# CSE 413 Programming Languages & Implementation

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Context-Free Grammars and Parsing

### The Plan

- Parsing overview
- Context free grammars
- Grammar problems ambiguity

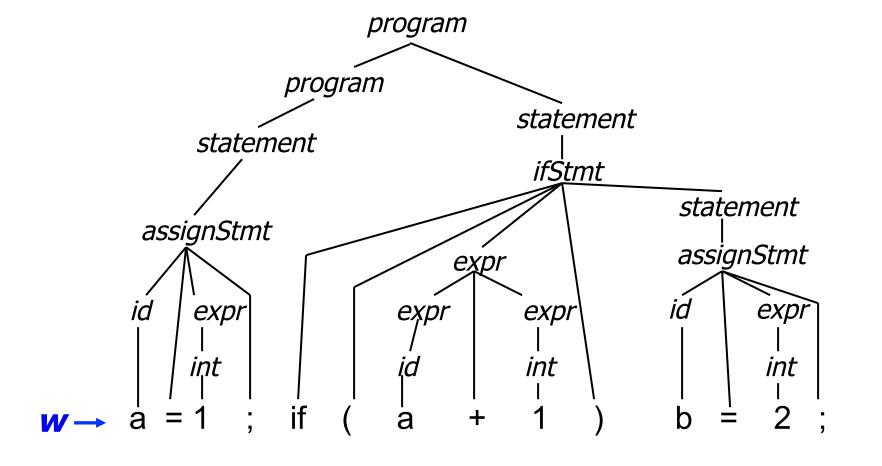
### Parsing

- The syntax of most programming languages can be specified by a context-free grammar (CGF)
  - A grammar allowing recursive rules (A ::= ... A ...)
- Parsing: Given a grammar G and a sentence w in L(G), traverse the derivation (parse tree) for w in some standard order and do something useful at each node
  - The tree might not be produced explicitly, but the control flow of a parser corresponds to a traversal

### Old Example

G

```
program ::= statement | program statement
statement ::= assignStmt | ifStmt
assignStmt ::= id = expr;
ifStmt ::= if ( expr ) statement
expr ::= id | int | expr + expr
id ::= a | b | c | i | j | k | n | x | y | z
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```



### "Standard Order"

- For practical reasons we want the parser to be deterministic (no backtracking), and we want to examine the source program from left to right.
  - (i.e., parse the program in linear time in the order it appears in the source file)

### Common Orderings

- Top-down
  - Start with the root
  - Traverse the parse tree depth-first, left-to-right (leftmost derivation)
  - LL(k), recursive-descent
- Bottom-up
  - Start at leaves and build up to the root
    - Effectively a rightmost derivation in reverse(!)
  - LR(k) and subsets (LALR(k), SLR(k), etc.)

### "Something Useful"

- At each point (node) in the traversal, perform some semantic action
  - Construct nodes of full parse tree (rare)
  - Construct abstract syntax tree (common)
  - Construct linear, lower-level representation (more common in later parts of a modern compiler)
  - Generate target code or interpret on the fly (1-pass compilers & interpreters; not common in production compilers – but works for our project)

### Context-Free Grammars (review)

- Formally, a grammar G is a tuple <N,Σ,P,S> where:
  - N a finite set of non-terminal symbols
  - $-\Sigma$  a finite set of terminal symbols
  - P a finite set of productions
    - A subset of  $N \times (N \cup \Sigma)^*$
  - S the start symbol, a distinguished element of N
    - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

### **Standard Notations**

- a, b, c elements of Σ
- w, x, y, z elements of  $\Sigma^*$
- A, B, C elements of N
- X, Y, Z elements of  $N \cup \Sigma$
- $\alpha$ ,  $\beta$ ,  $\gamma$  elements of  $(N \cup \Sigma)^*$
- $A\rightarrow \alpha$  or  $A := \alpha$  if A,  $\alpha > in P$

### Derivation Relations (1)

- $\alpha A \gamma => \alpha \beta \gamma$  iff  $A := \beta$  in P
  - derives
- A =>\* w if there is a chain of productions starting with A that generates w
  - transitive closure

### Derivation Relations (2)

- $W A \gamma =>_{lm} W \beta \gamma$  iff  $A ::= \beta$  in P
  - derives leftmost
- $\alpha A w =>_{rm} \alpha \beta w$  iff  $A ::= \beta$  in P
  - derives rightmost
- Parsers normally deal with only leftmost or rightmost derivations – not random orderings

### Languages

- For A in N,  $L(A) = \{ w \mid A = >^* w \}$ 
  - i.e., set of strings (words, terminal symbols)
     generated by nonterminal A
- If S is the start symbol of grammar G, we define L(G) = L(S)

### Reduced Grammars

Grammar G is reduced iff for every production
 A ::= α in G there is some derivation

$$S =>^* x A z => x \alpha z =>^* xyz$$

- i.e., no production is useless
- Convention: we will use only reduced grammars

### Example

