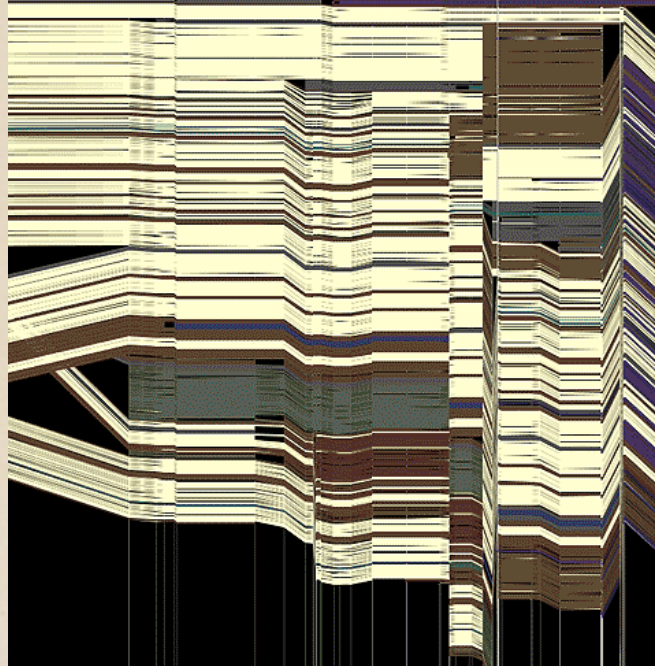
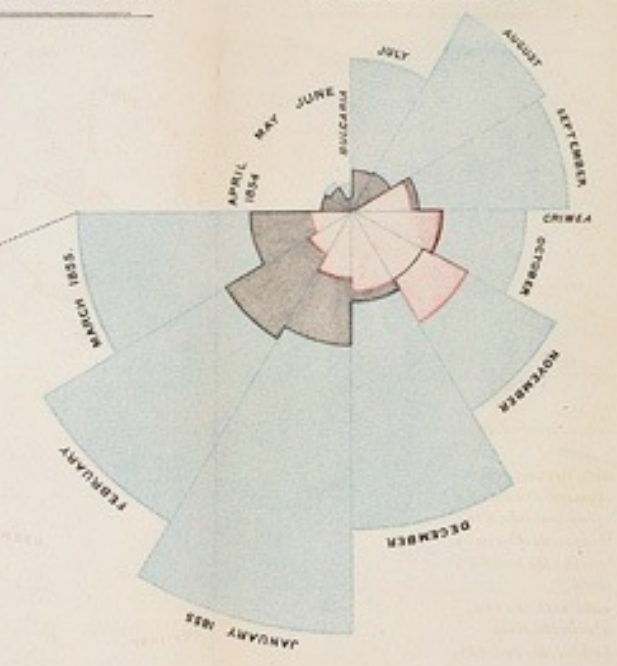


# CSE 412 - Intro to Data Visualization

# Hierarchies



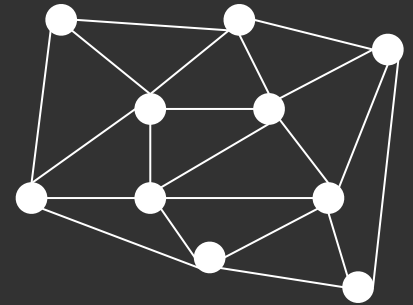
Jane Hoffswell University of Washington

# Graphs and Trees

## Graphs

Model relations among data

*Nodes and edges*

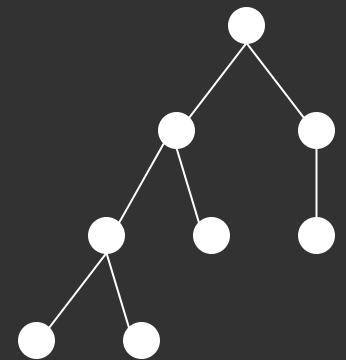


## Trees

Graphs with hierarchical structure

Connected graph with  $N-1$  edges

Nodes as *parents* and *children*



# Spatial Layout

A primary concern of tree/graph drawing is the spatial arrangement of nodes and edges.

Often (but not always) the goal is to effectively depict the graph structure:

- Connectivity, path-following
- Topological distance
- Clustering / grouping
- Ordering (e.g., hierarchy level)

# Applications

Tournaments

Organization Charts

Genealogy

Diagramming (e.g., Visio)

Biological Interactions (Genes, Proteins)

Computer Networks

Social Networks

Simulation and Modeling

Integrated Circuit Design

# Network Analysis Tasks [Pretorius '13]

**Structure-based:** relationships and connectivity

**Attribute-based:** specific node/link attributes

**Browsing:** understand paths in the data

**Estimation:** summarization and temporal changes

# Network Analysis Tasks [Pretorius '13]

**Structure-based:** relationships and connectivity

*Find all of the friends of friends for Taylor.*

*Find all of the people who are friends with Jordan and Alex.*

*Six degrees of separation: shortest path between two individuals.*

**Attribute-based:** specific node/link attributes

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**Attribute-based:** specific node/link attributes

*Find all "students" attending CSE412.*

*Find all the "friends" and "family" of Alex.*

**Browsing:** understand paths in the data

**Estimation:** summarization and temporal changes

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*Find all the "friends" and "family" of Alex.*

**Browsing:** understand paths in the data

*Find Alex's friend Taylor, and then Taylor's friend Jordan.*

**Estimation:** summarization and temporal changes



# Network Analysis Tasks [Pretorius '13]

**Structure-based:** relationships and connectivity

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*Six degrees of separation: shortest path between two individuals.*

**Attribute-based:** specific node/link attributes

*Find all "students" attending CSE412.*

*Find all the "friends" and "family" of Alex.*

**Browsing:** understand paths in the data

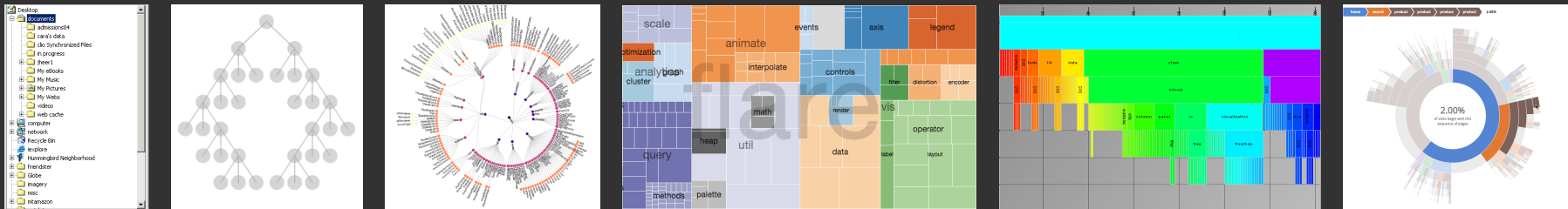
*Find Alex's friend Taylor, and then Taylor's friend Jordan.*

