
CSE 427 Computational Biology

BLAST
Alignment score significance
PCR and DNA sequencing

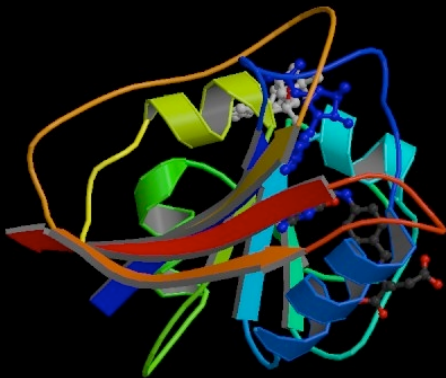
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The Plan

- BLAST
- Scoring
- Another Bio Interlude: PCR & Sequencing

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A Protein Structure: (Dihydrofolate Reductase)



Sequence Evolution

Nothing in Biology Makes Sense Except in the Light of Evolution

– Theodosius Dobzhansky, 1973

- Changes happen at random
- Deleterious/neutral/advantageous changes unlikely/possibly/likely spread widely in a population
- Changes are less likely to be tolerated in positions involved in many/close interactions, e.g.
 - enzyme binding pocket
 - protein/protein interaction surface
 - ...

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BLAST: Basic Local Alignment Search Tool

Altschul, Gish, Miller, Myers, Lipman, J Mol Biol 1990

- *The* most widely used comp bio tool
- Which is better: long mediocre match or a few nearby, short, strong matches with the same total score?
 - score-wise, exactly equivalent
 - biologically, later may be more interesting, & is common
 - at least, if must miss some, rather miss the former
- BLAST is a heuristic emphasizing the later
 - speed/sensitivity tradeoff: BLAST may miss former, but gains greatly in speed

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BLAST: What

- Input:
 - a query sequence (say, 300 residues)
 - a data base to search for other sequences similar to the query (say, 10^6 - 10^9 residues)
 - a score matrix $\sigma(r,s)$, giving cost of substituting r for s (& perhaps gap costs)
 - various score thresholds & tuning parameters
- Output:
 - “all” matches in data base above threshold
 - “E-value” of each

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BLAST: How

Idea: find parts of data base near a good match to some short subword of the query

- Break query into overlapping words w_i of small fixed length (e.g. 3 aa or 11 nt)
- For each w_i , find (empirically, ~50) “neighboring” words v_{ij} with ungapped score $\sigma(w_i, v_{ij}) > \text{thresh}_1$
- Look up each v_{ij} in database (via prebuilt index) -- i.e., exact match to short, high-scoring word
- Extend each such “seed match” (bidirectional)
- Report those scoring $> \text{thresh}_2$, calculate E-values

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BLAST: Example

query → deadly ≥ 7 (thresh₁)

de	(11)	→	de ee dd dq dk
ea	(9)	→	ea
ad	(10)	→	ad sd
dl	(10)	→	dl di dm dv
ly	(11)	→	ly my iy vy fy lf

DB → ddgearlyk . . .

hits	→	ddge	10	} ≥ 10 (thresh ₂)
	→	early	18	

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BLOSUM 62

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2
E	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3
H	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4

BLAST Refinements

- “Two hit heuristic” -- need 2 nearby, nonoverlapping, gapless hits before trying to extend either
- “Gapped BLAST” -- run heuristic version of Smith-Waterman, bi-directional from hit, until score drops by fixed amount below max
- PSI-BLAST -- For proteins, iterated search, using “weight matrix” pattern from initial pass to find weaker matches in subsequent passes

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Significance of Alignments

- Is “42” a good score?
- *Compared to what?*
- Usual approach: compared to a specific “null model”, such as “random sequences”

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Hypothesis Testing: A Very Simple Example

- Given: A coin, either fair ($p(H)=1/2$) or biased ($p(H)=2/3$)
 - Decide: which
 - How? Flip it 5 times. Suppose outcome D = HHHTH
 - Null Model/Null Hypothesis M_0 : $p(H)=1/2$
 - Alternative Model/Alt Hypothesis M_1 : $p(H)=2/3$
 - Likelihoods:
 - $P(D | M_0) = (1/2) (1/2) (1/2) (1/2) (1/2) = 1/32$
 - $P(D | M_1) = (2/3) (2/3) (2/3) (1/3) (2/3) = 16/243$
 - Likelihood Ratio: $\frac{P(D | M_1)}{P(D | M_0)} = \frac{16/243}{1/32} = \frac{512}{243} \approx 2.1$
- I.e., alt model is ≈ 2.1 x more likely than null model, given data

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Hypothesis Testing, II

- Log of likelihood ratio is equivalent, often more convenient
 - add logs instead of multiplying...
- “Likelihood Ratio Tests”: reject null if LLR > threshold
 - LLR > 0 disfavors null, but higher threshold gives stronger evidence against
- Neyman-Pearson Theorem: For a given error rate, LRT is as good a test as any (subject to some fine print).

