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# Grammar

CSE 413, Autumn 2005  
Programming Languages

<http://www.cs.washington.edu/education/courses/413/05au/>

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# Recall: Programming Language Specs

- Syntax of every significant programming language is specified by a formal grammar
  - » BNF or some variation there on
- As language engineering has developed, formal methods have improved for defining useful grammars and tools for processing them

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# Recall: Productions

- The rules of a grammar are called *productions*
- Rules contain
  - » Nonterminal symbols: grammar variables (*program*, *statement*, *id*, etc.)
  - » Terminal symbols: concrete syntax that appears in programs: a, b, c, 0, 1, if, (, ...
- Meaning of
  - nonterminal* → <sequence of terminals and nonterminals>
  - In a derivation, an instance of *nonterminal* can be replaced by the sequence of terminals and nonterminals on the right of the production
- Often, there are two or more productions for a single nonterminal – can use either at different times

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# Grammar for fm, a little language

1. *program* → **movie** *name* { *movieBody* } **EOF**
2. *movieBody* → *prologBlock* *pageBlocks* | *pageBlocks*
3. *prologBlock* → **prolog** { *prologStatements* }
4. *prologStatements* → *prologStatement* | *prologStatements* *prologStatement*
5. *prologStatement* → *variableDeclaration*
11. *variableDeclaration* → *id* : *type*() ; | *id* : *type*(*exprList*) ;
12. *pageBlocks* → *pageBlock* | *pageBlocks* *pageBlock*
13. *pageBlock* → **show** ( *integer* ) { *pageStatements* }
14. *pageStatements* → *pageStatement* | *pageStatements* *pageStatement*
15. *pageStatement* → { *pageStatements* } | *methodCall* ; | *id* = *expr* ;  
| **if** (*boolExpr*) *pageStatement* | **if** (*boolExpr*) *pageStatement* **else** *pageStatement*
16. *expr* → *term* | *expr* + *term* | *expr* - *term*
17. *term* → *factor* | *term* \* *factor* | *term* / *factor*
18. *factor* → *integer* | *real* | ( *expr* ) | *id* | *methodCall*
19. *methodCall* → *id*() | *id*(*exprList*) | *id*.*id* ( ) | *id*.*id*(*exprList*)
20. *exprList* → *expr* | *exprList* , *expr*
21. *boolExpr* → *relExpr* | ! ( *relExpr* )
22. *relExpr* → *expr* == *expr* | *expr* > *expr* | *expr* < *expr*
23. *type* → *id*

## Grammar for Java, a big language

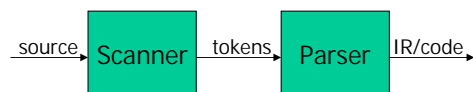
- The Java™ Language Specification, 2<sup>nd</sup> Edition
  - » *Entire document*
    - 500+ pages
    - Grammar productions with explanatory text
  - » *Chapter 18, Syntax*
    - 8 pages of grammar productions, presented in "BNF-style"

## Java grammar *extract*

```
Type:
  Identifier { . Identifier } BracketsOpt
  BasicType
StatementExpression:
  Expression
ConstantExpression:
  Expression
Expression1:
  Expression2 [Expression1Rest]
Expression1Rest:
  [ ? Expression : Expression1 ]
Expression2 :
  Expression3 [Expression2Rest]
Expression2Rest:
  { Infixop Expression3 }
  Expression3 instanceof Type
```

## Recall Parsing

- Parsing: reconstruct the derivation (syntactic structure) of a program)
- In principle, a single recognizer could work directly from the concrete, character-by-character grammar
- In real compilers the recognizer is split into two phases
  - » Scanner: translate input characters to tokens
  - » Parser: read token stream and reconstruct the derivation



## Parsing

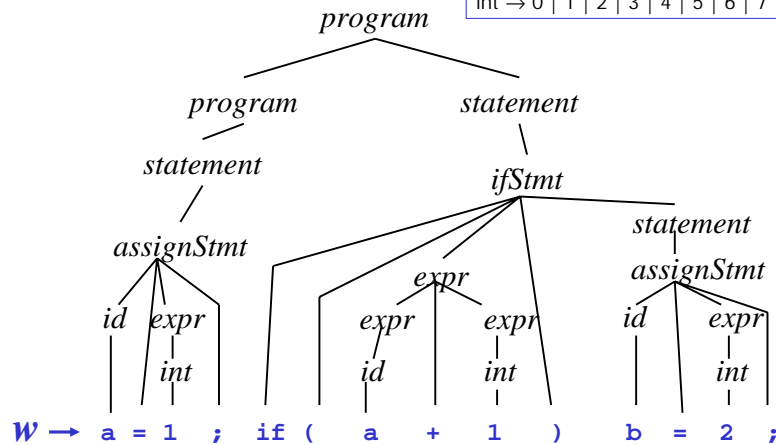
- The syntax of most programming languages can be specified by a *context-free grammar*
- Parsing
  - » Given a grammar  $G$  and a sentence  $w$  in  $L(G)$ , traverse the derivation (parse tree) for  $w$  in some *standard order* and do *something useful* at each node
  - » The tree might not be produced explicitly, but the control flow of a parser corresponds to a traversal