**Estimation:** summarization and temporal changes

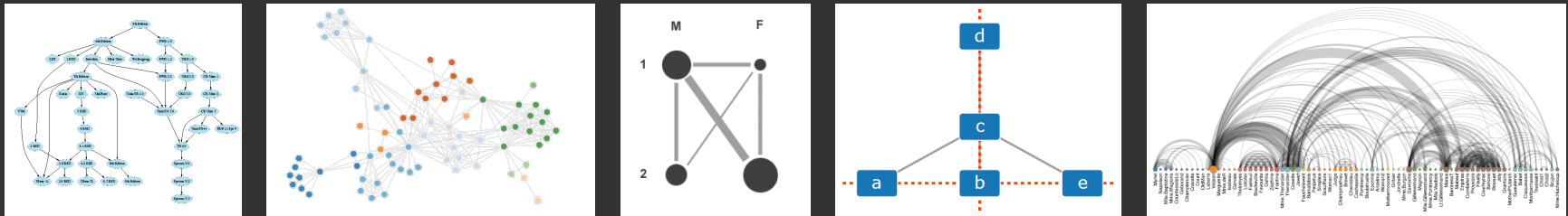
*How does Jordan's friend group change over the course of the year?*

# Topics

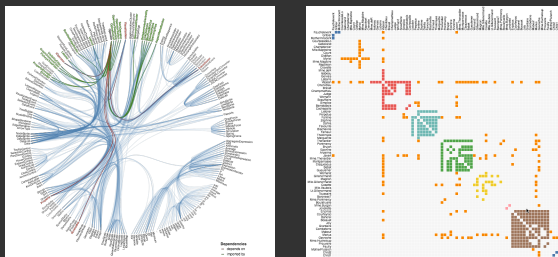
## TODAY - Tree Visualization



## Wed - Graph Layout: Node-Link Diagrams



## Wed - Alternative Visualizations and Techniques



Select an image to jump to those slides.

