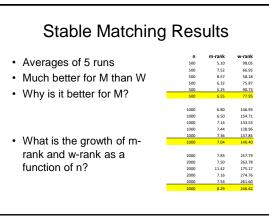
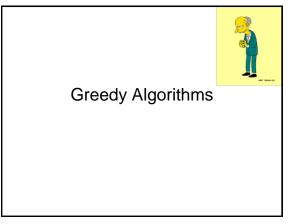
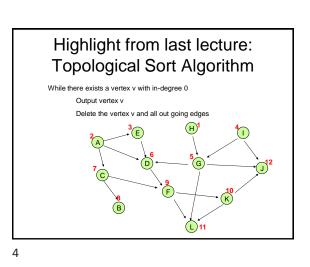


2

1







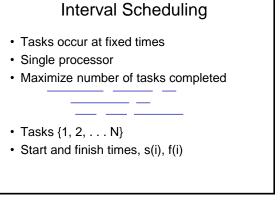


- Solve problems with the simplest possible algorithm
- The hard part: showing that something simple actually works
- · Pseudo-definition
 - An algorithm is Greedy if it builds its solution by adding elements one at a time using a simple rule

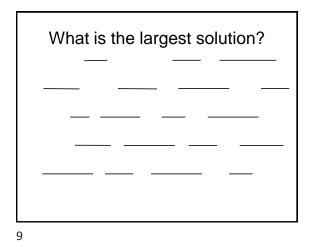
Scheduling Theory

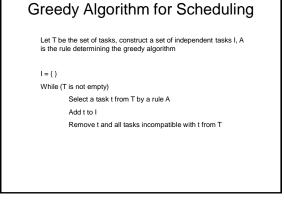
- Tasks
 - Processing requirements, release times, deadlines
- Processors
- Precedence constraints
- Objective function
 Jobs scheduled, lateness, total execution time

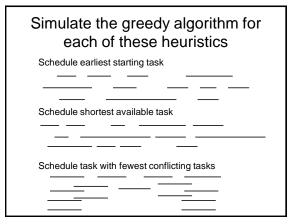


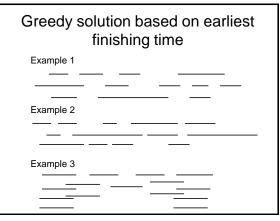


8









Theorem: Earliest Finish Algorithm is Optimal

- Key idea: Earliest Finish Algorithm stays ahead
- Let A = {i₁, ..., i_k} be the set of tasks found by EFA in increasing order of finish times
- Let $B = \{j_1, \ldots, j_m\}$ be the set of tasks found by a different algorithm in increasing order of finish times
- Show that for r<= min(k, m), f(i_r) <= f(j_r)

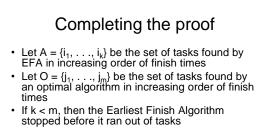
13

Stay ahead lemma

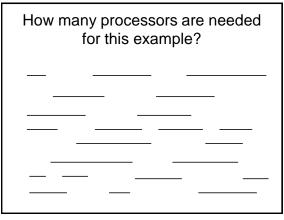
- A always stays ahead of B, $f(i_r) \le f(j_r)$
- Induction argument

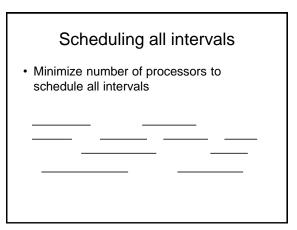
 f(i₁) <= f(j₁)
 f(i₁) <= f(j₁)
 - $\text{ If } f(i_{r\text{-}1}) <= f(j_{r\text{-}1}) \text{ then } f(i_r) <= f(j_r)$

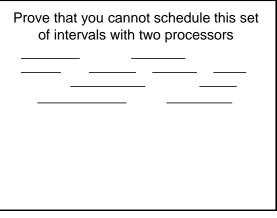
14

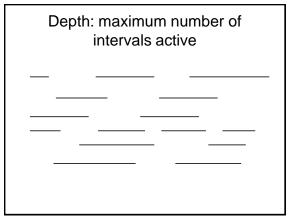


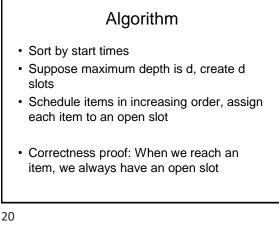


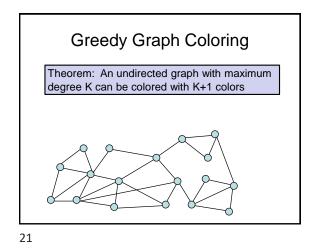


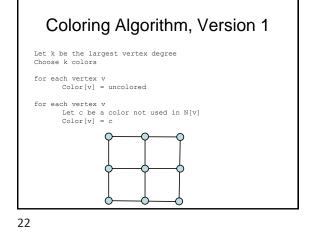


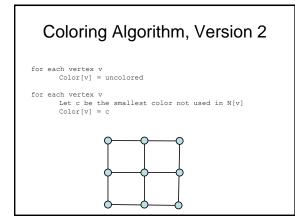


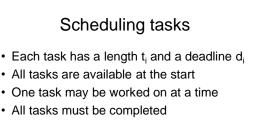












Goal minimize maximum lateness
 Lateness = f_i - d_i if f_i >= d_i

		Example	
	Time	Deadline	
	2	2	
	3	4	
	2	3 Lateness 1	
	3	2 Lateness 3	
25			

Determi	e the minimum lateness
Time	Deadline
2	6
3	4
4	5
5	12