CSE 421, Su '14: Introduction to Algorithms

Lecture: EEB 026 (schematic) MW 10:50-12:20
Office Hours Location Phone
Instructor: Larry Ruzzo, ruzzo@cs CSE 554 206-543-6298

Course Email: cse421a_su14@uw.edu. Staff announcements and general interest student/staff Q&A about how subscribed to this list. Enrolled students are as well, but probably should change their default subscriptions.

Catalog Description: Techniques for design of efficient algorithms. Methods for sorting, searching, set manipulation, arithmetic, graph problems, patterns.

Prerequisites: either CSE 312 or CSE 322; either CS 221.

Credits: 3
Grading: Homework, Final Project, Lab — programming. Overall weights 60%, 40%, no late policy.

Extra Credit: There are "extra credit" sections. These will enrich your understanding of the material, but at a lower weight. Don't start extra credit until the basics are complete.


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Computer Science & Engineering
University of Washington
Box 352350
Seattle, WA 98195-2350
(206) 543-1695 voice, (206) 543-2969 FAX
What you have to do

Weekly Homework (~60% of grade)
  Programming
    some small projects
  Written homework assignments
    English exposition and pseudo-code
    Analysis and argument as well as design

Final Exam (~40%)

Late Policy:
  Papers and/or electronic turnins generally due Fridays by 5:00 pm; minus 20% per calendar day thereafter
Textbook

What the course is about

Design of Algorithms

design methods

common or important types of problems

analysis of algorithms - efficiency

correctness proofs
What the course is about

Complexity, NP-completeness and intractability

solving problems in principle is not enough

algorithms must be efficient

some problems have no efficient solution

NP-complete problems

important & useful class of problems whose solutions
(seemingly) cannot be found efficiently, but can be
checked easily
Very Rough Division of Time

Algorithms (6-7 weeks)
  Analysis
  Techniques: greedy, divide & conquer, dynamic programming,
  Toolkit: e.g., flows & matchings
Applications

Complexity & NP-completeness (2-3 weeks)

Check online schedule page for (evolving) details
Complexity Example

Cryptography (e.g., RSA, SSL in browsers)

Secret: $p,q$ prime, say 512 bits each

Public: $n$ which equals $p \times q$, 1024 bits

In principle

*there is an algorithm* that given $n$ will find $p$ and $q$:

try all $2^{512} > 1.3 \times 10^{154}$ possible $p$’s: kinda slow…

In practice

*no fast algorithm* known for this problem (on non-quantum computers)

security of RSA depends on this fact

(“quantum computing”: strongly driven by possibility of changing this)
Algorithms versus Machines

We all know about Moore’s Law and the exponential improvements in hardware...

Ex: sparse linear equations over 25 years

10 orders of magnitude improvement!
Algorithms or Hardware?

25 years progress solving sparse linear systems

hardware: 4 orders of magnitude

Source: Sandia, via M. Schultz
Algorithms or Hardware?

25 years progress solving sparse linear systems

hardware: 4 orders of magnitude

software: 6 orders of magnitude

Source: Sandia, via M. Schultz
Algorithms or Hardware?

The N-Body Problem:

in 30 years
$10^7$ hardware
$10^{10}$ software

Source: T. Quinn
Algorithm: definition

Procedure to accomplish a task or solve a well-specified problem

Well-specified: know what all possible inputs look like and what output looks like given them

“accomplish” via simple, well-defined steps

Ex: sorting names (via comparison)

Ex: checking for primality (via +, -, *, /, ≤)
Goals

Correctness
  often subtle
Analysis
  often subtle
Generality, Simplicity, ‘Elegance’
Efficiency
  time, memory, network bandwidth, …
Algorithms: a sample problem

Printed circuit-board company has a robot arm that solders components to the board.

Time: proportional to total distance the arm must move from initial rest position around the board and back to the initial position.

For each board design, find best order to do the soldering.
Printed Circuit Board
Printed Circuit Board
A Well-defined Problem

Input: Given a set $S$ of $n$ points in the plane
Output: The shortest cycle tour that visits each point in the set $S$ once.

Better known as “TSP”

How might you solve it?
Nearest Neighbor Heuristic

Start at some point $p_0$
Walk first to its nearest neighbor $p_1$
Repeatedly walk to the nearest unvisited neighbor $p_2$, then $p_3$, ... until all points have been visited
Then walk back to $p_0$

**heuristic:**
A rule of thumb, simplification, or educated guess that reduces or limits the search for solutions in domains that are difficult and poorly understood. May be good, but usually not guaranteed to give the best or fastest solution.
Nearest Neighbor Heuristic
An input where NN works badly

length ~ 84
An input where NN works badly

optimal soln for this example
length = 63.8
Revised idea - Closest pairs first

Repeatedly join the closest pair of points (s.t. result can still be part of a single loop in the end. I.e., join endpoints, but not points in middle, of path segments already created.)

How does this work on our bad example?
Another bad example
Another bad example

\[6 + \sqrt{10} = 9.16\]

vs

8
Something that works

“Brute Force Search”: For each of the $n! = n(n-1)(n-2)\ldots 1$ orderings of the points, check the length of the cycle you get. Keep the best one.
Two Notes

The two incorrect algorithms were “greedy”

Often very natural & tempting ideas
They make choices that look great “locally” (and never reconsider them)
When greed works, the algorithms are typically efficient
BUT: often does not work - you get boxed in

Our correct alg avoids this, but is incredibly slow

20! is so large that checking one billion orderings per second would take 2.4 billion seconds (around 70 years!)
And growing: \( n! \sim \sqrt{2 \pi n} \cdot (n/e)^n \sim 2^{O(n \log n)} \)
The Morals of the Story

Algorithms are important
   Many performance gains outstrip Moore’s law
Simple problems can be hard
   Factoring, TSP
Simple ideas don’t always work
   Nearest neighbor, closest pair heuristics
Simple algorithms can be very slow
   Brute-force factoring, TSP
For some problems, even the best algorithms are slow

Course Goals:
   formalize these ideas, and
   develop more sophisticated approaches