• Please read all instructions (including these) carefully.
• This is a closed-book exam. You are allowed a one-page handwritten cheat sheet.
• Write your name and UW student number below.
• No electronic devices are allowed, including cell phones used merely as watches. Silence your cell phones and place them in your bag.
• Solutions will be graded on correctness and clarity. Each problem has a relatively simple and straightforward solution. Partial solutions will be graded for partial credit.
• There are 6 pages in this exam, not including this one.
• There are 3 questions, each with multiple parts. If you get stuck on a question move on and come back to it later.
• You have 50 minutes to work on the exam.
• Please write your answers in the space provided on the exam, and clearly mark your solutions. You may use the last blank page as scratch paper. Do not use any additional scratch paper. Good luck!

By writing your name below, you certify that you have not received any unpermitted aid for this exam, and that you will not disclose the contents of the exam to anyone in the class who has not taken it.

NAME: _______________________

STUDENT NUMBER: ___________________________

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Problem 1: Warm up (10 points total)

Select either True or False for each of the following questions. For each question you get 1 point for answering it correctly, -0.5 point for an incorrect answer, and 0 point for no answer. The minimum you will get for this entire problem is 0.

a) The arity of the relation R(A int, B int) with tuples (4,2), (2,2), (4,2), (3,3), (4,2) is 3.  
   True   False

b) Data is encoded in JSon documents using key-value pairs.  
   True   False

c) A relation can have a clustered index on a set of attributes.  
   True   False

d) A datalog rule is safe if and only if every variable appears in a relational atom.  
   True   False

e) A SQL query with GROUP BY can select all attributes that are grouped on, joined upon, or are aggregates.  
   True   False

f) Every natural join can be rewritten using cross product and selection. 
   True   False

g) A foreign key does not have to reference a primary key.  
   True   False

h) An inner join between relations R and S always includes all tuples from R in the result.  
   True   False

i) Queries with universal quantifiers cannot be unnested.  
   True   False

j) A subquery in the SELECT clause in SQL can refer to tuple variables defined in the WHERE clause. 
   True   False
Problem 2: Writing Queries (52 points total)

Write the following queries using the schema below:
Product (pid, name, cid) -- cid is foreign key to Company.cid
Company (cid, cname, city)
Purchase(pid, custId, quantity, price)
-- pid is foreign key to Product.pid, custId is foreign key to Customer.custId
Customer(custId, name, city)

a) Write a SQL query that returns the name of companies, along with the number of products sold, for companies that have sold at least 2 different types of products anywhere. (13 points)

b) Write a relational algebra query that returns the distinct names of all customers from Seattle who purchased any one type of product with quantity > 10. Write your query as a tree or a single relational algebra expression. (13 points)
Schema repeated here for your reference:
Product (pid, name, cid) -- cid is foreign key to Company.cid
Company (cid, cname, city)
Purchase(pid, custId, quantity, price)
-- pid is foreign key to Product.pid, custId is foreign key to Customer.custId
Customer(custId, name, city)

c) Write a domain-independent relational calculus query that returns the CIDs of all companies where all of their products have been sold at least once. (13 points)

d) Write a safe Datalog+negation program that returns the PIDs of the products that have never been sold, along with the names of the companies that made them. Label your answer relation Ans. (13 points)
Problem 3: Short Questions (38 points total)

For the following schema:

Purchase(pid, custId, quantity, price)
-- pid is foreign key to Product.pid, custId is foreign key to Customer.custId
Customer(custId, name, city)

With statistics:

T(Purchase) = 1000
B(Purchase) = 100
V(Purchase, price) = 100, ranging from 0 to 200, with all values equally likely

T(Customer) = 3000
B(Customer) = 200
V(Customer, custId) = 50

Number of memory pages available = 20

a) (6 points) Given this query:

```
SELECT *
FROM Purchase p, Customer c
WHERE p.custId = c.custId AND p.price < 100 AND c.custId = 42
```

Indicate if each of the indexes below can help speeding up query execution, assuming that it is the only index available. For each below you get 1 point for answering it correctly, -0.5 point for an incorrect answer, and 0 point for no answer. The minimum you will get for this problem is 0.

1) Hashtable index on Purchase(price)  Yes  No
2) B-tree index on Purchase(pid, price) Yes  No
3) Hashtable index on Customer(custId) Yes  No
4) Hashtable index on Purchase(custId) Yes  No
5) B-tree index on Purchase(price, pid) Yes  No
6) Hashtable index on Purchase(price, pid) Yes  No
b) Which join algorithm would you use to execute the join in a) to minimize execution time? Assume that there are no indexes available. Be clear about how the join will be executed, i.e., what attribute will you sort on if sorting is involved, what relation will you construct a hashtable on if one is needed, etc. Briefly explain why. (8 points)

c) Are these two queries semantically equivalent?

Query 1: SELECT COUNT(*) FROM A
            WHERE A.a IN (SELECT x FROM B WHERE B.c = A.b)

Query 2: SELECT COUNT(*) FROM A, B
            WHERE A.a = B.x AND B.c = A.b

If equivalent, write “equivalent” below. If not, write “not equivalent,” and describe the contents of A and B such that the two queries output different results. (8 points)
d) Describe two differences between how relational and semi-structured data models manage data instances. (8 points)


e) Would using an unclustered index ever perform worse than a sequential scan on the same table? If yes, describe a scenario for which it is true, otherwise write “no” below. (8 points)