# Tree Visualization

# Tree Visualization

## Indentation

Linear list, indentation encodes depth



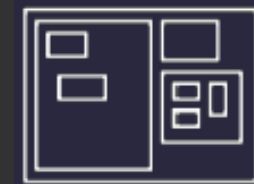
## Node-Link diagrams

Nodes connected by lines/curves



## Enclosure diagrams

Represent hierarchy by enclosure



## Layering

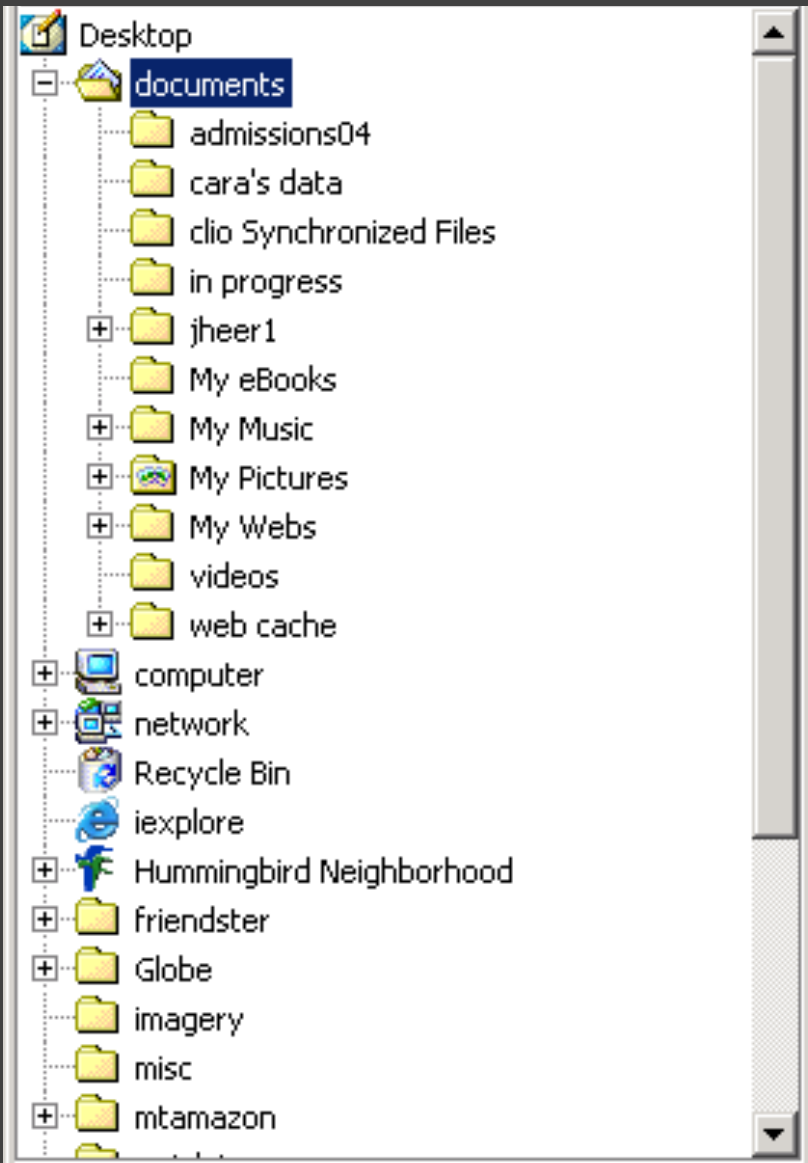
Relative position and alignment



Typically fast:  $O(n)$  or  $O(n \log n)$ , interactive layout

# Indentation

# Indentation



Places all items along vertically spaced rows

Indentation used to show parent/child relationships

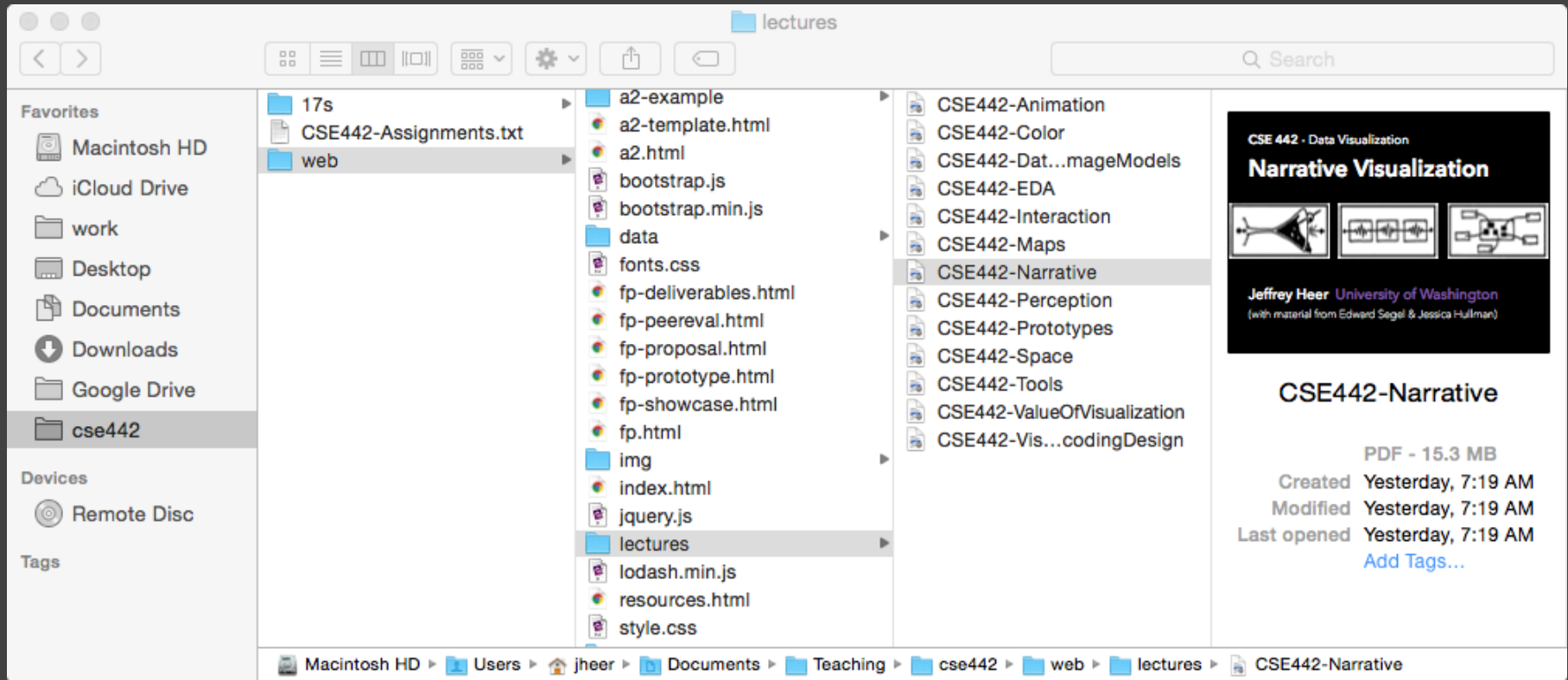
Commonly used as a component in an interface

Breadth and depth contend for space

Often requires a great deal of scrolling

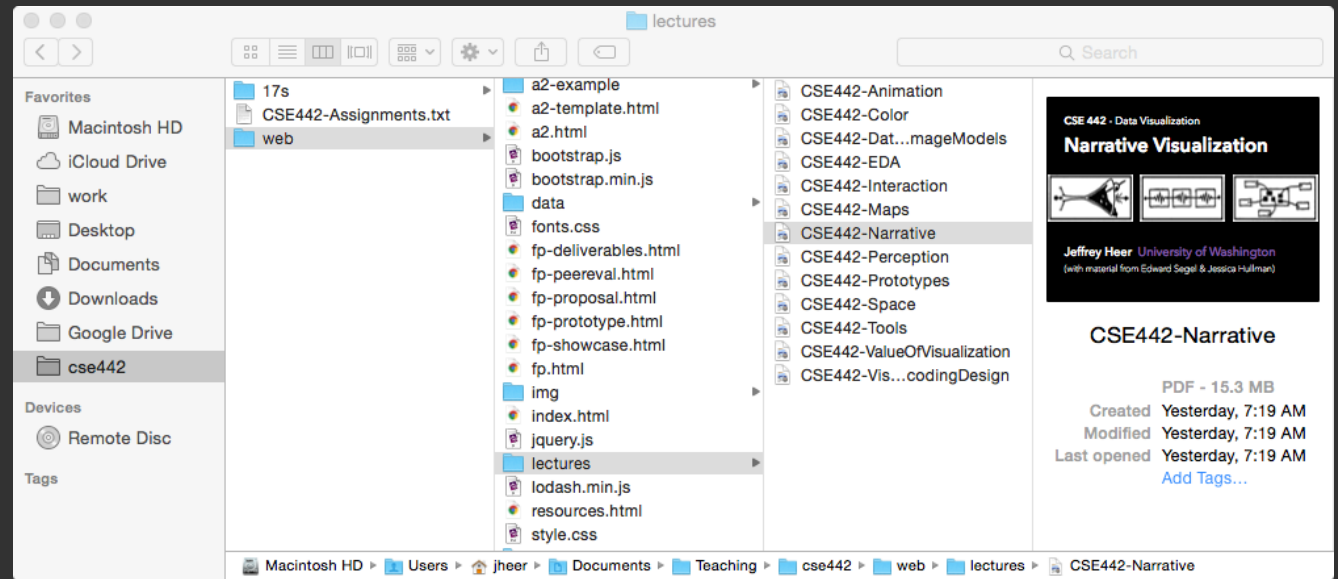
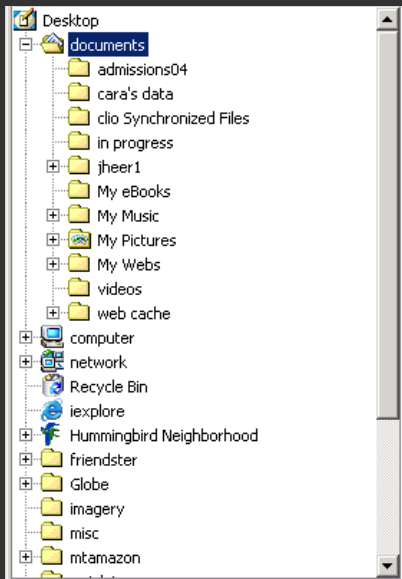


# Single-Focus (Accordion) List



Separate breadth & depth along 2D.  
Focus on a single path at a time.

