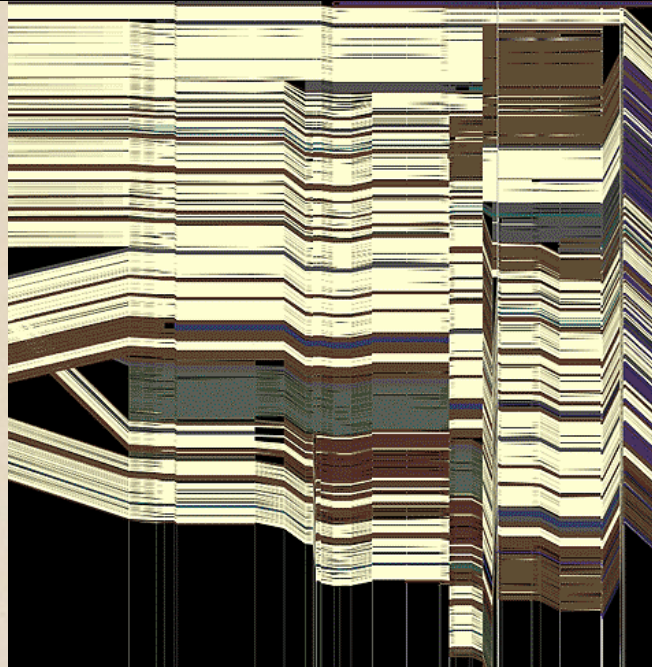
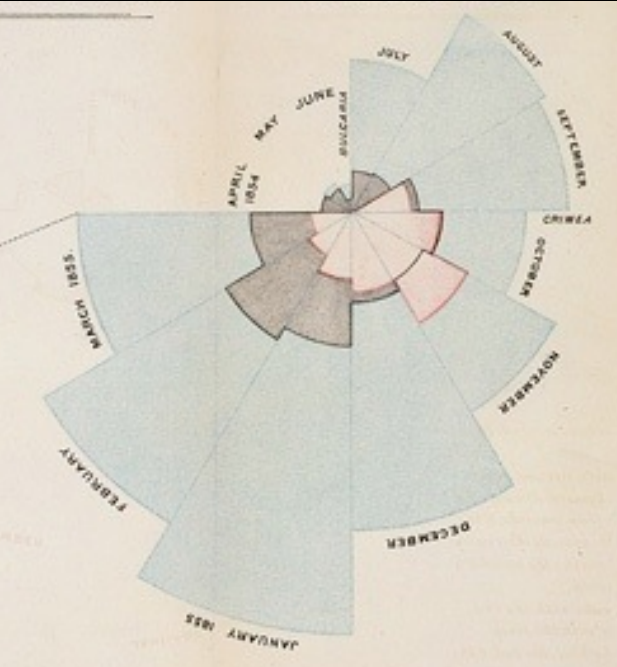


CSE 412 - Intro to Data Visualization

# Multidimensional Data

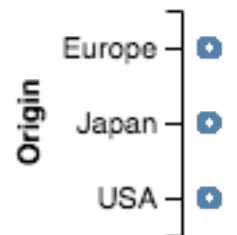


Jane Hoffswell University of Washington

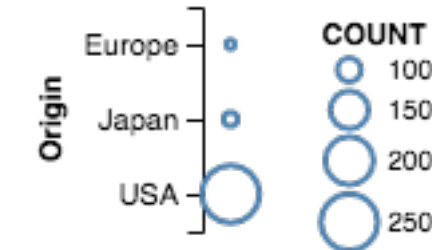
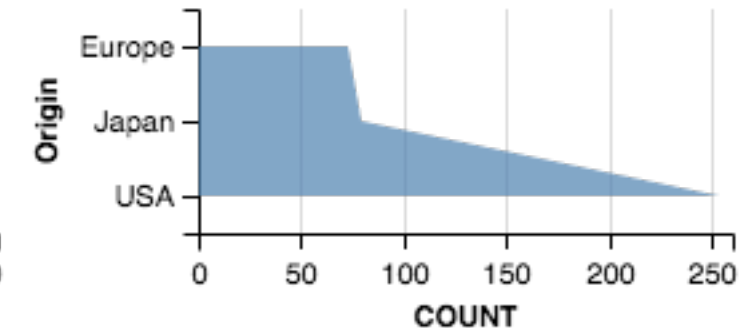
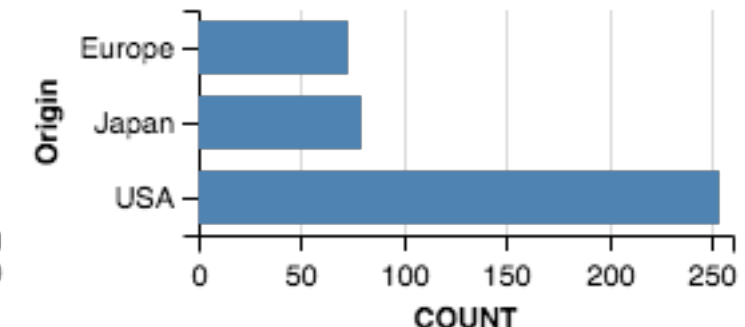
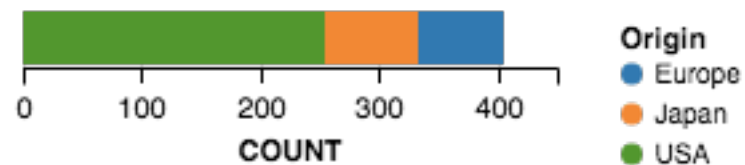
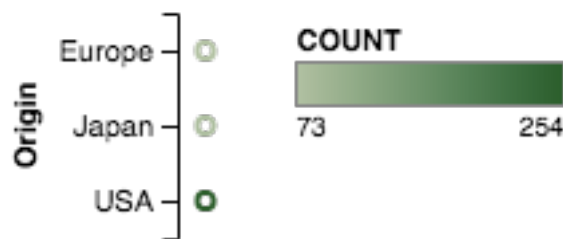
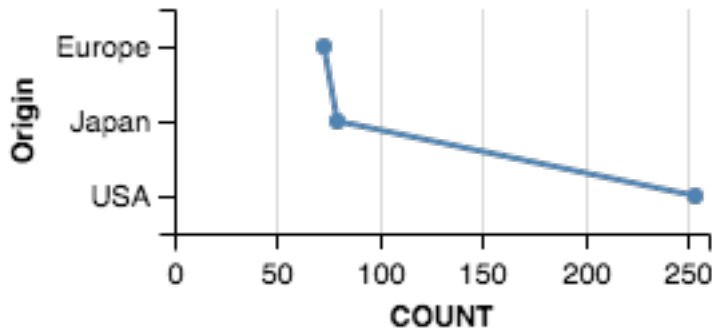
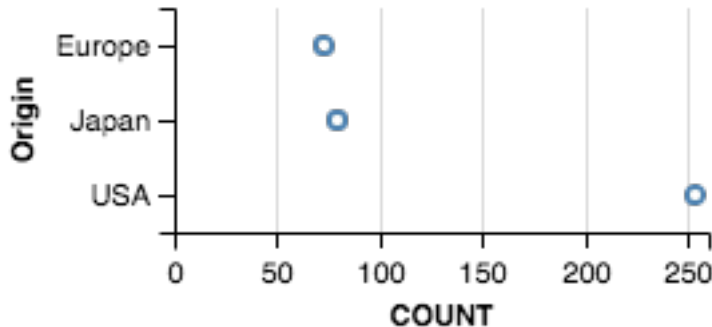
# A Design Space of Visual Encodings

# 1D: Nominal

Raw



Aggregate (Count)

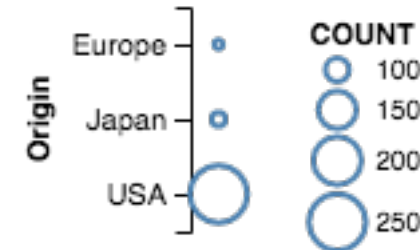
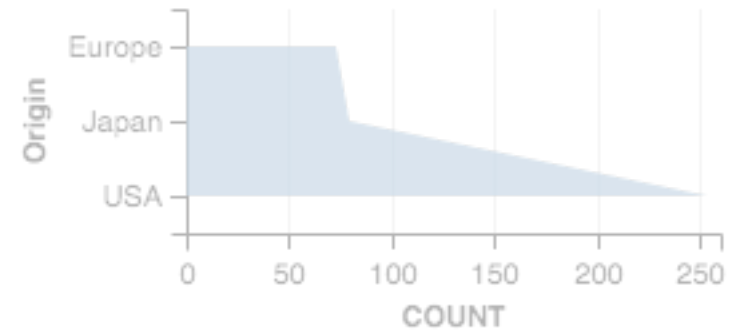
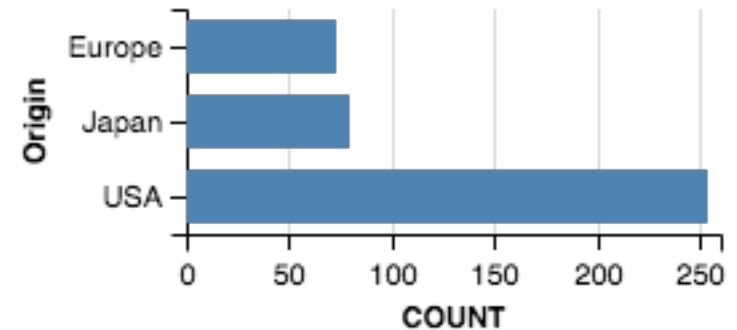
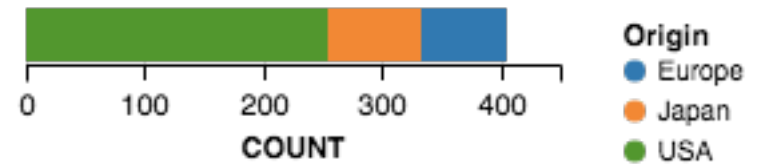
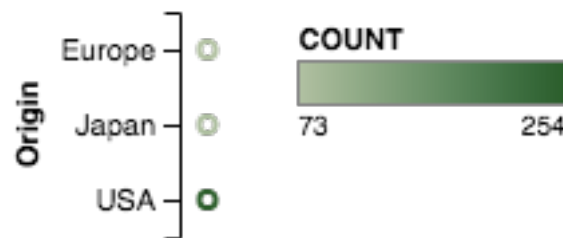
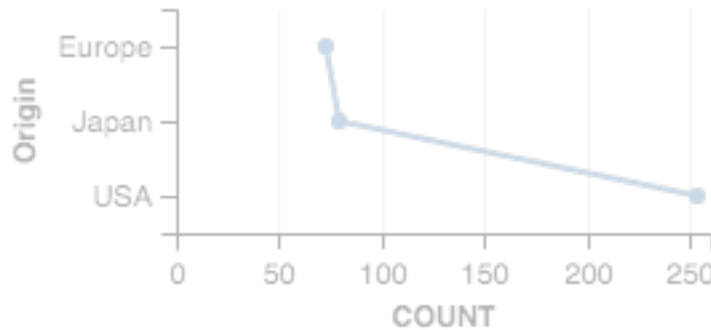
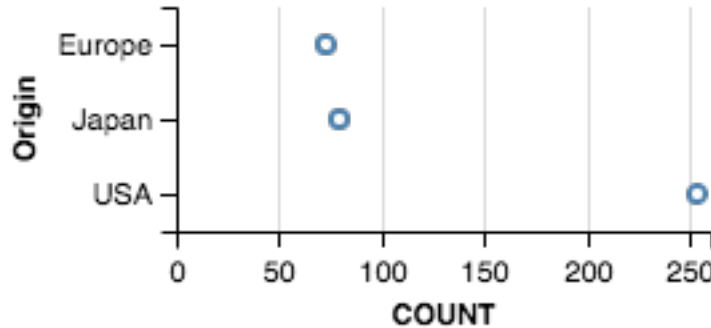


# 1D (N): Expressive?

Raw

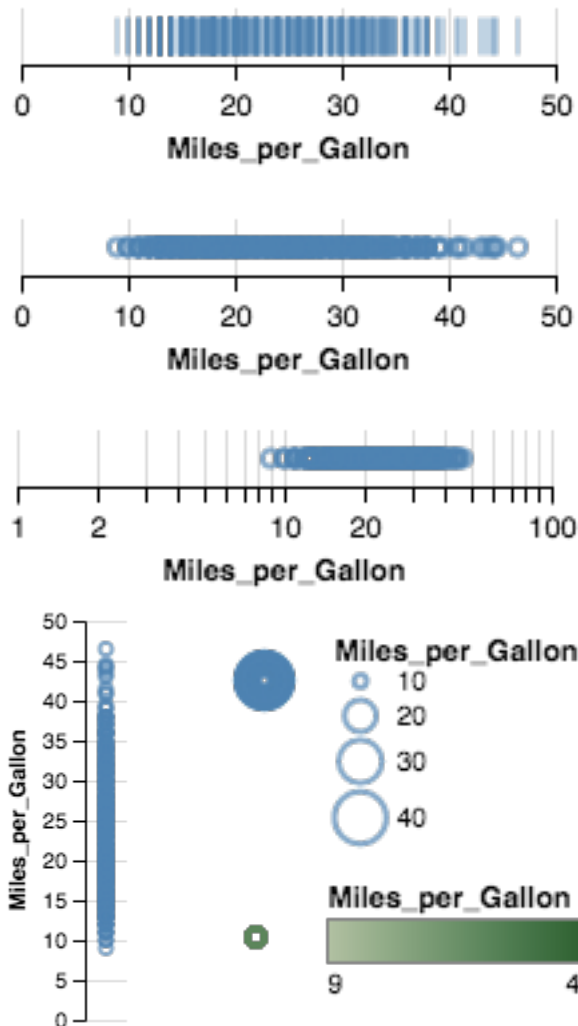


Aggregate (Count)

