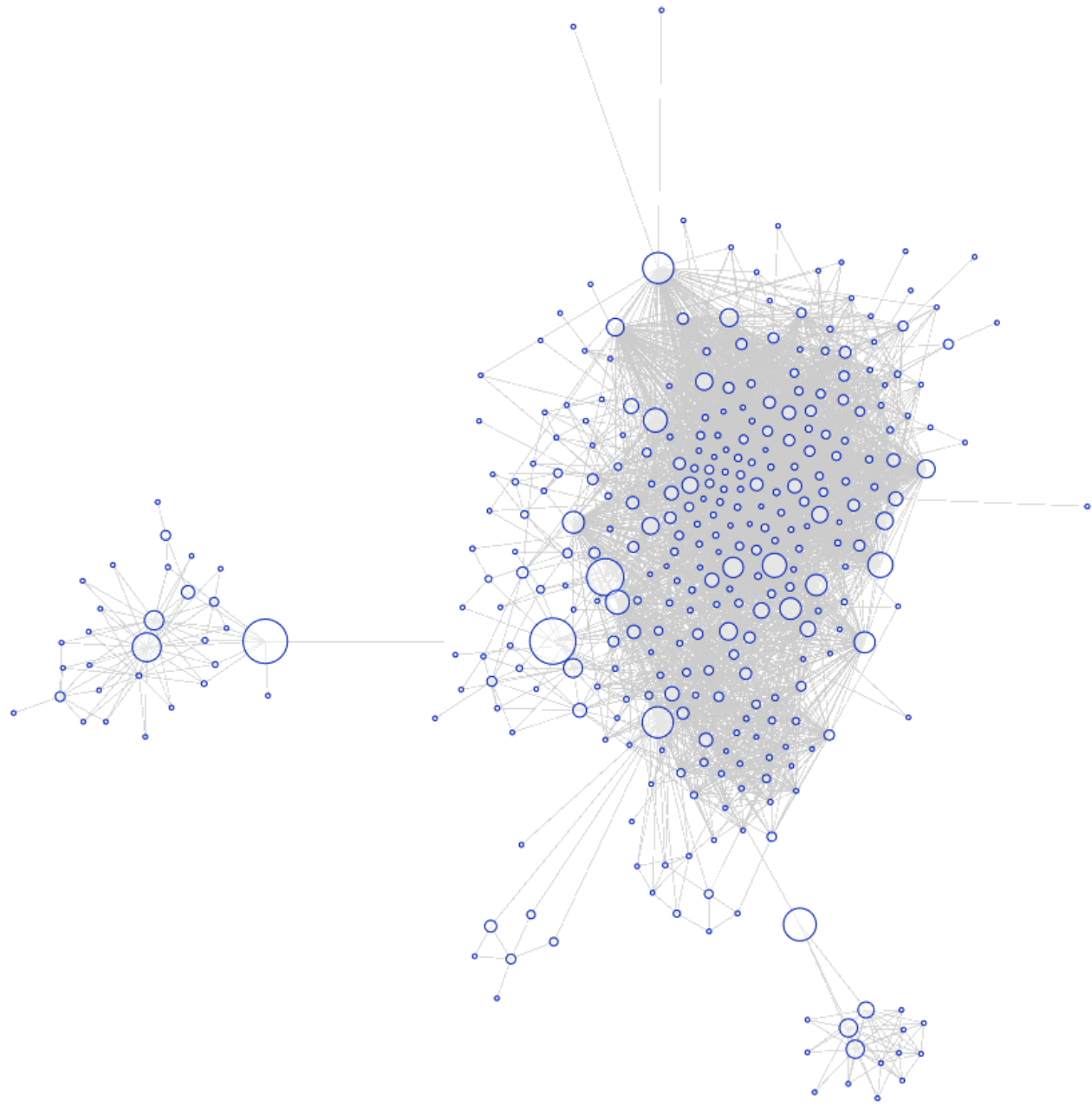
Node-Link

Sort by:

None

Edge centrality filters:

Two horizontal sliders for edge centrality filtering, both currently set to the minimum value.



- Images
- Animate

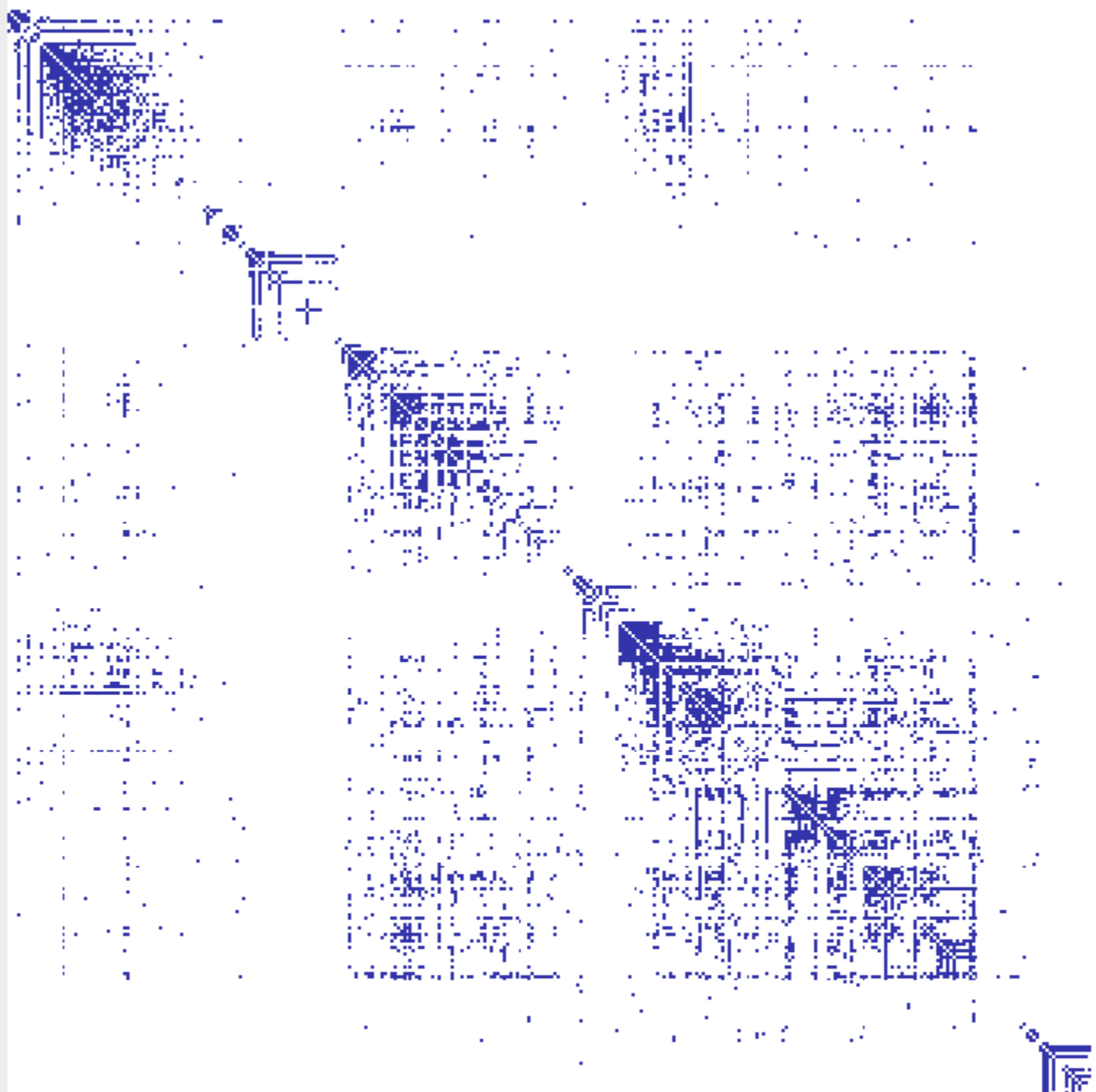
Graph Viewer

Roll-up by:

Visualization:

Sort by:

Edge centrality filters:



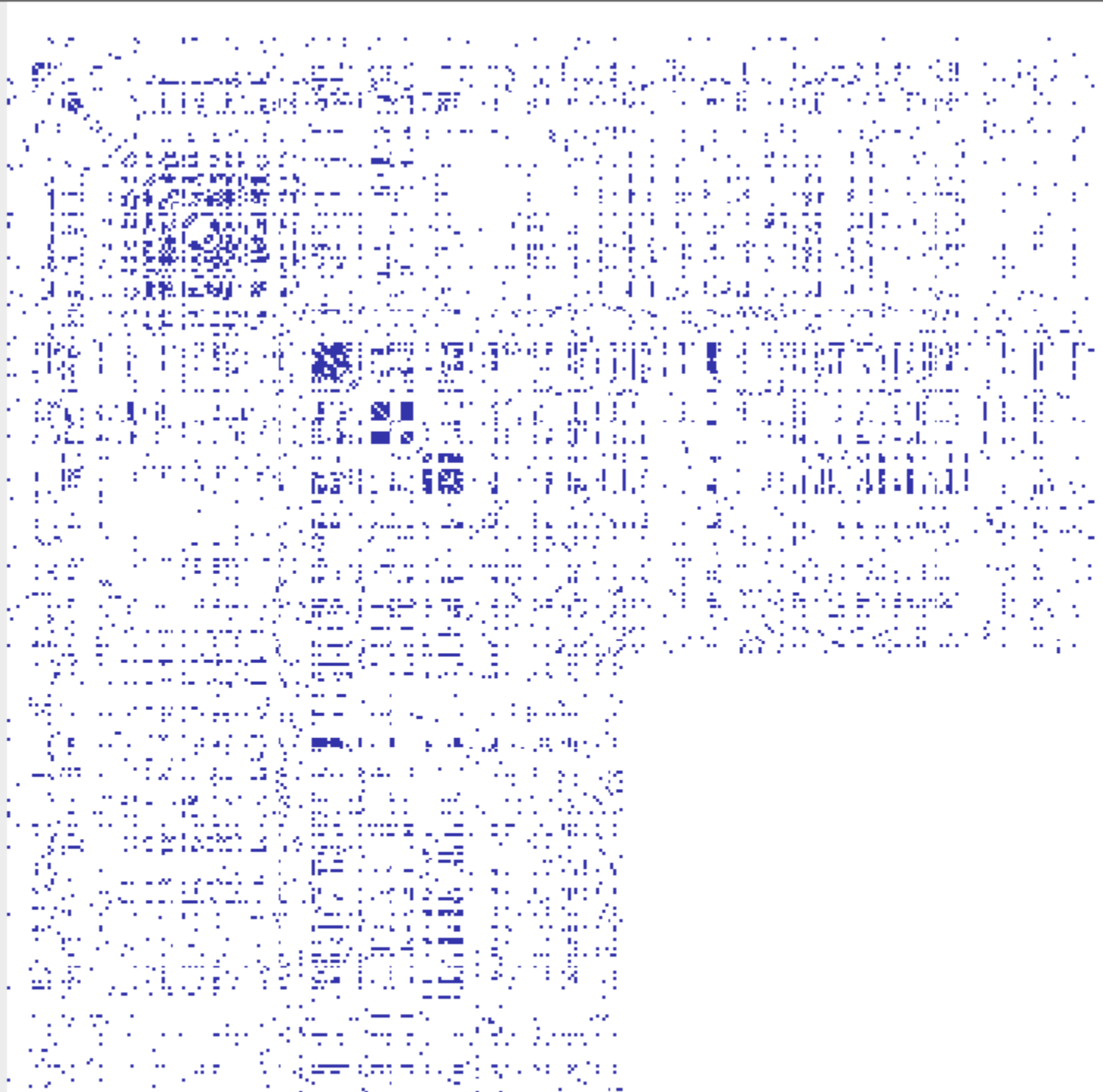
Graph Viewer

Roll-up by:

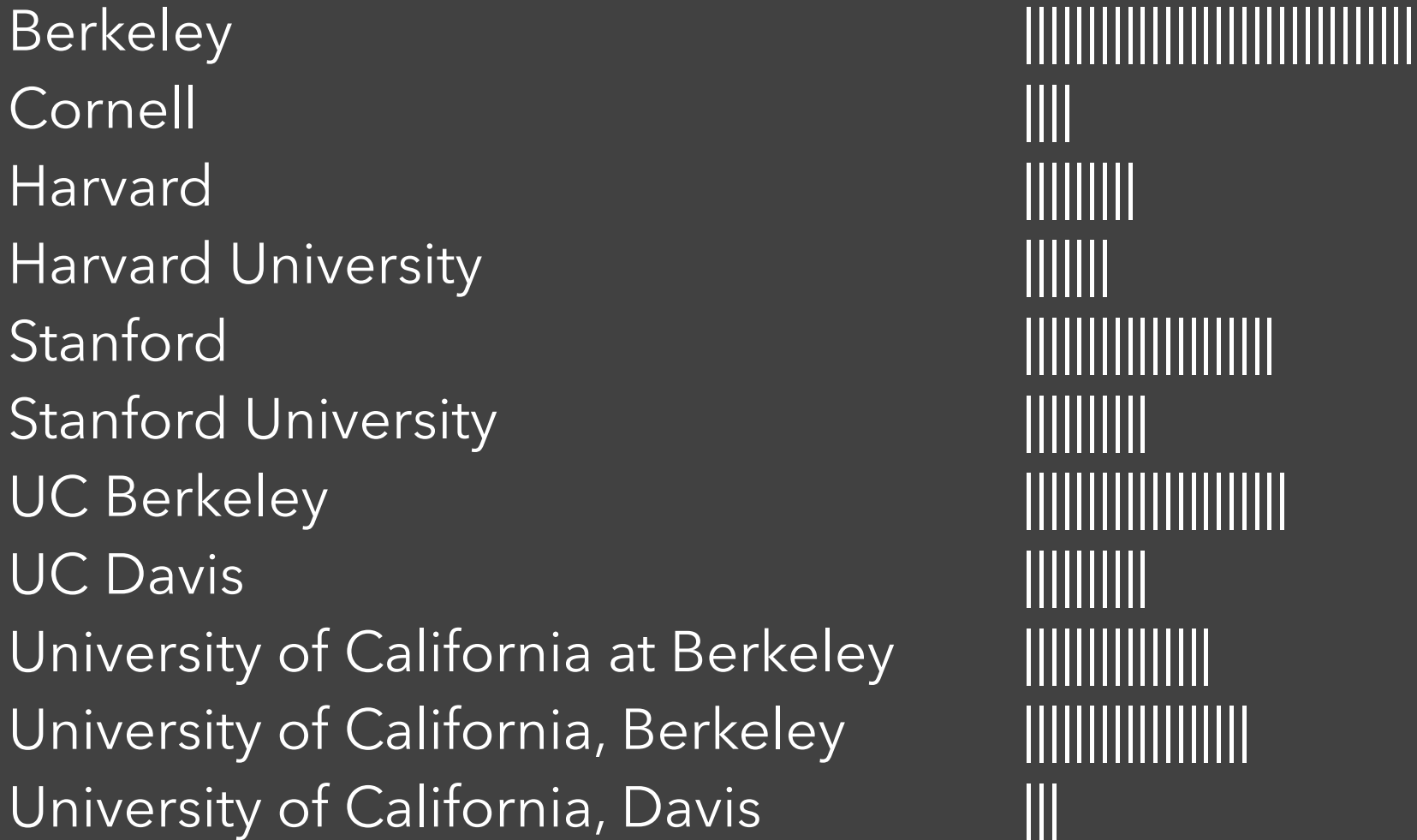
Visualization:

Sort by:

Edge centrality filters:



Visualize Friends by School?