# What tasks are these good for?



## Benefits:

Navigation + Browsing, Parent-Child Relationships

## Disadvantages:

Estimation, Comparison, Network Overview



# Node-Link Diagrams

# Node-Link Diagrams



Nodes are distributed in space, connected by straight or curved lines

Typical approach is to use 2D space to break apart breadth and depth

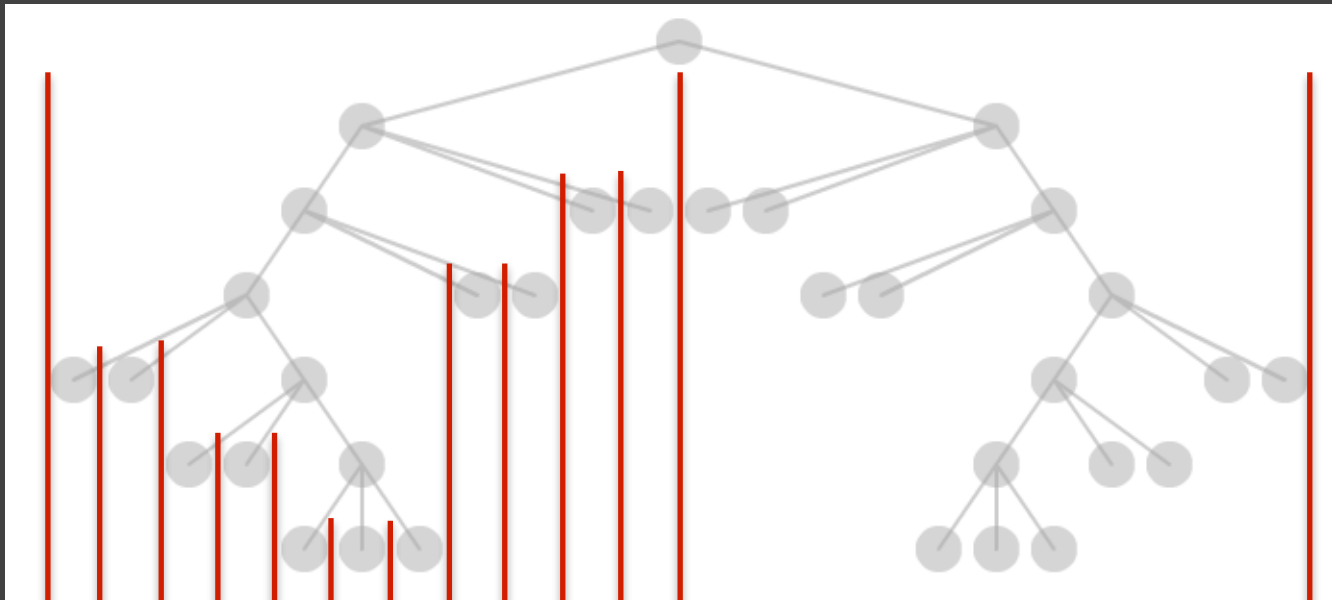
Often space is used to communicate hierarchical orientation (e.g., towards authority or generality)

# Naïve Recursive Layout

Repeatedly divide space for subtrees by leaf count

Breadth of tree along one dimension

Depth along the other dimension



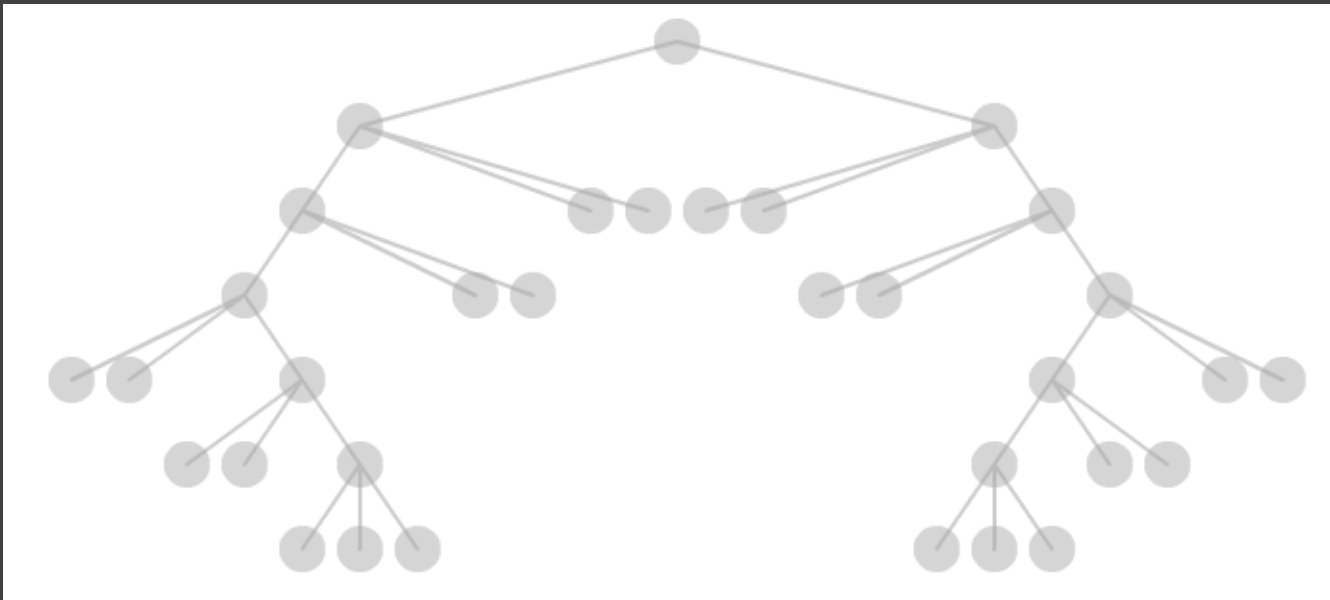
# Naïve Recursive Layout

Repeatedly divide space for subtrees by leaf count

Breadth of tree along one dimension

Depth along the other dimension

Problems?