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p-values

- the *p-value* of such a test is the probability, assuming that the null model is true, of seeing data as extreme or more extreme than what you actually observed
- e.g., we observed 4 heads; p-value is prob of seeing 4 or 5 heads in 5 tosses of a fair coin
- Why interesting? It measures probability that we would be making a mistake in rejecting null.
- Usual scientific convention is to reject null only if p-value is < 0.05; sometimes demand $p \ll 0.05$
- can analytically find p-value for simple problems like coins; often turn to simulation/permutation tests for more complex situations; as below

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A Likelihood Ratio Test for Alignment

- Defn: two proteins are *homologous* if they are alike because of shared ancestry; similarity by descent
- suppose among proteins overall, residue x occurs with frequency p_x
- then in a random alignment of 2 random proteins, you would expect to find x aligned to y with prob $p_x p_y$
- suppose among *homologs*, x & y align with prob p_{xy}
- are seqs X & Y homologous? Which is more likely, that the alignment reflects chance or homology? Use a *likelihood ratio test*.

$$\sum_i \log \frac{P_{x_i y_i}}{p_{x_i} p_{y_i}}$$

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Non-*ad hoc* Alignment Scores

- Take alignments of homologs and look at frequency of x-y alignments vs freq of x, y overall
- Issues
 - biased samples
 - evolutionary distance
- BLOSUM approach
 - large collection of trusted alignments (the BLOCKS DB),
 - subsetted by similarity, e.g. BLOSUM62 => 62% identity
 - e.g. <http://blocks.fhcr.org/blocks-bin/getblock.pl?IPB013598>

$$\frac{1}{\lambda} \log_2 \frac{P_{x y}}{p_x p_y}$$

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ad hoc Alignment Scores?

- Make up any scoring matrix you like
- Somewhat surprisingly, under pretty general assumptions**, it is *equivalent* to the scores constructed as above from some set of probabilities p_{xy} , so you might as well understand what they are

** e.g., average scores should be negative, but you probably want that anyway, otherwise local alignments turn into global ones, and some score must be > 0 , else best match is empty

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BLOSUM 62

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2
E	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3
H	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4

Alignment Scores vs Test Statistic

- Alignment alg *works hard* to contort data into a high-scoring alignment
- Goal of test statistic is to discriminate good/bad ones
- Why use same score? Doesn't a better alg just push up scores? Maybe better to test via an *independent* criterion?
- A: Yes, better alg may raise background scores. *But*, want best discrimination in both phases, so use best possible score/test statistic, with appropriate threshold, rather than an indep. criterion
- Note: best random match looks like real match (e.g. same matching-letter frequencies), except for score.
- One reason to score/test differently—if score is too expensive for search, might try search w/ approx score, look at multiple hits

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Overall Alignment Significance, I A Theoretical Approach: EVD

Let X_i , $1 \leq i \leq N$, be indep. random variables drawn from some (non-pathological) distribution

Q. what can you say about distribution of $y = \sum\{X_i\}$?

A. y is approximately *normally* distributed

Q. what can you say about distribution of $y = \max\{X_i\}$?

A. it's approximately an *Extreme Value Distribution (EVD)*

$$P(y \leq z) \approx \exp(-KNe^{-\lambda(z-\mu)}) \quad (*)$$

For ungapped local alignment of seqs x, y , $N \sim |x|^*|y|$
 λ, K depend on scores, etc., or can be estimated by curve-fitting random scores to (*). (cf. reading)

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EVD Pro/Con

- Pro:
 - gives p-values for alignment scores
- Con:
 - It's only approximate
 - parameter estimation
 - theory may not apply. E.g., it is NOT known to hold for gapped alignments (although empirically it seems to work pretty well).