Data Quality Hurdles

| | |
|-------------------|-----------------------------------|
| Missing Data | no measurements, redacted, ...? |
| Erroneous Values | misspelling, outliers, ...? |
| Type Conversion | e.g., zip code to lat-lon |
| Entity Resolution | diff. values for the same thing? |
| Data Integration | effort/errors when combining data |

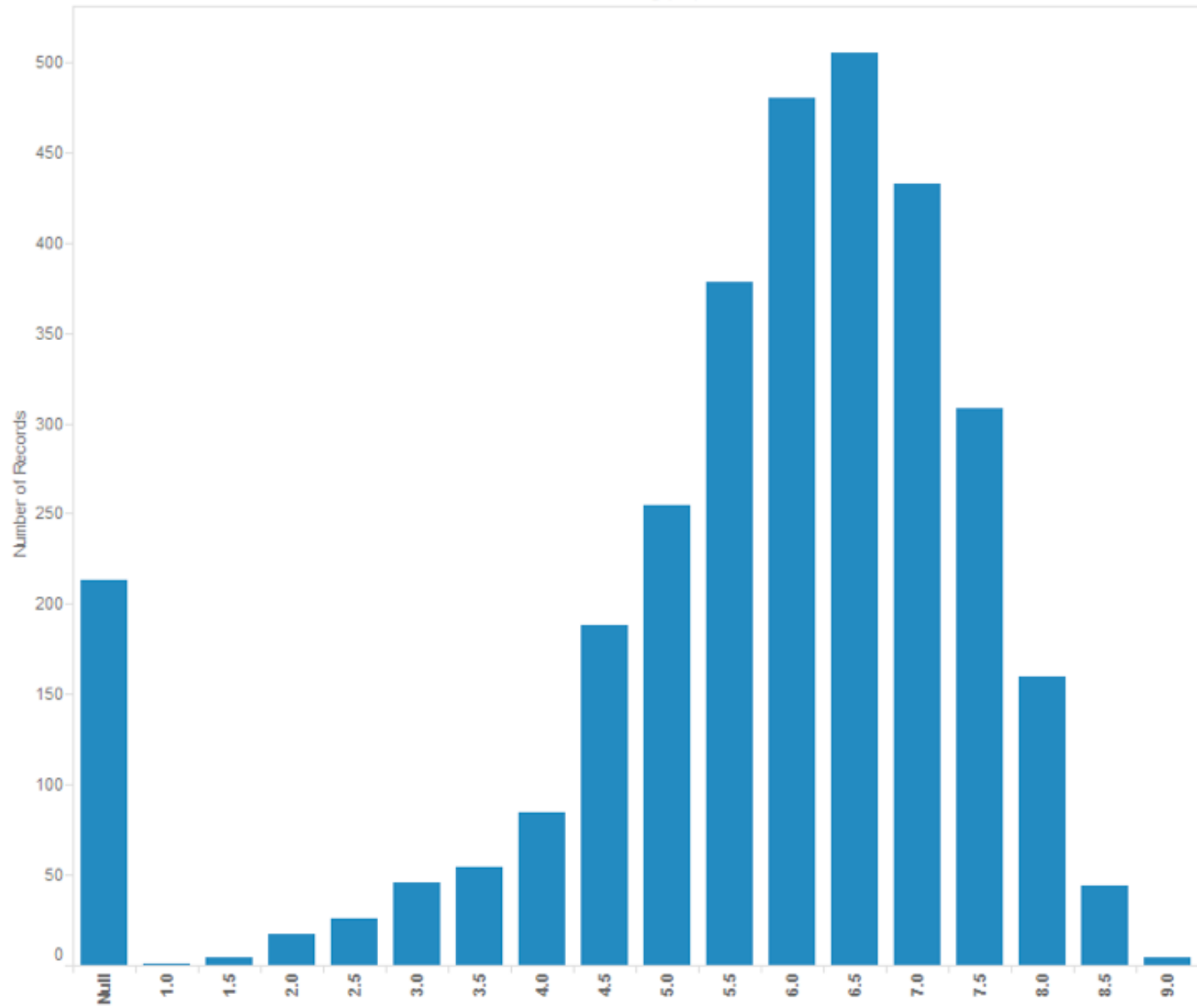
LESSON: Anticipate problems with your data.
Many research problems around these issues!

Analysis Example: Motion Pictures Data

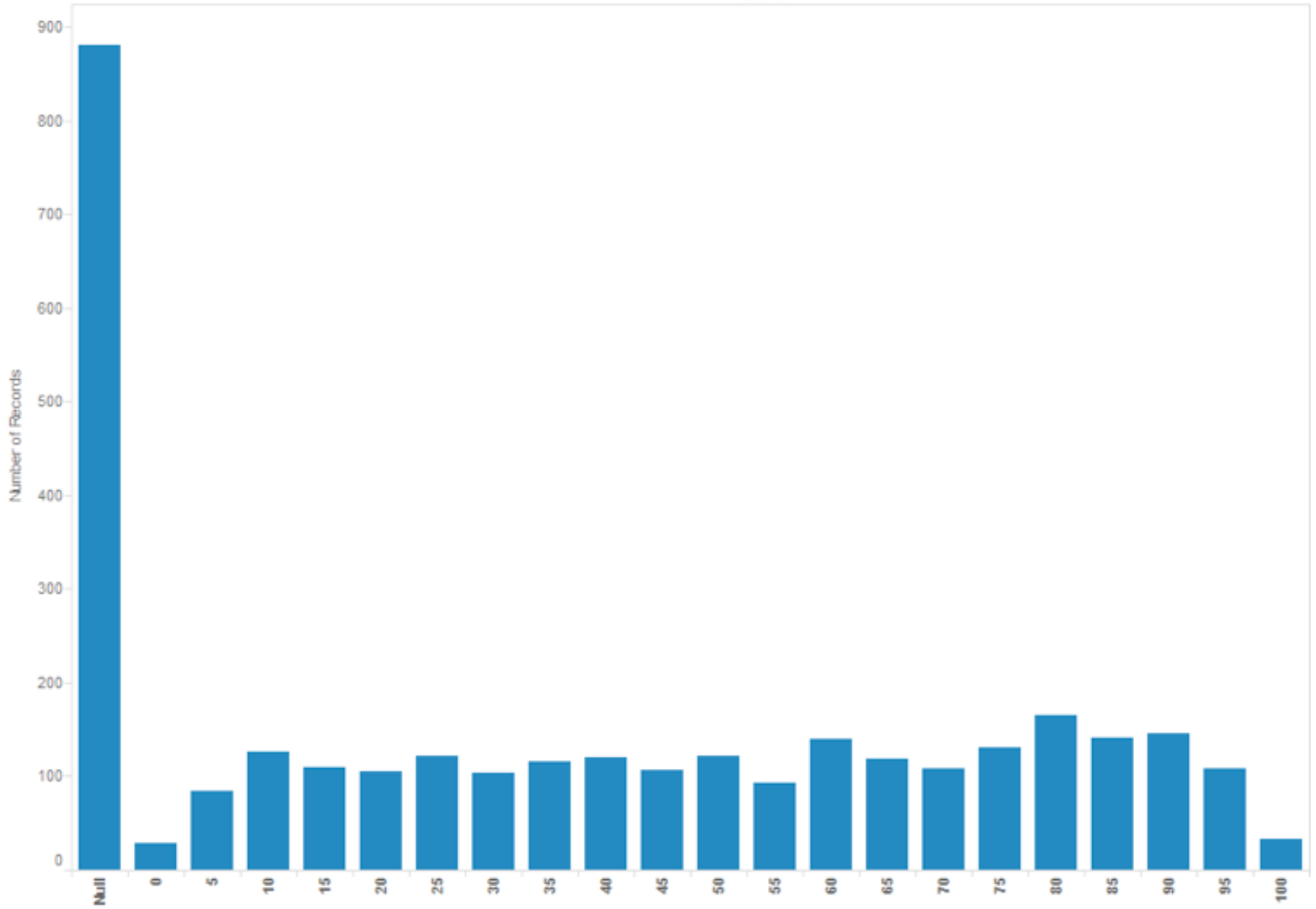
Motion Pictures Data

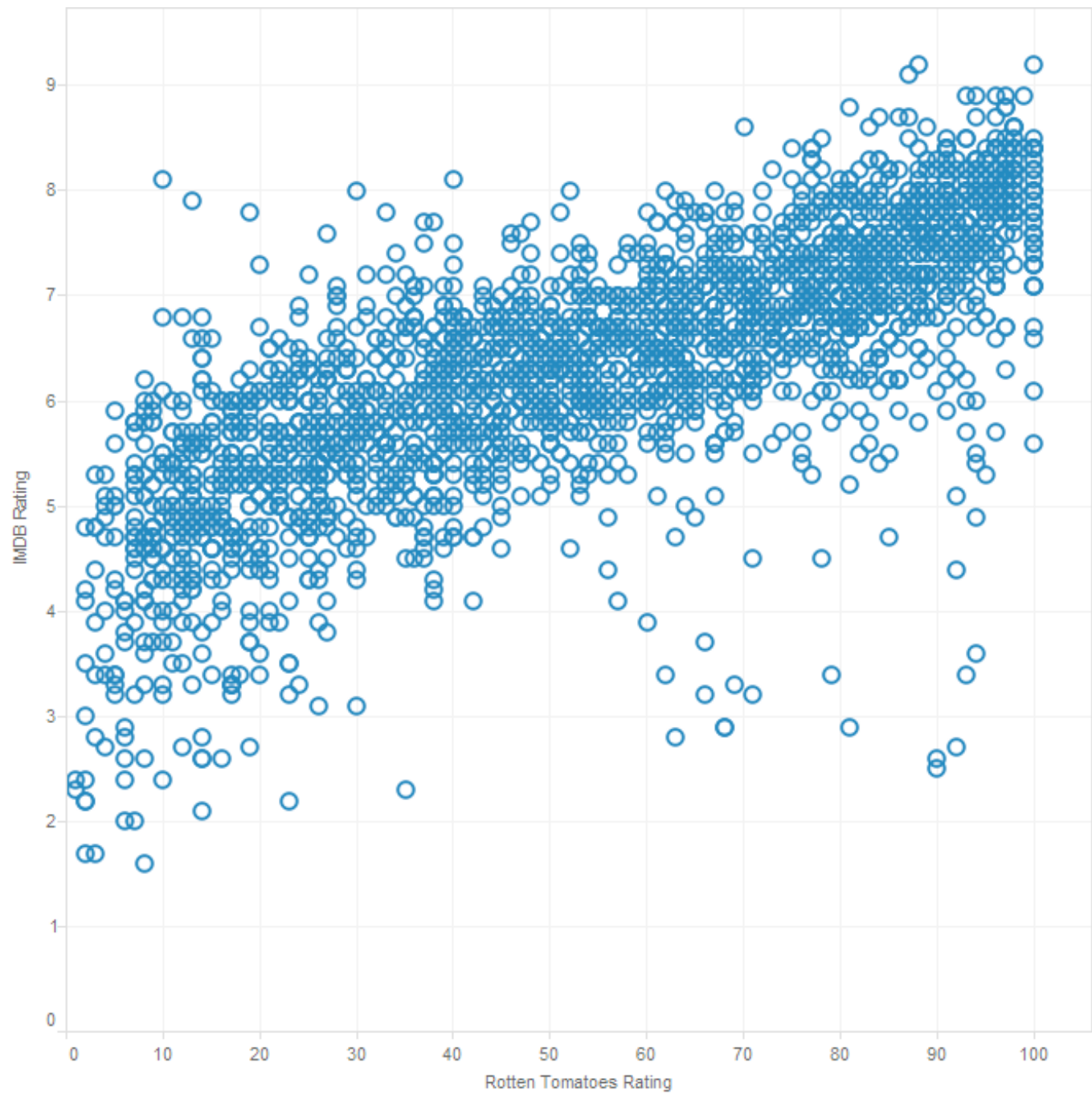
| | |
|------------------------|------------|
| Title | String (N) |
| IMDB Rating | Number (Q) |
| Rotten Tomatoes Rating | Number (Q) |
| MPAA Rating | String (O) |
| Release Date | Date (T) |

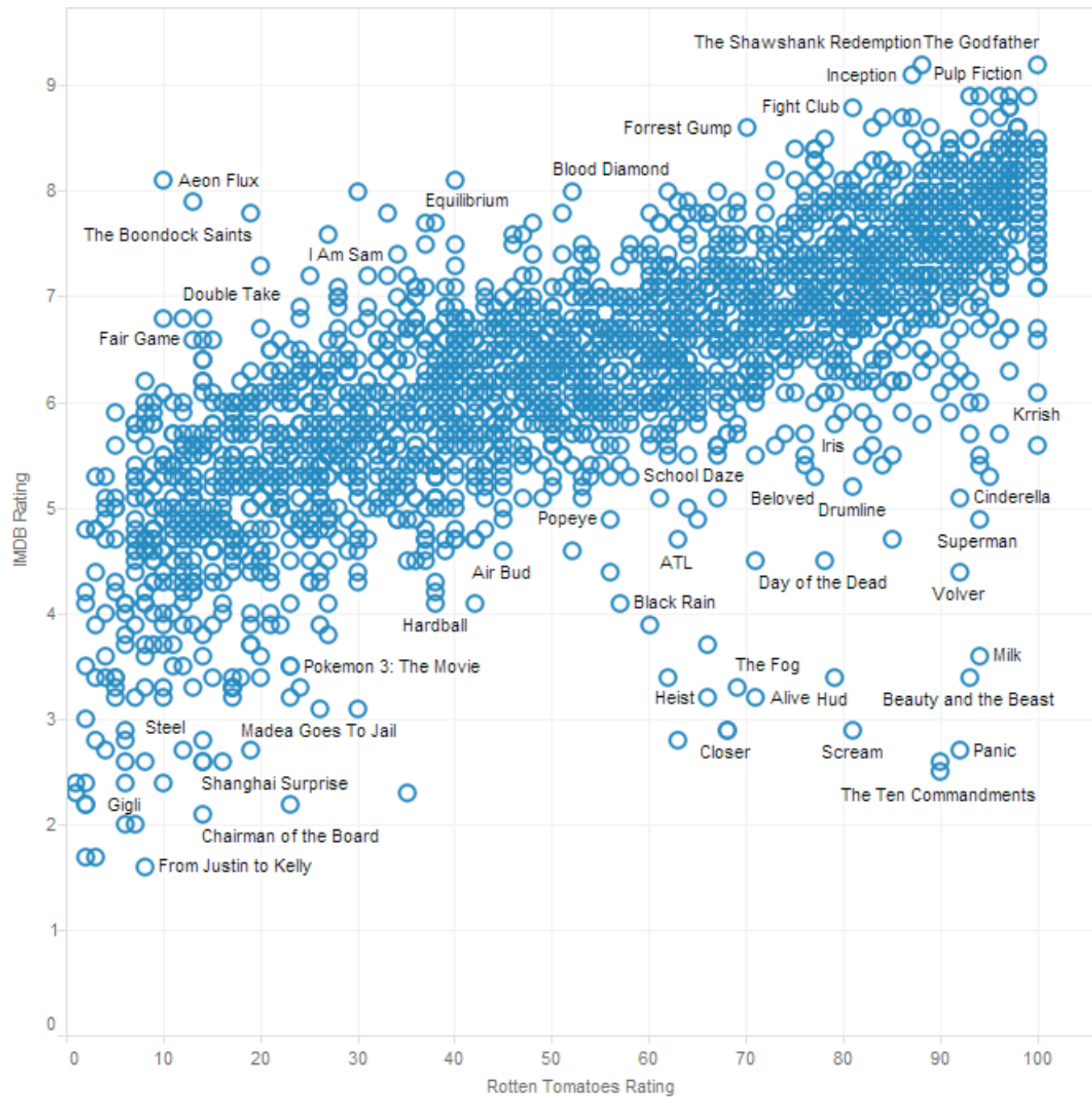
IMDB Rating (bin)