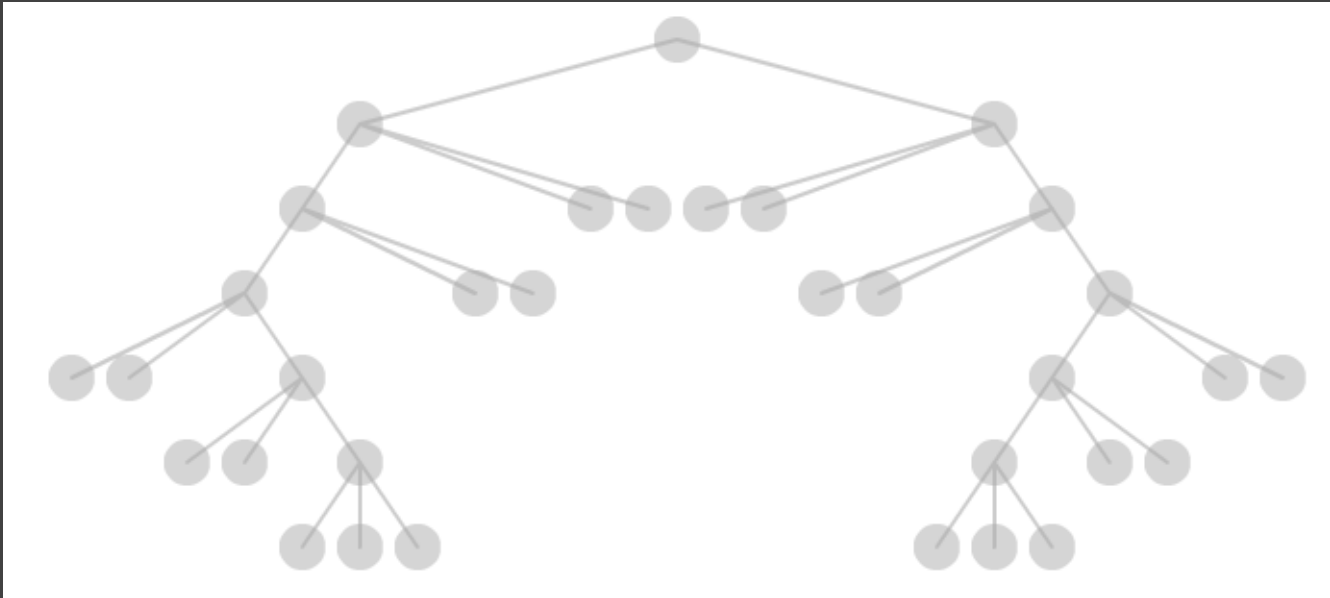
# Naïve Recursive Layout

Repeatedly divide space for subtrees by leaf count

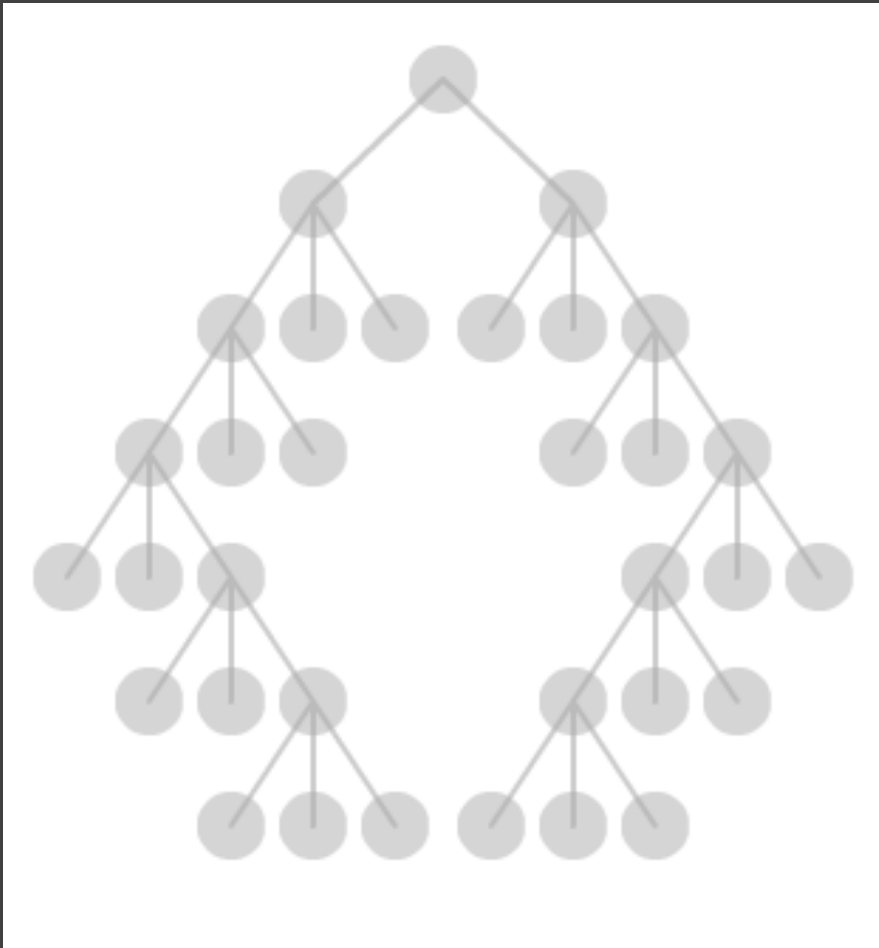
Breadth of tree along one dimension

Depth along the other dimension

Problem: exponential growth of breadth



# Reingold & Tilford's "Tidy" Layout

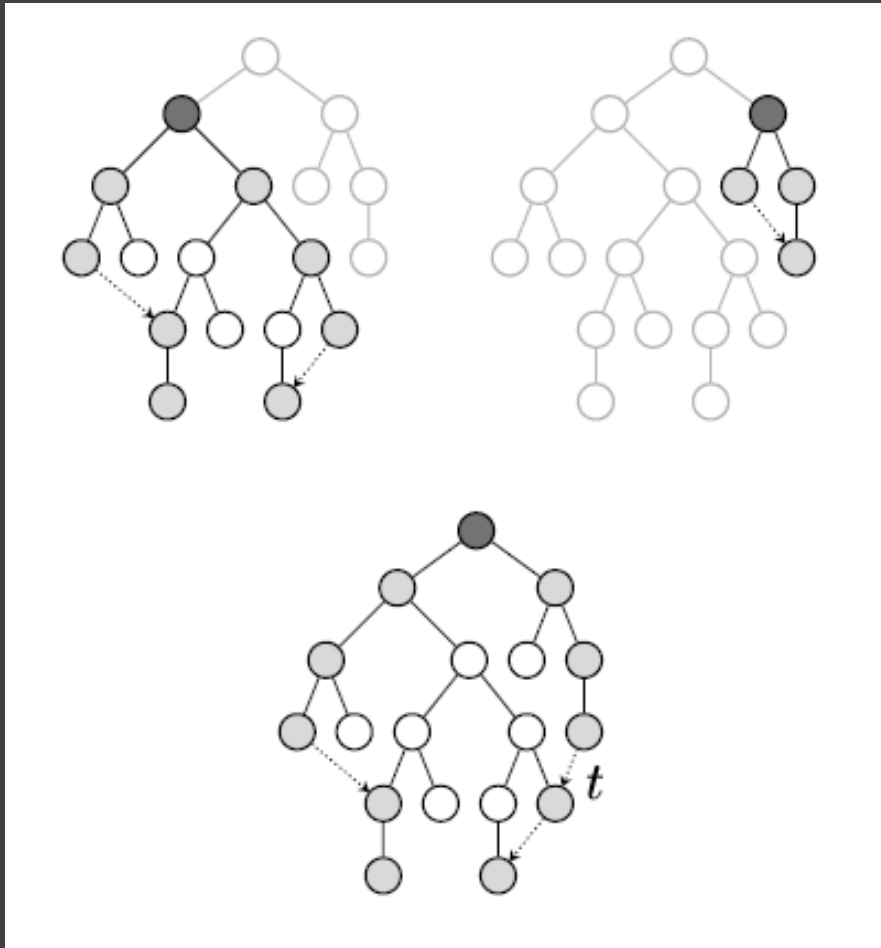


Goal: make smarter use of space, maximize density and symmetry.