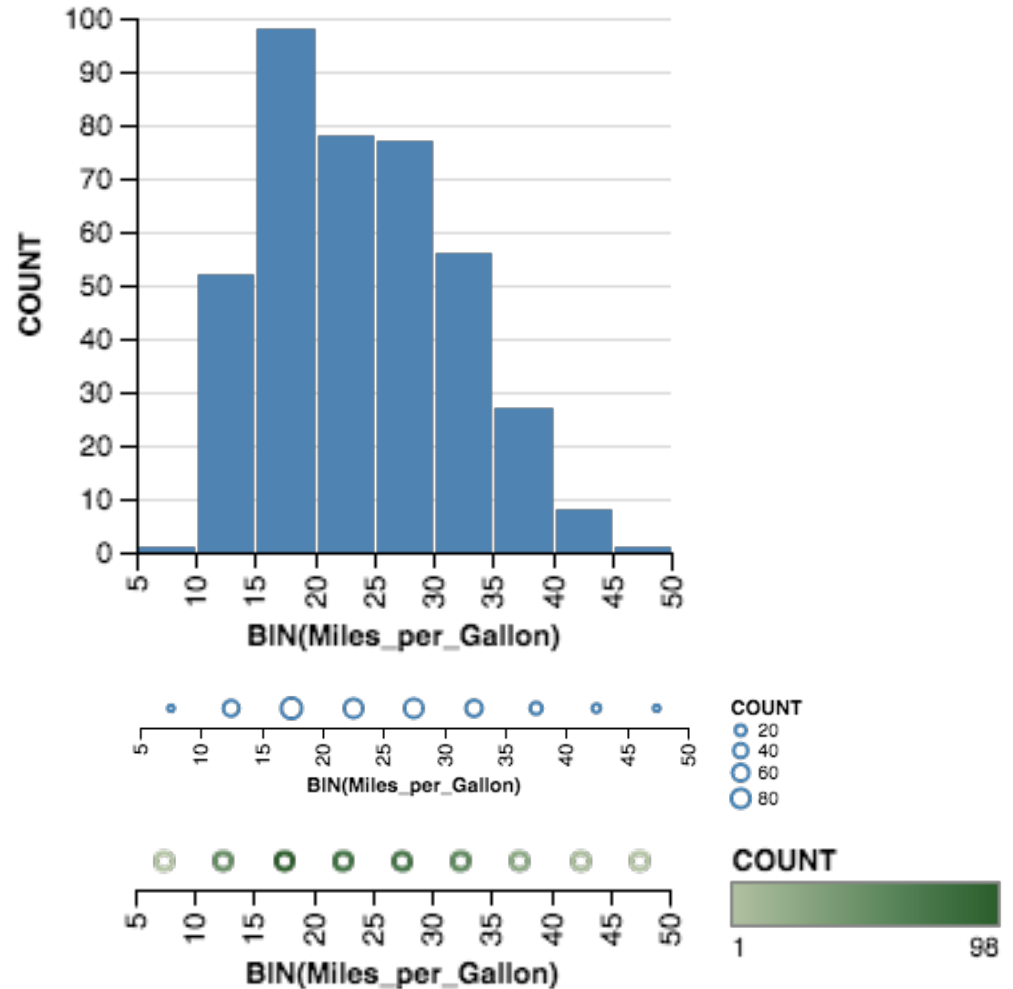


# 1D: Quantitative

## Raw

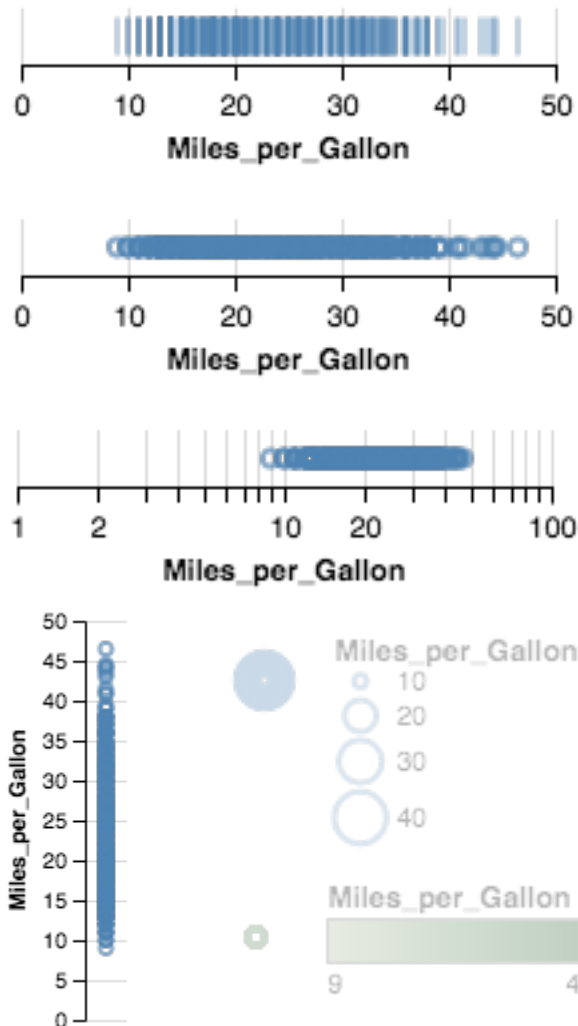


## Aggregate (Count)

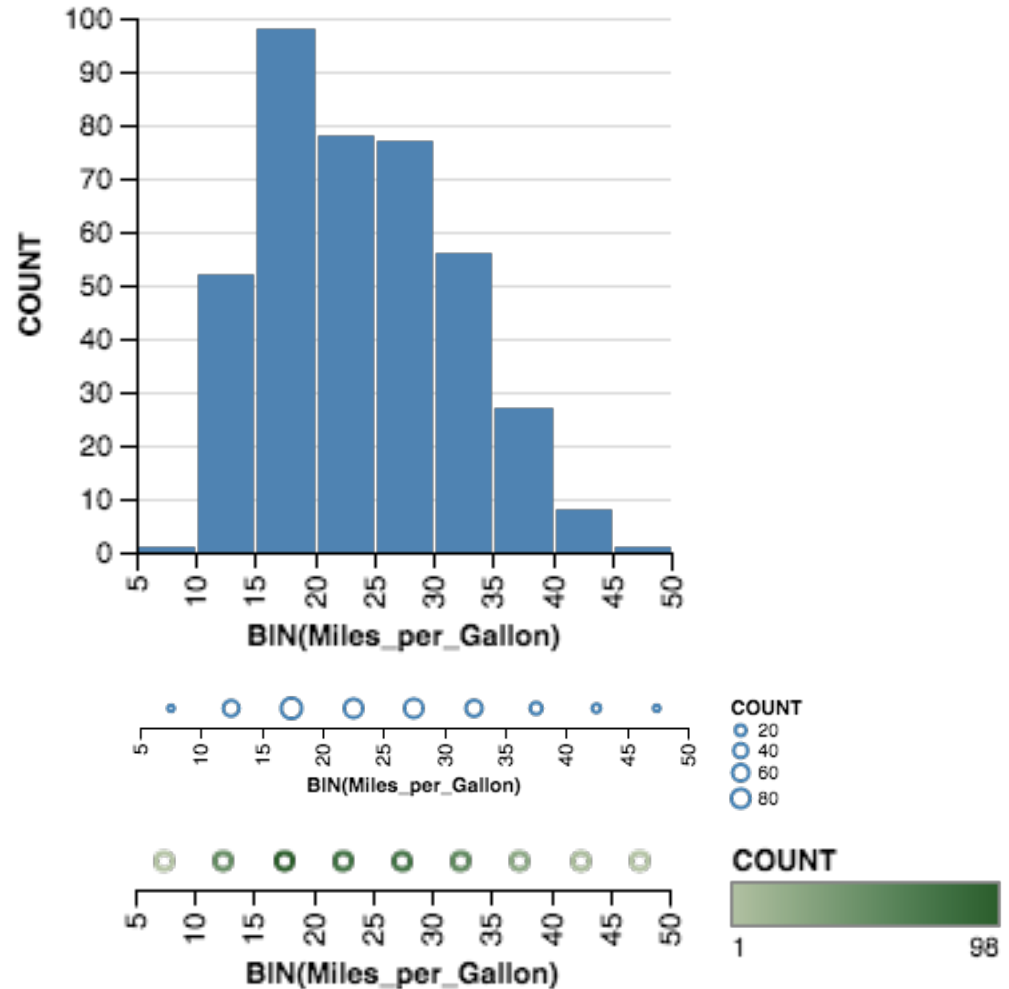


# 1D: Quantitative - Expressive?

Raw

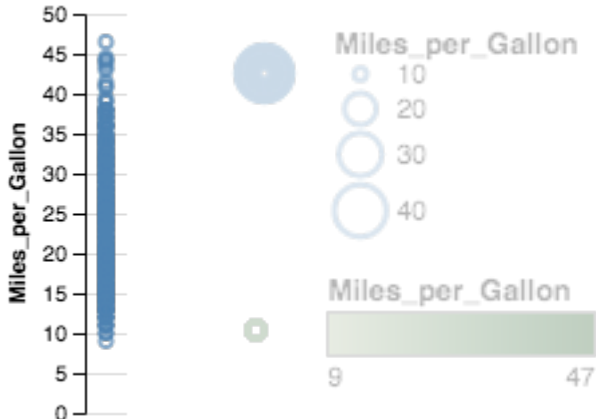
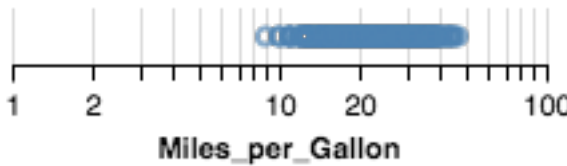
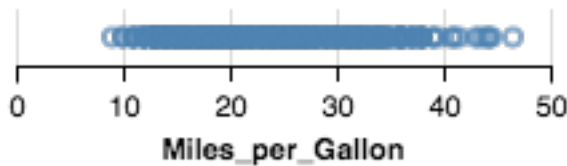
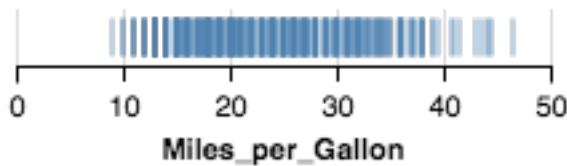


Aggregate (Count)

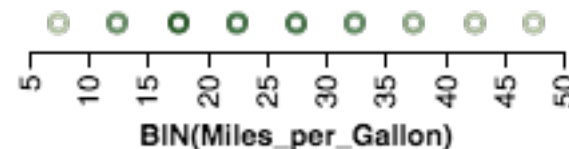
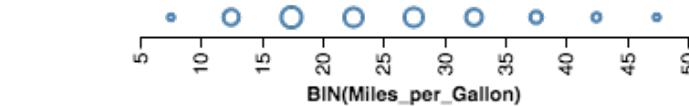
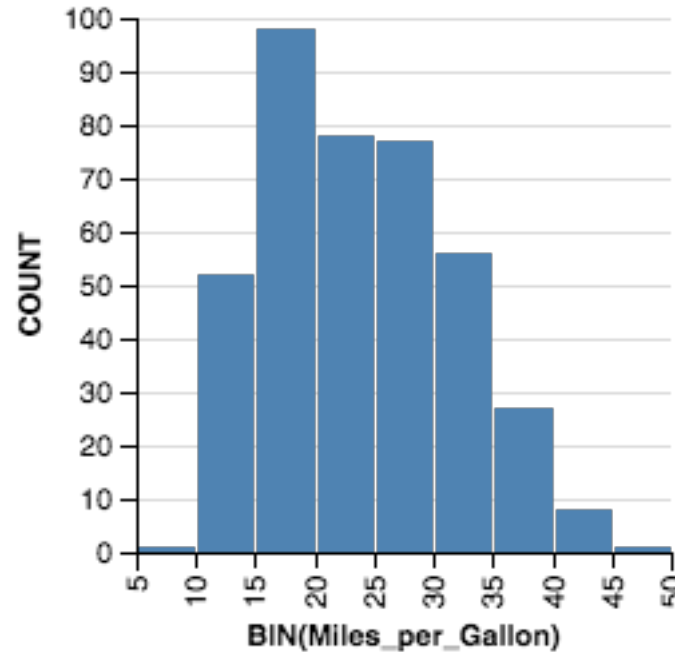


# 1D: Quantitative - Effective?

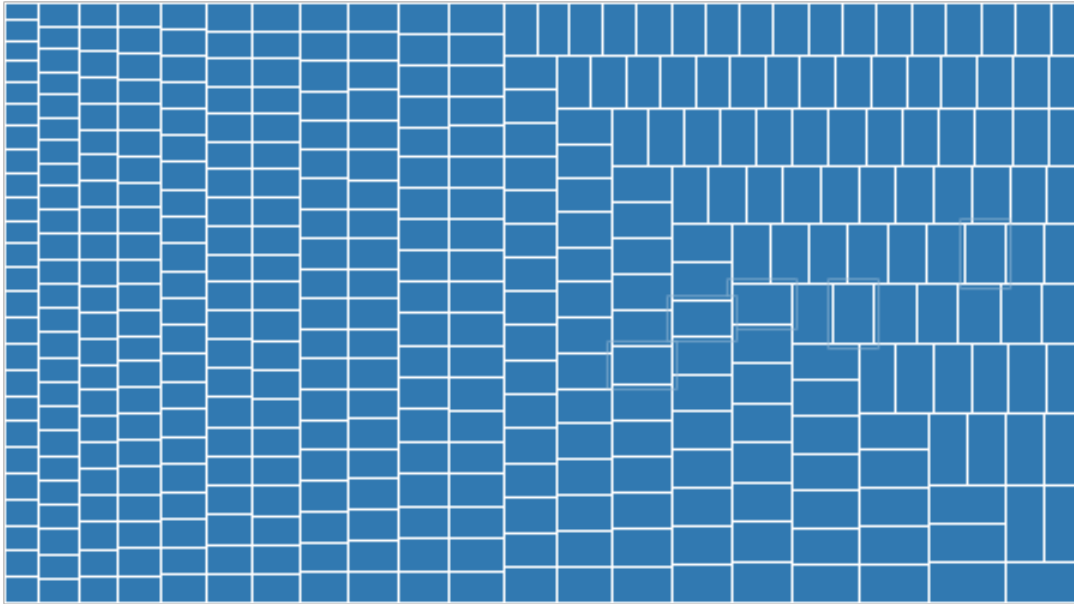
Raw



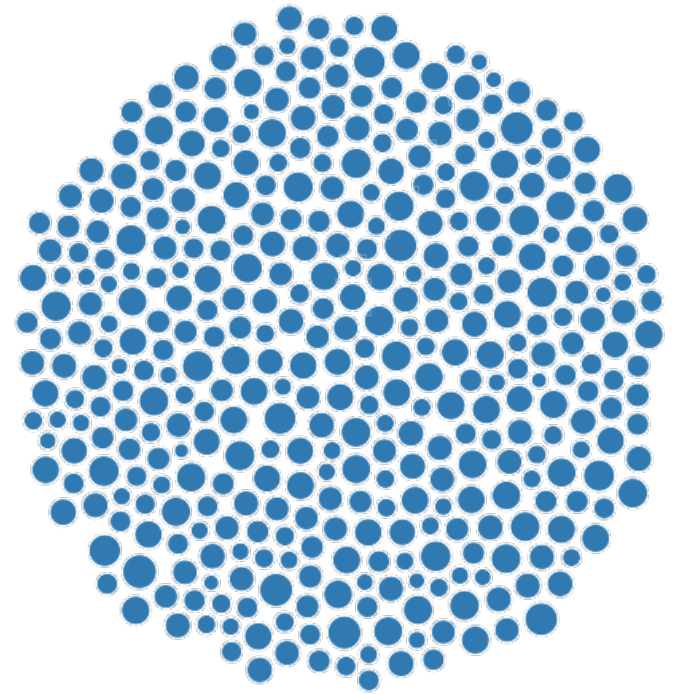
Aggregate (Count)



## Raw (with Layout Algorithm)

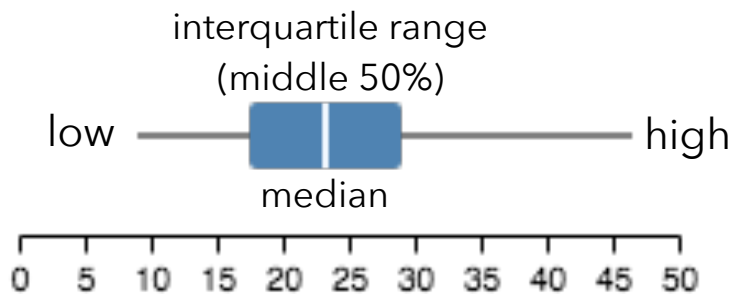


Treemap

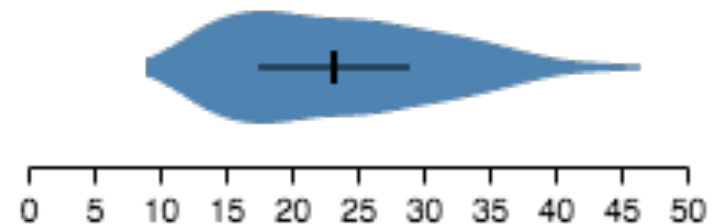


Bubble Chart

## Aggregate (Distributions)



Box Plot

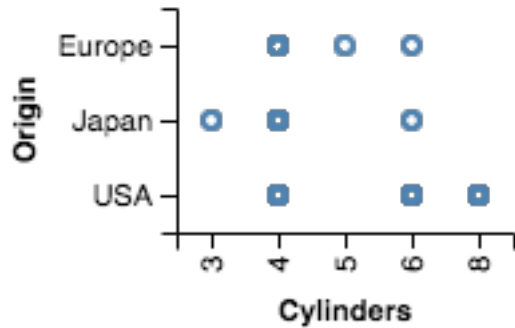


Violin Plot

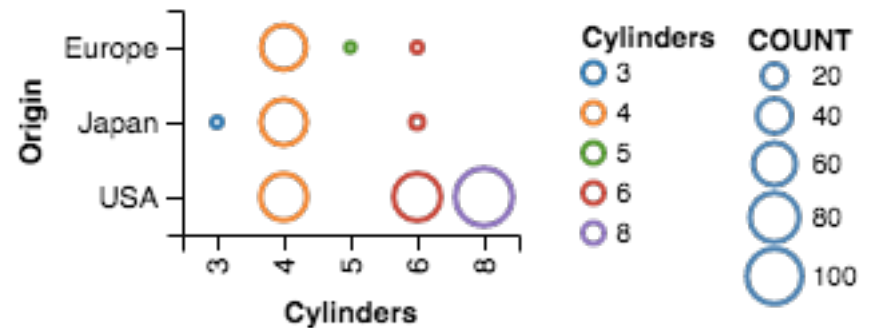
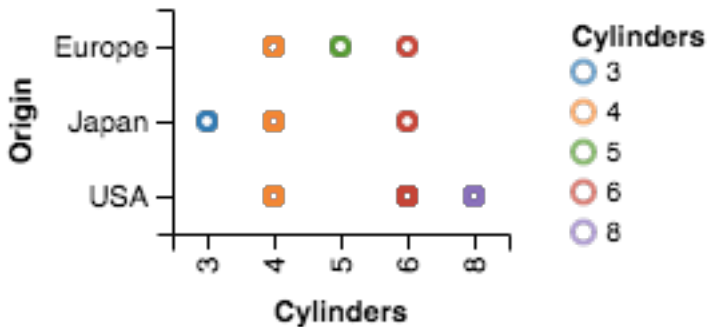
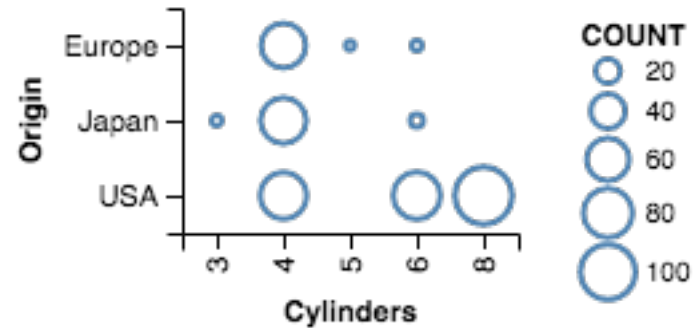
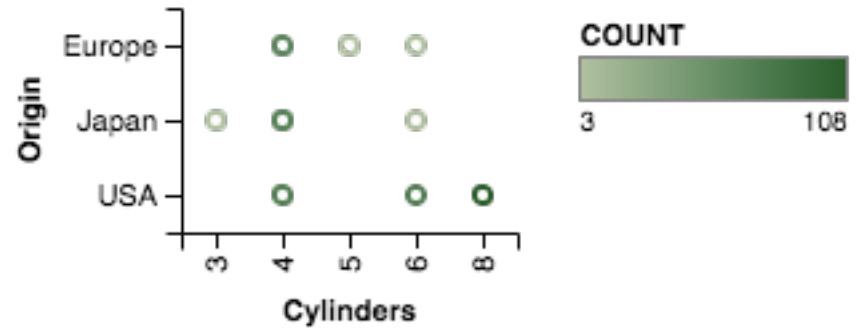


# 2D: Nominal x Nominal

Raw

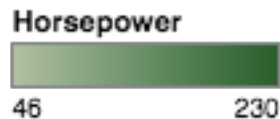
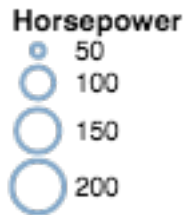
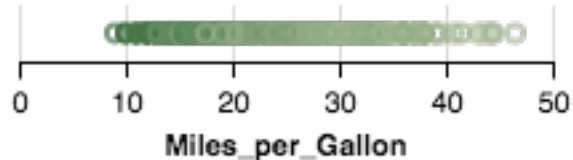
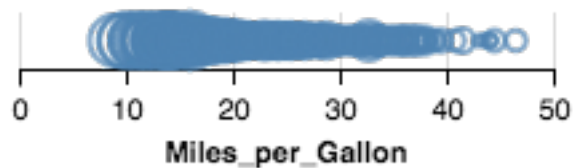
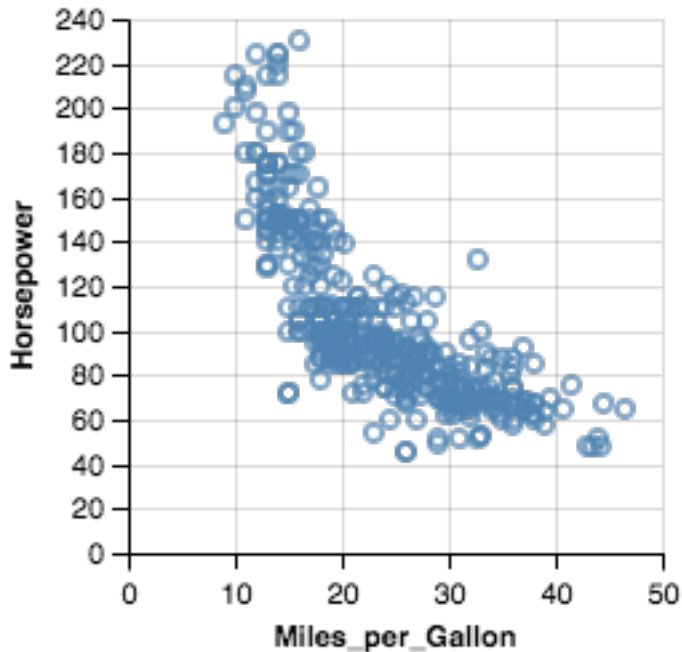