## Parse Tree Example

G

```

program → statement | program statement
statement → assignStmt | ifStmt
assignStmt → id = expr ;
ifStmt → if ( expr ) stmt
expr → id | int | expr + expr
Id → a | b | c | i | j | k | n | x | y | z
int → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
    
```



## “Standard Order”

- For practical reasons we want the parser to be *deterministic* (no backtracking), and we want to examine the source program from *left to right*.
  - » in other words, parse the program in linear time in the order it appears in the source file

## Common Orderings

- Top-down
  - » Start with the root
  - » Traverse the parse tree depth-first
- Bottom-up
  - » Start at leaves and build up to the root

## “Something Useful”

- At each point (node) in the traversal, perform some *semantic action*
  - » Construct nodes of full parse tree (rare)
  - » Construct abstract syntax tree (common)
  - » Construct linear, lower-level representation (more common in later parts of a modern compiler)
  - » Generate target code on the fly → 1-pass compiler
    - relatively simple to program by hand
    - not common in production compilers because can't generate very good code in one pass

## Context-Free Grammars

- Formally, a grammar  $G$  is a tuple  $\langle N, \Sigma, P, S \rangle$  where
  - »  $N$  a finite set of non-terminal symbols
  - »  $\Sigma$  a finite set of terminal symbols
  - »  $P$  a finite set of productions
    - A subset of  $N \times (N \cup \Sigma)^*$
  - »  $S$  the *start symbol*, a distinguished element of  $N$ 
    - If not specified otherwise, this is usually assumed to be the non-terminal on the left of the first production

## Standard Notations

$a, b, c$	elements of $\Sigma$	<i>terminals</i>
$w, x, y, z$	elements of $\Sigma^*$	<i>strings of terminals</i>
$A, B, C$	elements of $N$	<i>non-terminals</i>
$X, Y, Z$	elements of $N \cup \Sigma$	<i>grammar symbols</i>
$\alpha, \beta, \gamma$	elements of $(N \cup \Sigma)^*$	<i>strings of symbols</i>
$A \rightarrow \alpha$ (or $A ::= \alpha$ ) if $\langle A, \alpha \rangle$ in $P$		<i>productions</i>
	"non-terminal $A$ can take the form $\alpha$ "	

## Derivation Relations

- $\alpha A \gamma \Rightarrow \alpha \beta \gamma$  iff  $A \rightarrow \beta$  in  $P$ 
  - » " $\Rightarrow$ " is read "derives"
- $A \Rightarrow^* w$  if there is a chain of productions starting with  $A$  that generates  $w$ 
  - » "Non-terminal  $A$  derives the string of terminals  $w$ "
  - » You can get from  $A$  to  $w$  using a series of productions
    - for example, if  $S$  is the start symbol "program" and  $w$  is the actual source code, then  $S \Rightarrow^* w$  says that  $w$  is a valid program (ie, it compiles)

## Languages

- For  $A$  in  $N$ ,  $L(A) = \{ w \mid A \Rightarrow^* w \}$ 
  - » for any non-terminal  $A$  defined for a grammar, the language generated by  $A$  is the set of strings  $w$  that can be derived from  $A$  using the productions
- If  $S$  is the start symbol of grammar  $G$ , define  $L(G) = L(S)$ 
  - » The language derived by  $G$  is the language derived by the start symbol  $S$

## Reduced Grammars

- Grammar  $G$  is *reduced* iff for every production  $A \rightarrow \alpha$  in  $G$  there is a derivation  $S \Rightarrow^* x A z \Rightarrow x \alpha z \Rightarrow^* xyz$ 
  - » i.e., no production is useless
- Convention: we will use only reduced grammars

## Ambiguity

- Grammar  $G$  is *unambiguous* iff every  $w$  in  $L(G)$  has a unique derivation
- A grammar without this property is *ambiguous*
  - » Note that other grammars that generate the same language may be unambiguous
- We need unambiguous grammars for parsing