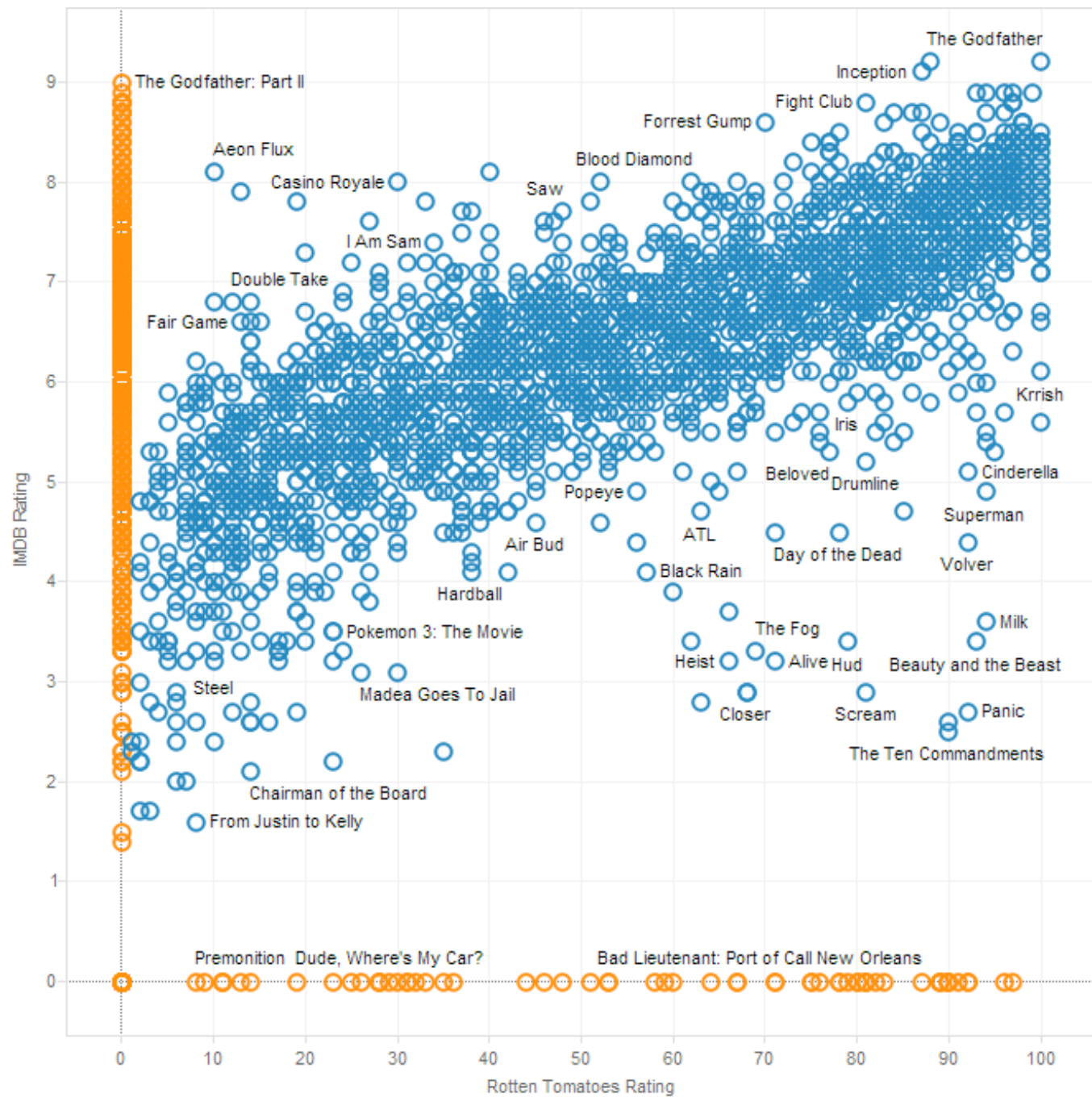


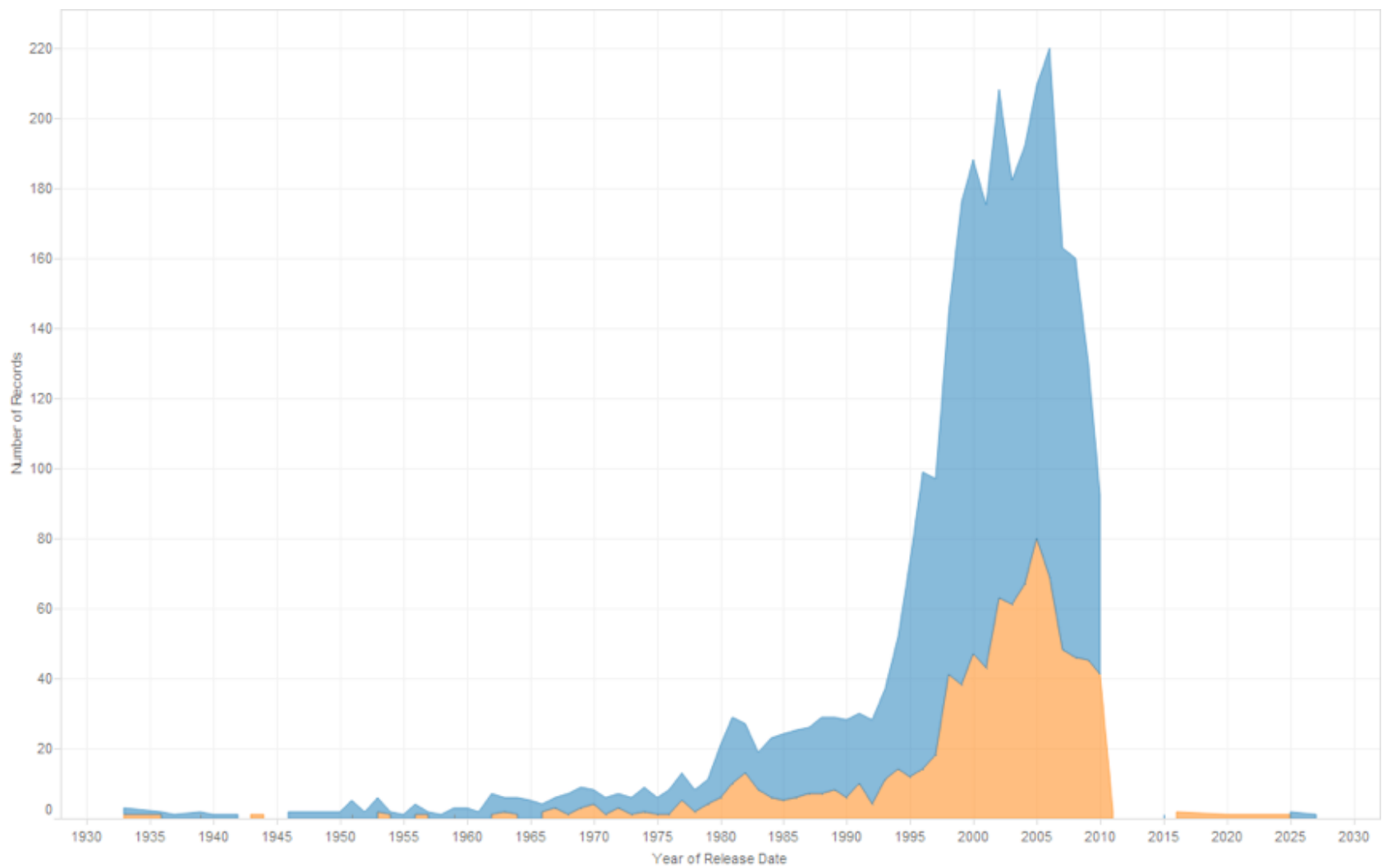
Rotten Tomatoes Rating (bin)











Lesson: Exercise Skepticism

Check **data quality** and your **assumptions**.

Start with **univariate summaries**, then start to consider **relationships among variables**.

Avoid premature fixation!

Analysis Example: Antibiotic Effectiveness

Data Set: Antibiotic Effectiveness

| | |
|------------------------------|---------------|
| Genus of Bacteria | String (N) |
| Species of Bacteria | String (N) |
| Antibiotic Applied | String (N) |
| Gram-Staining? | Pos / Neg (N) |
| Min. Inhibitory Concent. (g) | Number (Q) |

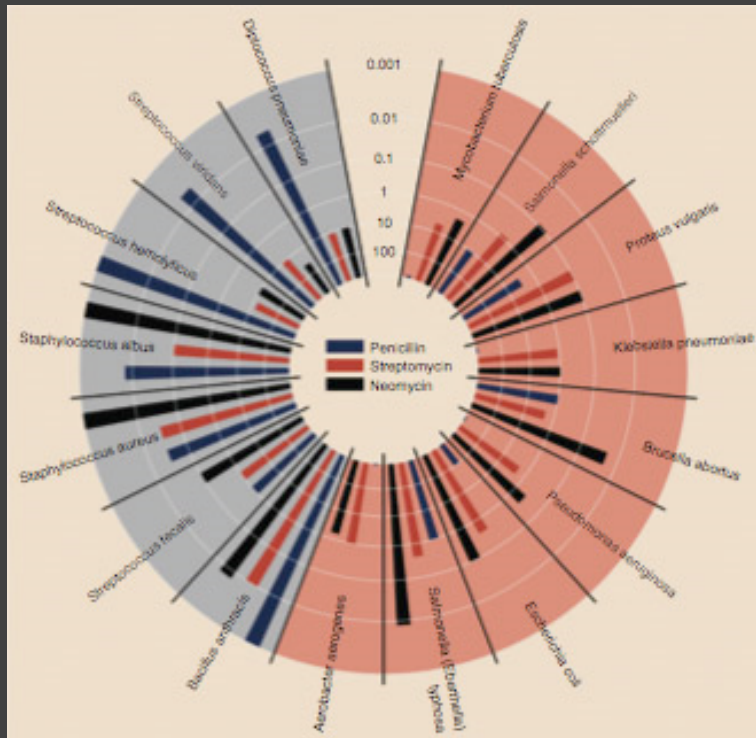
Collected prior to 1951.

What questions might we ask?

Table 1: Burtin's data.

| Bacteria | Antibiotic | | | Gram Staining |
|--|------------|--------------|----------|---------------|
| | Penicillin | Streptomycin | Neomycin | |
| <i>Aerobacter aerogenes</i> | 870 | 1 | 1.6 | negative |
| <i>Brucella abortus</i> | 1 | 2 | 0.02 | negative |
| <i>Brucella anthracis</i> | 0.001 | 0.01 | 0.007 | positive |
| <i>Diplococcus pneumoniae</i> | 0.005 | 11 | 10 | positive |
| <i>Escherichia coli</i> | 100 | 0.4 | 0.1 | negative |
| <i>Klebsiella pneumoniae</i> | 850 | 1.2 | 1 | negative |
| <i>Mycobacterium tuberculosis</i> | 800 | 5 | 2 | negative |
| <i>Proteus vulgaris</i> | 3 | 0.1 | 0.1 | negative |
| <i>Pseudomonas aeruginosa</i> | 850 | 2 | 0.4 | negative |
| <i>Salmonella (Eberthella) typhosa</i> | 1 | 0.4 | 0.008 | negative |
| <i>Salmonella schottmuelleri</i> | 10 | 0.8 | 0.09 | negative |
| <i>Staphylococcus albus</i> | 0.007 | 0.1 | 0.001 | positive |
| <i>Staphylococcus aureus</i> | 0.03 | 0.03 | 0.001 | positive |
| <i>Streptococcus fecalis</i> | 1 | 1 | 0.1 | positive |
| <i>Streptococcus hemolyticus</i> | 0.001 | 14 | 10 | positive |
| <i>Streptococcus viridans</i> | 0.005 | 10 | 40 | positive |

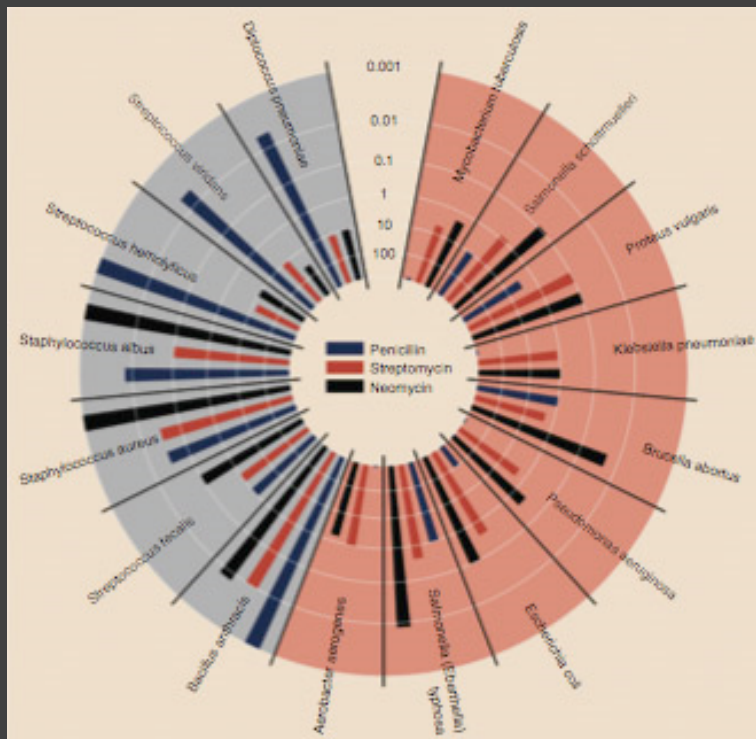
How do the drugs compare?



| Bacteria | Penicillin | Antibiotic Streptomycin | Neomycin | Gram stain |
|--|------------|-------------------------|----------|------------|
| <i>Aerobacter aerogenes</i> | 870 | 1 | 1.6 | - |
| <i>Brucella abortus</i> | 1 | 2 | 0.02 | - |
| <i>Bacillus anthracis</i> | 0.001 | 0.01 | 0.007 | + |
| <i>Diplococcus pneumoniae</i> | 0.005 | 11 | 10 | + |
| <i>Escherichia coli</i> | 100 | 0.4 | 0.1 | - |
| <i>Klebsiella pneumoniae</i> | 850 | 1.2 | 1 | - |
| <i>Mycobacterium tuberculosis</i> | 800 | 5 | 2 | - |
| <i>Proteus vulgaris</i> | 3 | 0.1 | 0.1 | - |
| <i>Pseudomonas aeruginosa</i> | 850 | 2 | 0.4 | - |
| <i>Salmonella (Eberthella) typhosa</i> | 1 | 0.4 | 0.008 | - |
| <i>Salmonella schottmuelleri</i> | 10 | 0.8 | 0.09 | - |
| <i>Staphylococcus albus</i> | 0.007 | 0.1 | 0.001 | + |
| <i>Staphylococcus aureus</i> | 0.03 | 0.03 | 0.001 | + |
| <i>Streptococcus fecalis</i> | 1 | 1 | 0.1 | + |
| <i>Streptococcus hemolyticus</i> | 0.001 | 14 | 10 | + |
| <i>Streptococcus viridans</i> | 0.005 | 10 | 40 | + |

Original graphic by Will Burtin, 1951

How do the drugs compare?



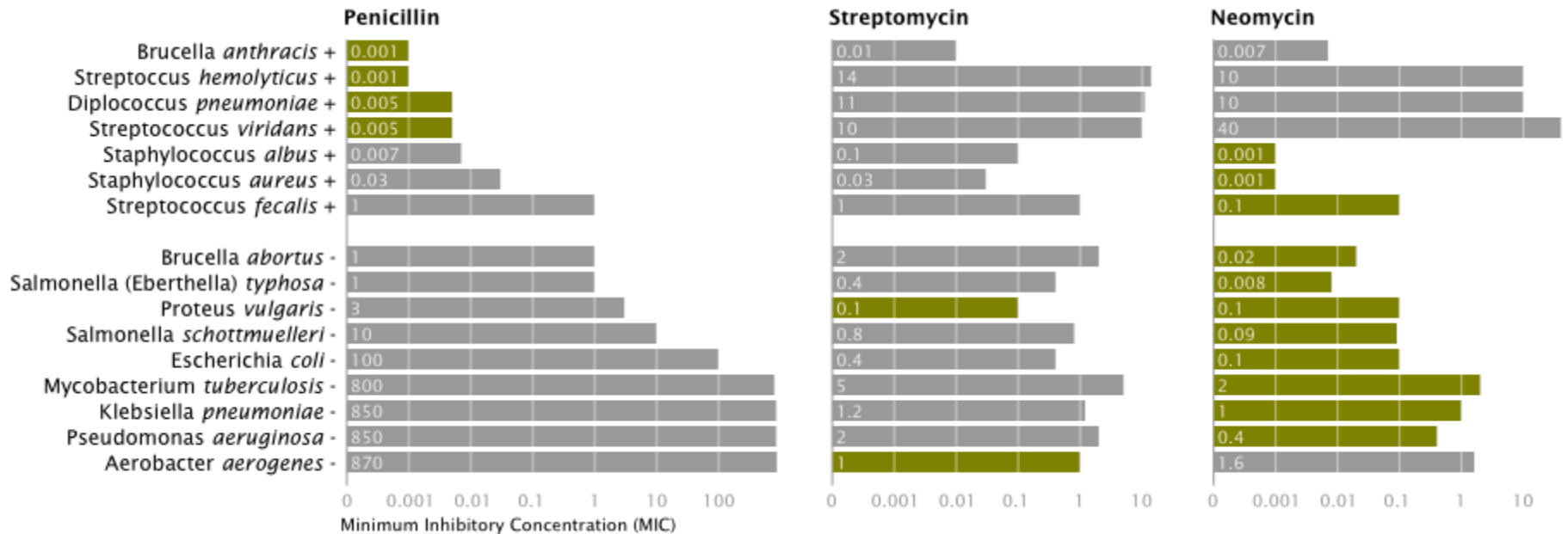
| Bacteria | Penicillin | Antibiotic Streptomycin | Neomycin | Gram stain |
|--|------------|-------------------------|----------|------------|
| <i>Aerobacter aerogenes</i> | 870 | 1 | 1.6 | - |
| <i>Brucella abortus</i> | 1 | 2 | 0.02 | - |
| <i>Bacillus anthracis</i> | 0.001 | 0.01 | 0.007 | + |
| <i>Diplococcus pneumoniae</i> | 0.005 | 11 | 10 | + |
| <i>Escherichia coli</i> | 100 | 0.4 | 0.1 | - |
| <i>Klebsiella pneumoniae</i> | 850 | 1.2 | 1 | - |
| <i>Mycobacterium tuberculosis</i> | 800 | 5 | 2 | - |
| <i>Proteus vulgaris</i> | 3 | 0.1 | 0.1 | - |
| <i>Pseudomonas aeruginosa</i> | 850 | 2 | 0.4 | - |
| <i>Salmonella (Eberthella) typhosa</i> | 1 | 0.4 | 0.008 | - |
| <i>Salmonella schottmuelleri</i> | 10 | 0.8 | 0.09 | - |
| <i>Staphylococcus albus</i> | 0.007 | 0.1 | 0.001 | + |
| <i>Staphylococcus aureus</i> | 0.03 | 0.03 | 0.001 | + |
| <i>Streptococcus fecalis</i> | 1 | 1 | 0.1 | + |
| <i>Streptococcus hemolyticus</i> | 0.001 | 14 | 10 | + |
| <i>Streptococcus viridans</i> | 0.005 | 10 | 40 | + |

Radius: $1 / \log(\text{MIC})$

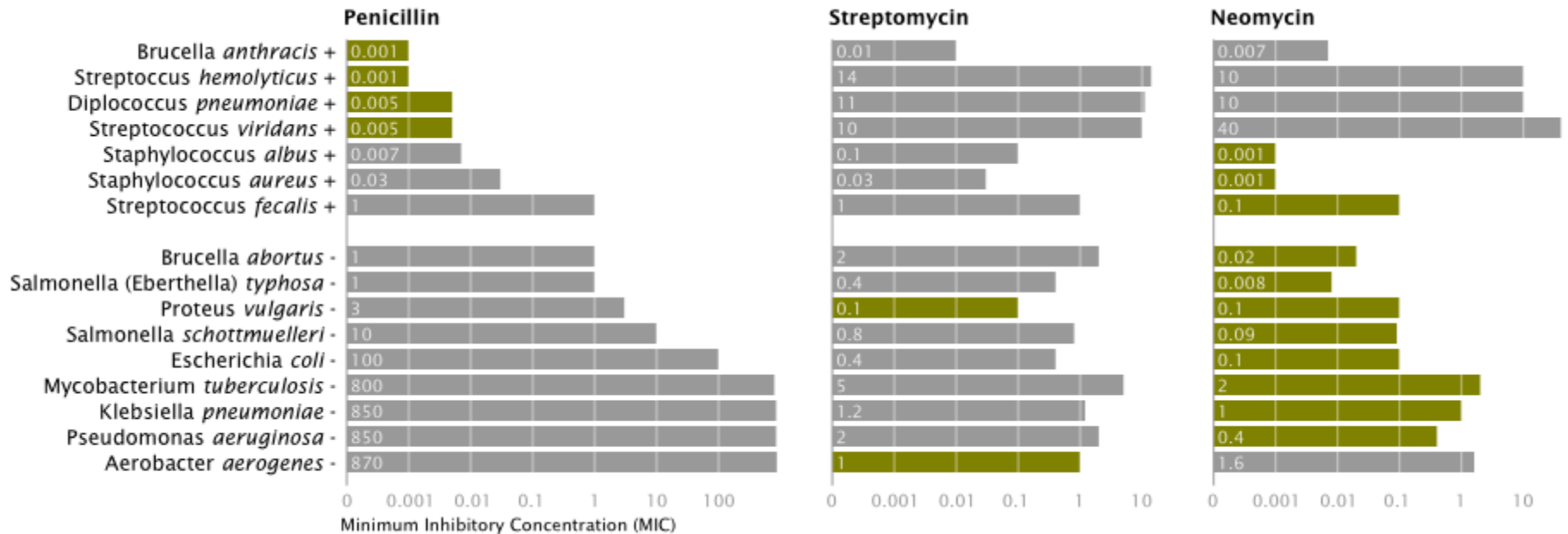
Bar Color: Antibiotic

Background Color: Gram Staining

How do the drugs compare?