Aggregate (Count)

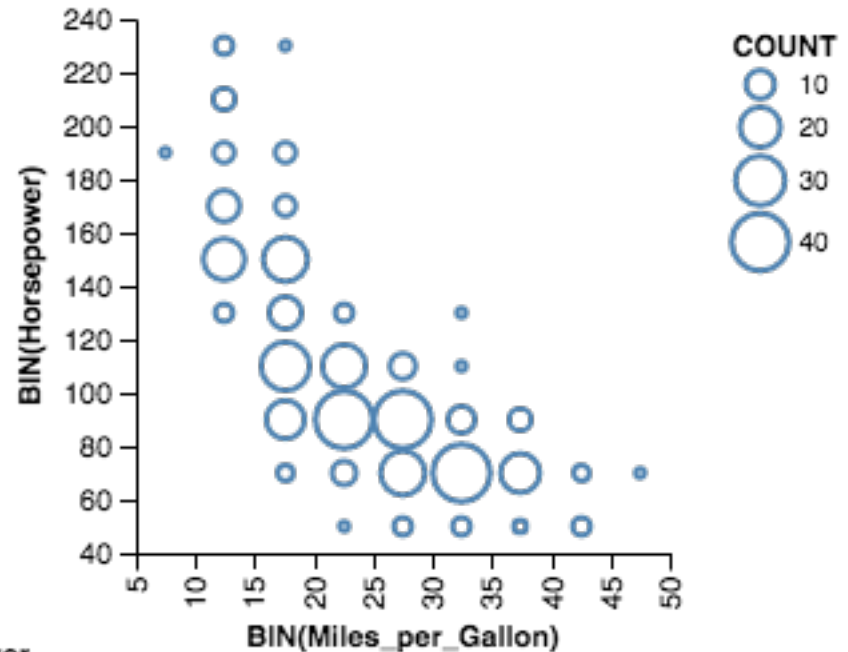


# 2D: Quantitative x Quantitative

Raw

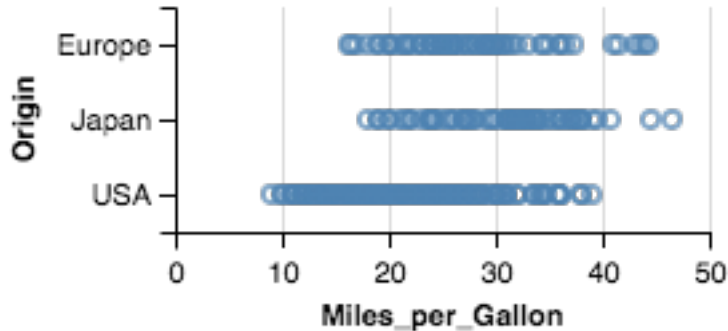


Aggregate (Count)

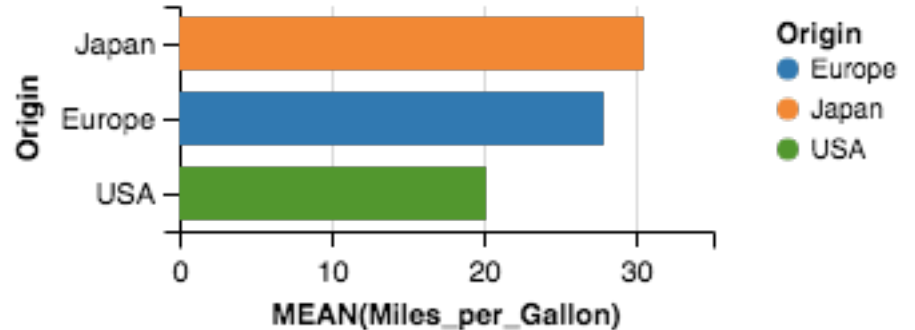
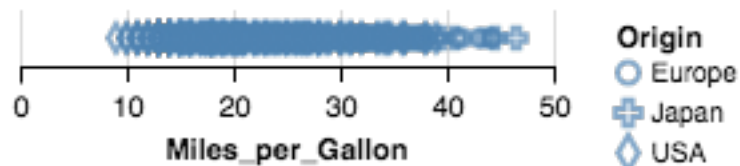
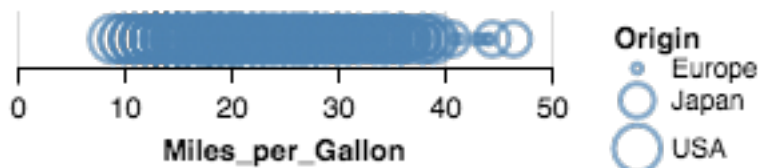
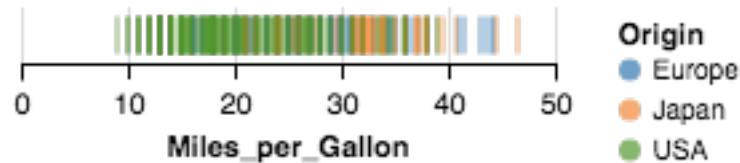
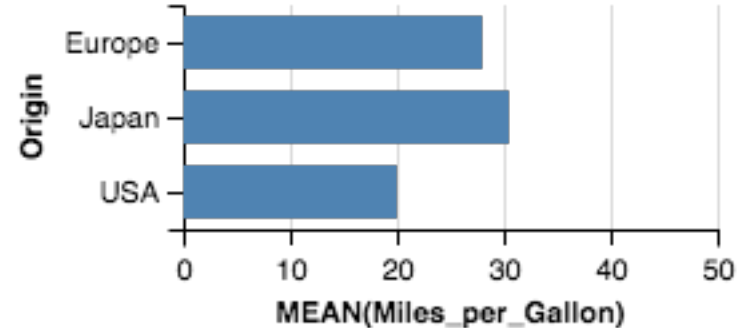


# 2D: Nominal x Quantitative

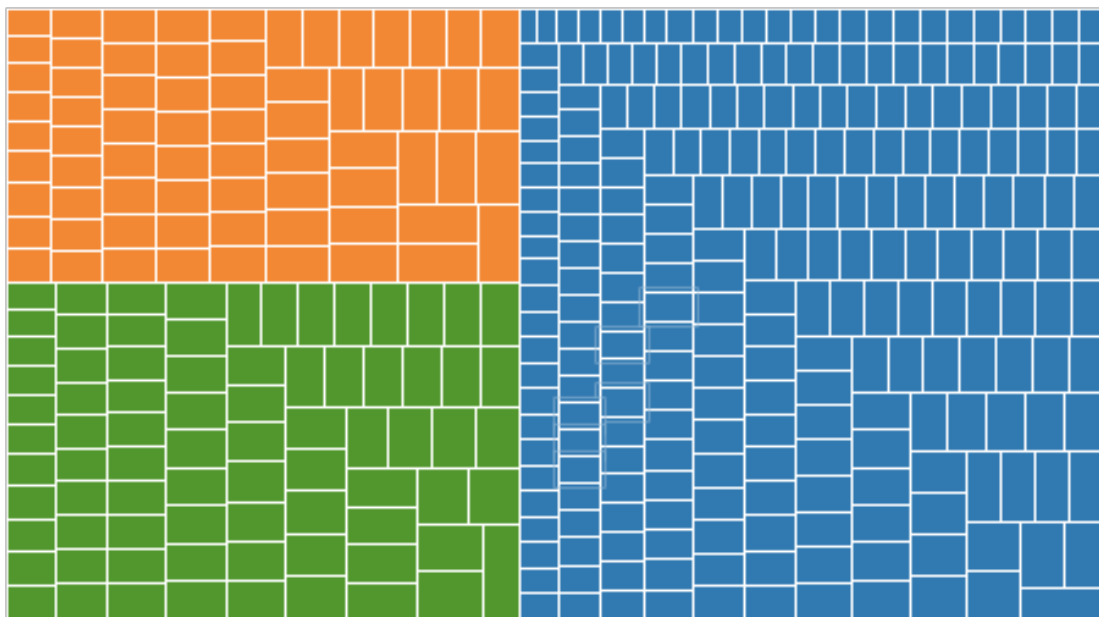
## Raw



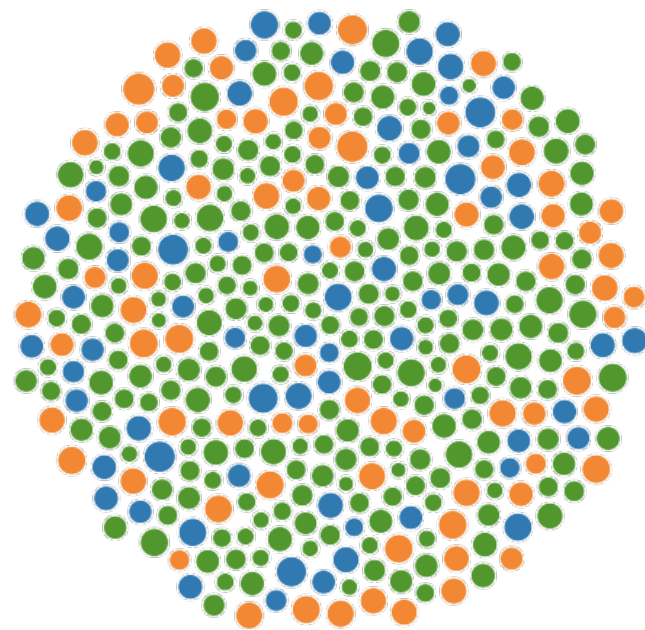
## Aggregate (Mean)



# Raw (with Layout Algorithm)

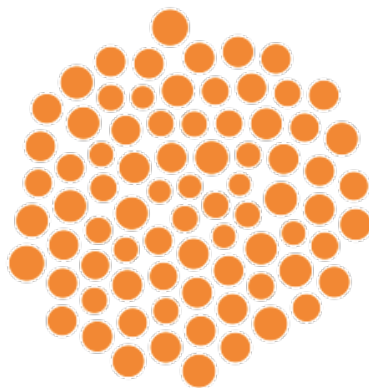
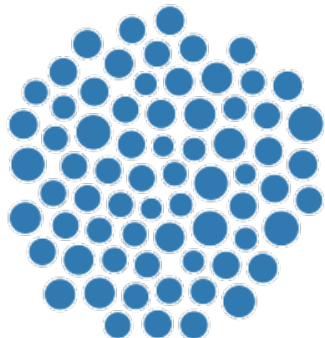


Treemap

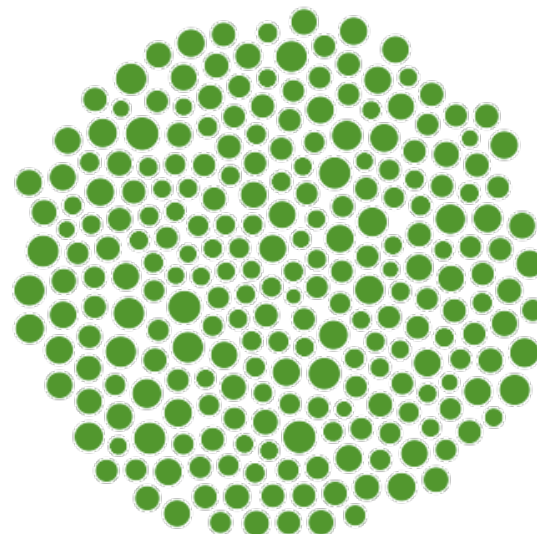


Bubble Chart

Origin  
● Europe  
● Japan  
● USA



Beeswarm Plot



# 3D and Higher

## Two variables [x,y]

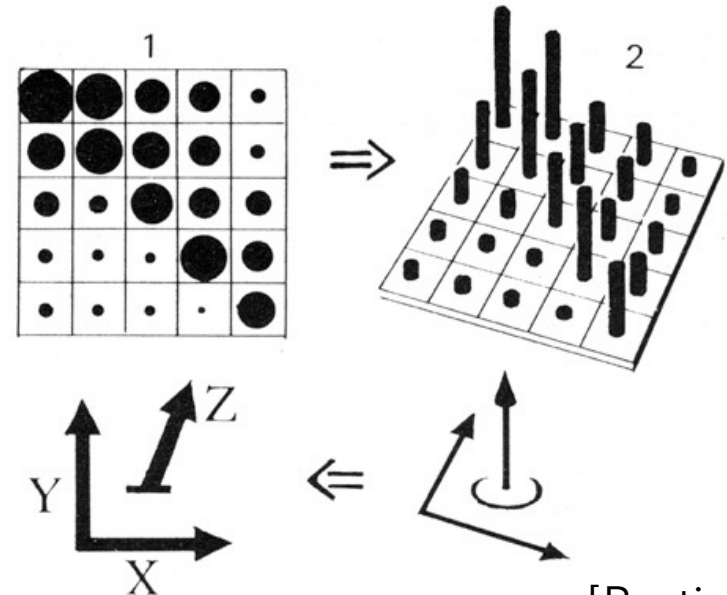
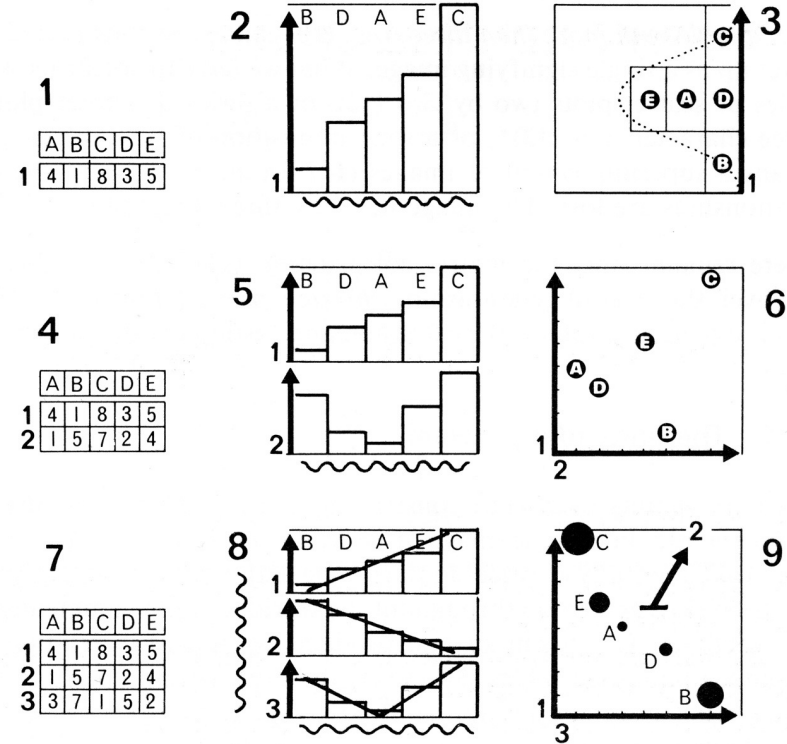
Can map to 2D points.

Scatterplots, maps, ...

## Third variable [z]

Often use one of size, color, opacity, shape, etc. Or, one can further partition space.

*What about 3D rendering?*



# Encoding Effectiveness

# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

Position  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Density (Value)  
Color Sat  
Color Hue  
Texture  
Connection  
Containment  
Shape

## ORDINAL

Position  
Density (Value)  
Color Sat  
Color Hue  
Texture  
Connection  
Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

Position  
Color Hue  
Texture  
Connection  
Containment  
Density (Value)  
Color Sat  
Shape  
Length  
Angle  
Slope  
Area  
Volume

# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

### **Position** .....

Length  
Angle  
Slope  
Area (Size)  
Volume  
Density (Value)  
Color Sat  
Color Hue  
Texture  
Connection  
Containment  
Shape

## ORDINAL

### **Position** .....

Density (Value)  
Color Sat  
Color Hue  
Texture  
Connection  
Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

### **Position**

Color Hue  
Texture  
Connection  
Containment  
Density (Value)  
Color Sat  
Shape  
Length  
Angle  
Slope  
Area  
Volume



# Effectiveness Rankings [Mackinlay 86]

## QUANTITATIVE

Position  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Density (Value)  
Color Sat  
**Color Hue**  
Texture  
Connection  
Containment  
Shape

## ORDINAL

Position  
Density (Value)  
Color Sat  
**Color Hue**  
Texture  
Connection  
Containment  
Length  
Angle  
Slope  
Area (Size)  
Volume  
Shape

## NOMINAL

Position  
**Color Hue**  
Texture  
Connection  
Containment  
Density (Value)  
Color Sat  
Shape  
Length  
Angle  
Slope  
Area  
Volume

# Mapping Data to Visual Variables

Assign **data fields** (e.g., with  $N$ ,  $O$ ,  $Q$  types) to **visual channels** ( $x$ ,  $y$ ,  $color$ ,  $shape$ ,  $size$ , ...) for a chosen **graphical mark** type ( $point$ ,  $bar$ ,  $line$ , ...).

Additional concerns include choosing appropriate **encoding parameters** ( $log\ scale$ ,  $sorting$ , ...) and **data transformations** ( $bin$ ,  $group$ ,  $aggregate$ , ...).

These options define a large combinatorial space, containing both useful and questionable charts!

