CSE 413 Programming Languages & Implementation

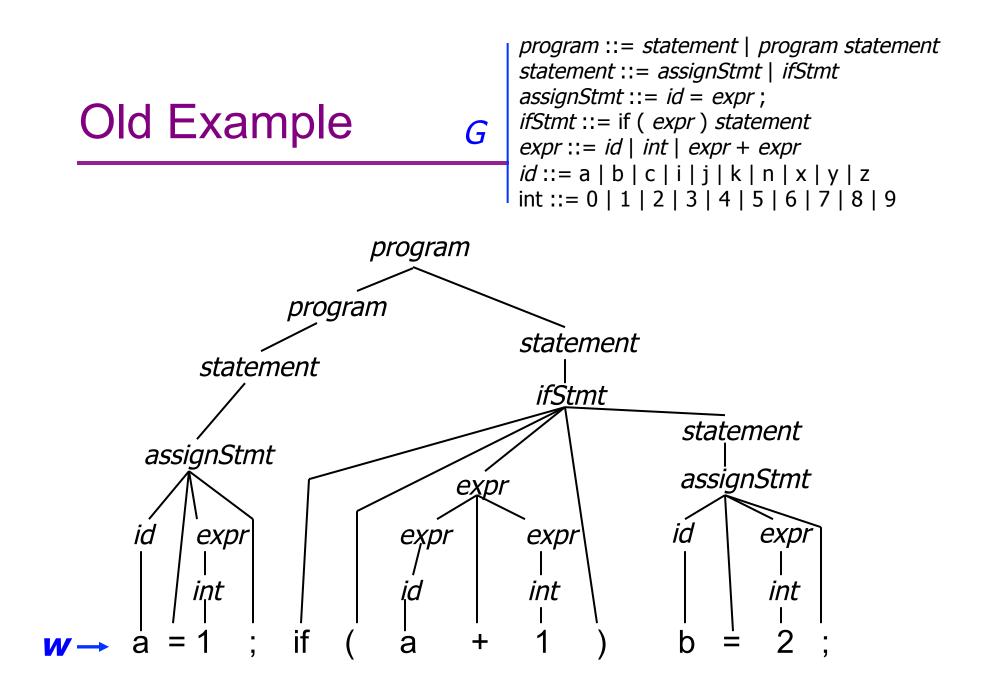
Hal Perkins Autumn 2014 Context-Free Grammars and Parsing

The Plan

- Parsing overview
- Context free grammars
- Grammar problems ambiguity

Parsing

- The syntax of most programming languages can be specified by a *context-free grammar* (CGF)
 - A grammar allowing recursive rules (A ::= ... A ...)
- Parsing: Given a grammar G and a sentence w in L(G), traverse the derivation (parse tree) for w in some standard order and do something useful at each node
 - The tree might not be produced explicitly, but the control flow of a parser corresponds to a traversal



"Standard Order"

- For practical reasons we want the parser to be *deterministic* (no backtracking), and we want to examine the source program from *left to right*.
 - (i.e., parse the program in linear time in the order it appears in the source file)

Common Orderings

- Top-down
 - Start with the root
 - Traverse the parse tree depth-first, left-to-right (leftmost derivation)
 - LL(k), recursive-descent
- Bottom-up
 - Start at leaves and build up to the root
 - Effectively a rightmost derivation in reverse(!)
 - LR(k) and subsets (LALR(k), SLR(k), etc.)

"Something Useful"

- At each point (node) in the traversal, perform some semantic action
 - Construct nodes of full parse tree (rare)
 - Construct abstract syntax tree (common)
 - Construct linear, lower-level representation (more common in later parts of a modern compiler)
 - Generate target code or interpret on the fly (1-pass compilers & interpreters; not common in production compilers – but works for our project)

Context-Free Grammars (review)

- Formally, a grammar G is a tuple <N,Σ,P,S> where:
 - *N* a finite set of non-terminal symbols
 - $-\Sigma$ a finite set of terminal symbols
 - -P a finite set of productions
 - A subset of $N \times (N \cup \Sigma)^*$
 - S the start symbol, a distinguished element of N
 - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

Standard Notations

- a, b, c elements of Σ
- w, x, y, z elements of Σ^*
- A, B, C elements of N
- X, Y, Z elements of $N \cup \Sigma$
- α , β , γ elements of ($N \cup \Sigma$)*
- $A \rightarrow \alpha$ or $A ::= \alpha$ if $\langle A, \alpha \rangle$ in *P*

Derivation Relations (1)

- $\alpha \land \gamma \Rightarrow \alpha \land \gamma$ iff $A ::= \beta in P$ - derives
- A =>* w if there is a *chain* of productions starting with A that generates w
 - transitive closure