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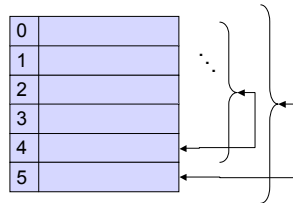
Overall Alignment Significance, II Empirical (via randomization)

- generate N random sequences (say $N = 10^3 - 10^6$)
- align x to each & score
- if k of them have better score than alignment of x to y, then the (empirical) probability of a chance alignment as good as observed x:y alignment is $(k+1)/N$
 - e.g., if 0 of 100 are better, you can say “estimated $p < .01$ ”
- How to generate “random” sequences?
 - Alignment scores often sensitive to sequence composition
 - so uniform 1/20 or 1/4 is a bad idea
 - even background p_i can be dangerous
 - Better idea: *permute* y N times

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Generating Random Permutations

```
for (i= n-1; i > 0; i--){  
  j = random(0..i);  
  swap X[i]<-> X[j];  
}
```



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Permutation Pro/Con

- Pro:
 - Gives empirical p-values for alignments with characteristics like sequence of interest, e.g. residue frequencies
- Con:
 - Can be inaccurate if your method of generating random sequences is unrepresentative
 - E.g., probably better to preserve di-, tri-residue statistics and/or other higher-order characteristics, but increasingly hard to know exactly what to model & how
 - Slow
 - Especially if you want to assess low-probability p-values

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p-values & multiple testing

Above give "p-values": probability of a score more extreme than observed if the target sequence were random
must be careful whether p-value means wrt comparison to one other random protein, or best of a database of n random proteins

E.g., suppose p-value for x:y match is 10^{-3} , then you'd expect to see a score that good only one time in a thousand among non-homologous sequences

Sounds good

What if you *found y* by picking best match among 10^4 proteins?

Sounds not so good

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E-values

- "p-value": probability of a score more extreme than observed in a given random target data base
- E-value: expected number of matches that good or better in a random data base of the given size & composition
- Related: $P = 1 - \exp(-E)$
 - $E = 5 \leftrightarrow P = .993$
 - $E = 10 \leftrightarrow P = .99995$
 - $E = .01 \leftrightarrow P = E - E^2/2 + E^3/3! \dots \approx E$
- both equally valid; E-value is perhaps a more intuitively interpretable quantity, & perhaps makes role of data base size more explicit

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Issues

- What if the model is wrong?
- E.g., are adjacent positions really independent?

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Summary

- BLAST is a highly successful search/alignment heuristic. It looks for alignments anchored by short, strong, ungapped "seed" alignments
- Assessing statistical significance of alignment scores is crucial to practical applications
 - score matrices derived from "likelihood ratio" test of trusted alignments vs random "null" model
 - for gapless alignments, Extreme Value Distribution (EVD) is theoretically justified for overall significance of alignment scores; empirically seems ok for gapped alignments, too
 - permutation tests are a simple (but brute force) alternative

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Another Bio(tech) Interlude

2 Nobel Prizes:
 PCR: Kary Mullis, 1993
 DNA Sequencing: Frederick Sanger, 1980

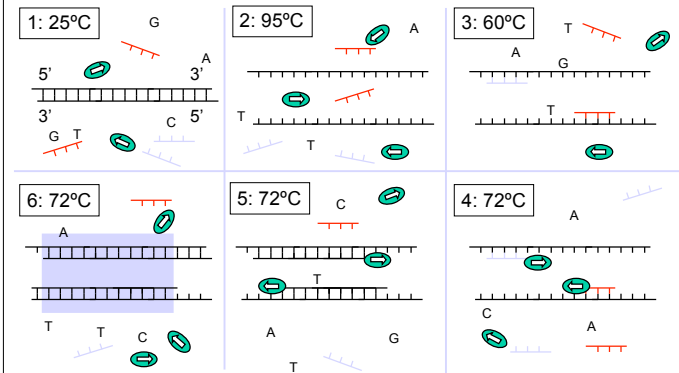
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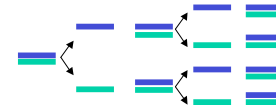
Hot spring, near Great Fountain
 Geyser, Yellowstone National Park

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PCR



PCR



- **Ingredients:**
 - many copies of deoxy nucleotide triphosphates
 - many copies of two primer sequences (~20 nt each)
 - readily synthesized
 - many copies of Taq polymerase (*Thermus aquaticus*),
 - readily available commercially
 - as little as 1 strand of template DNA
 - a programmable “thermal cycler”
- **Amplification:** million to billion fold
- **Range:** up to 2k bp routinely; 50k with other enzymes & care
- **Very widely used;** forensics, archeology, cloning, sequencing, ...