# Designing Charts

# Example: Cars

Properties of different models of cars

9-Dimensions, 406 rows

Name	N	Horsepower	Q
MPG	Q	Weight (lbs)	Q
Cylinders	Q	Acceleration	Q
Displacement	Q	Year	T
Origin	N {USA, Europe, Japan}		

# Visual Encoding Variables

Position (X)

Position (Y)

Area

Value

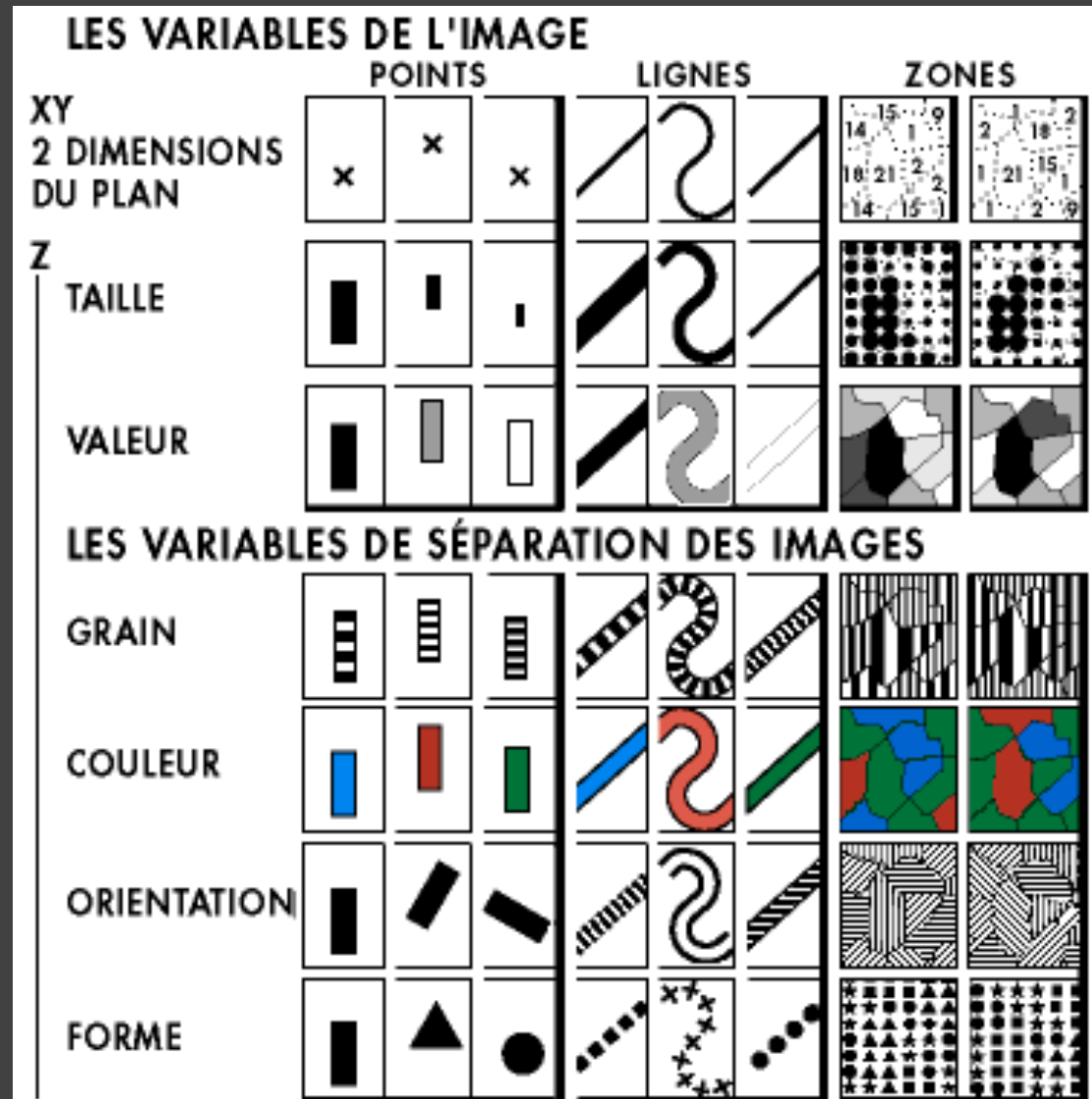
Texture

Color

Orientation

Shape

~9 dimensions?



# Example: Cars

Properties of different models of cars

9-Dimensions, 406 rows

Name	N	Horsepower	Q
MPG	Q	Weight (lbs)	Q
Cylinders	Q	Acceleration	Q
Displacement	Q	Year	T
Origin	N {USA, Europe, Japan}		

# Example: Cars

Horsepower

MPG

Origin

Displacement

Cylinders

Weight (lbs)

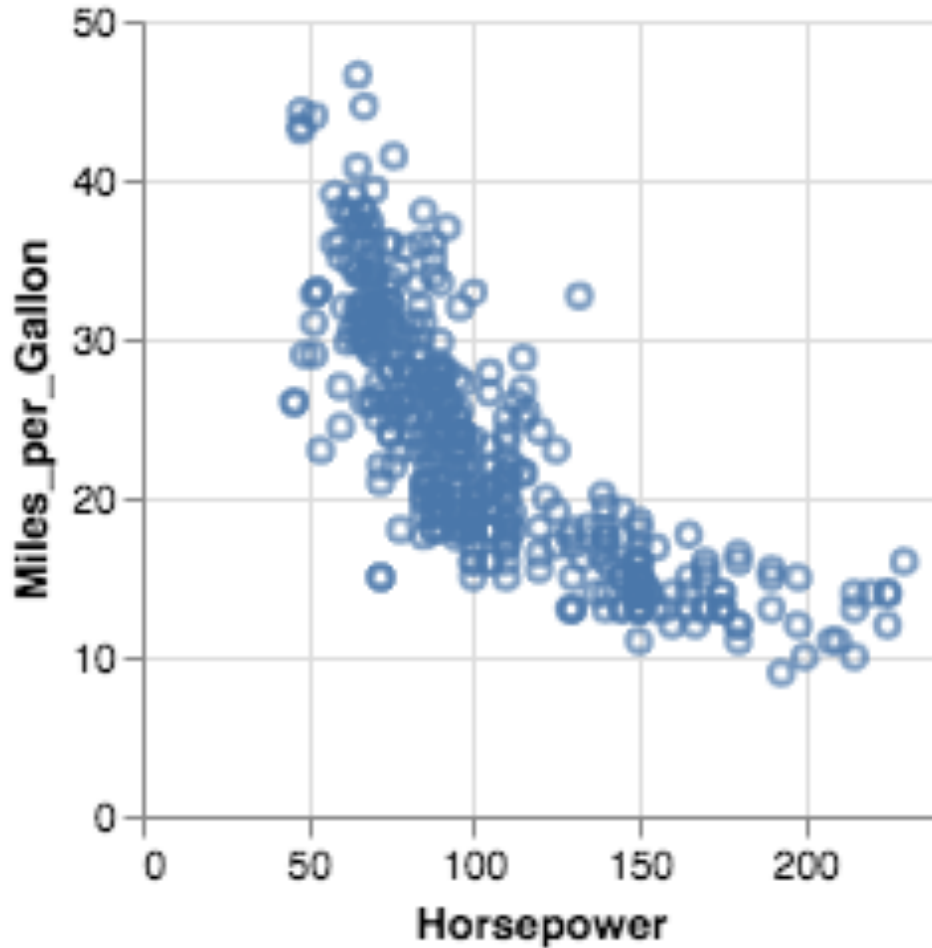
Acceleration

Year

Name

# 2-Dimensions

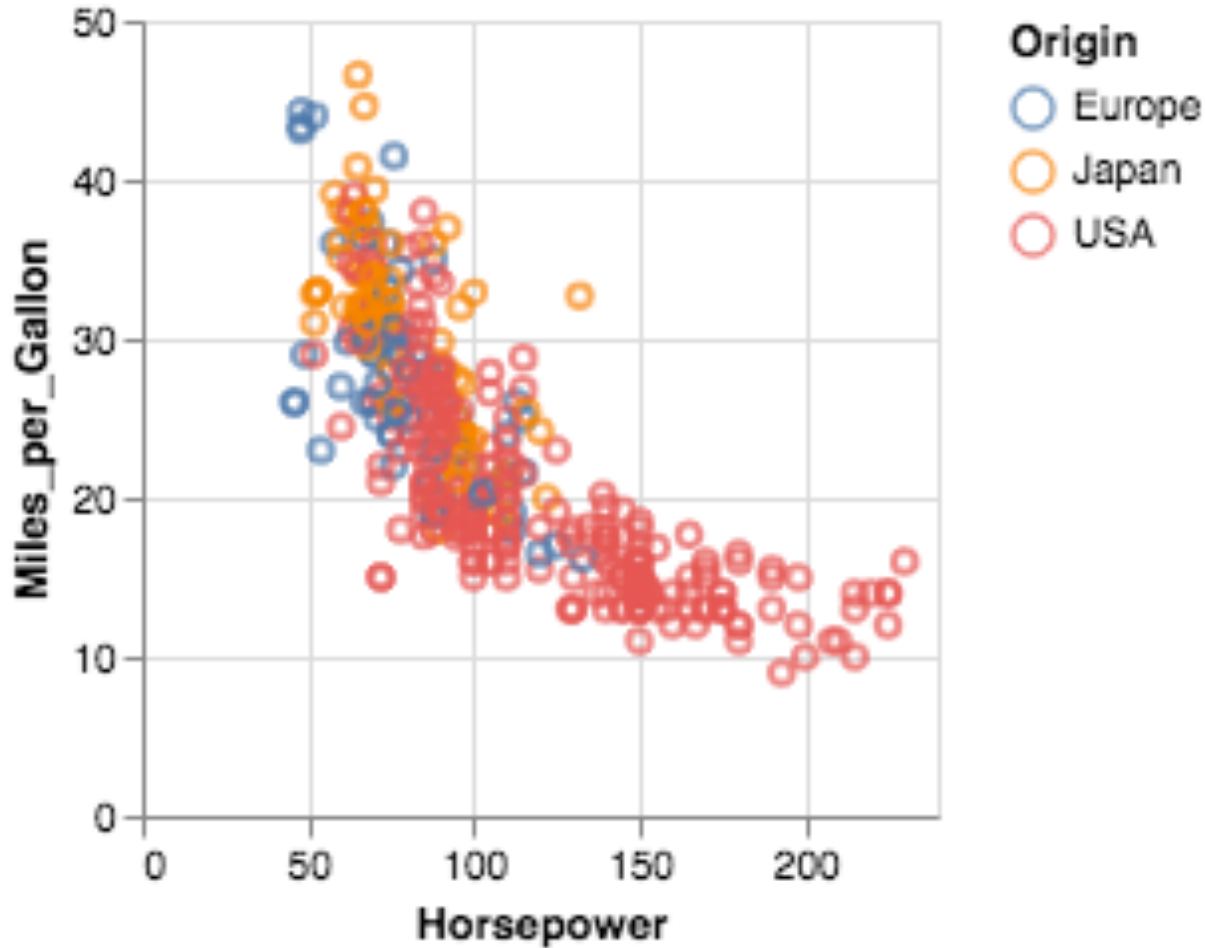
Next Up: Origin (N)





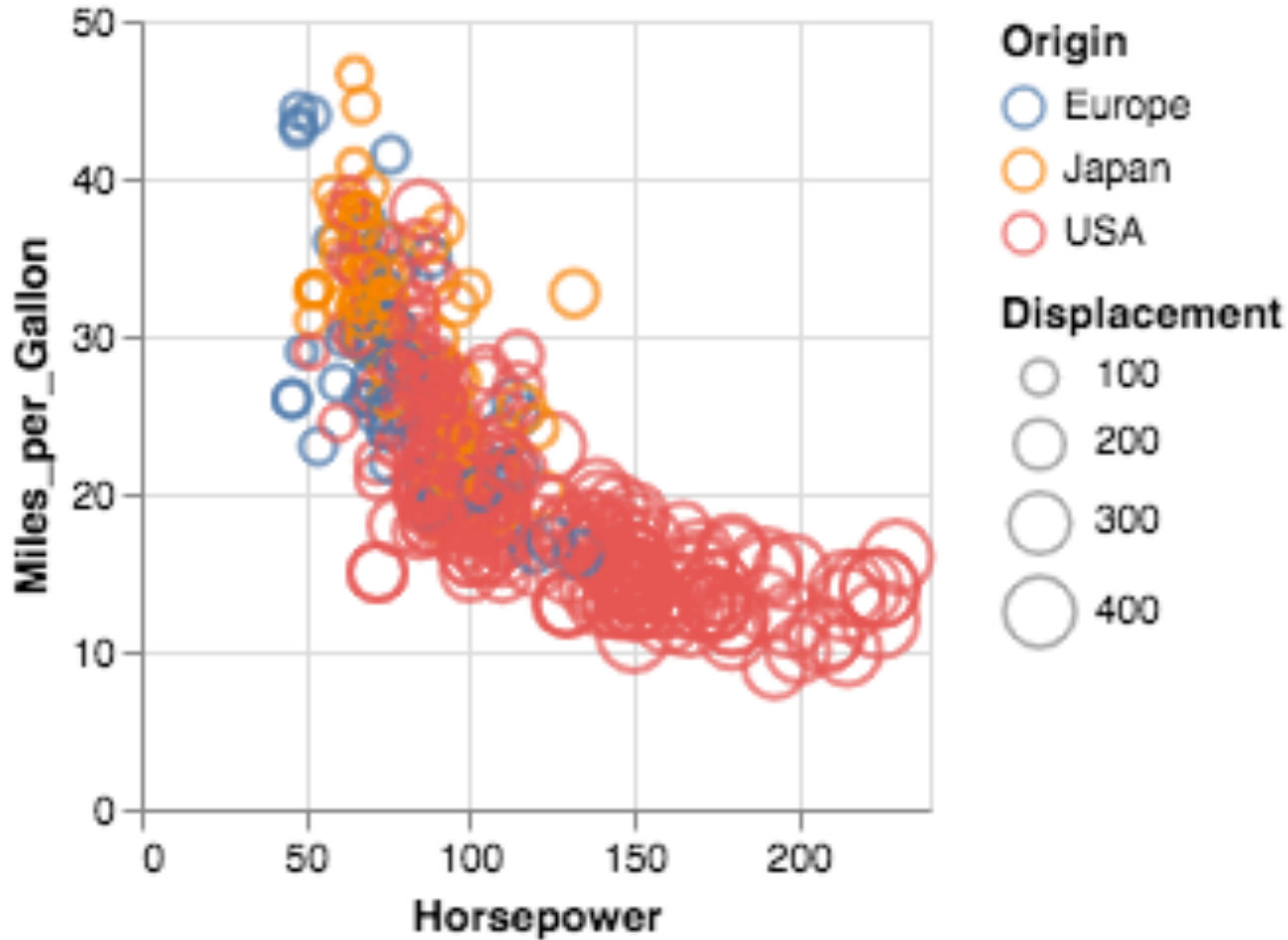
# 3-Dimensions

Next Up:  
Displacement (Q)



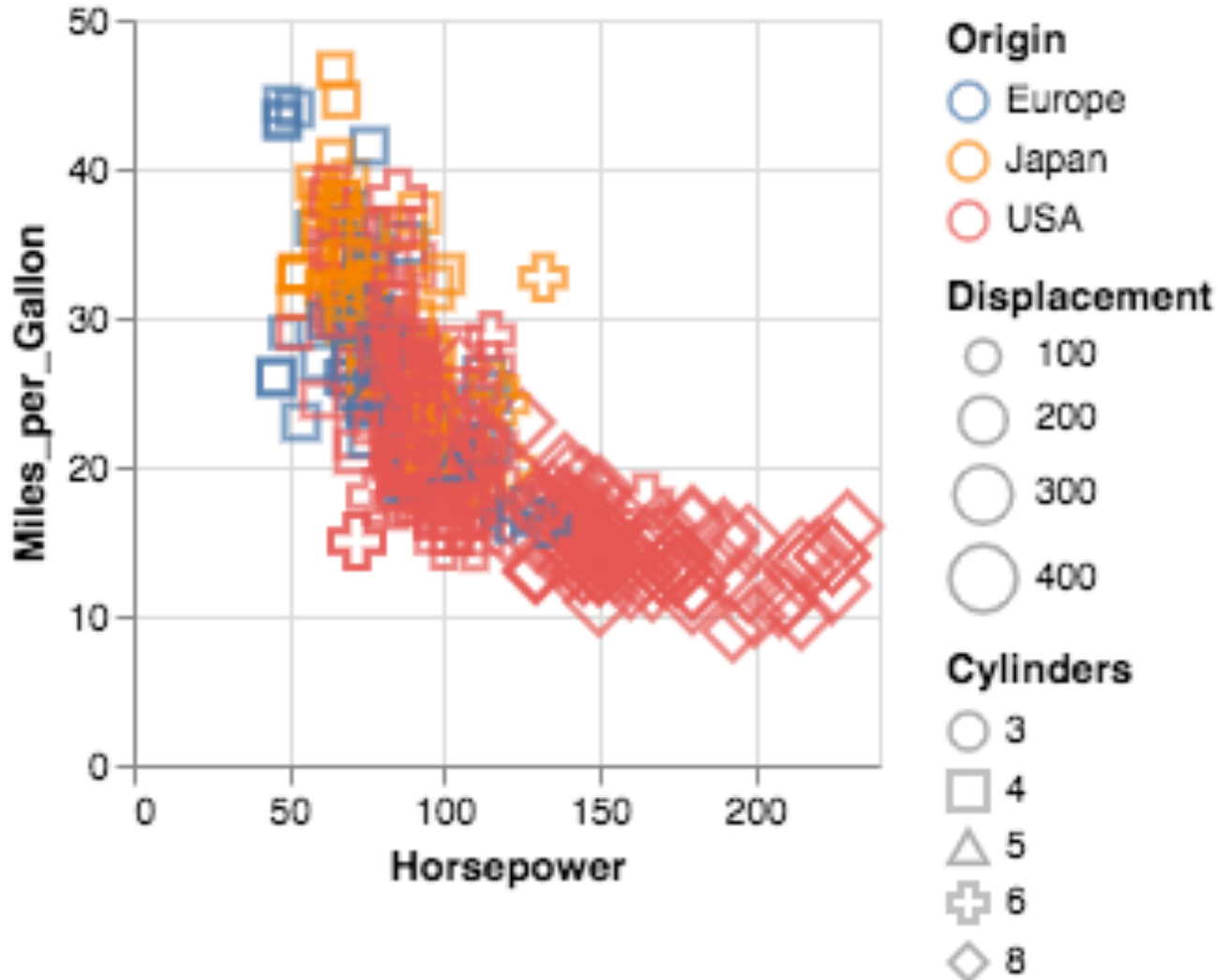
# 4-Dimensions

Next Up:  
Cylinders (O/Q)