Derivation Relations (2)

- w A $\gamma =>_{Im} w \beta \gamma$ iff A ::= β in P - derives leftmost
- $\alpha A w = \sum_{rm} \alpha \beta w$ iff $A ::= \beta$ in *P* - derives rightmost
- Parsers normally deal with only leftmost or rightmost derivations not random orderings

Languages

- For A in N, L(A) = { w | A =>* w }
 - i.e., set of strings (words, terminal symbols) generated by nonterminal A
- If S is the start symbol of grammar G, we define
 L(G) = L(S)

Reduced Grammars

• Grammar G is *reduced* iff for every production A ::= α in G there is some derivation

 $S =>^* x A z => x \alpha z =>^* xyz$

– i.e., no production is useless

• Convention: we will use only reduced grammars

	program ::= statement program statement
	statement ::= assignStmt ifStmt
Example	assignStmt ::= id = expr ;
	<i>ifStmt</i> ::= if (<i>expr</i>) <i>stmt</i>
	expr ::= id int expr + expr
	<i>id</i> ::= a b c i j k n x y z
	int ::= 0 1 2 3 4 5 6 7 8 9

Top down, Leftmost derivation for: a = 1 + b;

Example

- Grammar
 - S ::= aABe A ::= Abc | b B ::= d

• Top down, leftmost derivation of: abbcde

Ambiguity

- Grammar G is unambiguous iff every w in L(G) has a unique leftmost (or rightmost) derivation
 - Fact: either unique leftmost or unique rightmost implies the other
- A grammar without this property is *ambiguous*
 - Other grammars that generate the same language may be unambiguous
- We need unambiguous grammars for parsing

Example: Ambiguous Grammar for Arithmetic Expressions

expr ::= expr + expr | expr - expr | expr * expr | expr / expr | int int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

- Exercise: show that this is ambiguous
 - How? Show two different leftmost or rightmost derivations for the same string
 - Equivalently: show two different parse trees for the same string

 expr ::= expr + expr | expr - expr
 | expr * expr | expr / expr | int

 Image: Example (cont)
 int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a leftmost derivation of 2+3*4 and show the parse tree

 expr ::= expr + expr | expr - expr
 | expr * expr | expr / expr | int

 Image: Example (cont)
 int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

 Give a different leftmost derivation of 2+3*4 and show the parse tree

 expr ::= expr + expr | expr - expr
 | expr * expr | expr / expr | int

 Another example
 int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

• Give two different derivations of 5+6+7

What's going on here?

- This grammar has no notion of precedence or associatively
- Standard solution
 - Create a non-terminal for each level of precedence
 - Isolate the corresponding part of the grammar
 - Force the parser to recognize higher precedence subexpressions first

Classic Expression Grammar

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check:	
Derive 2+3*4	

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

Check:	
Derive 5+6+7	

expr ::= expr + term | expr - term | term term ::= term * factor | term / factor | factor factor ::= int | (expr) int ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7

• Note interaction between left- vs right-recursive rules and resulting associativity

Check:	expr ::= expr + term expr – term term term ::= term * factor term / factor factor
Derive 5+(6+7)	factor ::= int (expr) int ::= 0 1 2 3 4 5 6 7

Another Classic Example

- Grammar for conditional statements stmt ::= if (cond) stmt

 if (cond) stmt else stmt

 assign
- Exercise: show that this is ambiguous
 How?

stmt ::= if (cond) stmt| if (cond) stmt else stmtOne Derivation| assign

if (cond) if (cond) stmt else stmt

stmt ::= if (cond) stmt| if (cond) stmt else stmtAnother Derivation| assign

if (cond) if (cond) stmt else stmt

Solving if Ambiguity

- Fix the grammar to separate if statements with else from if statements with no else
 - Done in original Java reference grammar
 - Adds lots of non-terminals
 - Need productions for things like "while statement that contains an unmatched if" and "while statement with only matched ifs", etc. etc. etc.
- Use some ad-hoc rule in parser
 - "else matches closest unpaired if"

Parser Tools and Operators

- Most parser tools can cope with ambiguous grammars
 - Makes life simpler if used with discipline
- Typically one can specify operator precedence & associativity
 - Allows simpler, ambiguous grammar with fewer nonterminals as basis for generated parser, without creating problems

Parser Tools and Ambiguous Grammars

- Possible rules for resolving other problems
 - Earlier productions in the grammar preferred to later ones
 - Longest match used if there is a choice
- Parser tools normally allow for this
 - But be sure that what the tool does is really what you want

Or...

• If the parser is hand-written, either fudge the grammar or the parser, or cheat where it helps.

to be continued...