How do the drugs compare?



X-axis: Antibiotic | $\log(\text{MIC})$

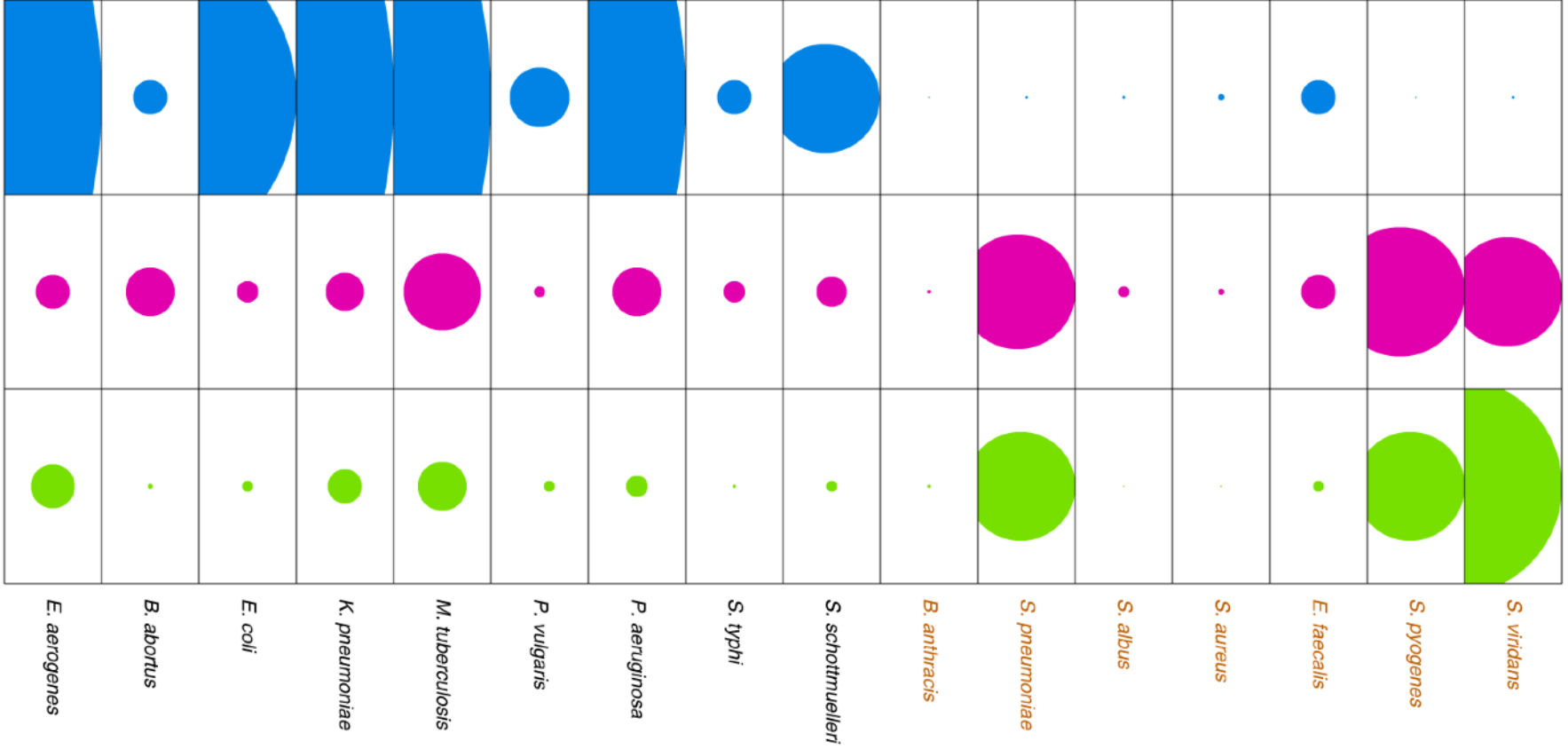
Y-axis: Gram-Staining | Species

Color: Most-Effective?

penicillin

streptomycin

neomycin

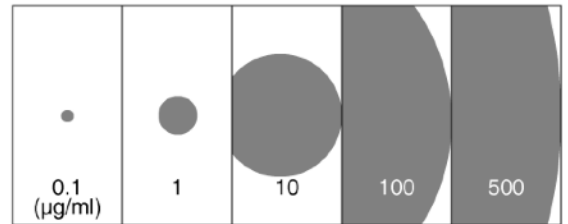


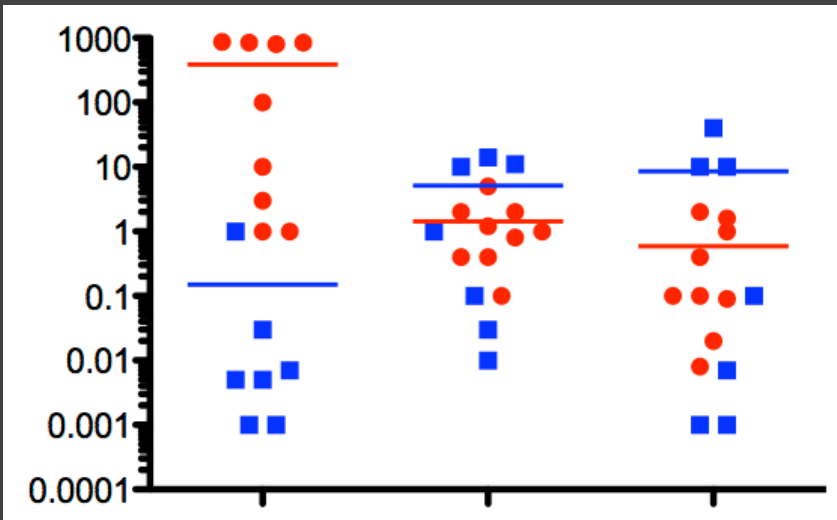
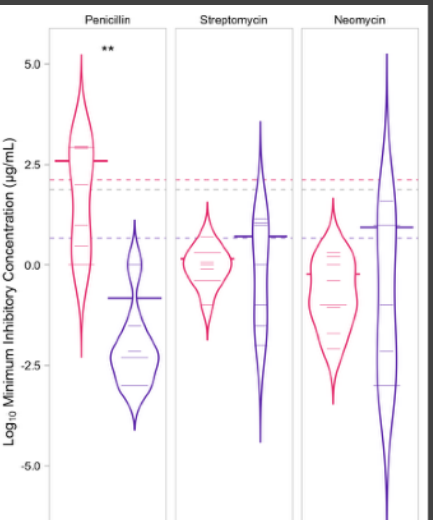
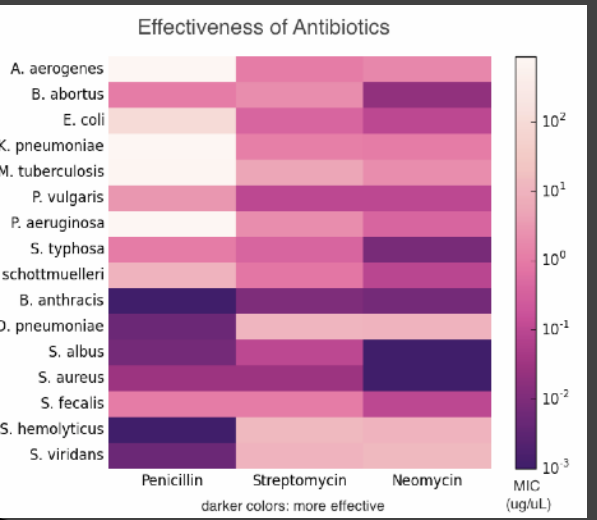
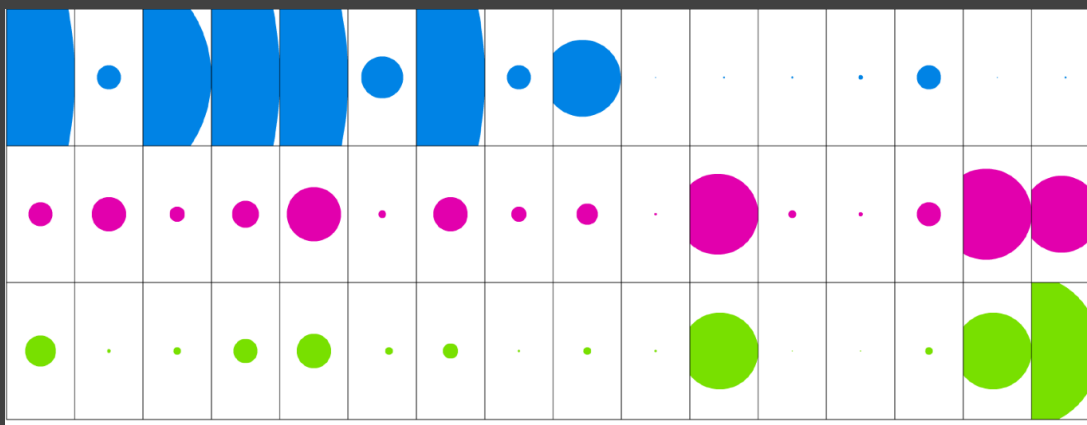
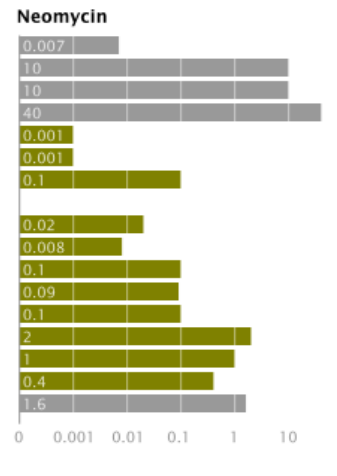
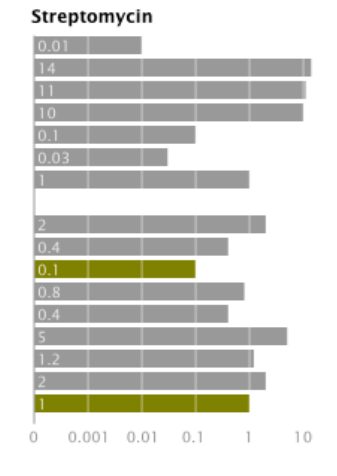
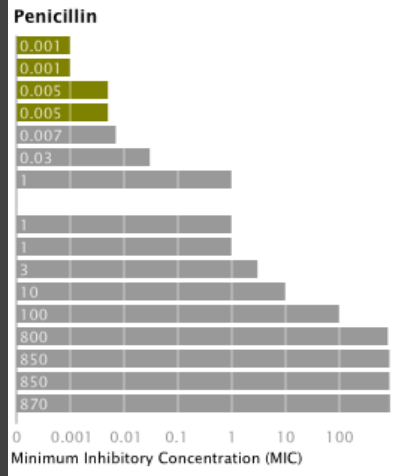
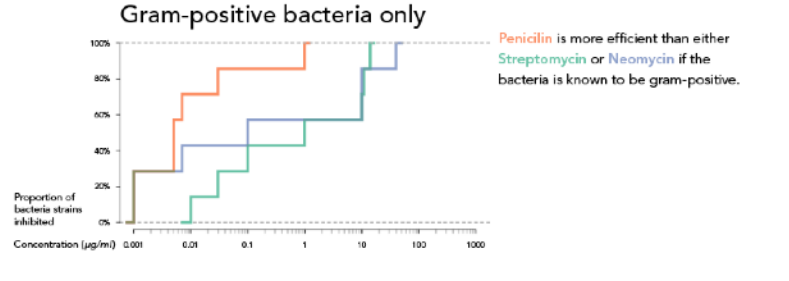
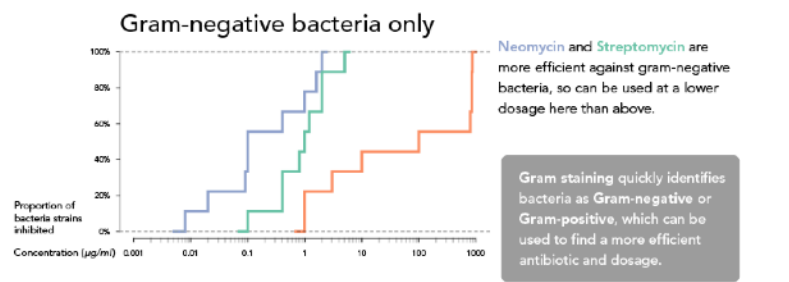
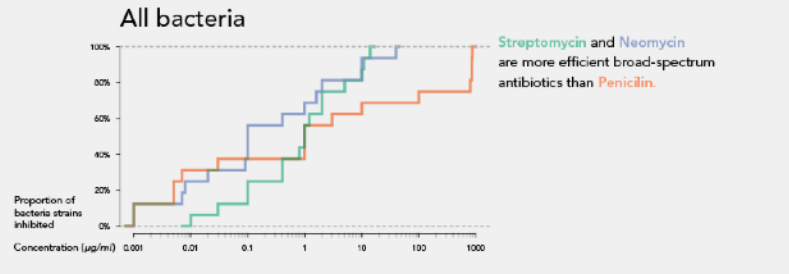
Gram positive

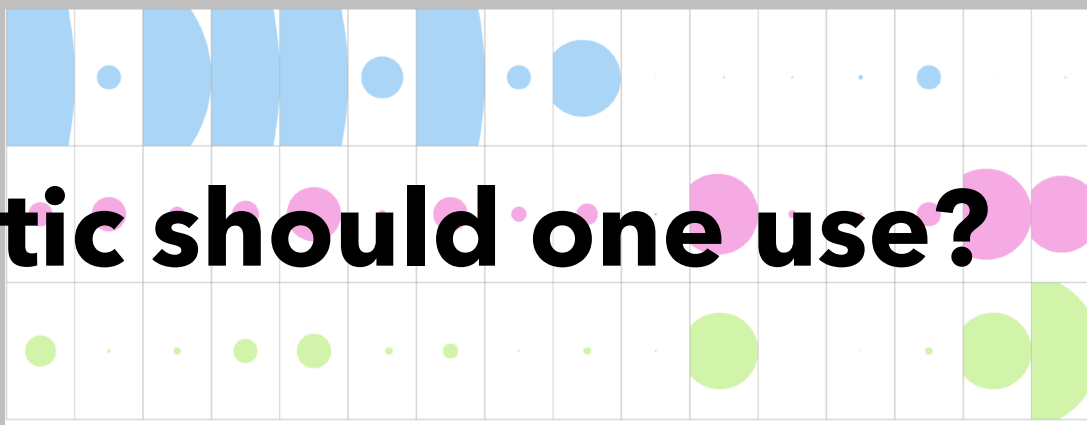
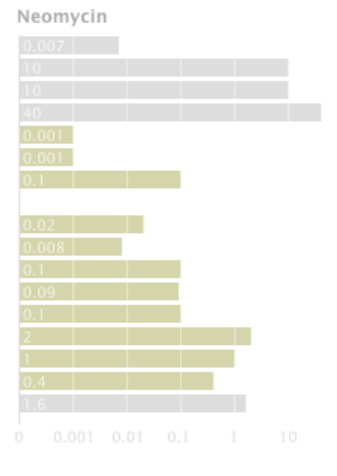
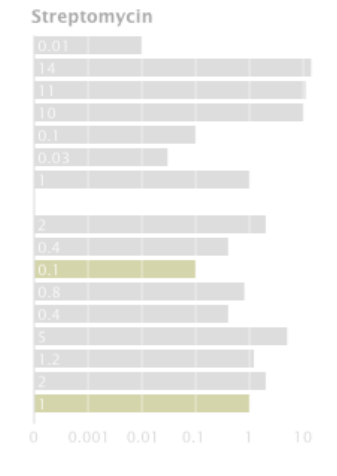
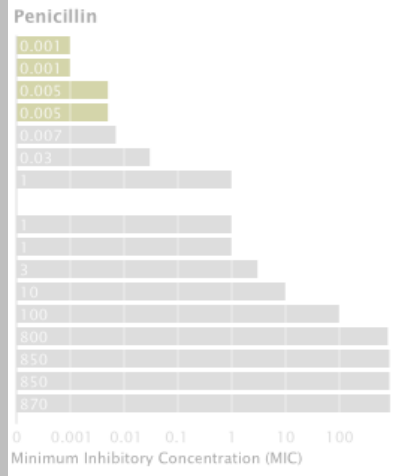
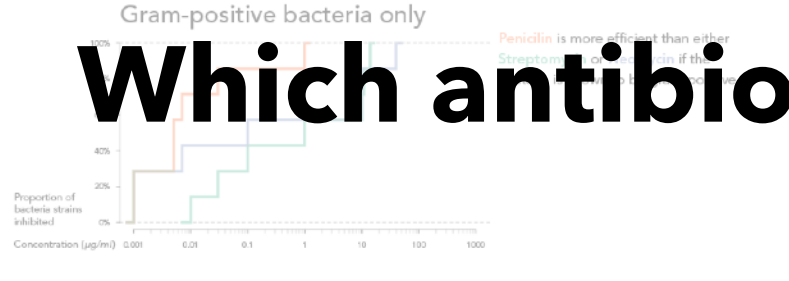
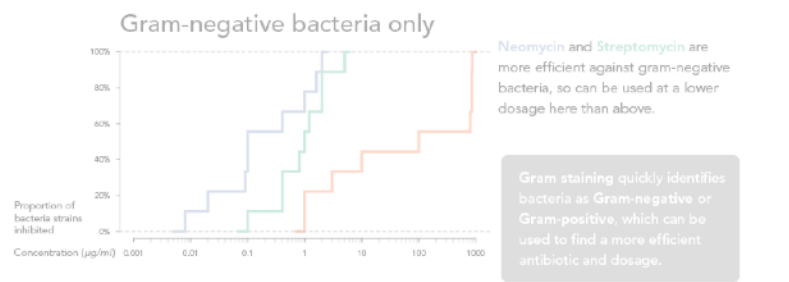
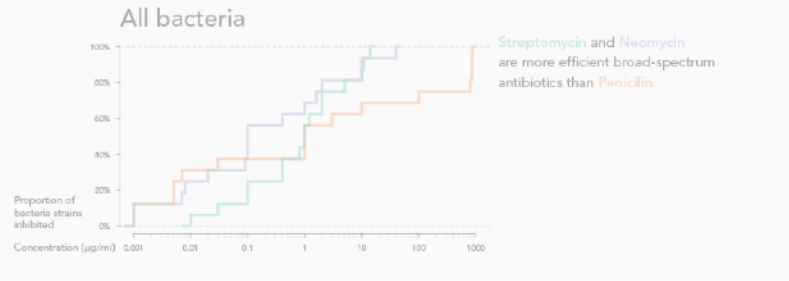
Gram negative