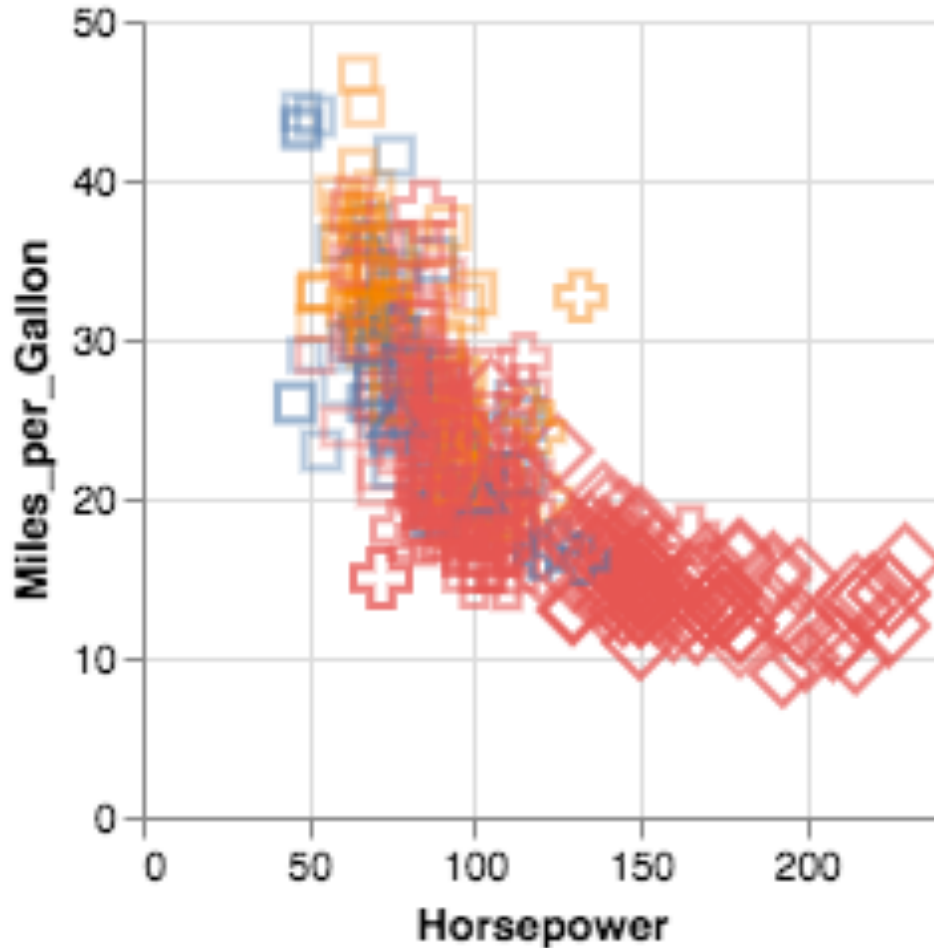
# 5-Dimensions

Next Up:  
Weight (Q)



# 6-Dimensions

Next Up:  
Acceleration (Q)



## Origin

- Europe
- Japan
- USA

## Displacement

- 100
- 200
- 300
- 400

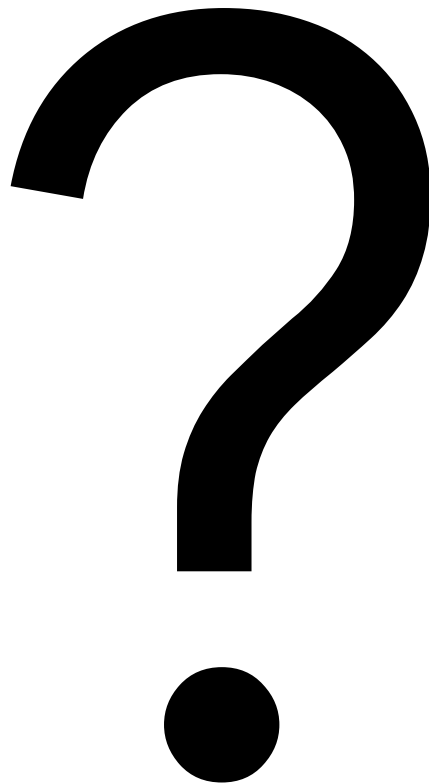
## Cylinders

- 3
- 4
- 5
- 6
- 8

## Weight\_in\_lbs

- 2,000
- 2,500
- 3,000
- 3,500
- 4,000
- 4,500
- 5,000

# 7-Dimensions?



# Trellis Plots



A *trellis plot* subdivides space to enable comparison across multiple plots.

Typically nominal or ordinal variables are used as dimensions for subdivision.

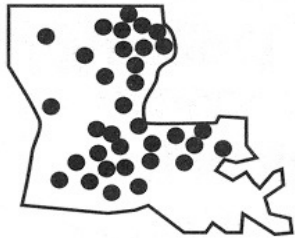
# Small Multiples



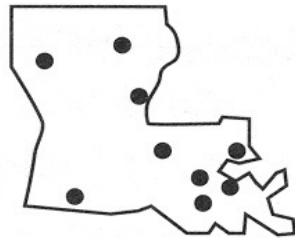
[MacEachren '95, Figure 2.11, p. 38]

# Small Multiples

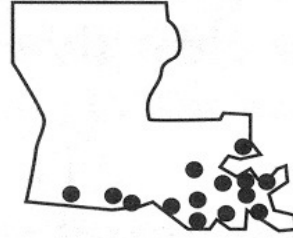
alfisol



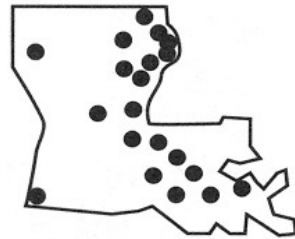
entisol



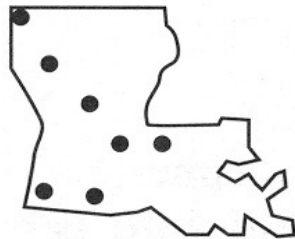
histosol



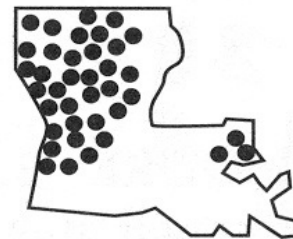
inceptisol



mollisol



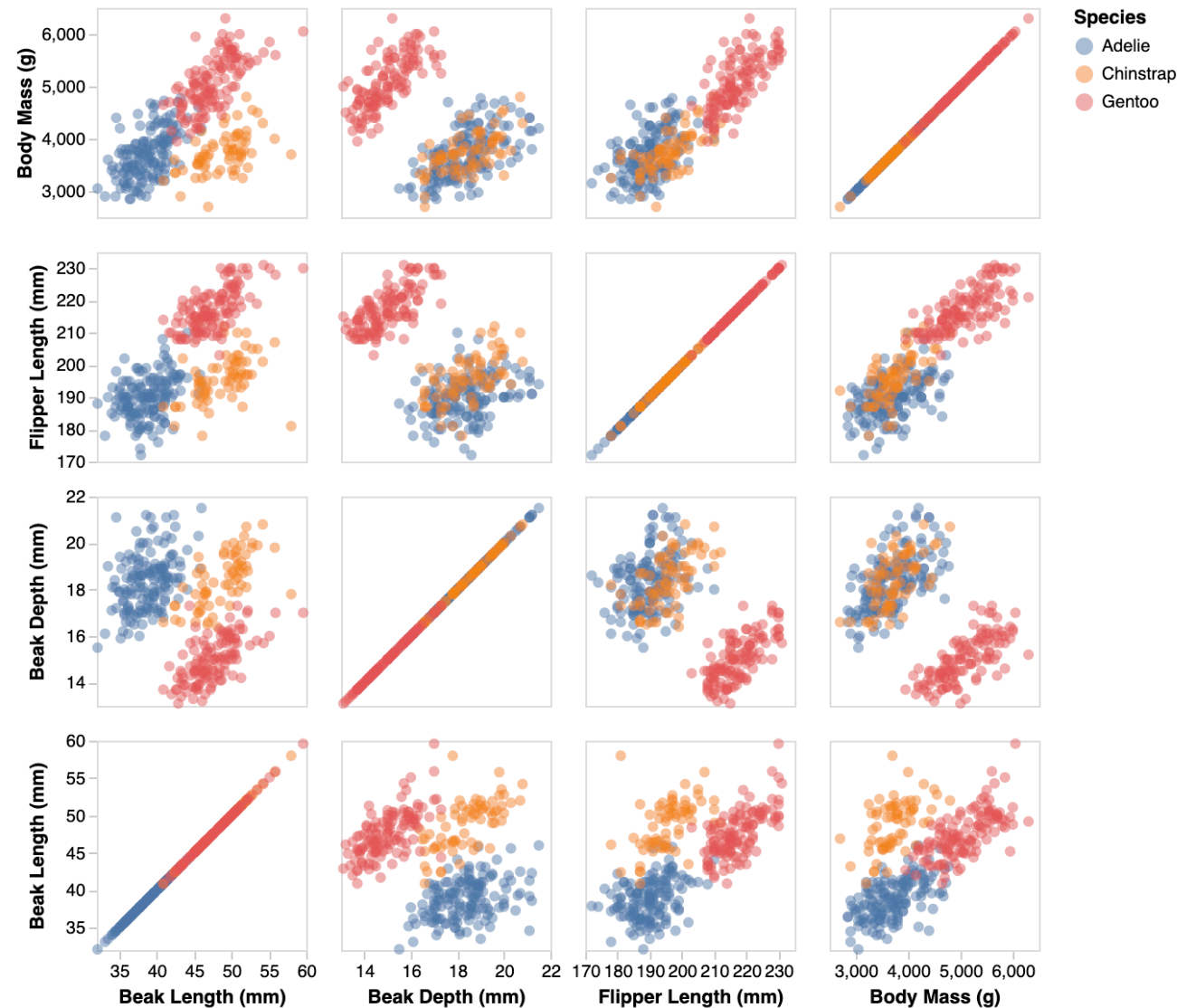
ultisol



[MacEachren '95, Figure 2.11, p. 38]



# Scatterplot Matrix (SPLOM)



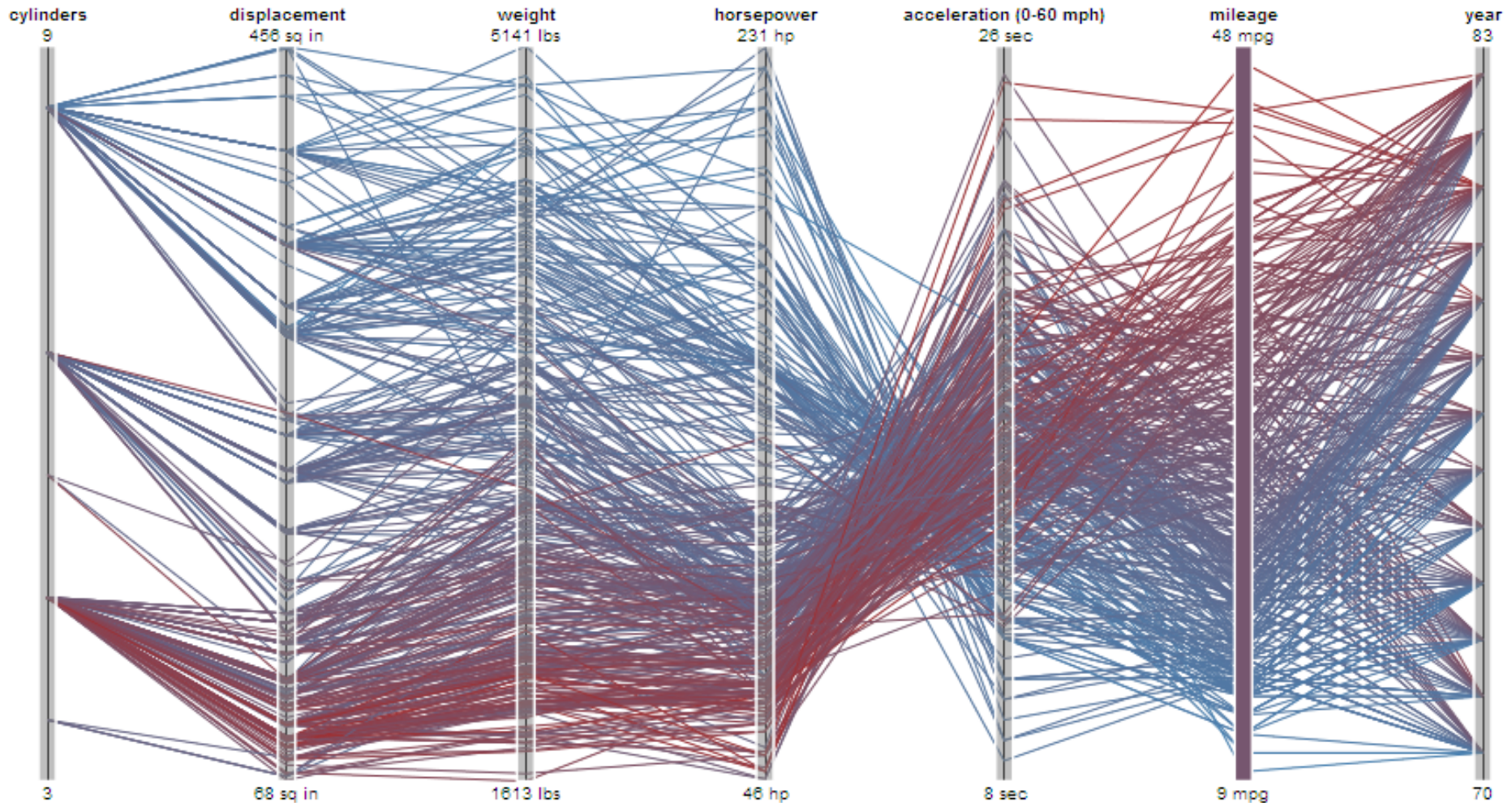
Scatter plots for pairwise comparison of each data dimension.

# Multiple Coordinated Views



# Parallel Coordinates

# Parallel Coordinates [Inselberg]



# Parallel Coordinates [Inselberg]

Visualize up to ~two dozen dimensions at once

1. Draw parallel axes for each variable
2. For each tuple, connect points on each axis

Between adjacent axes: line crossings imply neg. correlation, shared slopes imply pos. correlation.

Full plot can be cluttered. **Interactive selection** can be used to assess multivariate relationships.

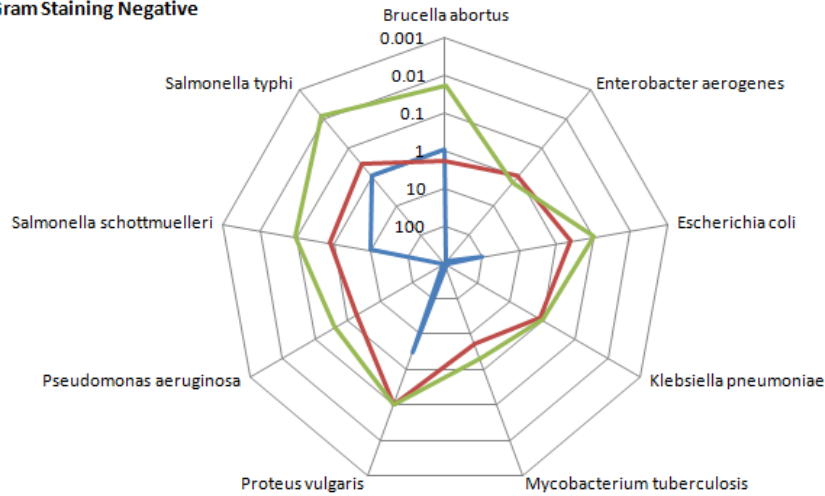
Highly sensitive to axis **scale** and **ordering**.

Expertise required to use effectively!

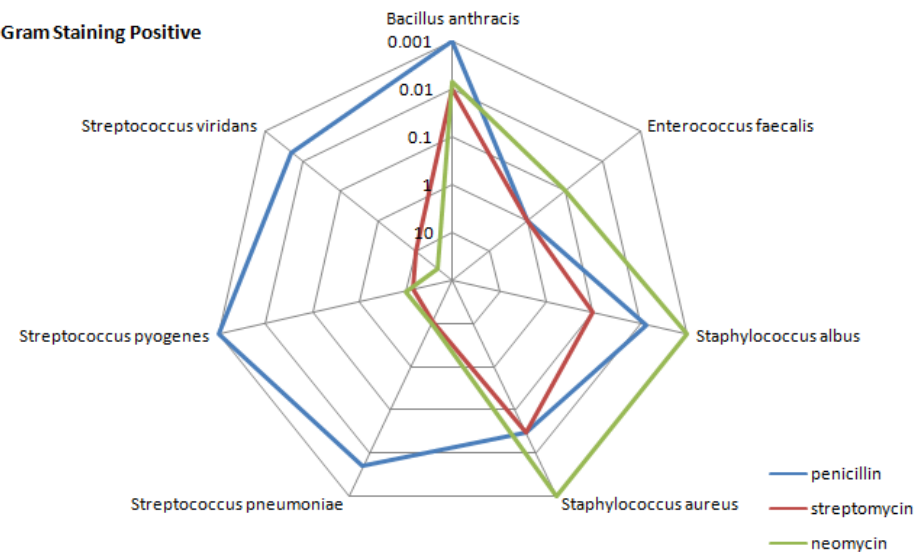
# Radar Plot / Star Graph

Antibiotics MIC Concentrations

Gram Staining Negative



Gram Staining Positive



“Parallel” dimensions in polar coordinate space  
Best if same units apply to each axis

# Dimensionality Reduction

# Dimensionality Reduction (DR)

Project  $nD$  data to 2D or 3D for viewing. Often used to interpret and sanity check high-dimensional representations fit by machine learning methods.

Different DR methods make different trade-offs: for example to **preserve global structure** (e.g., PCA) or **emphasize local structure** (e.g., nearest-neighbor approaches, including t-SNE and UMAP).



# Reduction Techniques

## **Principal Components Analysis (PCA)**

Linear transformation of basis vectors, ordered by amount of data variance they explain.