Originally binary trees, extended by Walker to cover general case.

Corrected by Buchheim et al. to achieve a linear time algorithm.

# Reingold-Tilford Layout



## Design Considerations

Clearly encode depth

No edge crossings

Draw isomorphic subtrees identically (same shape)

Preserve layout ordering and symmetry

*Compact, space-saving layout (don't waste space)*

# Reingold-Tilford Layout

## **Initial bottom-up (post-order) traversal of the tree**

Y-coordinates based on tree depth

X-coordinates initialized to zero

## **At each parent node: merge left and right subtrees**

Shift right subtree as close as possible to the left

Compute efficiently by maintaining subtree boundaries

Center the parent node above its children

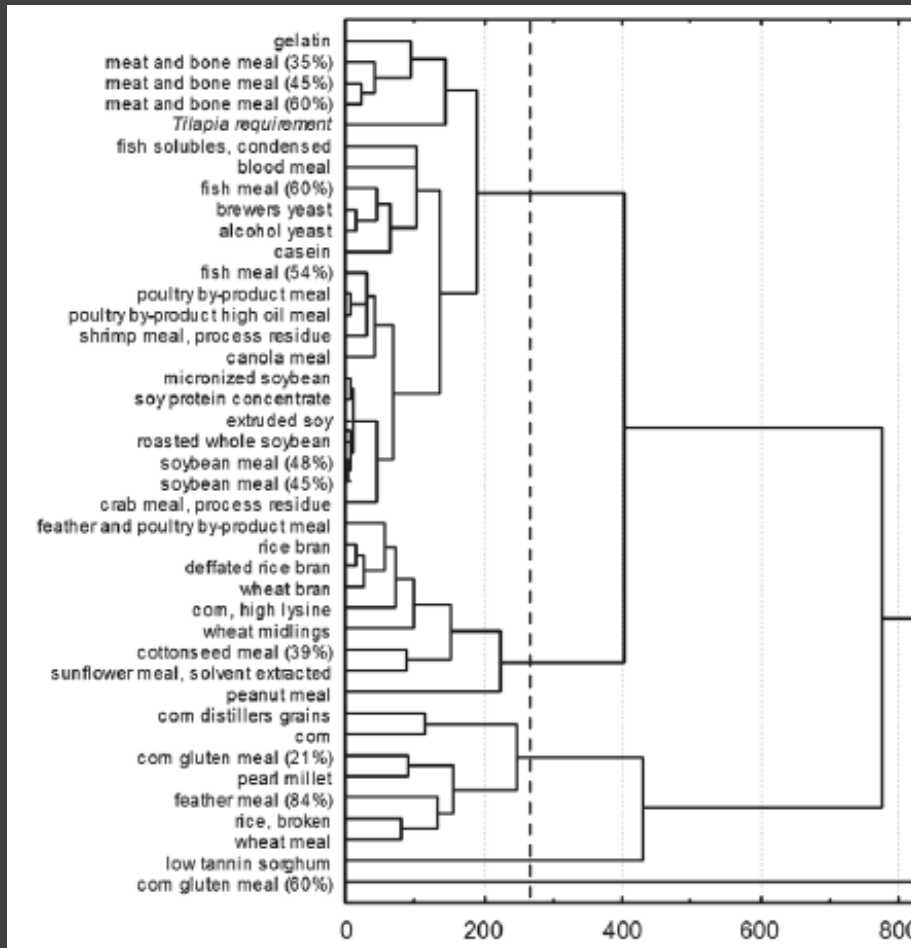
Record "shift" position offset for right subtree

## **Final top-down (pre-order) traversal to set X-coordinates**

Sum the aggregated shifts



# Cluster Dendrograms

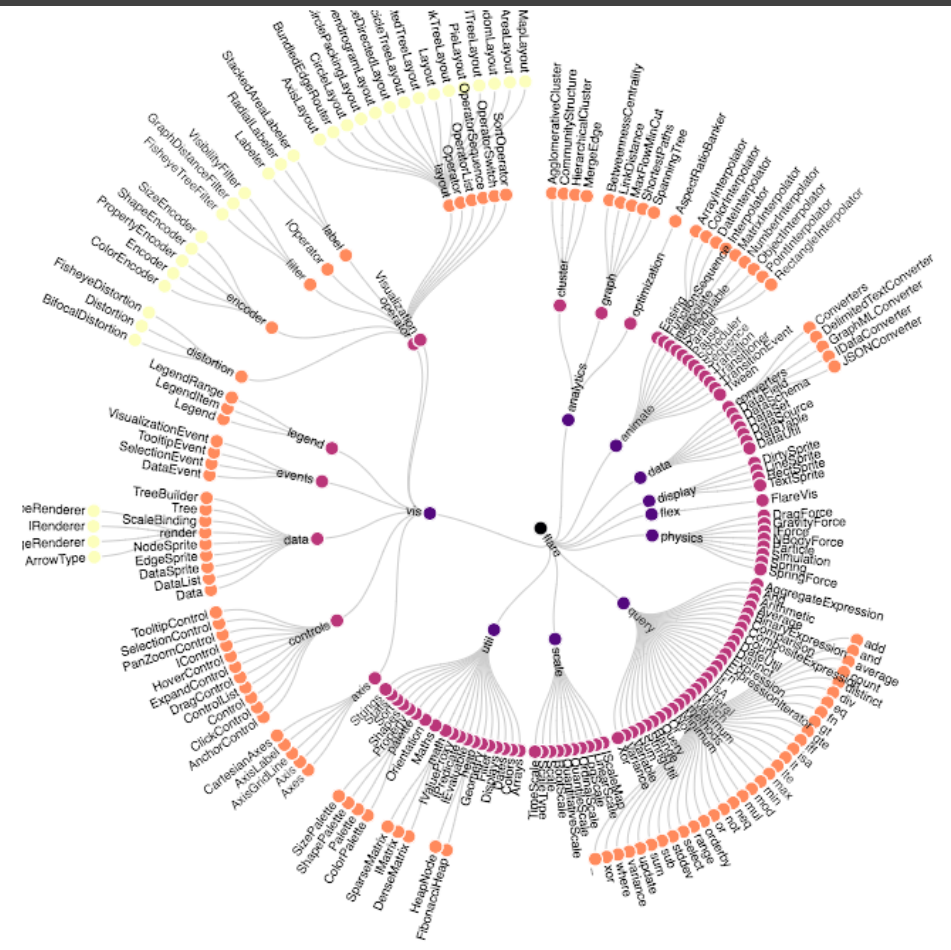


Depicts cluster trees produced by hierarchical clustering algorithms.