## Ambiguous Grammar for Expressions

$$\begin{aligned} \text{expr} &\rightarrow \text{expr} + \text{expr} \mid \text{expr} - \text{expr} \\ &\mid \text{expr} * \text{expr} \mid \text{expr} / \text{expr} \mid \text{int} \end{aligned}$$
$$\text{int} \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9$$

- Show that this is ambiguous
  - » How? Show two different derivations for the same string
  - » Equivalently: show two different parse trees for the same string

## Example Derivation

$$\begin{aligned} \text{expr} &\rightarrow \text{expr} + \text{expr} \mid \text{expr} - \text{expr} \\ &\mid \text{expr} * \text{expr} \mid \text{expr} / \text{expr} \mid \text{int} \\ \text{int} &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

Give a derivation of  $2+3*4$  and show the parse tree

## Another Derivation

$$\begin{aligned} \text{expr} &\rightarrow \text{expr} + \text{expr} \mid \text{expr} - \text{expr} \\ &\quad \mid \text{expr} * \text{expr} \mid \text{expr} / \text{expr} \mid \text{int} \\ \text{int} &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

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## Another Example

$$\begin{aligned} \text{expr} &\rightarrow \text{expr} + \text{expr} \mid \text{expr} - \text{expr} \\ &\quad \mid \text{expr} * \text{expr} \mid \text{expr} / \text{expr} \mid \text{int} \\ \text{int} &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \mid 8 \mid 9 \end{aligned}$$

Give two different derivations of  $5+6+7$

## What's going on here?

- The grammar has no notion of precedence or associativity
- Solution
  - » Create a non-terminal for each level of precedence
  - » Isolate the corresponding part of the grammar
  - » Force the parser to recognize higher precedence subexpressions first

## Classic Expression Grammar

$$\begin{aligned} \text{expr} &\rightarrow \text{expr} + \text{term} \mid \text{expr} - \text{term} \mid \text{term} \\ \text{term} &\rightarrow \text{term} * \text{factor} \mid \text{term} / \text{factor} \mid \text{factor} \\ \text{factor} &\rightarrow \text{int} \mid ( \text{expr} ) \\ \text{int} &\rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7 \end{aligned}$$

Derive  $2 + 3 * 4$

$expr \rightarrow expr + term \mid expr - term \mid term$   
 $term \rightarrow term * factor \mid term / factor \mid factor$   
 $factor \rightarrow int \mid ( expr )$   
 $int \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7$

Derive  $5 + 6 + 7$

$expr \rightarrow expr + term \mid expr - term \mid term$   
 $term \rightarrow term * factor \mid term / factor \mid factor$   
 $factor \rightarrow int \mid ( expr )$   
 $int \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7$

Derive  $5 + (6 + 7)$

$expr \rightarrow expr + term \mid expr - term \mid term$   
 $term \rightarrow term * factor \mid term / factor \mid factor$   
 $factor \rightarrow int \mid ( expr )$   
 $int \rightarrow 0 \mid 1 \mid 2 \mid 3 \mid 4 \mid 5 \mid 6 \mid 7$

## Another Classic Example

- Grammar for conditional statements

$ifStmt \rightarrow \mathbf{if} ( cond ) stmt$

$\mid \mathbf{if} ( cond ) stmt \mathbf{else} stmt$

» Exercise: show that this is ambiguous

- How?

## One Derivation

$$\begin{array}{l} \text{ifStmt} \rightarrow \text{if} ( \text{cond} ) \text{stmt} \\ \quad | \text{if} ( \text{cond} ) \text{stmt} \text{ else } \text{stmt} \end{array}$$

## Another Derivation

$$\begin{array}{l} \text{ifStmt} \rightarrow \text{if} ( \text{cond} ) \text{stmt} \\ \quad | \text{if} ( \text{cond} ) \text{stmt} \text{ else } \text{stmt} \end{array}$$

$\text{if} ( \text{cond} ) \text{ if} ( \text{cond} ) \text{ stmt} \text{ else } \text{stmt}$

$\text{if} ( \text{cond} ) \text{ if} ( \text{cond} ) \text{ stmt} \text{ else } \text{stmt}$

## Solving **if** Ambiguity

- Fix the grammar to separate if statements with else clause and if statements with no else
  - » Done in Java reference grammar
  - » Adds lots of non-terminals
- Use some ad-hoc rule in parser
  - » “else matches closest unpaired if”