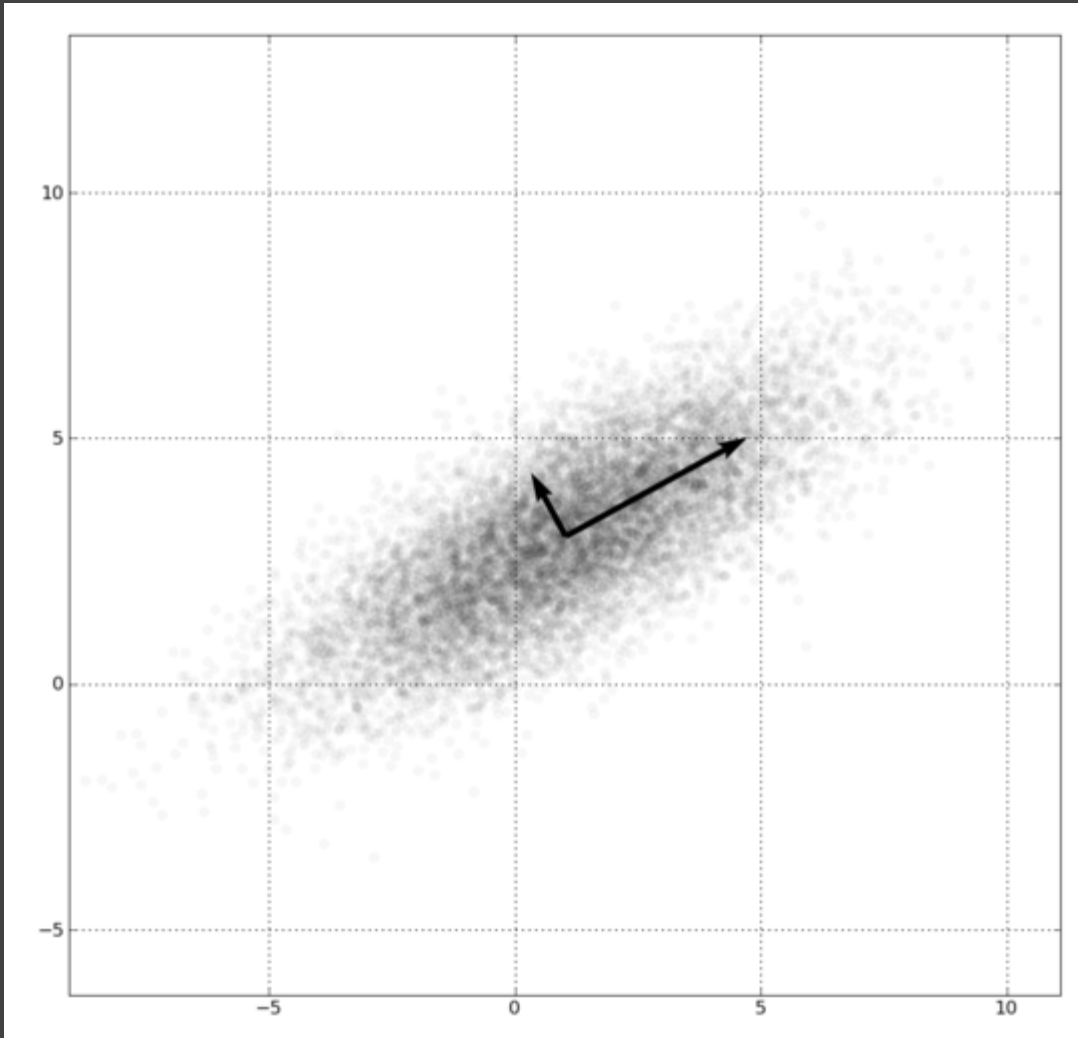
## **t-Dist. Stochastic Neighbor Embedding (t-SNE)**

Probabilistically model distance, optimize positions.

## **Uniform Manifold Approx. & Projection (UMAP)**

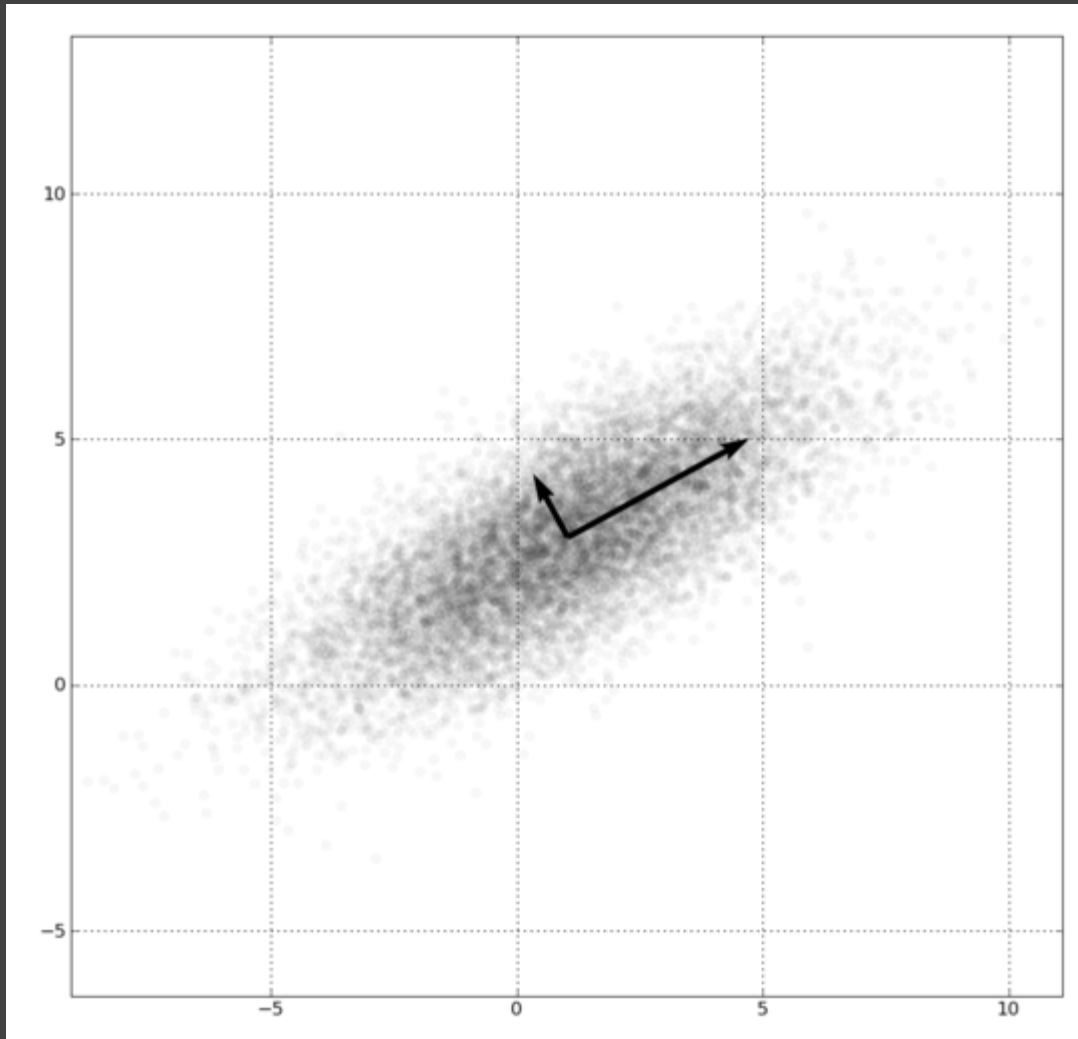
Identify local manifolds, then stitch them together.

# Principal Components Analysis



1. Mean-center the data.
2. Find  $\perp$  basis vectors that maximize the data variance.
3. Plot the data using the top vectors.

# Principal Components Analysis

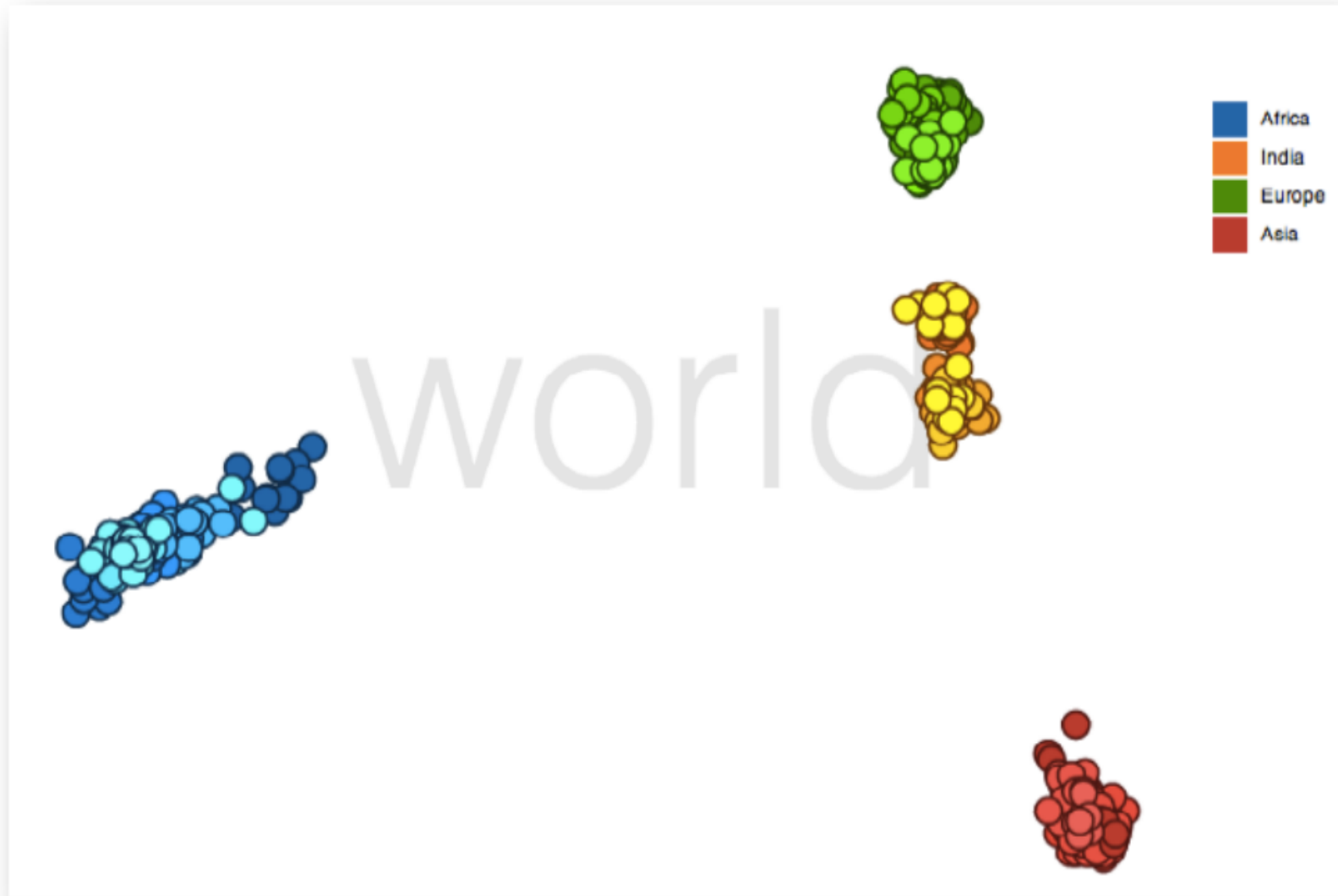


Linear transform:  
scale and rotate  
original space.

Lines (vectors)  
project to lines.

Preserves global  
distances.

# PCA of Genomes [Demiralp et al. '13]



# Non-Linear Techniques

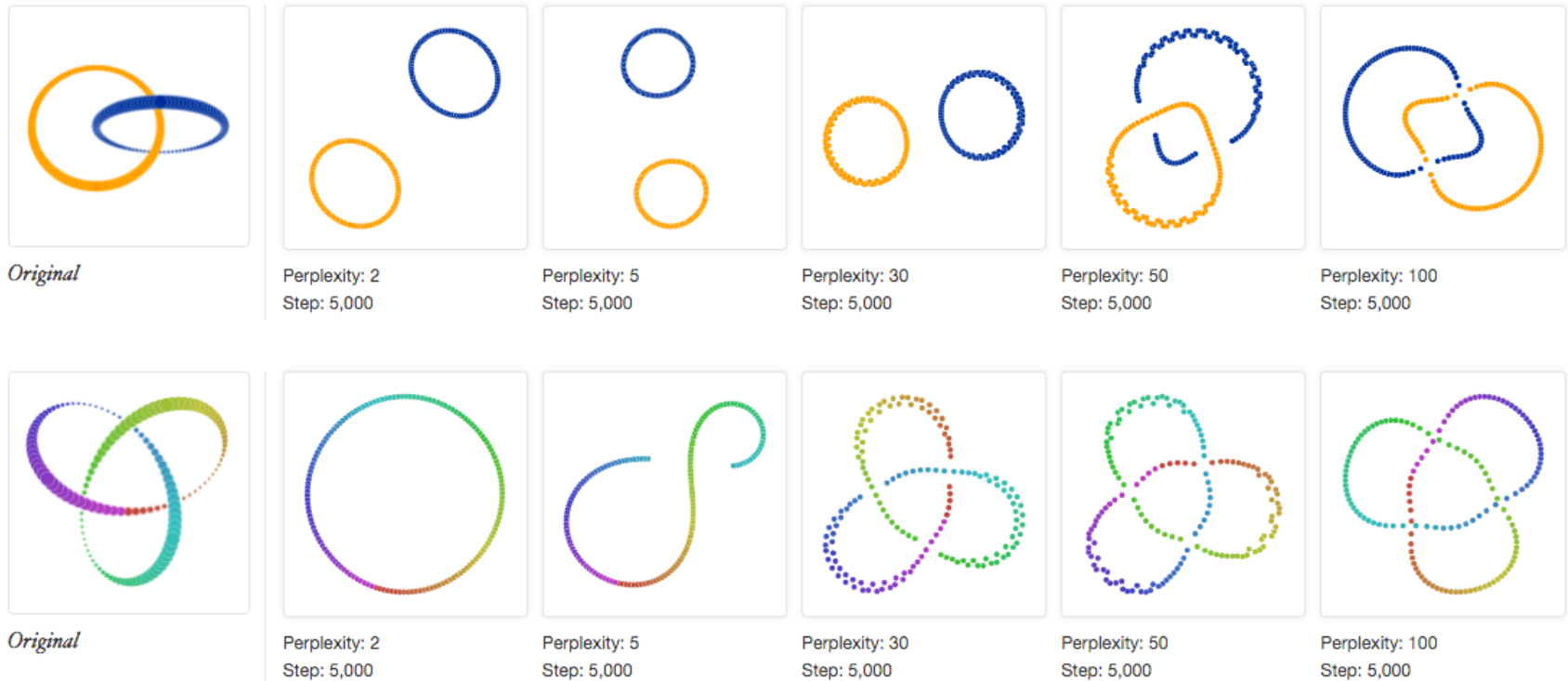
Distort the space, trade-off preservation of global structure to emphasize local neighborhoods. Use topological (nearest neighbor) analysis.

Two popular contemporary methods:

**t-SNE** - probabilistic interpretation of distance

**UMAP** - tries to balance local/global trade-off

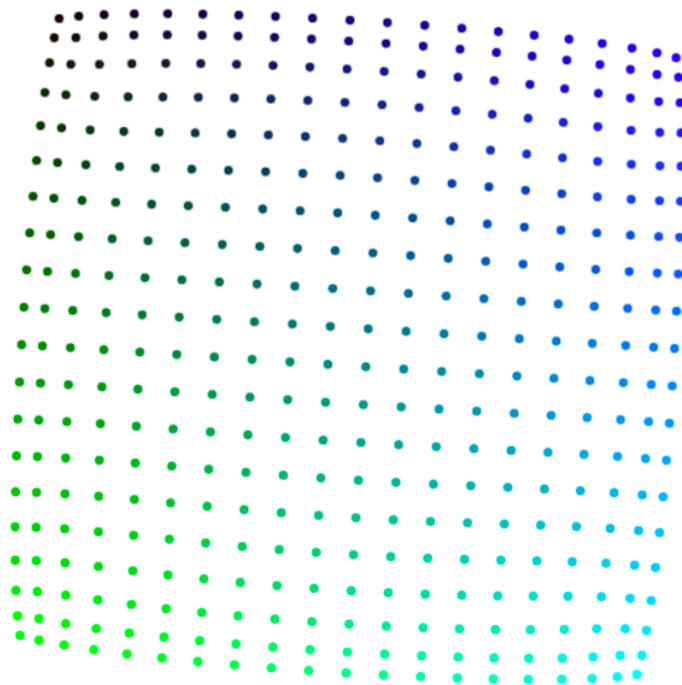
# Visualizing t-SNE [Wattenberg et al. '16]



Results can be highly sensitive to the algorithm parameters!

# How to Use t-SNE Effectively

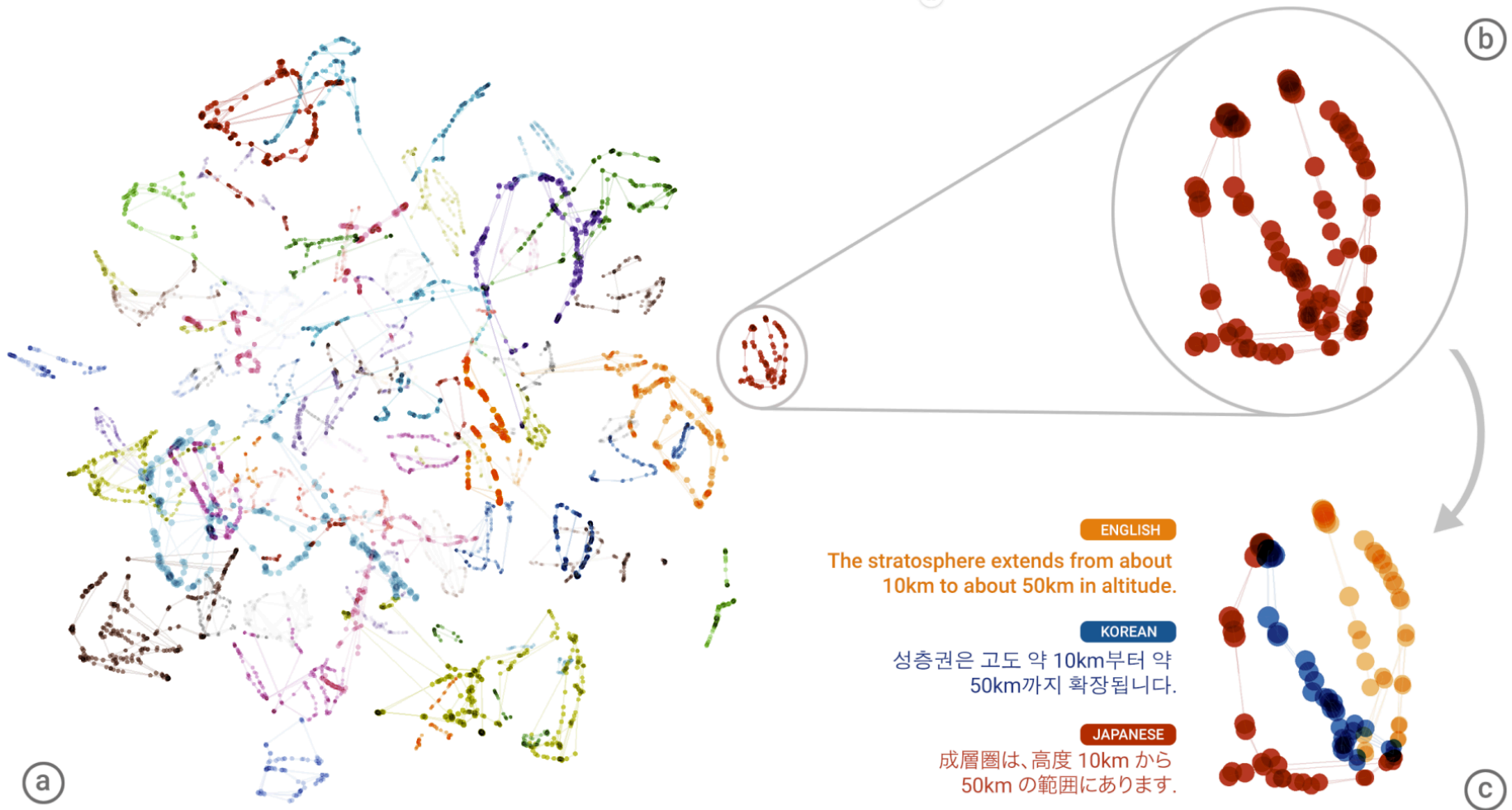
Although extremely useful for visualizing high-dimensional data, t-SNE plots can sometimes be mysterious or misleading. By exploring how it behaves in simple cases, we can learn to use it more effectively.