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DNA Forensics

- E.g. FBI “CODIS” (combined DNA indexing system) data base
- pick 13 short, variable regions of human genome
- amplify each from, e.g., small spot of dried blood
- measure product lengths (next slides)

- PCR is important in that sample size is reduced from grams of tissue to a few cells

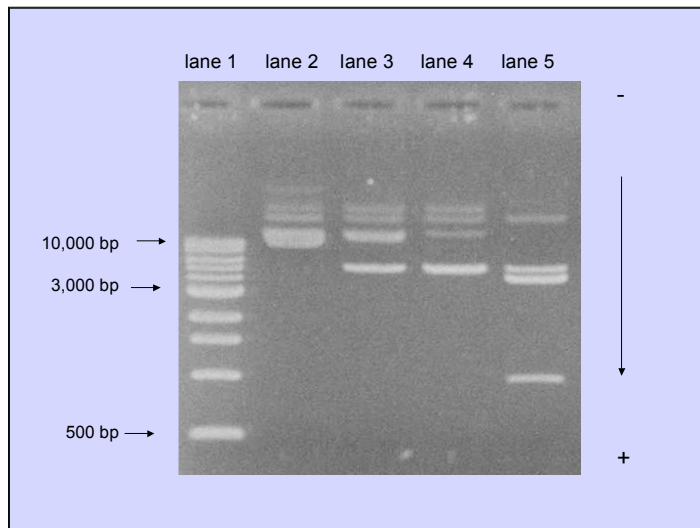
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Gel Electrophoresis

- DNA/RNA backbone is negatively charged
- Molecules move slowly in gels under an electric field
 - agarose gels for large molecules
 - polyacrylamide gels for smaller ones
- Smaller molecules move faster

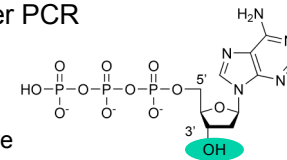
- So, you can *separate DNAs & RNAs by size*

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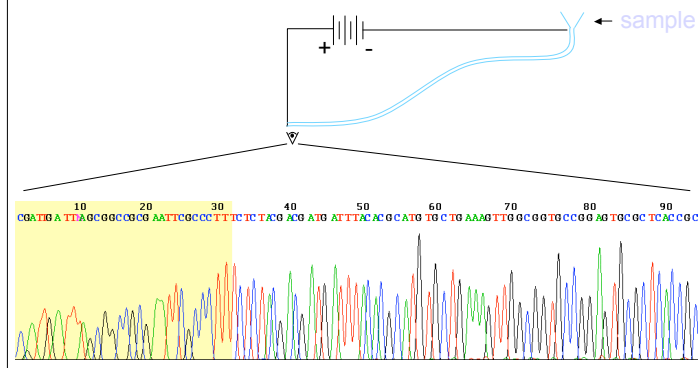
DNA Sequencing

- Like one-cycle, one-primer PCR
- Suppose 0.1% of A's:
 - are *di*-deoxy adenosine's; backbone can't extend
 - carry a green fluorescent dye
- Separate by capillary gel electrophoresis
- If frags of length 42, 49, 50, 55 ... glow green, those positions are A's
- Ditto C's (blue), G's (yellow), T's (red)



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DNA Sequencing



DNA Sequencing

- Highly automated
- Typically can “read” about 600 nt in one run
- “Whole Genome Shotgun” approach:
 - cut genome randomly into $\sim G / 600 \times 10$ fragments
 - sequence each
 - reassemble by computer



- Complications: repeated region, missed regions, sequencing errors, chimeric DNA fragments, ...
- But overall accuracy $\sim 10^{-4}$, if careful

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Summary

- PCR allows simple *in vitro* amplification of minute quantities of DNA (having pre-specified boundaries)
- Sanger sequencing uses
 - a PCR-like setup with modified chemistry to generate varying length prefixes of a DNA template with the last nucleotide of each color-coded
 - gel electrophoresis to separate DNA by size, giving sequence
- Sequencing random overlapping fragments allows genome sequencing

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