minimum inhibitory concentration of antibiotics

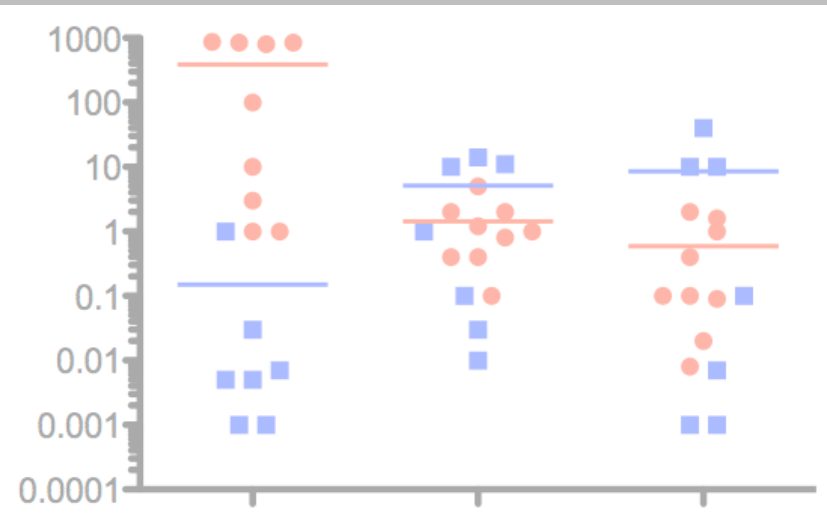
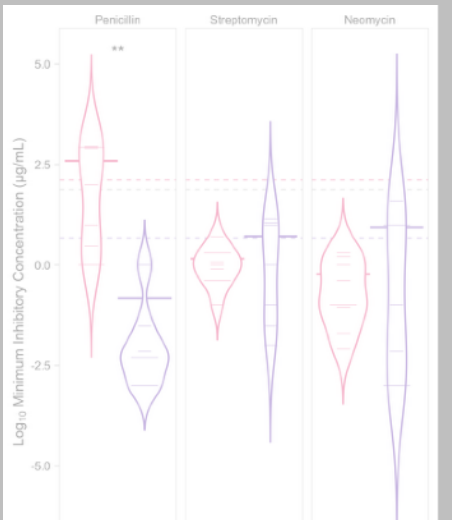
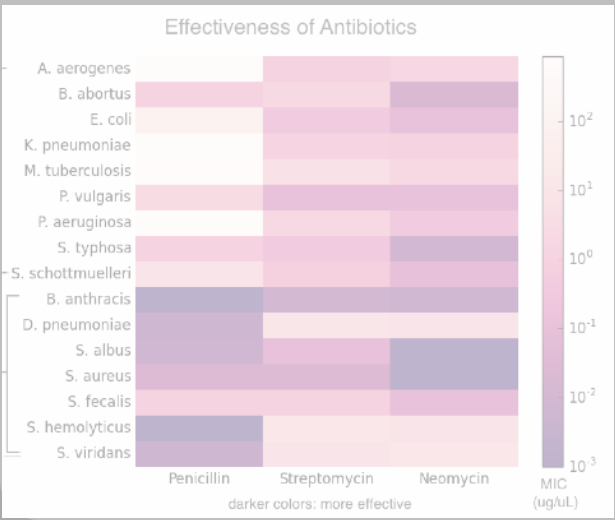
bowen li cs448b





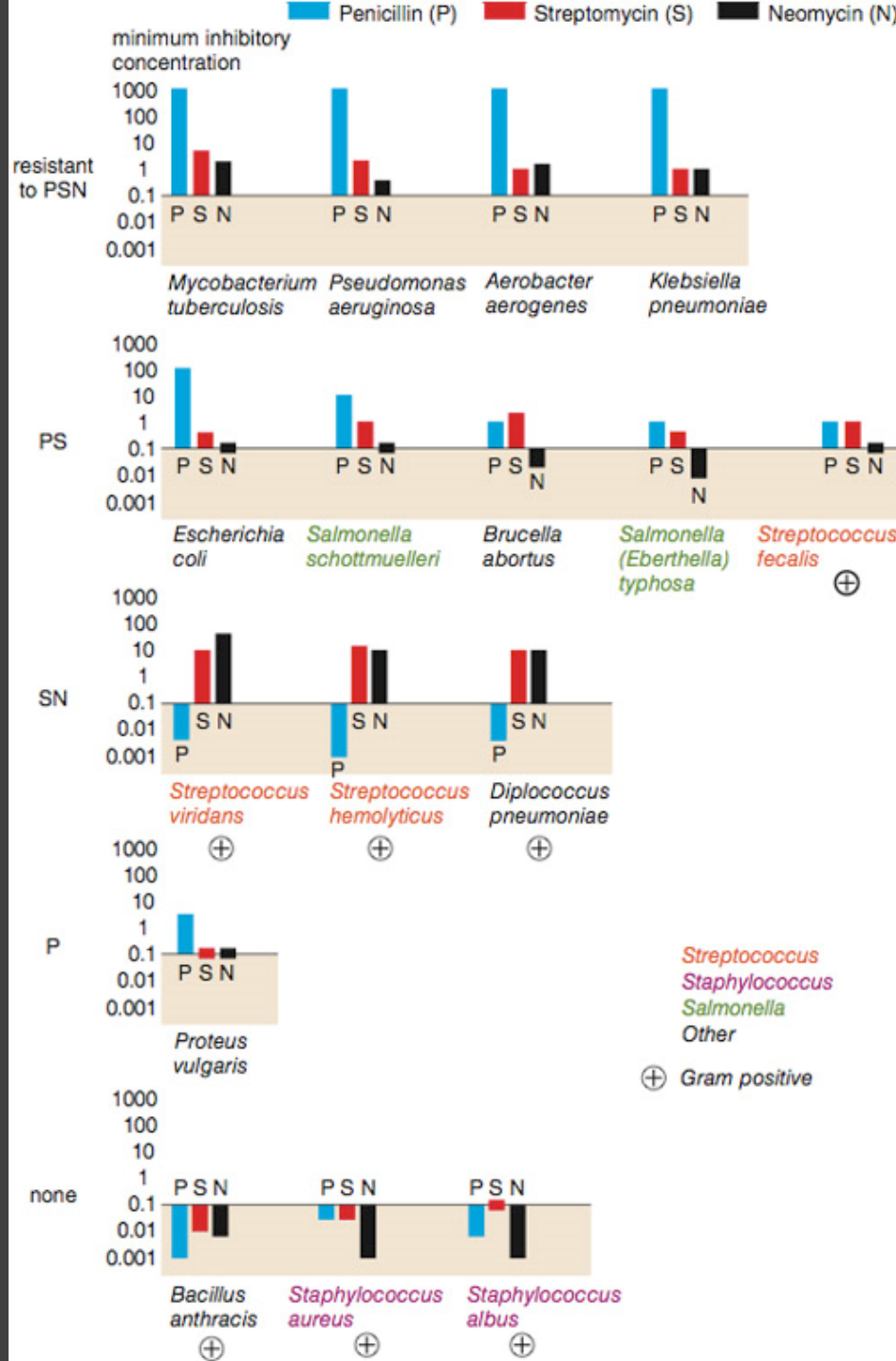


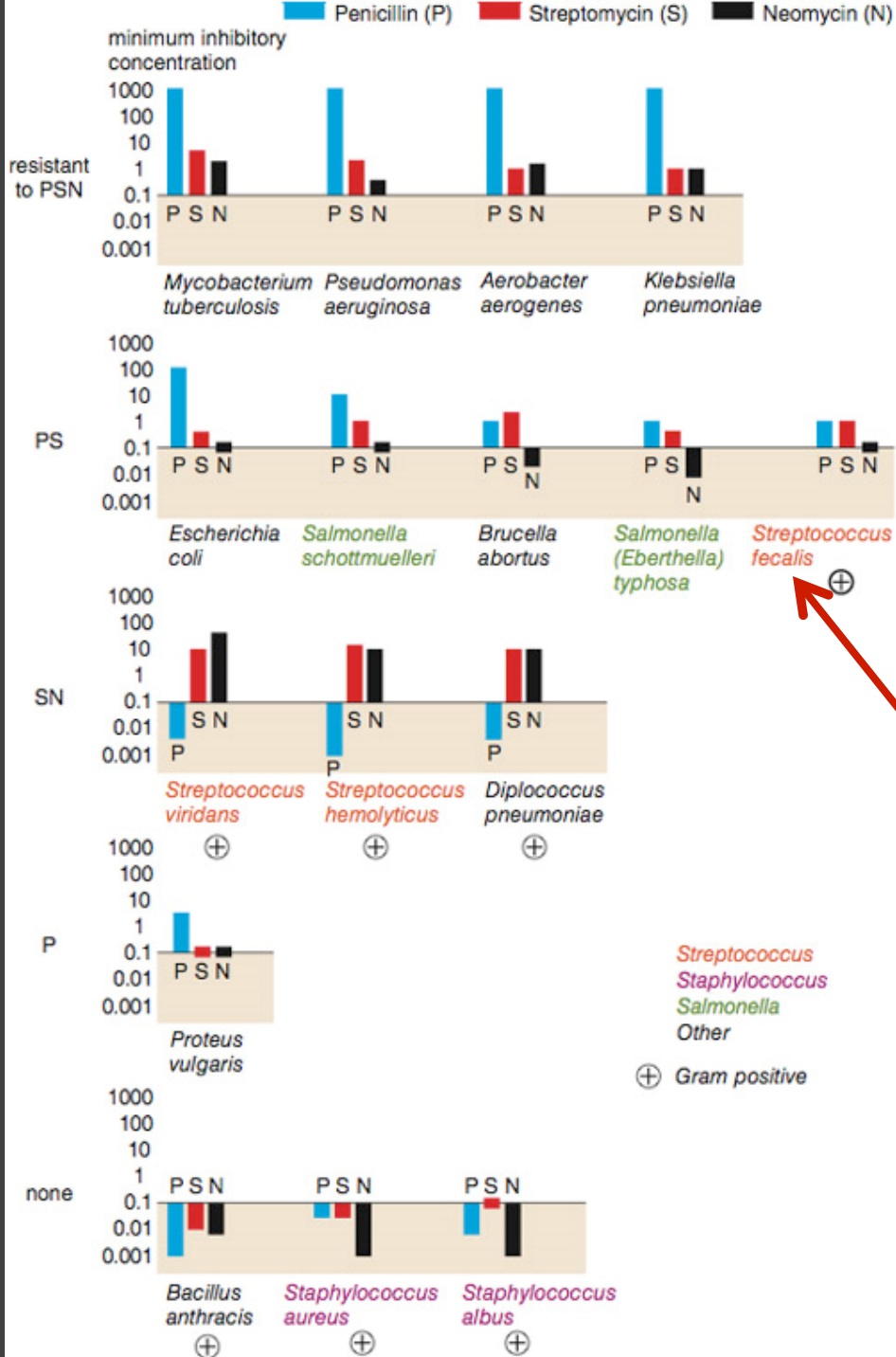
Which antibiotic should one use?



**Do the bacteria
group by antibiotic
resistance?**

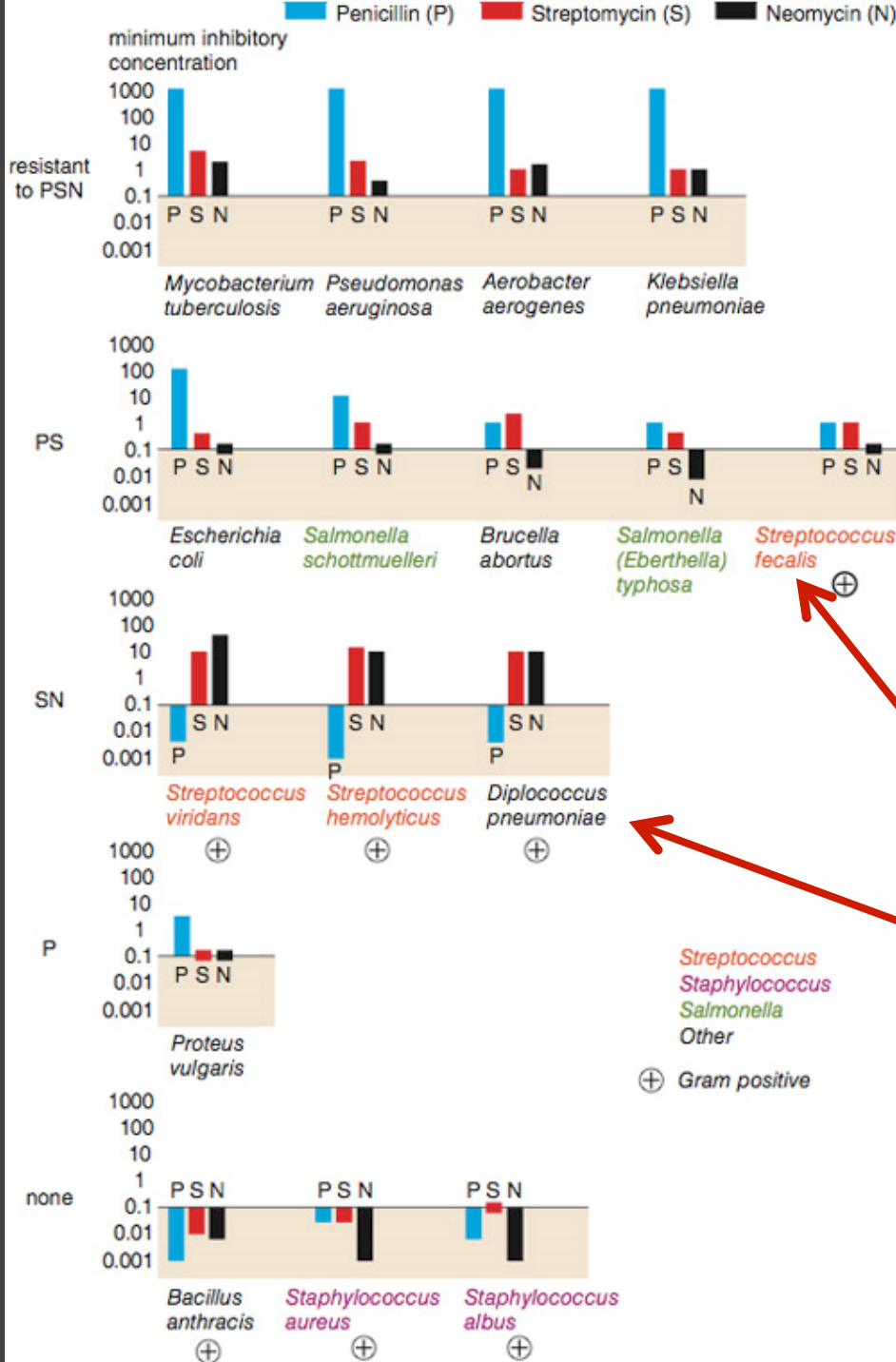
Do the bacteria group by antibiotic resistance?





Do the bacteria group by antibiotic resistance?