⏸ ↺ Step 1,910  
 Points Per Side 20  
 Perplexity 10  
 Epsilon 5

A square grid with equal spacing between points. Try convergence at different sizes.

# MT Embedding [Johnson et al. 2018]



t-SNE projection of latent space of language translation model.



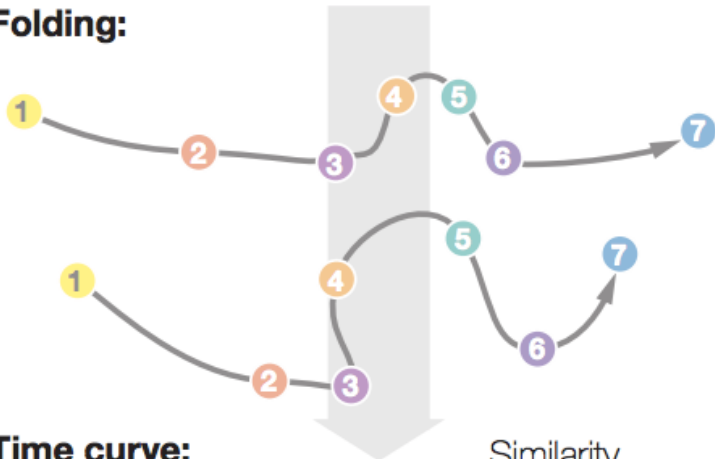
# Time Curves [Bach et al. '16]

## Timeline:



Circles are data cases with a time stamp.  
Similar colors indicate similar data cases.

## Folding:

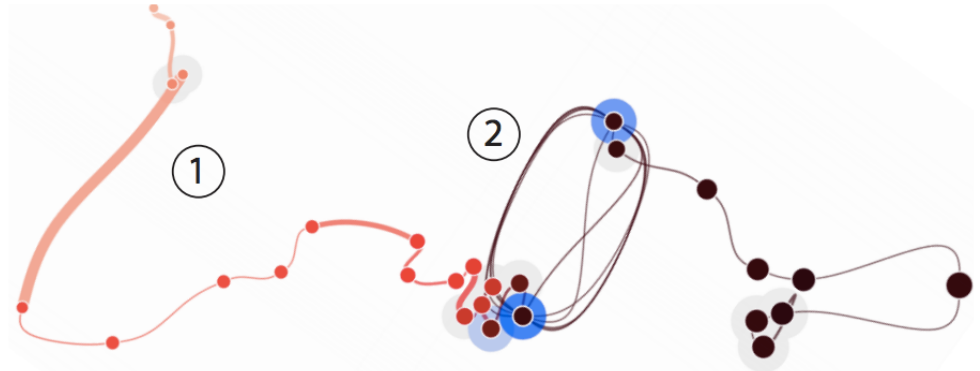


## Time curve:

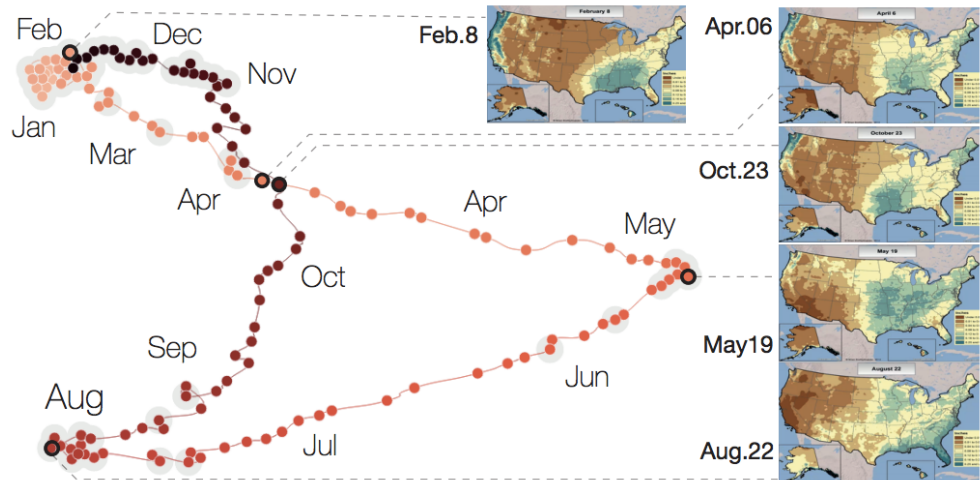


The temporal ordering of data cases is preserved.  
Spatial proximity now indicates similarity.

(a) Folding time



Wikipedia "Chocolate" Article



U.S. Precipitation over 1 Year

# Administrivia

# Final Project

Initial Project Prototype due **tonight Feb. 26th**  
Prototype Deliverables: must **submit link on Canvas**

## **Prototype Expectations:**

Outline of the overall project structure

Rough prototypes of visualizations and interactions

Basic descriptive (narrative) text

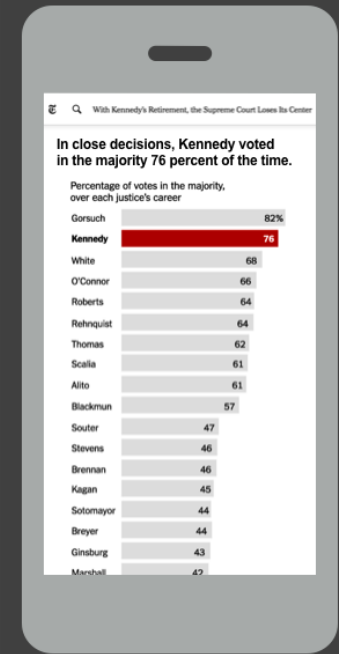
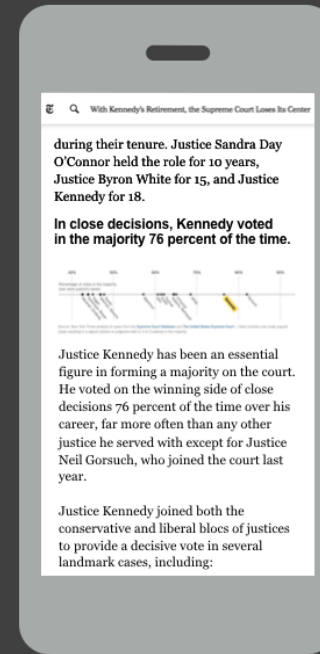
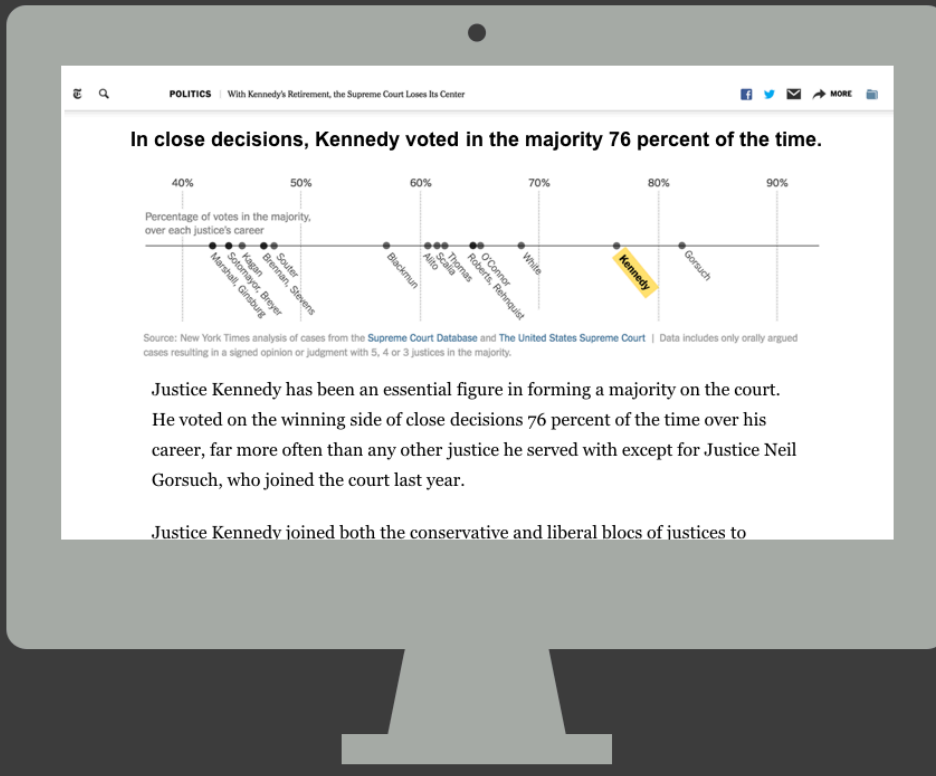
Discussion of any concerns or plans for next steps

***The more content you have on your page, the more specific feedback we can give to refine your project.***

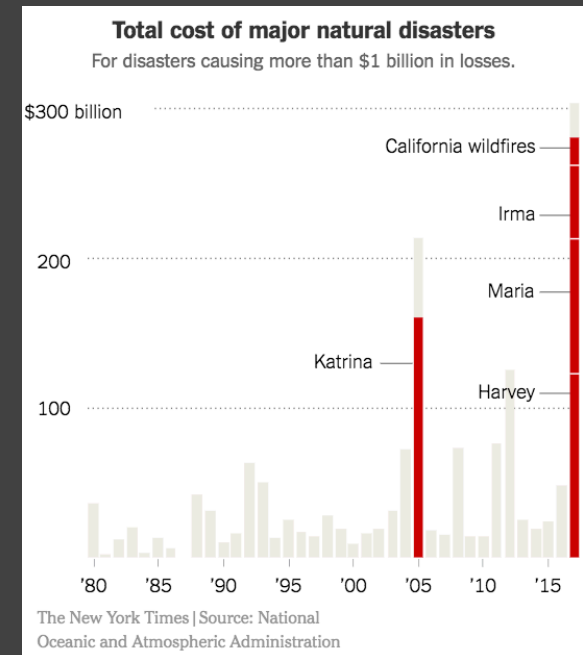
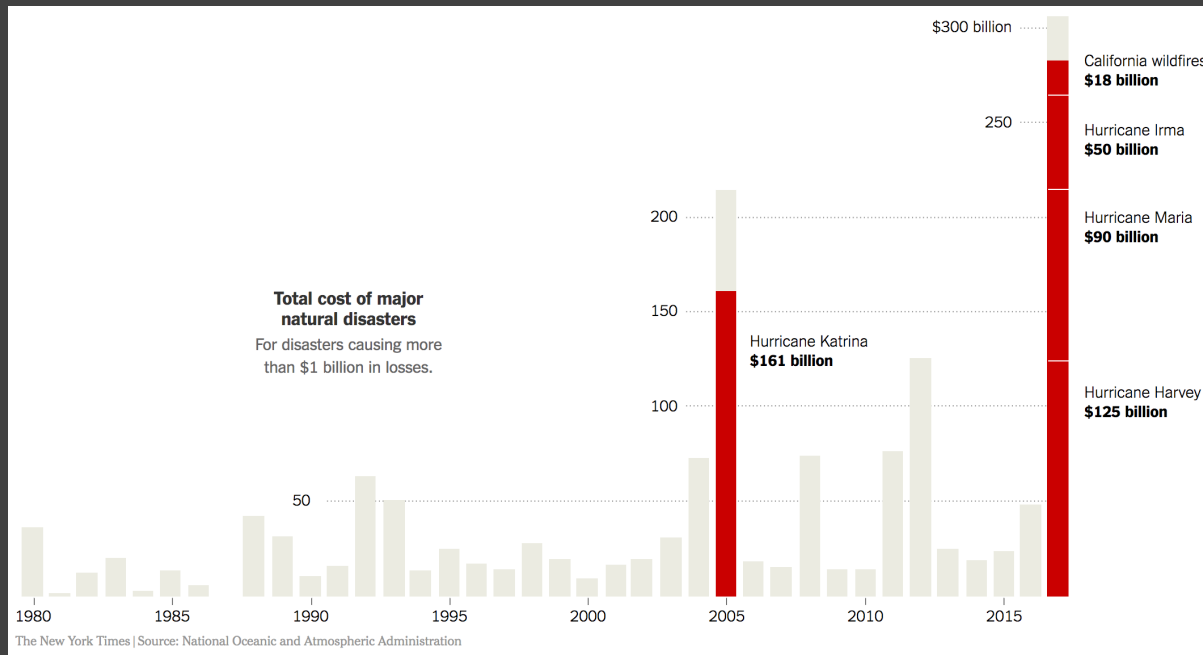
**BONUS TOPIC**

# **Responsive Visualization**

# Responsive Visualization



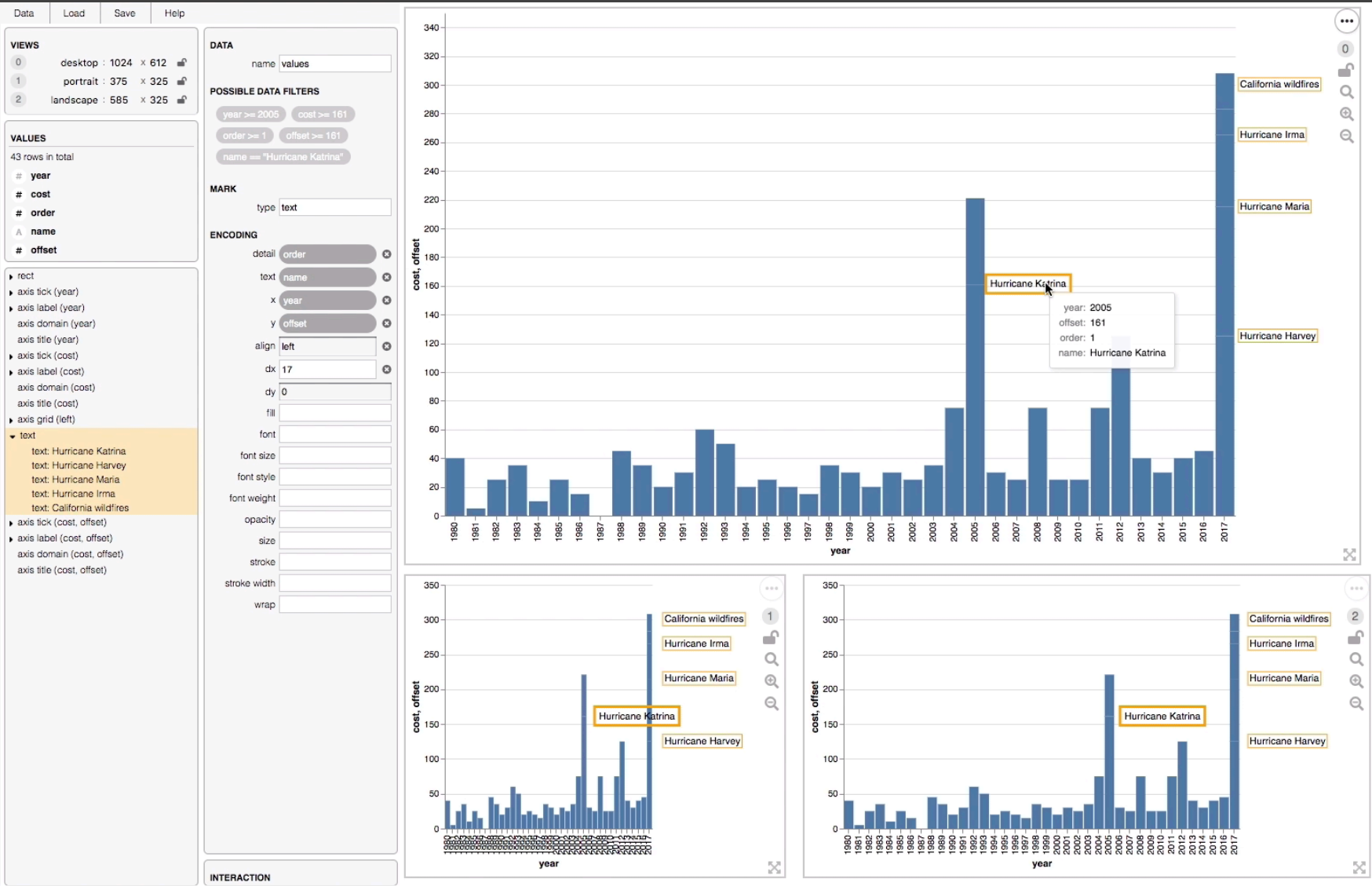
# Responsive Visualization [Hoffswell et al. 20]



# Responsive Visualization [Hoffswell et al. 20]

Action	Number of Visualizations (Portrait)										
no changes									6	205	
resize		1					7	1	172		
reposition	1	2			22		19	24	59	71	1
add	5	2		2	2		1	16	1	2	7
modify		3		2	1	4	3	29	1	7	5
remove	3	20	13	11	2		29	41		10	23
	axis	axis labels	axis ticks	gridlines	legend	data	marks	labels	title	view	interaction

# Responsive Visualization [Hoffswell et al. 20]





# Basic Selection Methods

## Point Selection

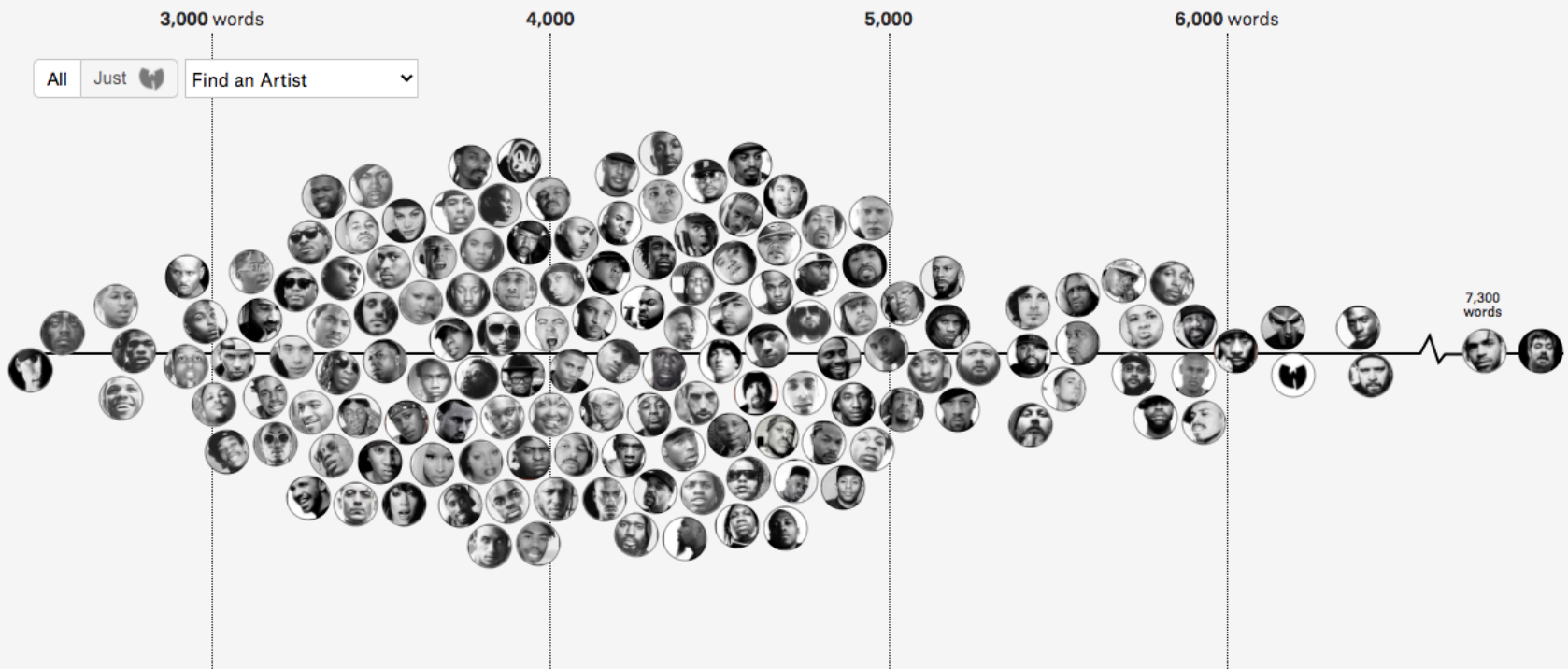
Mouse Hover / Click

Touch / Tap

Select Nearby Element (e.g., Bubble Cursor)

# Desktop vs. Mobile Tooltips

# of Unique Words Used Within Artist's First 35,000 Lyrics



Notes/sources:

All lyrics are via [Genius](#).

