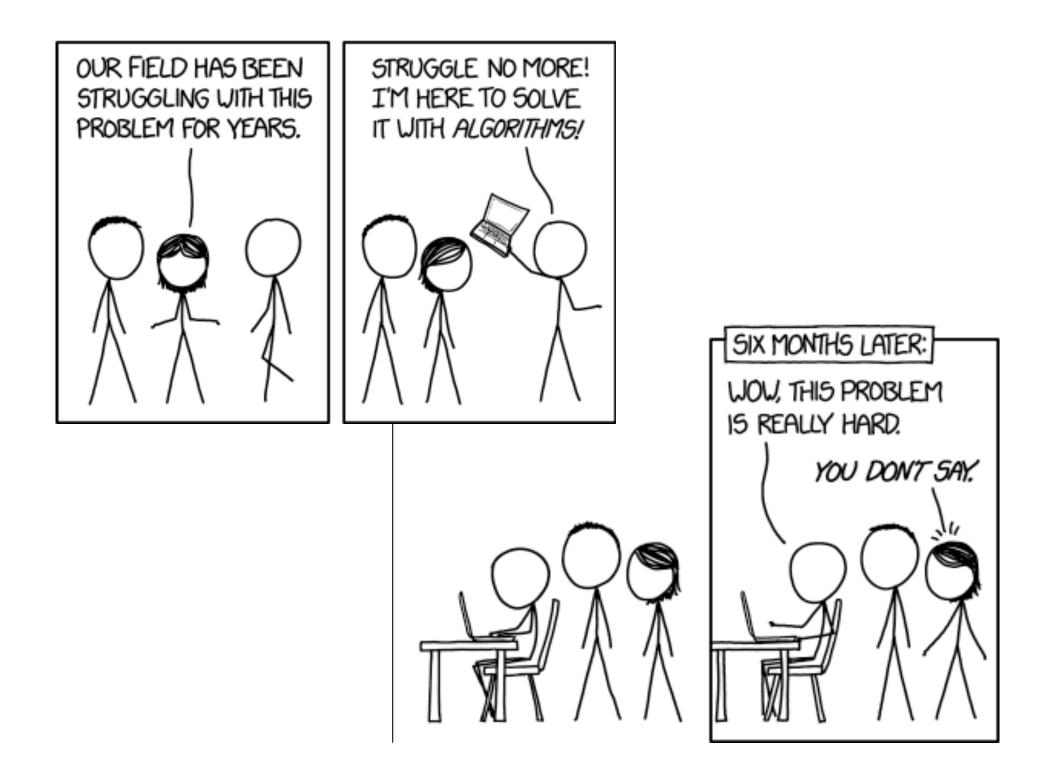
#### **Final Review**



## Final Exam Coverage

Comprehensive, all topics covered (but with post-midterm bias) assigned reading slides homework & solutions midterm review slides still relevant, plus those below

# **Design Paradigms**

Greedy

emphasis on correctness arguments, e.g. stay ahead, structural characterizations, exchange arguments

#### Divide & Conquer

recursive solution, superlinear work, balanced subproblems, recurrence relations, solutions, Master Theorem

#### **Dynamic Programming**

recursive solution, redundant subproblems, few do all in careful order and tabulate; <u>OPT table</u> (usually far superior to "memoization")

## Examples

Dynamic programming Fibonacci Making change/Stamps Knapsack Weighted Interval Scheduling RNA String Alignment



# Complexity, II

#### P vs NP

Big-O and poly vs exponential growth

Definition of NP – hints/certificates and verifiers

Example problems from slides, reading & hw

SAT, VertexCover, clique, independent set, TSP, Hamilton cycle, coloring, max cut, ...

 $P \subseteq NP \subseteq Exp$  (and worse)

Reduction, incl. definition of (polynomial time) reduction

 $\begin{array}{l} \mathsf{SAT} \leq_p \mathsf{Independent} \; \mathsf{Set} \; \mathsf{example} \\ \mathsf{SAT} \leq_p \mathsf{Knapsack} \; \mathsf{example} \end{array} \begin{array}{l} \mathsf{how, why \; correct,} \\ \mathsf{why} \leq_p, \mathsf{implications} \end{array}$ 

**Definition of NP-completeness** 

2x approximation to Euclidean TSP

And see how relevant it is to your daily life! Classic Nintendo Games are (NP-)Hard

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Abstract

We prove NP-hardness results for five of Nintendo's largest video game franchises: Mario, Donkey Kong, Legend of Zelda, Metroid, and Pokémon. Our results apply to Super Mario Bros. 1, 3, Lost Levels, and Super Mario World; Donkey Kong Country 1– 3; all Legend of Zelda games except Zelda II: The Adventure of Link; all Metroid games; and all Pokémon role-playing games. For Mario and Donkey Kong, we show NP-completeness. In addition, we observe that several games in the Zelda series are **PSPACE-complete**. 15

#### **Final Exam Mechanics**

Closed book, 1 pg notes (8.5x11, 2 sides, handwritten)

(no bluebook needed; scratch paper may be handy; calculators probably unnecessary)

Comprehensive: All topics covered

assigned reading

slides

homework & solutions

# Some Typical Exam Questions

Give O() bound on 17n\*(n-3+logn)

Give O() bound on some code {for i=1 to n {for j ...} True/False: If X is O(n<sup>2</sup>), then it's rarely more than n<sup>3</sup> + 14 steps.

Explain why a given greedy alg is/isn't correct

Give a run time recurrence for a recursive alg, or solve a simple one

Convert a simple recursive alg to a dynamic programming solution Simulate any of the algs we've studied

Give an alg for problem X, maybe a variant of one we've studied, or prove it's in NP

Understand parts of correctness proof for an algorithm or reduction Implications of NP-completeness



### Good Luck!

And please take a minute to fill out the online course evaluation: https://uw.iasystem.org/survey/205848