Not a streptococcus!
(realized ~30 yrs later)

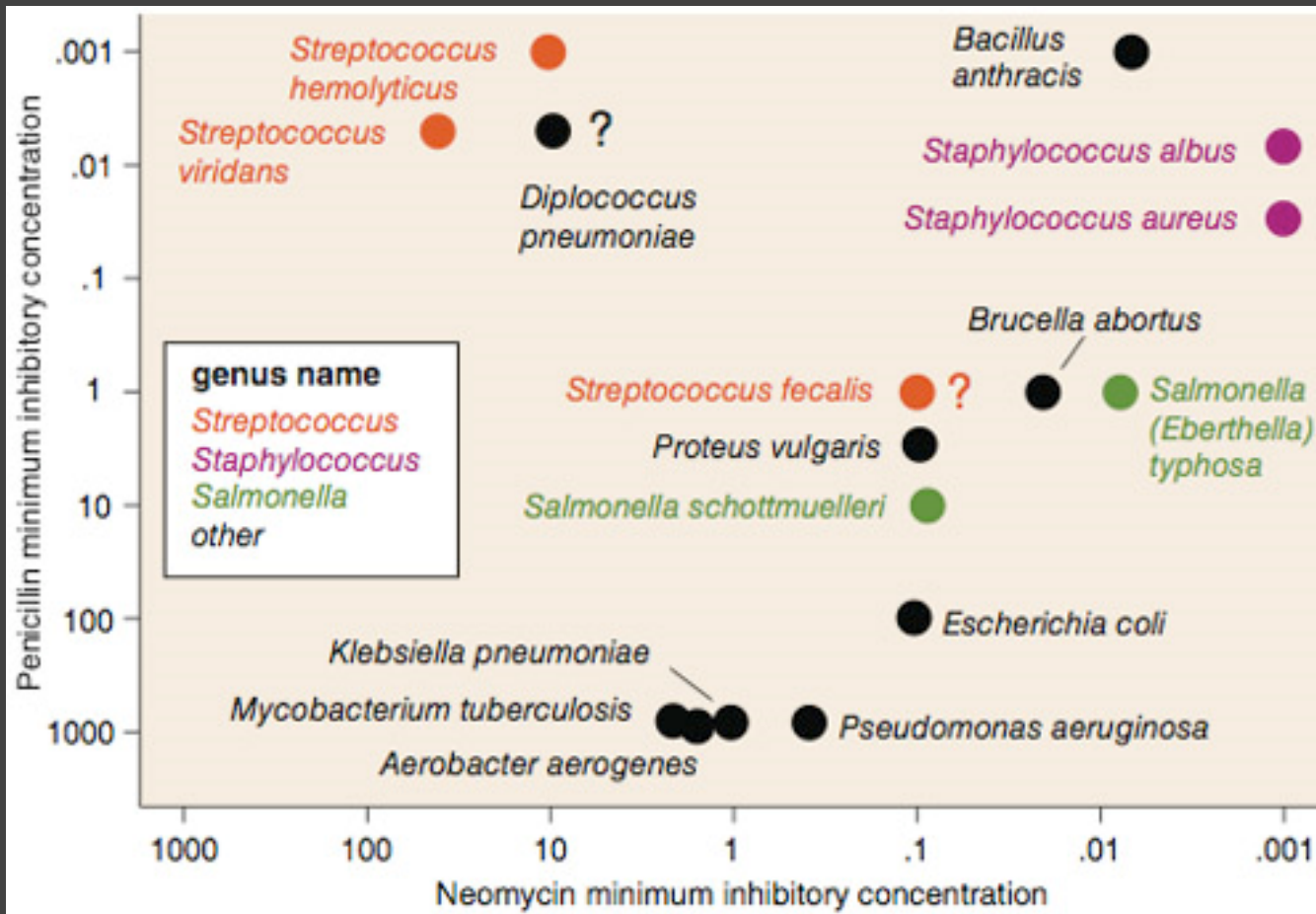


Do the bacteria group by antibiotic resistance?

Not a streptococcus!
(realized ~30 yrs later)

Really a streptococcus!
(realized ~20 yrs later)

**Do the bacteria group by resistance?
Do different drugs correlate?**



Do the bacteria group by resistance?
 Do different drugs correlate?

Lesson: Iterative Exploration

Exploratory Process

- 1 Construct graphics to address questions
- 2 Inspect “answer” and assess new questions
- 3 Repeat...

Transform data appropriately (e.g., invert, log)

Show data variation, not design variation [Tufte]

Administrivia

A2: Exploratory Data Analysis

Use visualization software to form & answer questions

First steps:

Step 1: Pick domain & data

Step 2: Pose questions

Step 3: Profile the data

Iterate as needed

Create visualizations

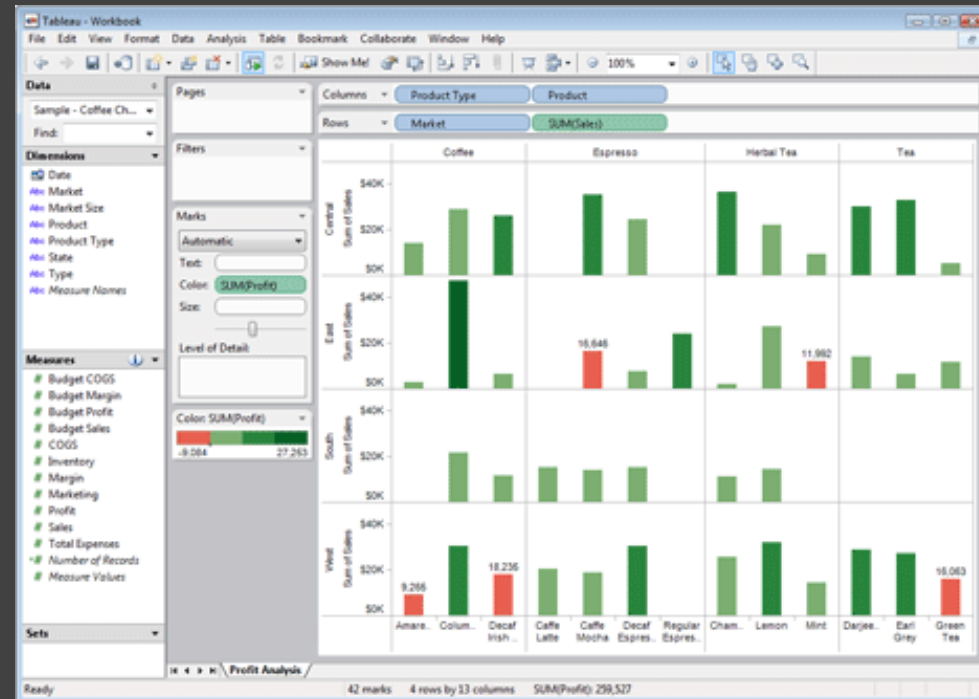
Interact with data

Refine your questions

Author a report

Screenshots of most insightful views (10+)

Include titles and captions for each view

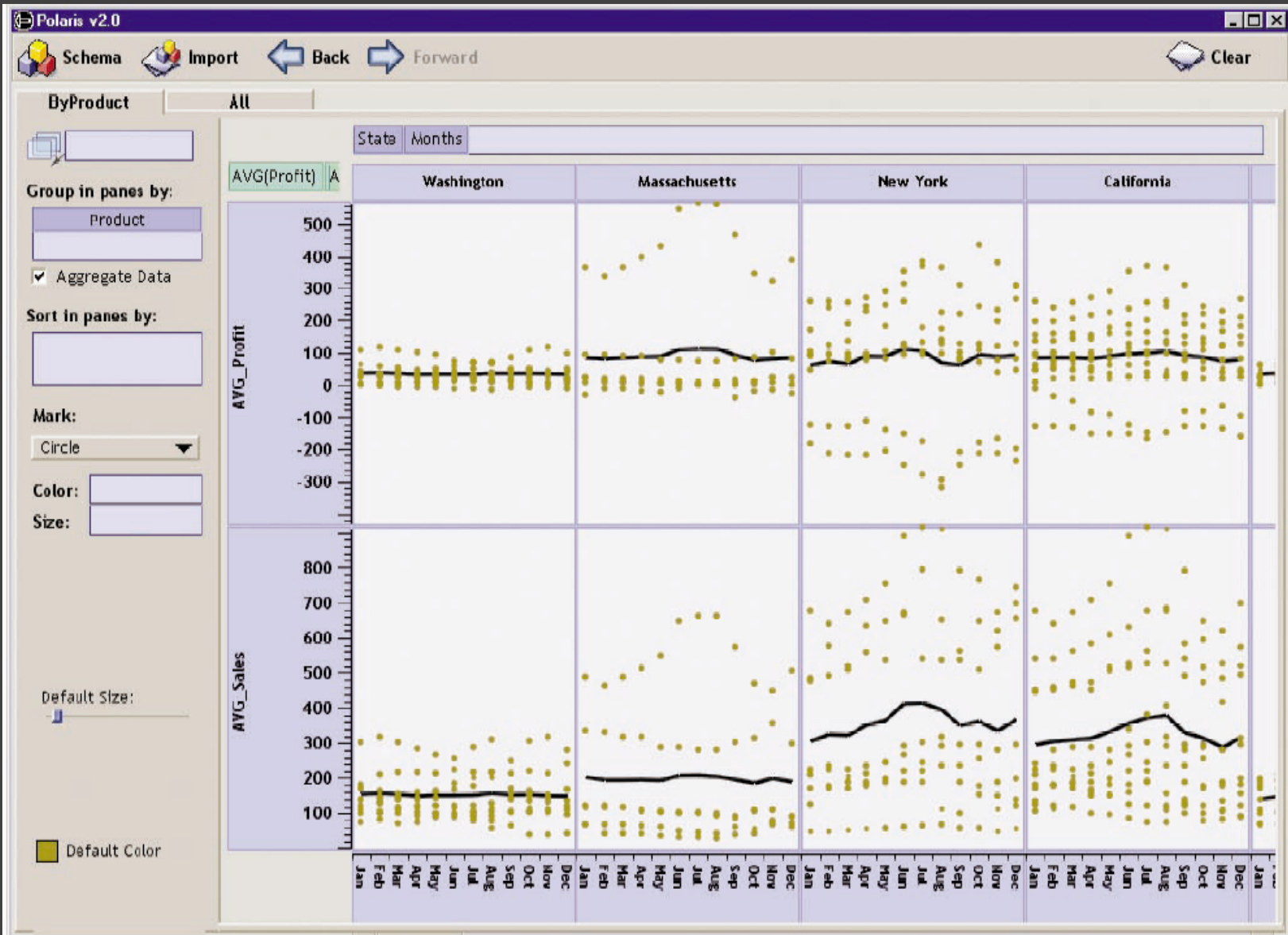


Due by 5:00pm

Monday, Oct 16

Tableau / Polaris

Polaris [Stolte et al.]



Tableau

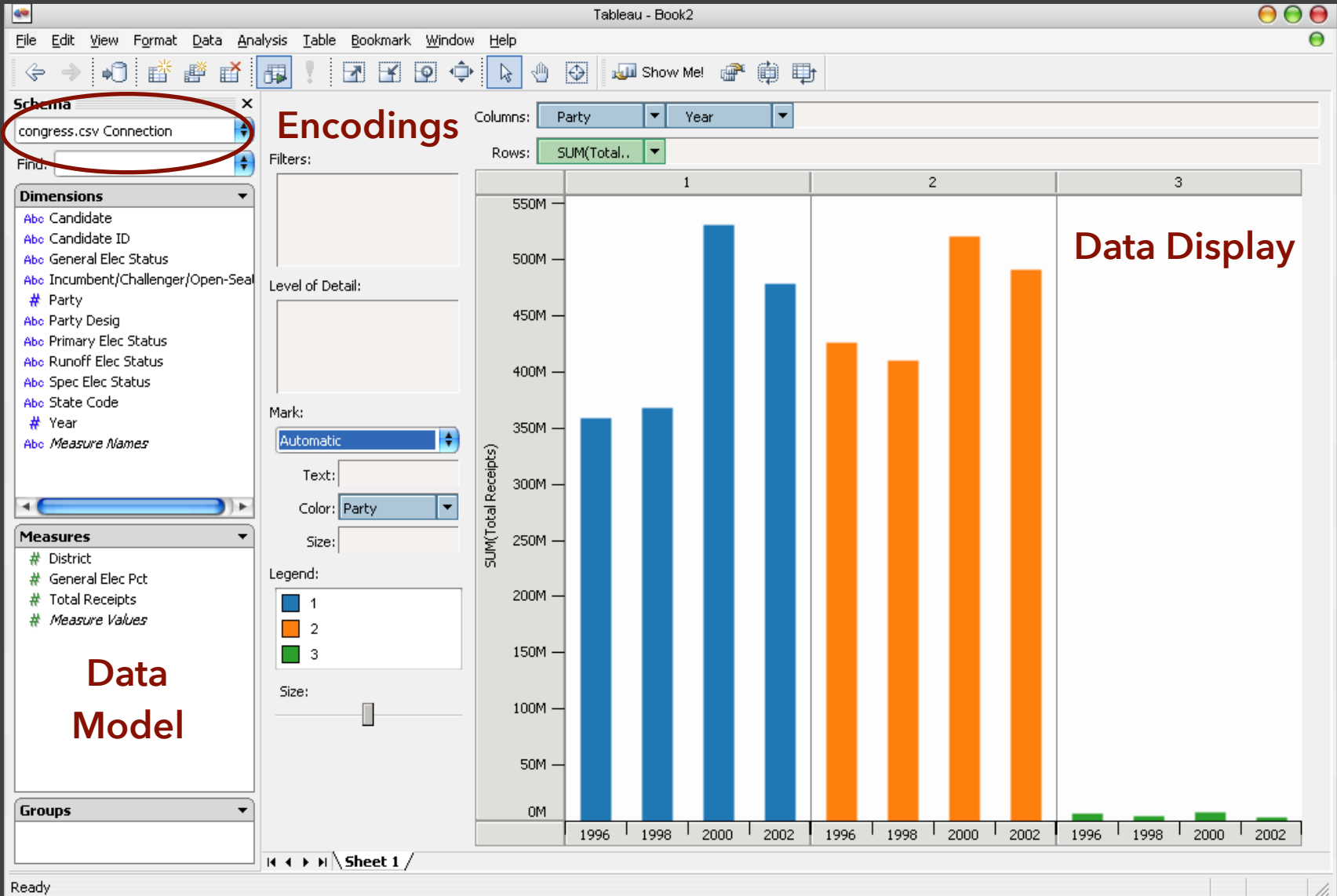


Tableau Demo

The dataset:

Federal Elections Commission Receipts

Every Congressional Candidate from 1996 to 2002

4 Election Cycles

9216 Candidacies

Dataset Schema

Year (Qi)

Candidate Code (N)

Candidate Name (N)

Incumbent / Challenger / Open-Seat (N)

Party Code (N) [1=Dem,2=Rep,3=Other]

Party Name (N)

Total Receipts (Qr)

State (N)

District (N)

This is a subset of the larger data set available from the FEC.

Hypotheses?

What might we learn from this data?

Hypotheses?

What might we learn from this data?

Correlation between receipts and winners?

Do receipts increase over time?

Which states spend the most?

Which party spends the most?

Margin of victory vs. amount spent?

Amount spent between competitors?