```
program ::= statement | program statement
statement ::= assignStmt | ifStmt
assignStmt ::= id = expr;
ifStmt ::= if ( expr ) stmt
expr ::= id | int | expr + expr
id ::= a | b | c | i | j | k | n | x | y | z
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

Top down, Leftmost derivation for: a = 1 + b;

### Example

Grammar

S ::= a*AB*e

 $A := Abc \mid b$ 

B := d

 Top down, leftmost derivation of: abbcde

### **Ambiguity**

- Grammar G is unambiguous iff every w in L(G) has a unique leftmost (or rightmost) derivation
  - Fact: either unique leftmost or unique rightmost implies the other
- A grammar without this property is ambiguous
  - Other grammars that generate the same language might be unambiguous
- We need unambiguous grammars for parsing

## Example: Ambiguous Grammar for Arithmetic Expressions

```
expr ::= expr + expr | expr - expr
| expr * expr | expr / expr | int
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

- Exercise: show that this is ambiguous
  - How? Show two different leftmost or rightmost derivations for the same string
  - Equivalently: show two different parse trees for the same string

expr ::= 
$$expr + expr | expr - expr$$
  
 $| expr * expr | expr | expr | int$   
 $int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9$ 

Give a leftmost derivation of 2+3\*4 and show the parse tree

expr ::= 
$$expr + expr | expr - expr$$
  
 $| expr^* expr | expr | expr | int$   
 $| expr^* expr | expr | expr | int$   
 $| expr^* expr | expr | expr | expr | int$ 

Give a different leftmost derivation of 2+3\*4 and show the parse tree

Give two different derivations of 5+6+7

### What's going on here?

- This grammar has no notion of precedence or associatively
- Standard solution
  - Create a non-terminal for each level of precedence
  - Isolate the corresponding part of the grammar
  - Force the parser to recognize higher precedence subexpressions first

### Classic Expression Grammar

```
expr ::= expr + term | expr - term | term
term ::= term * factor | term / factor | factor
factor ::= int | ( expr )
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7
```

### Check: Derive 2+3\*4

```
expr ::= expr + term | expr - term | term
term ::= term * factor | term / factor | factor
factor ::= int | (expr)
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7
```

### Check: Derive 5+6+7

```
expr ::= expr + term | expr - term | term
term ::= term * factor | term / factor | factor
factor ::= int | ( expr )
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7
```

 Note interaction between left- vs right-recursive rules and resulting associativity

### Check: Derive 5+(6+7)

```
expr ::= expr + term | expr - term | term
term ::= term * factor | term / factor | factor
factor ::= int | ( expr )
int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7
```

### **Another Classic Example**

Grammar for conditional statements

- Exercise: show that this is ambiguous
  - How?

### **One Derivation**

```
if ( cond ) if ( cond ) stmt else stmt
```

```
stmt ::= if ( cond ) stmt
| if ( cond ) stmt else stmt
Another Derivation | assign
```

if ( cond ) if ( cond ) stmt else stmt

### Solving if Ambiguity

- Fix the grammar to separate if statements with else from if statements with no else
  - Done in original Java reference grammar
  - Adds lots of non-terminals
    - Need productions for things like "while statement that contains an unmatched if" and "while statement with only matched ifs", etc. etc. etc.
- Use some ad-hoc rule in parser
  - "else matches closest unpaired if"

### Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
  - Makes life simpler if used with discipline
- Typically one can specify operator precedence & associativity
  - Allows simpler, ambiguous grammar with fewer nonterminals as basis for generated parser, without creating problems

### Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems
  - Earlier productions in the grammar preferred to later ones
  - Longest match used if there is a choice
- Parser tools normally allow for this
  - But be sure that what the tool does is really what you want
    - (Order in the input is particularly error-prone reordering the input lines can change the meaning! (3)

### Or...

• If the parser is hand-written, either fudge the grammar or the parser, or cheat where it helps.

to be continued...