Leaf nodes arranged in a line, internal node depth indicates order/value at which clusters merge.

Naïve recursive layout with orthogonal two-segment edges.

# Radial Tree Layout



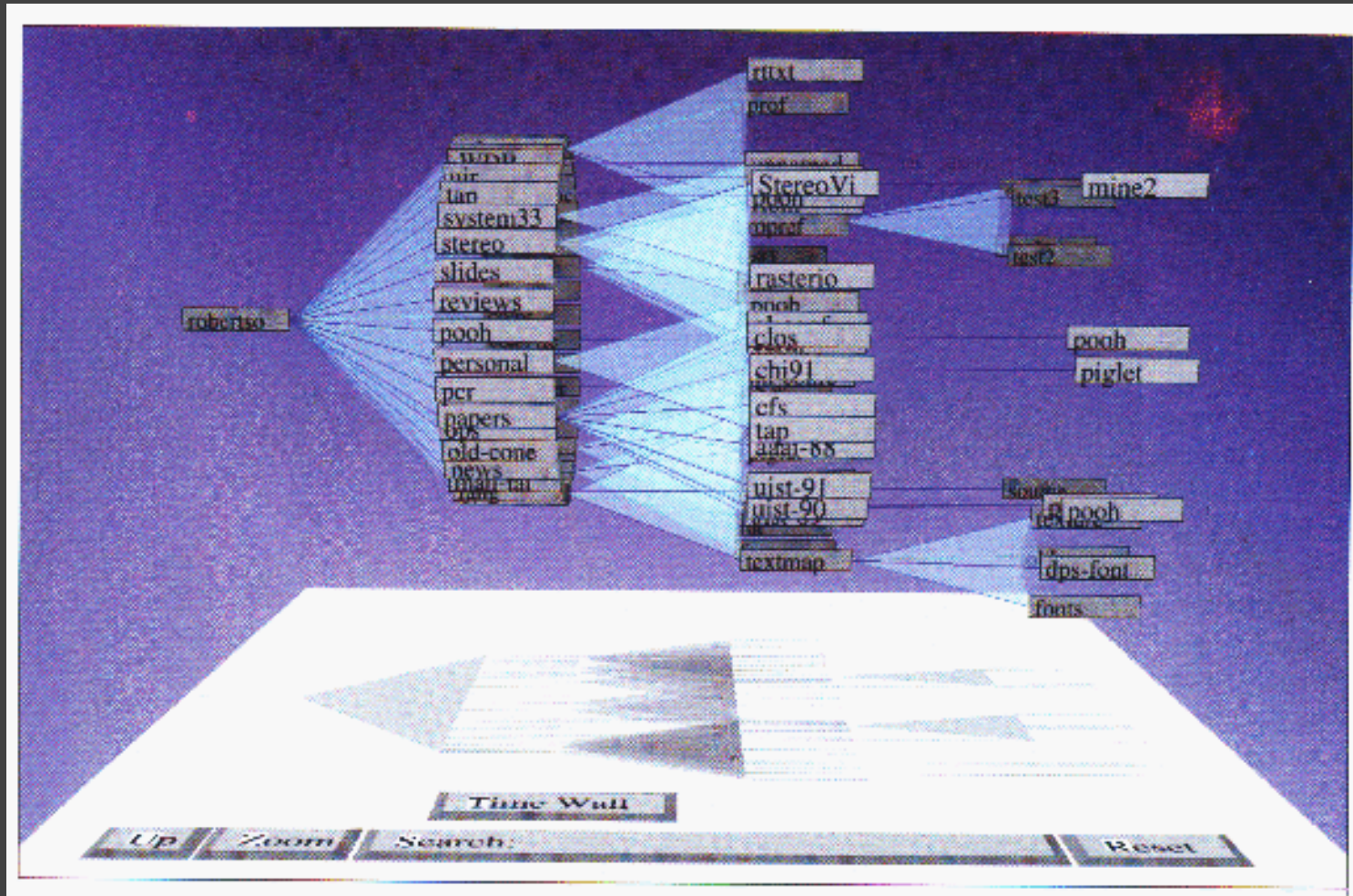
Node-link diagram in polar co-ordinates.

Radius encodes depth, with root in the center.

Angular sectors assigned to subtrees (often with naïve recursive layout).

Reingold-Tilford method can also be applied here.

# Cone Trees [Robertson 91]



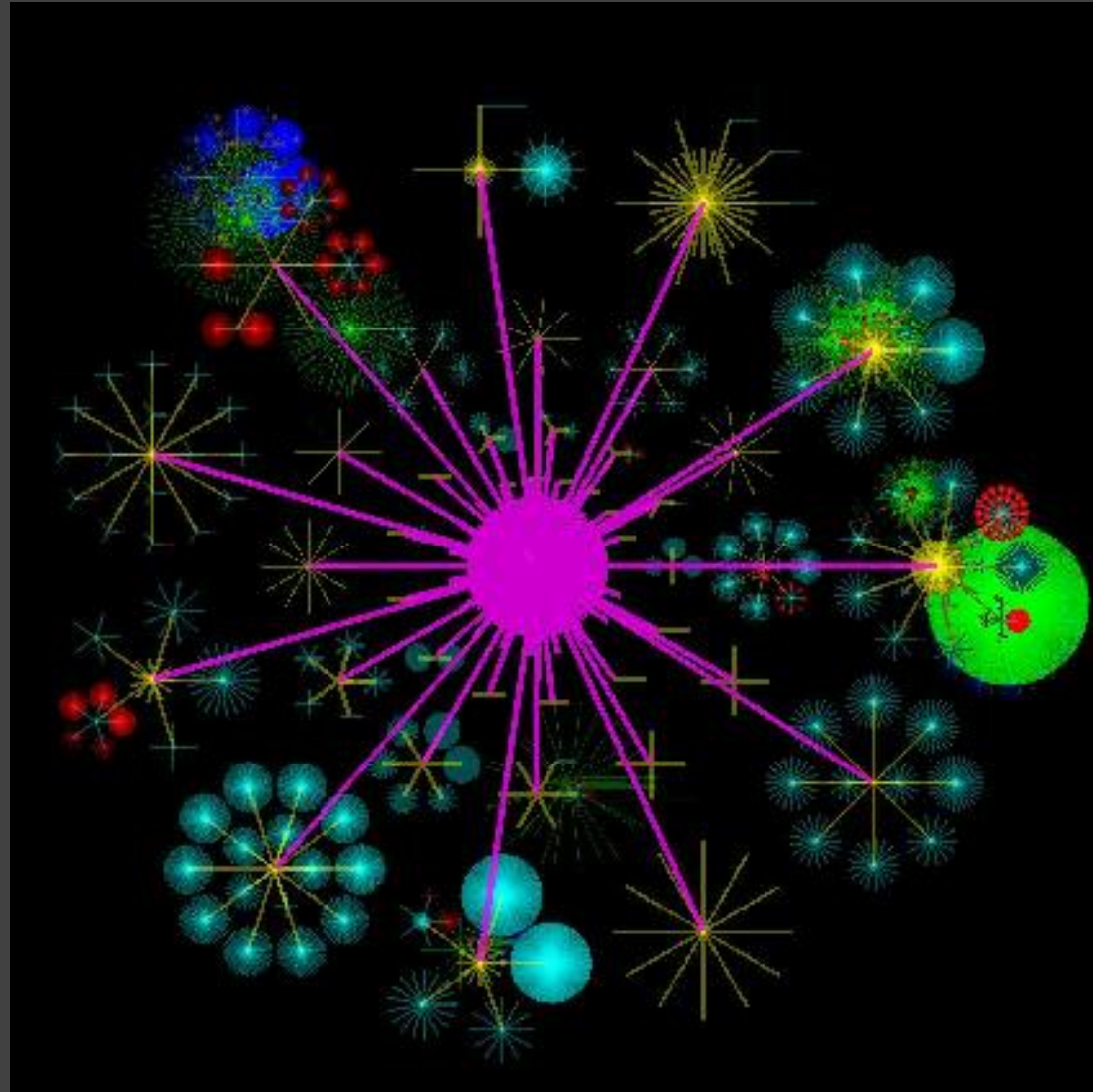
[Video](#)