Tableau Demo

Tableau / Polaris Approach

Insight: can simultaneously specify both database queries and visualization

Choose data, then visualization, not vice versa

Use smart defaults for visual encodings

Can also suggest encodings upon request

Specifying Table Configurations

Operands are the database fields

Each operand interpreted as a set {...}

Quantitative and Ordinal fields treated differently

Three operators:

concatenation (+)

cross product (x)

nest (/)

Data | Analytics

Sample - Superstore

Dimensions

- Customer
 - Customer Name
 - Segment
- Order
- Location
- Product
 - Category
 - Sub-Category
 - Manufacturer
 - Product Name
- Profit (bin)
- Region
- Measure Names

Measures

- Discount
- Profit
- Profit Ratio
- Quantity
- Sales
- Latitude (generated)
- Longitude (generated)
- Number of Records
- Measure Values

Pages

Filters

Marks

Automatic

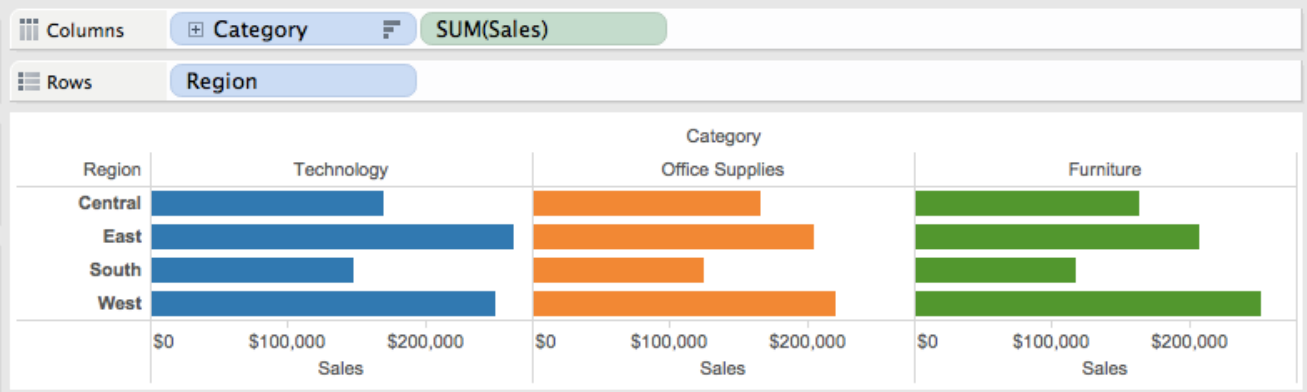
Color Size Label

Detail Tooltip

Category

Category

- Technology
- Office Supplies
- Furniture



Data | Analytics

Sample - Superstore

Dimensions

- Customer
 - Customer Name
 - Segment
- Order
 - Location
- Product
 - Category
 - Sub-Category
 - Manufacturer
 - Product Name
- Profit (bin)
- Region
- Measure Names

Measures

- Discount
- Profit
- Profit Ratio
- Quantity
- Sales
- Latitude (generated)
- Longitude (generated)
- Number of Records
- Measure Values

Pages

Filters

Marks

Automatic

Color Size Label

Detail Tooltip

Category

Category

- Technology
- Office Supplies
- Furniture



Data | Analytics

Sample - Superstore

Dimensions

- Customer
 - Customer Name
 - Segment
- Order
- Location
- Product
 - Category
 - Sub-Category
 - Manufacturer
 - Product Name
- Profit (bin)
- Region
- Measure Names

Measures

- Discount
- Profit
- Profit Ratio
- Quantity
- Sales
- Latitude (generated)
- Longitude (generated)
- Number of Records
- Measure Values

Pages

Filters

Marks

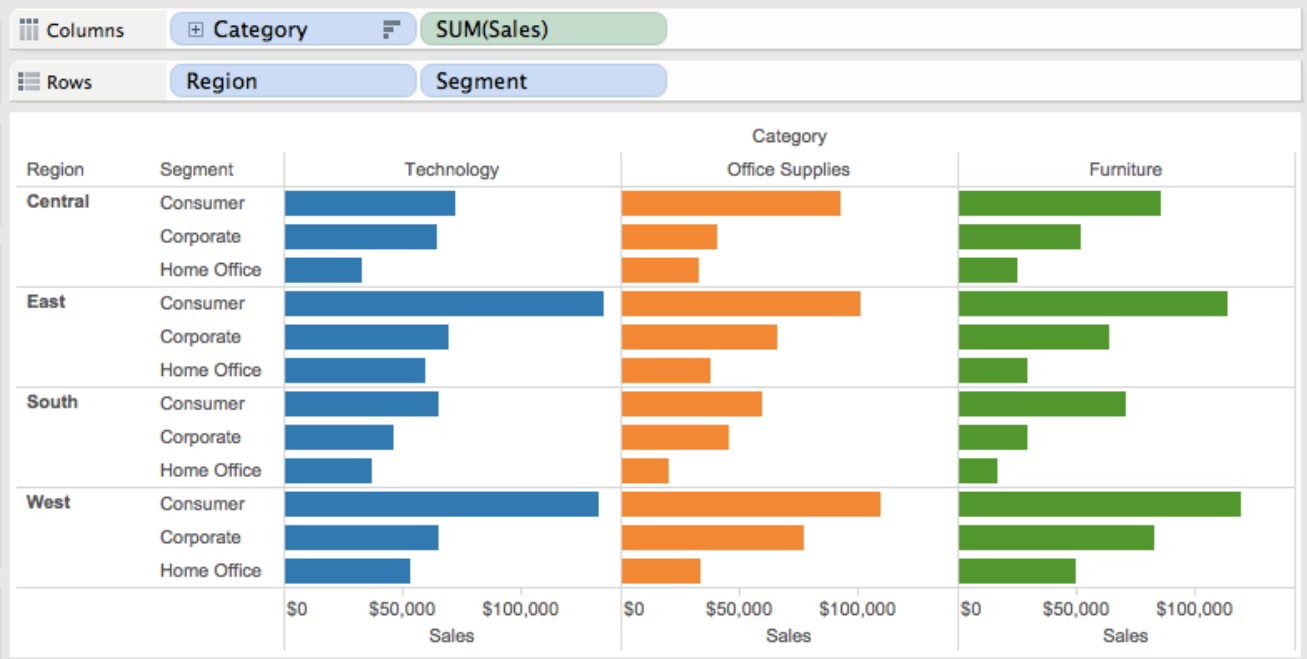
Automatic

Color Size Label

Detail Tooltip

Category

Technology
Office Supplies
Furniture



Data | Analytics

Sample - Superstore

Dimensions

- Customer
 - Customer Name
 - Segment
- Order
- Location
- Product
 - Category
 - Sub-Category
 - Manufacturer
 - Product Name
- Profit (bin)
- Region
- Measure Names

Measures

- Discount
- Profit
- Profit Ratio
- Quantity
- Sales
- Latitude (generated)
- Longitude (generated)
- Number of Records
- Measure Values

Pages

Filters

Marks

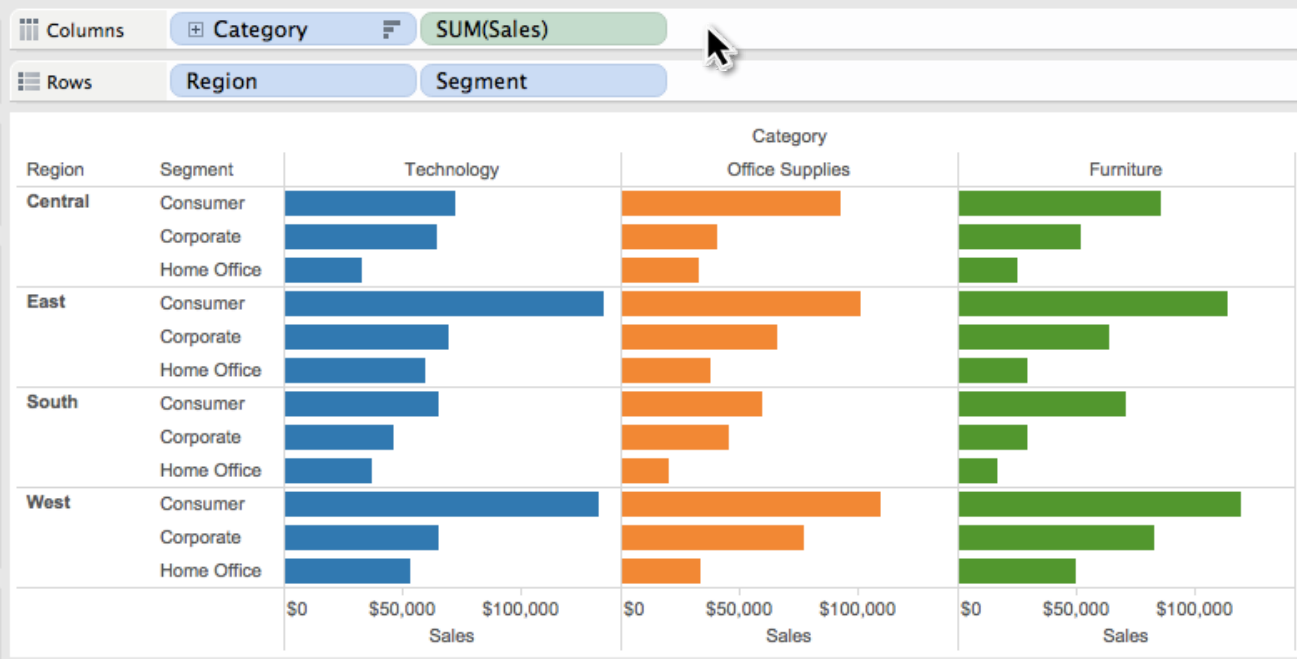
Automatic

Color Size Label

Detail Tooltip

Category

Technology
Office Supplies
Furniture



Data | Analytics

Sample - Superstore

Dimensions

- Customer
 - Customer Name
 - Segment
- Order
- Location
- Product
 - Category
 - Sub-Category
 - Manufacturer
 - Product Name
- Profit (bin)
- Region
- Measure Names

Measures

- Discount
- Profit
- Profit Ratio
- Quantity
- Sales
- Latitude (generated)
- Longitude (generated)
- Number of Records
- Measure Values

Pages

Filters

Marks

All

Automatic

Color Size Label

Detail Tooltip

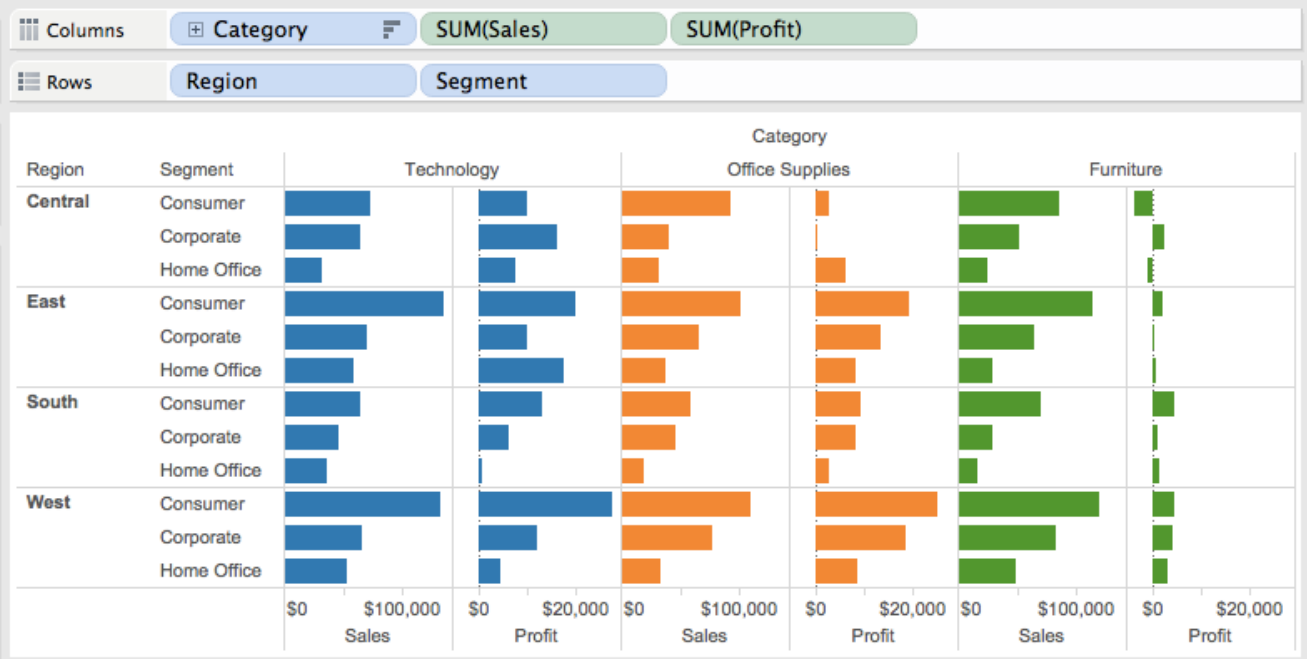
Category

SUM(Sales)

SUM(Profit)

Category

- Technology
- Office Supplies
- Furniture



Columns **Category** ~~SUM(Sales)~~ **SUM(Profit)**

Rows **Region** **Segment** **GROUP BY Category, Region, Segment**

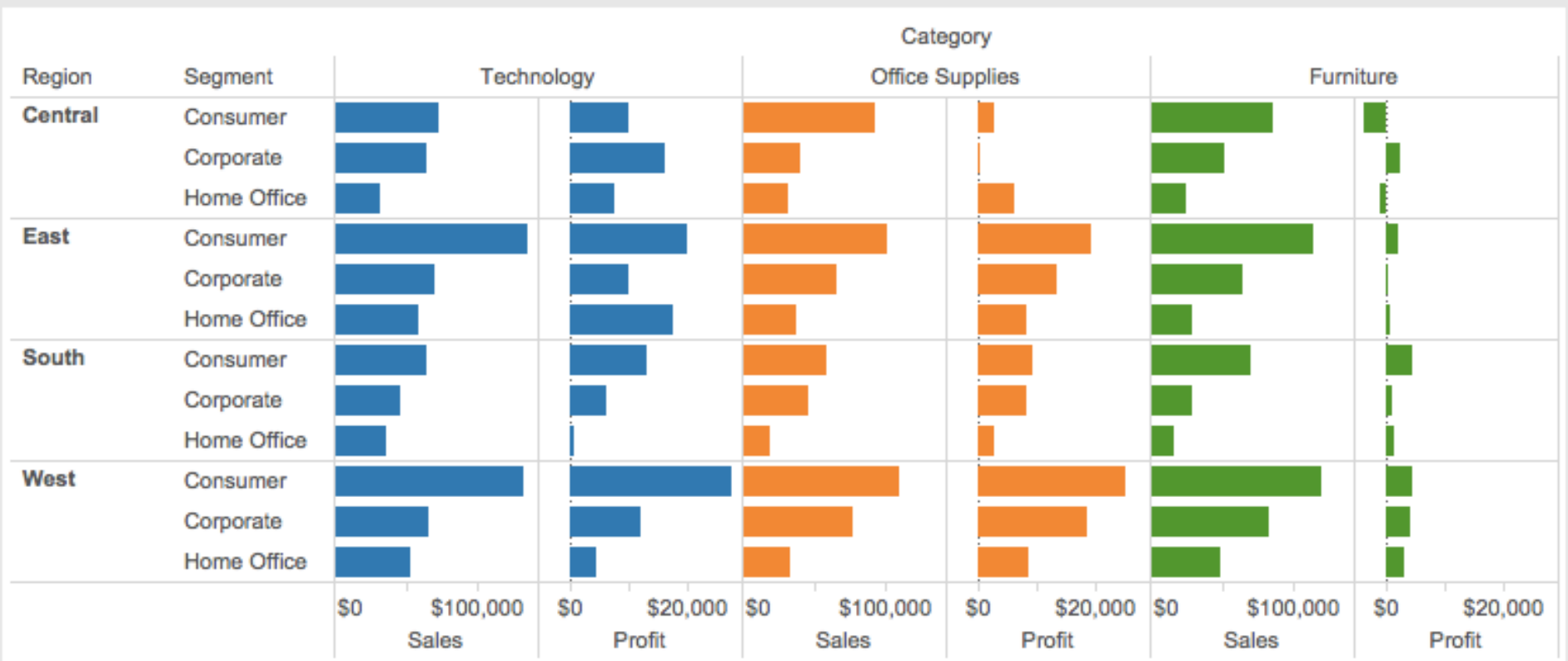


Table Algebra: Operands

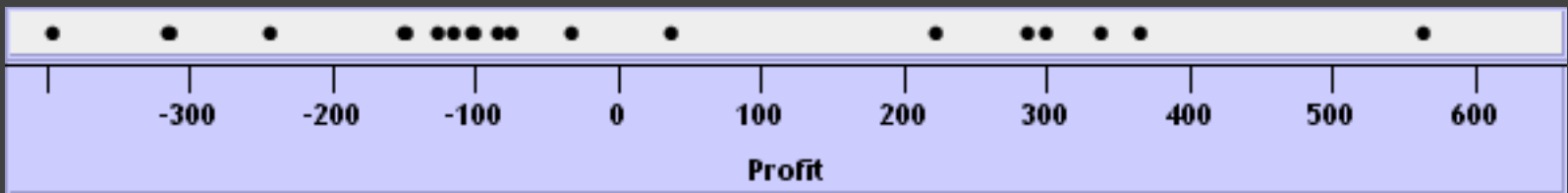
Ordinal fields: interpret domain as a set that partitions table into rows and columns.

Quarter = {(Qtr1),(Qtr2),(Qtr3),(Qtr4)} ->

| Qtr1 | Qtr2 | Qtr3 | Qtr4 |
|-------|--------|--------|-------|
| 95892 | 101760 | 105282 | 98225 |

Quantitative fields: treat domain as single element set and encode spatially as axes.