Right now we have at least 50%, sometimes 60% or 70%... of our readers that come through mobile phones to our site.

Gregor Aisch, *Information+ Conference 2016*

Right now we have at least 50%, sometimes 60% or 70%... of our readers that come through mobile phones to our site... Nobody is interacting with news graphics... it's like 10% of all users click that button.

Gregor Aisch, *Information+ Conference 2016*

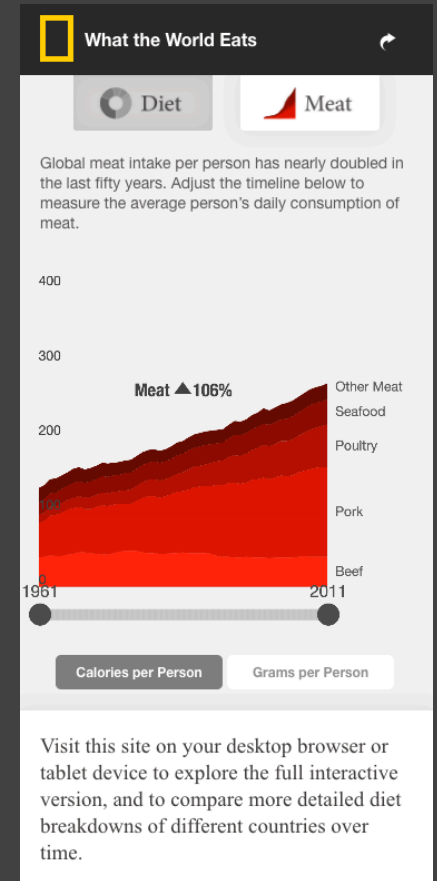
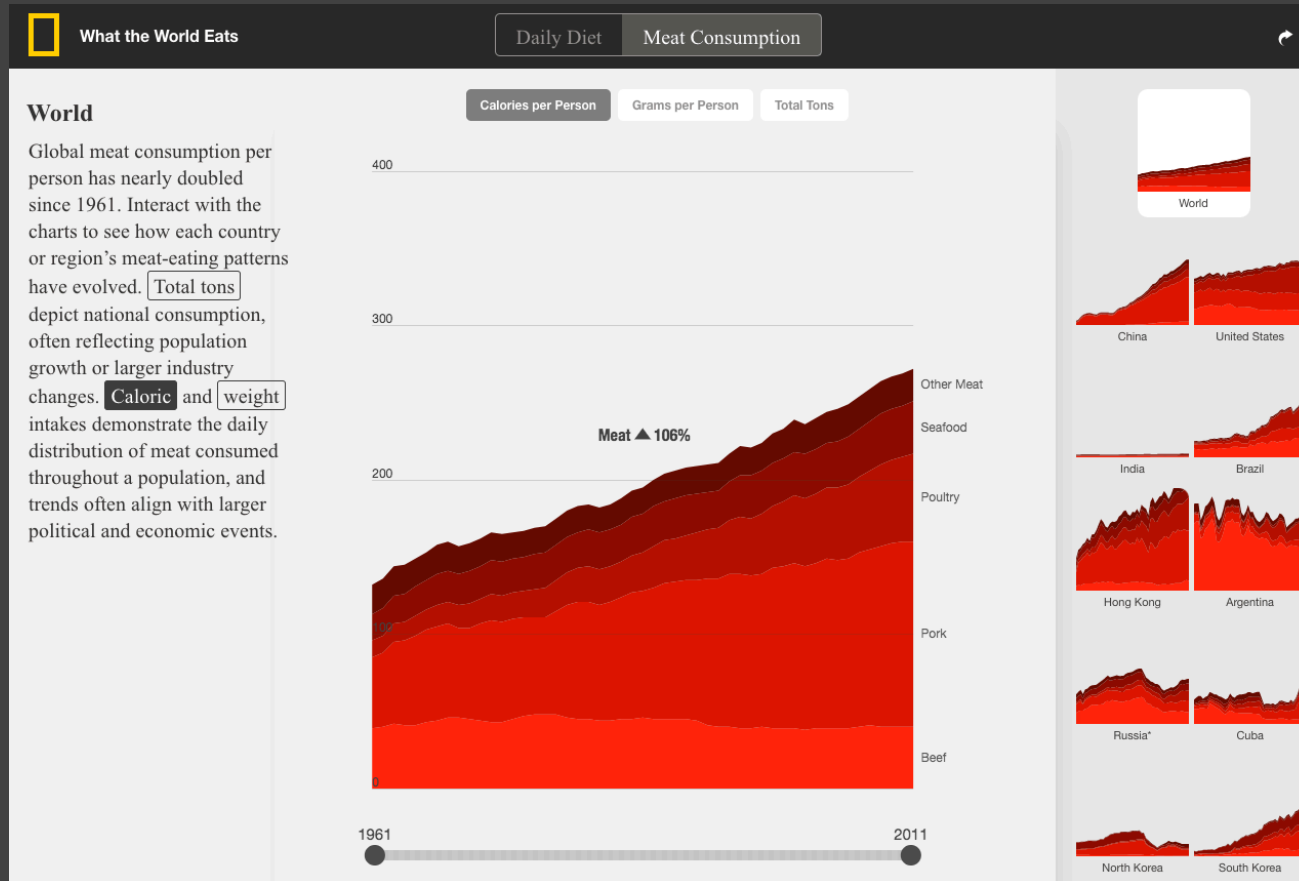
82% of mobile readers advanced through at least some of the content, even though they needed to dismiss a warning about download size; however, only 34% attempted to tune the guitar and just 6% tuned all six strings.

Conlen et al., *EuroVis 2019*

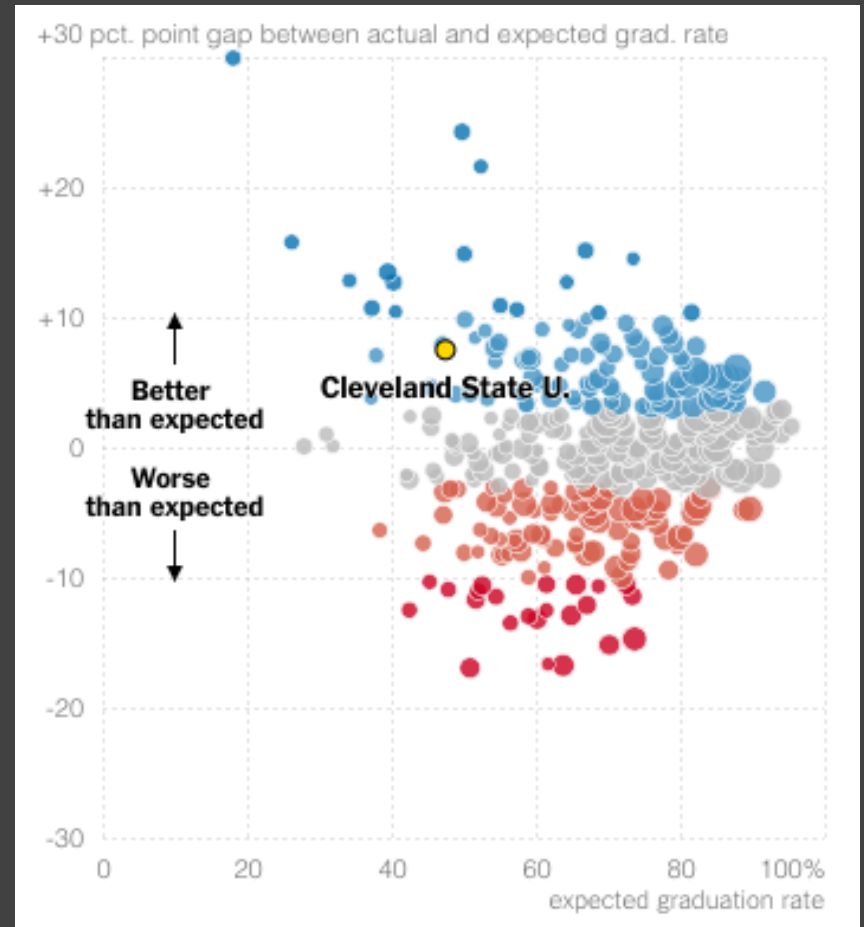
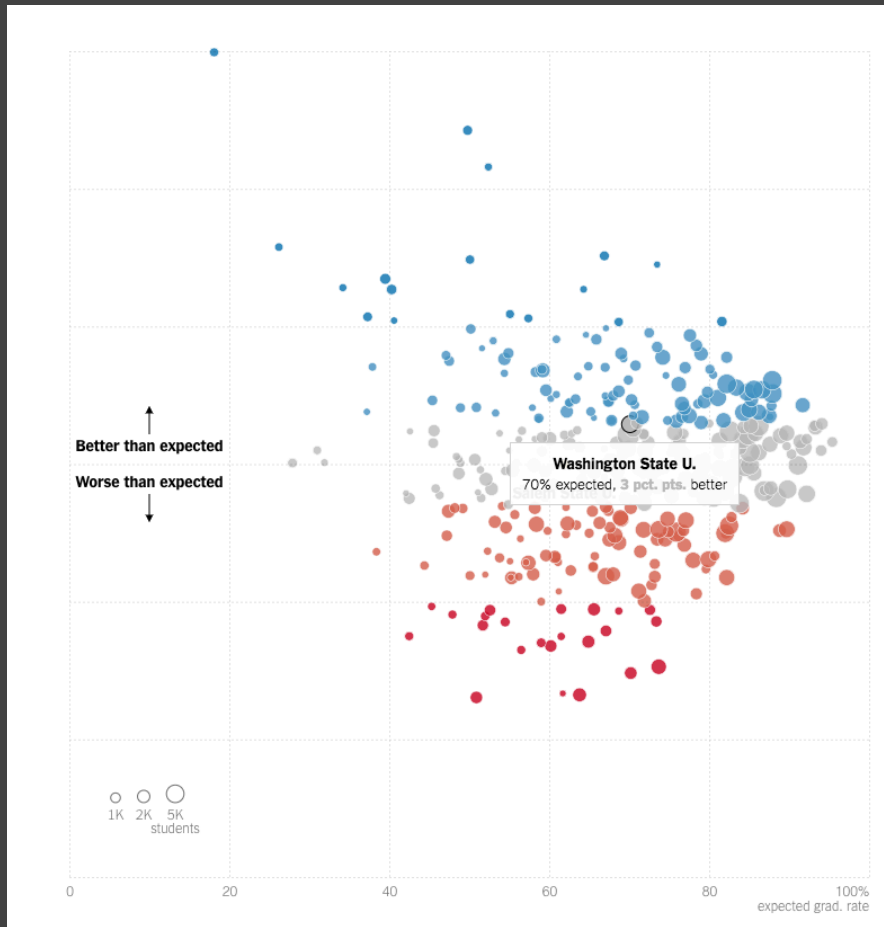
82% of mobile readers advanced through at least some of the content, even though they needed to dismiss a warning about download size; however, only 34% attempted to tune the guitar and just 6% tuned all six strings.

These observations suggest that mobile users are willing to engage with interactive content, and that the specific interactions should have been refined to better accommodate them.

# Interactions Disabled

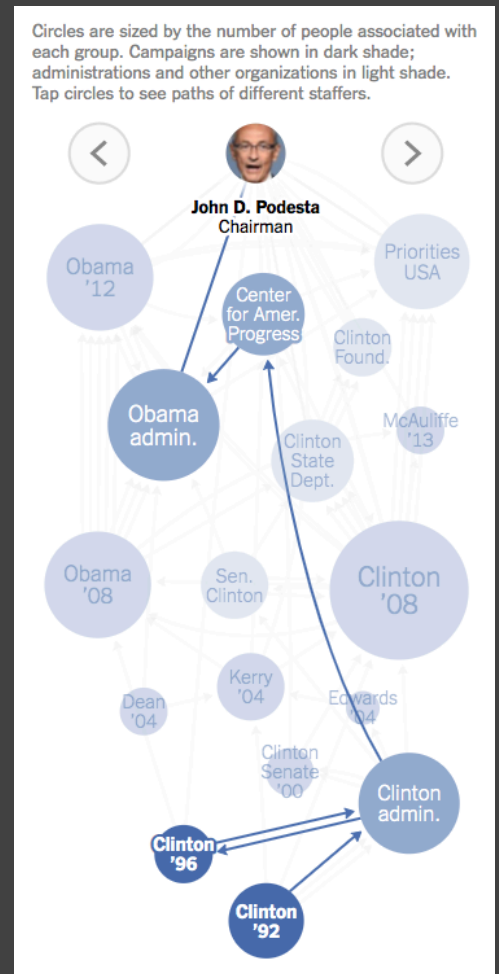
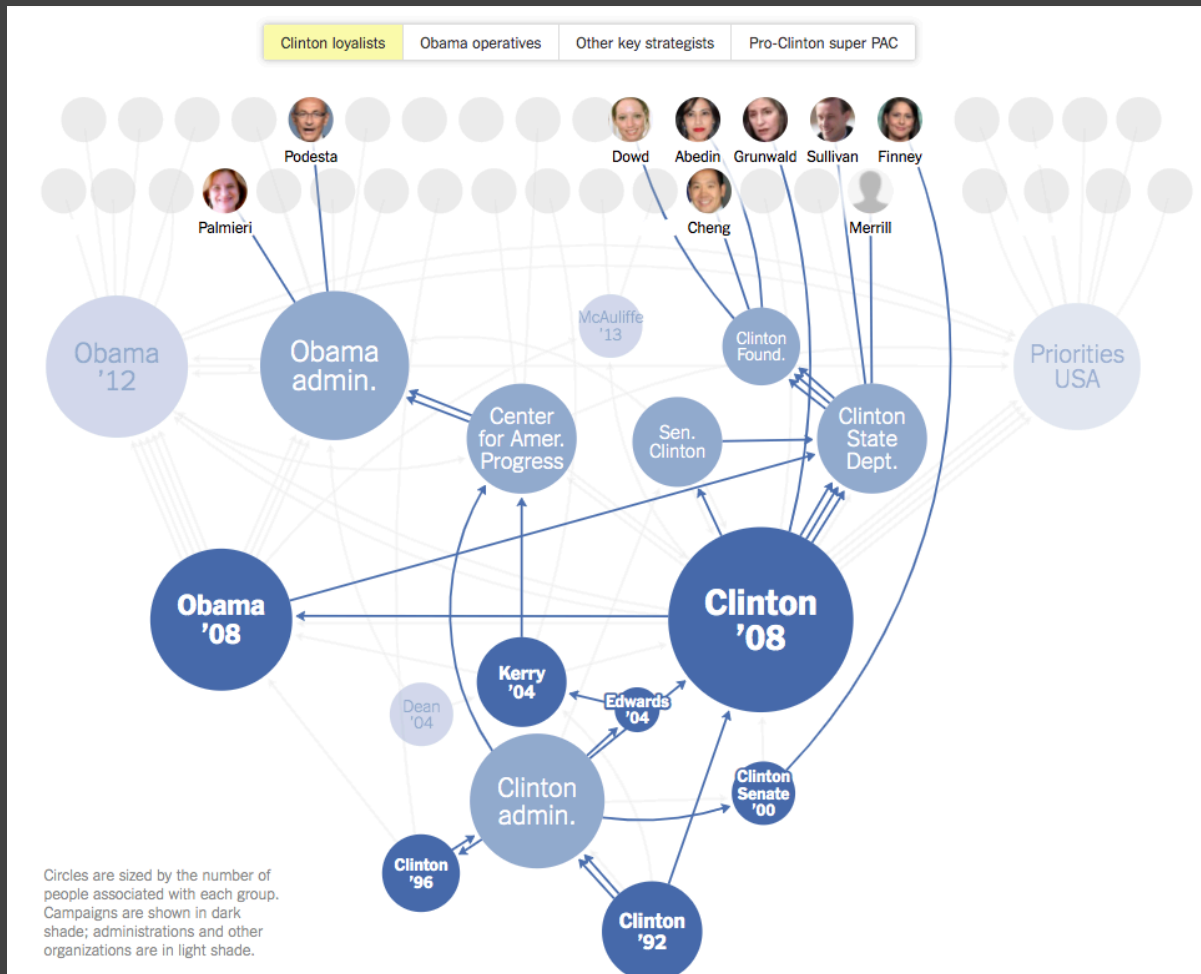


# Interactions Previewed





# Interactions Simplified



# Responsive Visualization Summary

**Good visualizations are task dependent**

Who is the audience and what is the task?

Pick the right interaction technique

**Visualizations are not one size fits all**

Context might change user goals