Profit = {(Profit[-410,650])} ->



Concatenation (+) Operator

Ordered union of set interpretations

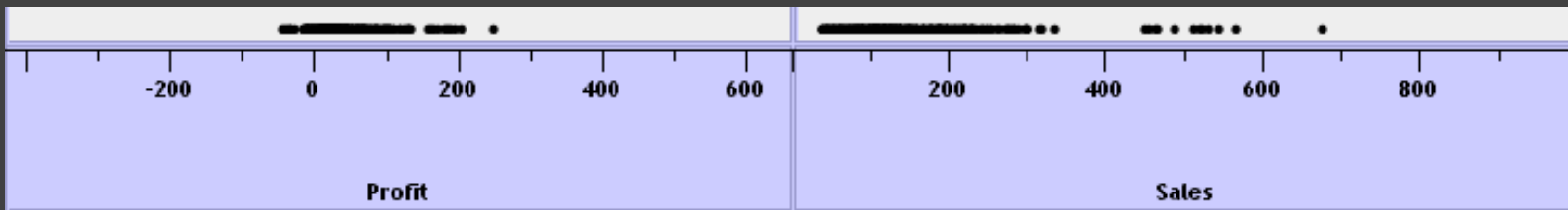
Quarter + Product Type

= {(Qtr1),(Qtr2),(Qtr3),(Qtr4)} + {(Coffee), (Espresso)}

= {(Qtr1),(Qtr2),(Qtr3),(Qtr4),(Coffee),(Espresso)}

| Qtr1 | Qtr2 | Qtr3 | Qtr4 | Coffee | Espresso |
|------|------|------|------|--------|----------|
| 48 | 59 | 57 | 53 | 151 | 21 |

Profit + Sales = {(Profit[-310,620]),(Sales[0,1000])}



Cross (x) Operator

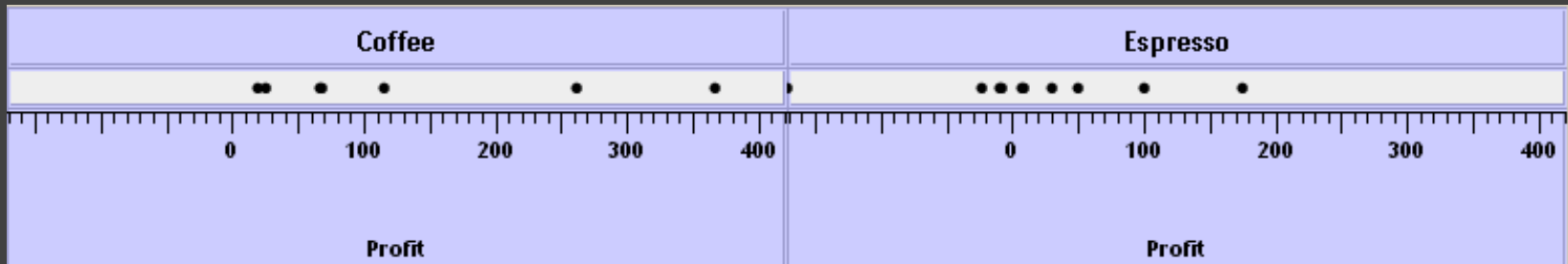
Cross-product of set interpretations

Quarter x Product Type =

{(Qtr1, Coffee), (Qtr1, Tea), (Qtr2, Coffee), (Qtr2, Tea), (Qtr3, Coffee), (Qtr3, Tea), (Qtr4, Coffee), (Qtr4, Tea)}

| Qtr1 | | Qtr2 | | Qtr3 | | Qtr4 | |
|--------|----------|--------|----------|--------|----------|--------|----------|
| Coffee | Espresso | Coffee | Espresso | Coffee | Espresso | Coffee | Espresso |
| 131 | 19 | 160 | 20 | 178 | 12 | 134 | 33 |

Product Type x Profit =



Nest (/) Operator

Cross-product filtered by existing records

Quarter x Month ->

creates twelve entries for each quarter. i.e.,
(Qtr1, December)

Quarter / Month ->

creates three entries per quarter based on
tuples in database (not semantics)

Table Algebra

The operators (+, x, /) and operands (O, Q) provide an *algebra* for tabular visualization.

Algebraic statements are then mapped to:

Visualizations - trellis plot partitions, visual encodings

Queries - selection, projection, group-by aggregation

In Tableau, users make statements via drag-and-drop

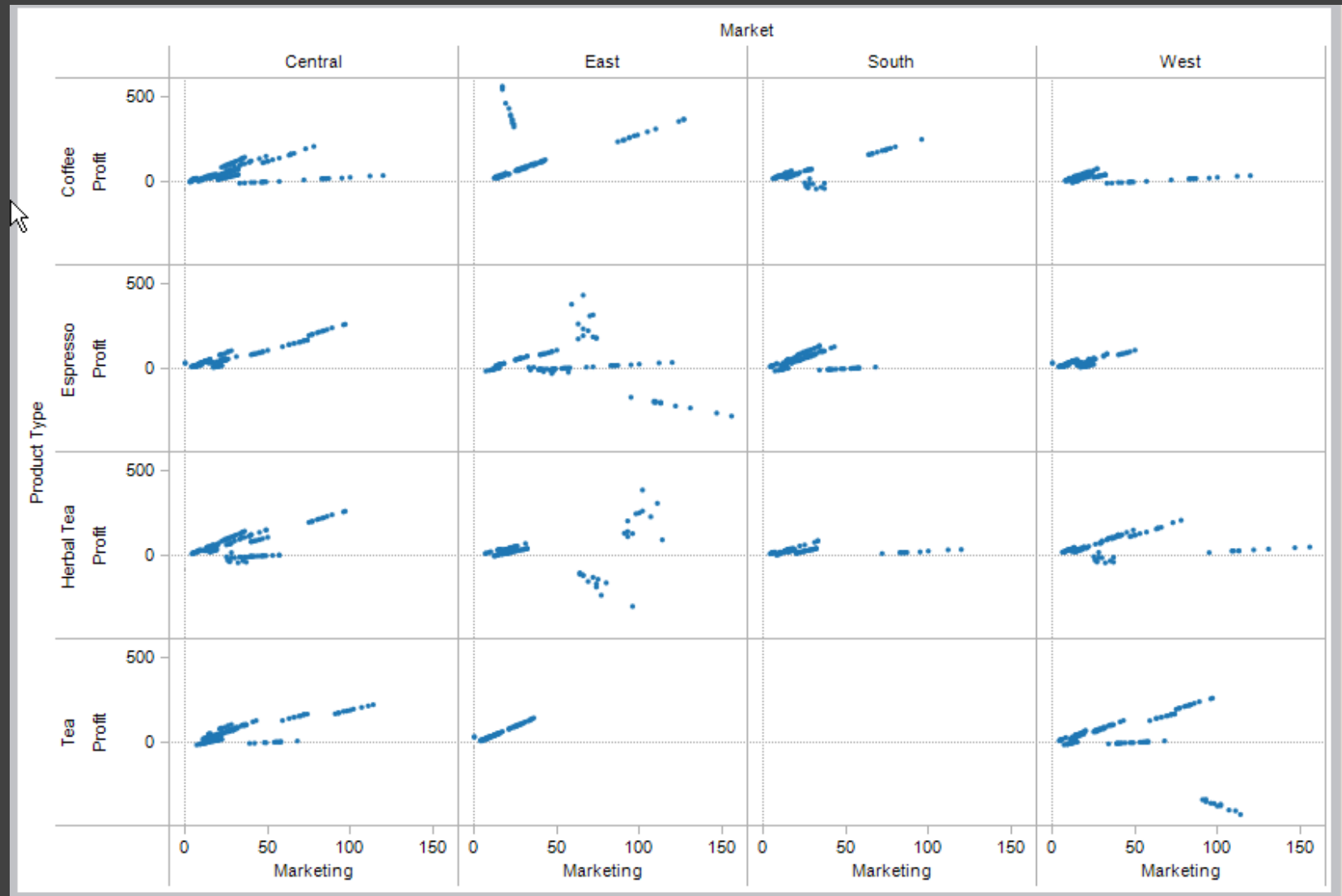
Note that this specifies operands *NOT* operators!

Operators are inferred by data type (O, Q)

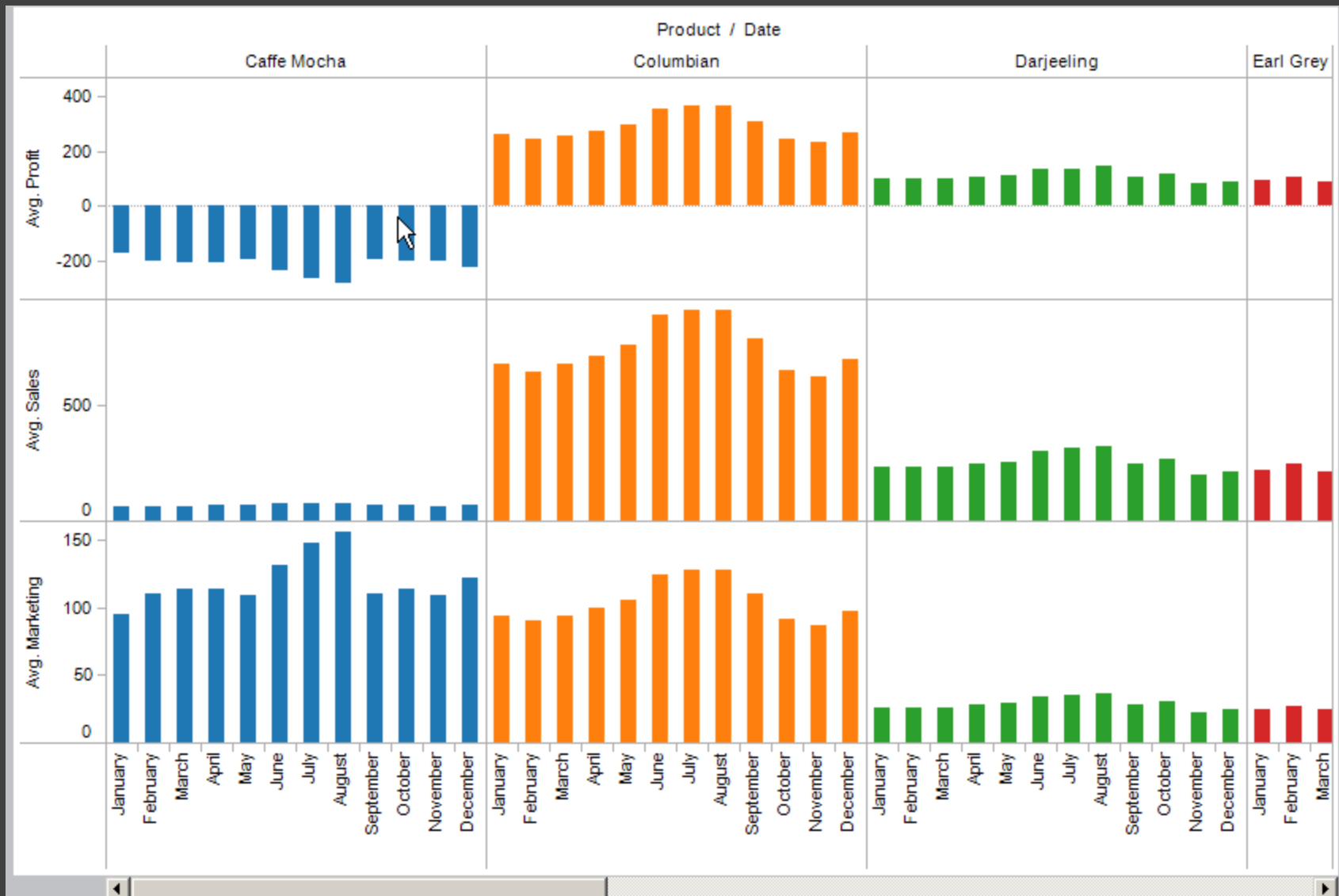
Ordinal-Ordinal

| State | Product Type | | | |
|---------------|--------------|----------|------------|-----|
| | Coffee | Espresso | Herbal Tea | Tea |
| Colorado | ● | ● | ● | ● |
| Connecticut | ● | ● | ● | ● |
| Florida | ● | ● | ● | ● |
| Illinois | ● | ● | ● | ● |
| Iowa | ● | ● | ● | ● |
| Louisiana | ● | ● | ● | ● |
| Massachusetts | ● | ● | ● | ● |
| Missouri | ● | ● | ● | ● |
| Nevada | ● | ● | ● | ● |
| New Hampshire | ● | ● | ● | ● |
| New Mexico | ● | ● | ● | ● |
| New York | ● | ● | ● | ● |
| Ohio | ● | ● | ● | ● |
| Oklahoma | ● | ● | ● | ● |
| Oregon | ● | ● | ● | ● |
| Texas | ● | ● | ● | ● |
| Utah | ● | ● | ● | ● |
| Washington | ● | ● | ● | ● |
| Wisconsin | ● | ● | ● | ● |

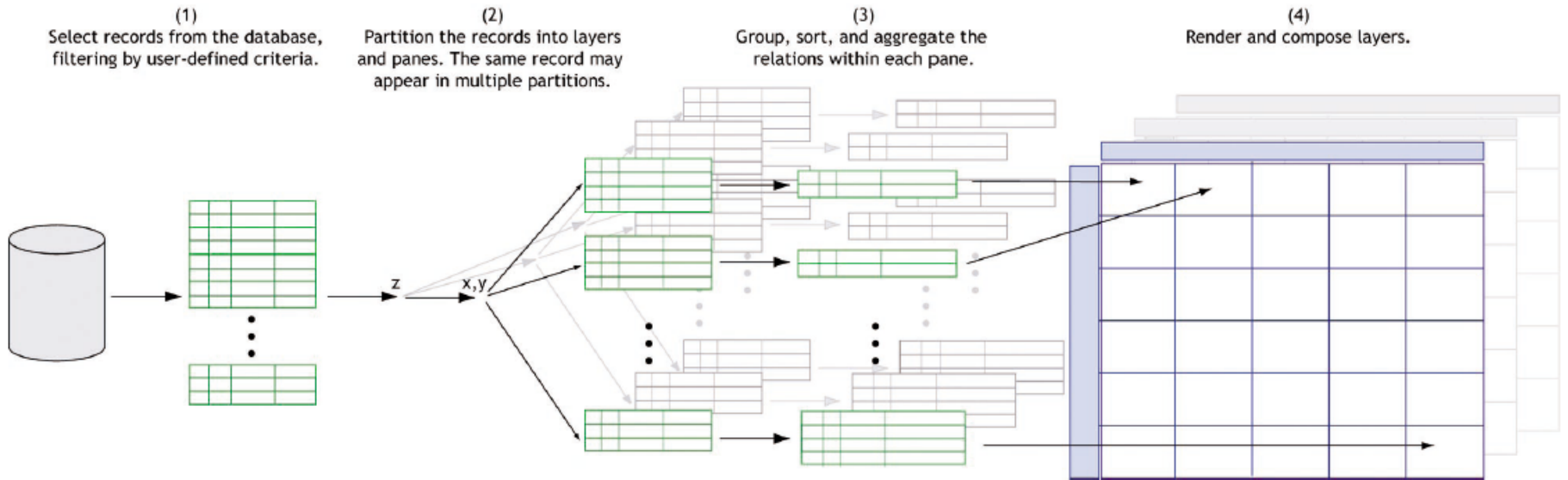
Quantitative-Quantitative



Ordinal-Quantitative



Querying the Database



BONUS TOPIC

Data Fraud

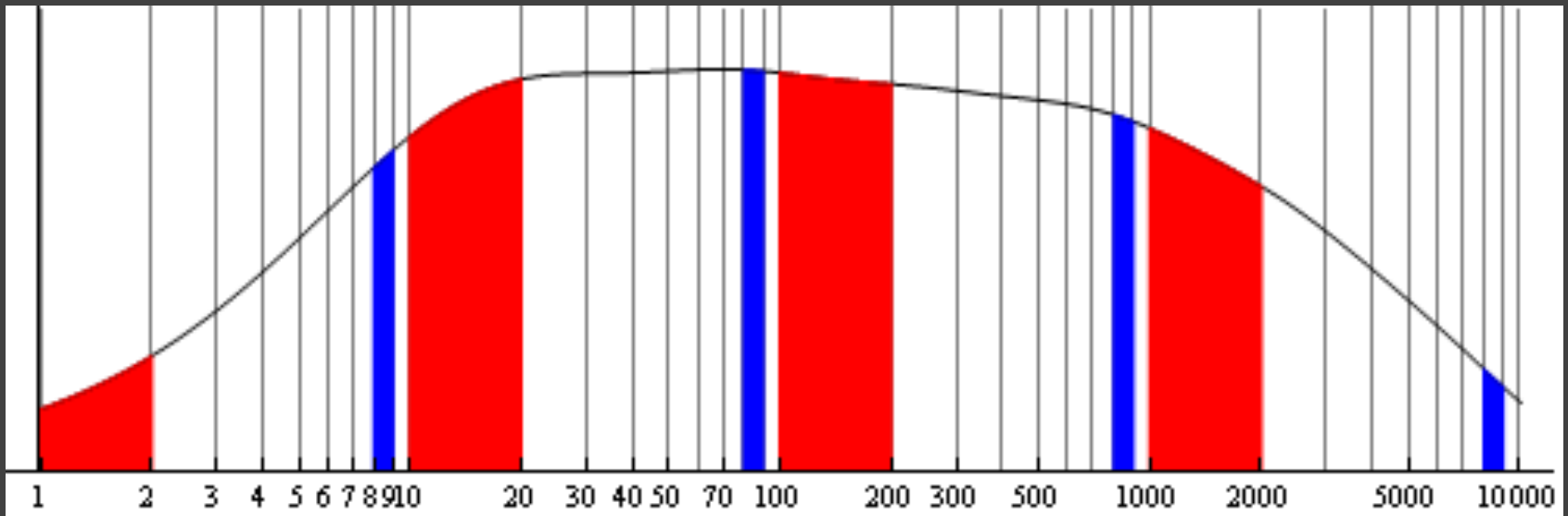
A Detective Story

You have accounting records for two firms that are in dispute. One is lying. *How to tell?*

| <i>Firm A</i> | | <i>Firm B</i> | LIARS! |
|-----------------------|----------|------------------------|---------------|
| 283.08 | 25.23 | 283.08 | 75.23 |
| 153.86 | 385.62 | 353.86 | 185.25 |
| 1448.97 | 12371.32 | 5322.79 | 9971.42 |
| 18595.91 | 1280.76 | 8795.64 | 4802.43 |
| 21.33 | 257.64 | 61.33 | 57.64 |
| Amt. Paid: \$34823.72 | | Amt. Rec'd: \$29908.67 | |

Benford's Law (Benford 1938, Newcomb 1881)

The *logarithms* of the values (not the values themselves) are uniformly randomly distributed.



Hence the leading digit **1** has a ~30% likelihood. Larger digits are increasingly less likely.

Benford's Law (Benford 1938, Newcomb 1881)

The *logarithms* of the values (not the values themselves) are uniformly randomly distributed.

Holds for many (but certainly not all) real-life data sets: Addresses, Bank accounts, Building heights, ...

Data must span multiple orders of magnitude.

Evidence that records do not follow Benford's Law is admissible in a court of law!