# Balloon Trees

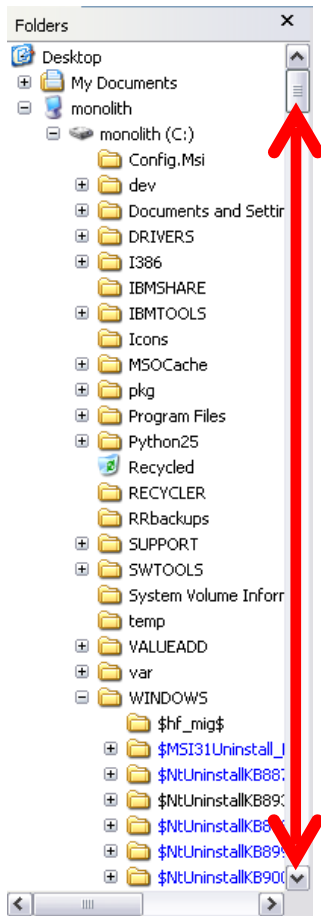
Described as a 2D  
variant of a Cone Tree.

Not just a flattening  
process: circles must  
not overlap.

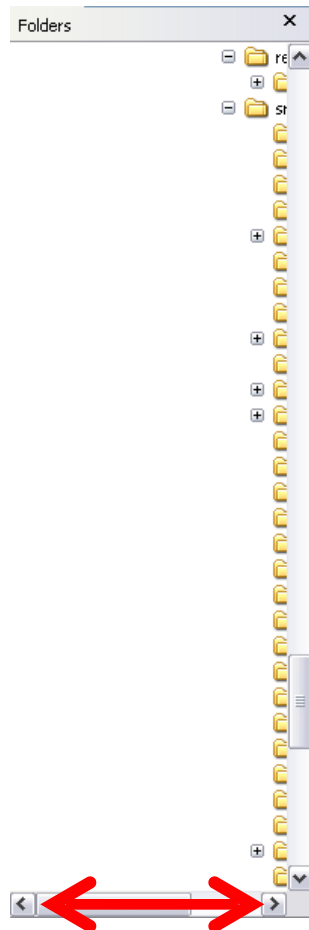


# Analysis Tasks: Focus+Context

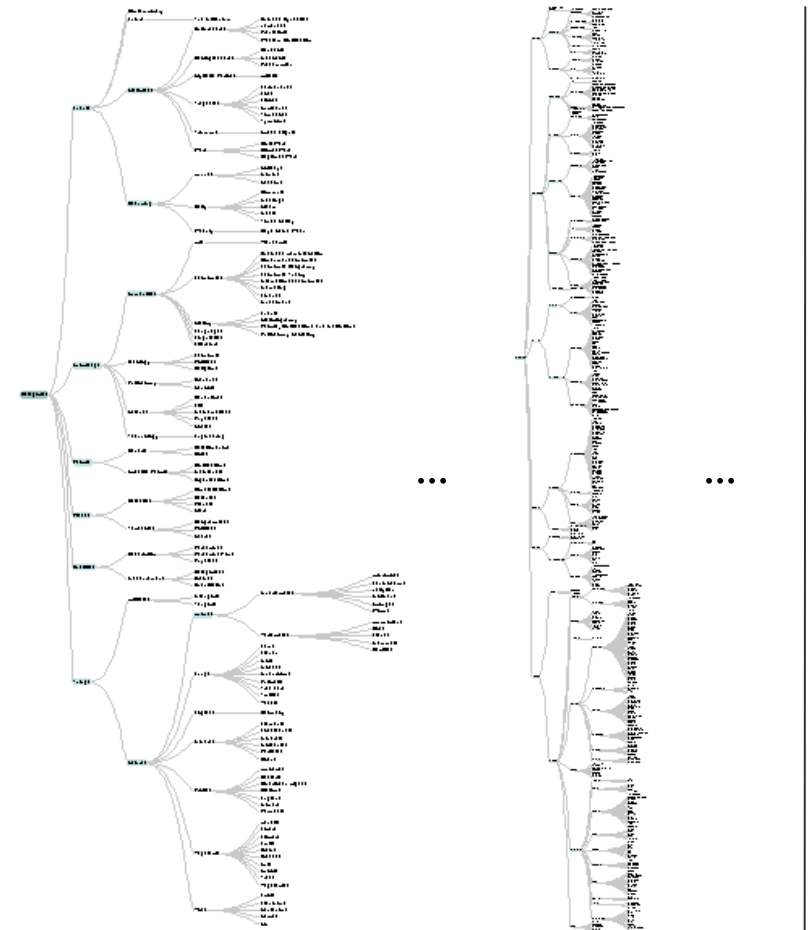
# Visualizing Large Hierarchies



...



...



Indented Layout

Reingold-Tilford Layout

# More Nodes, More Problems...

## **Scale**

Tree breadth often grows exponentially  
Even with tidy layout, quickly run out of space

## **Possible Solutions**

Filtering

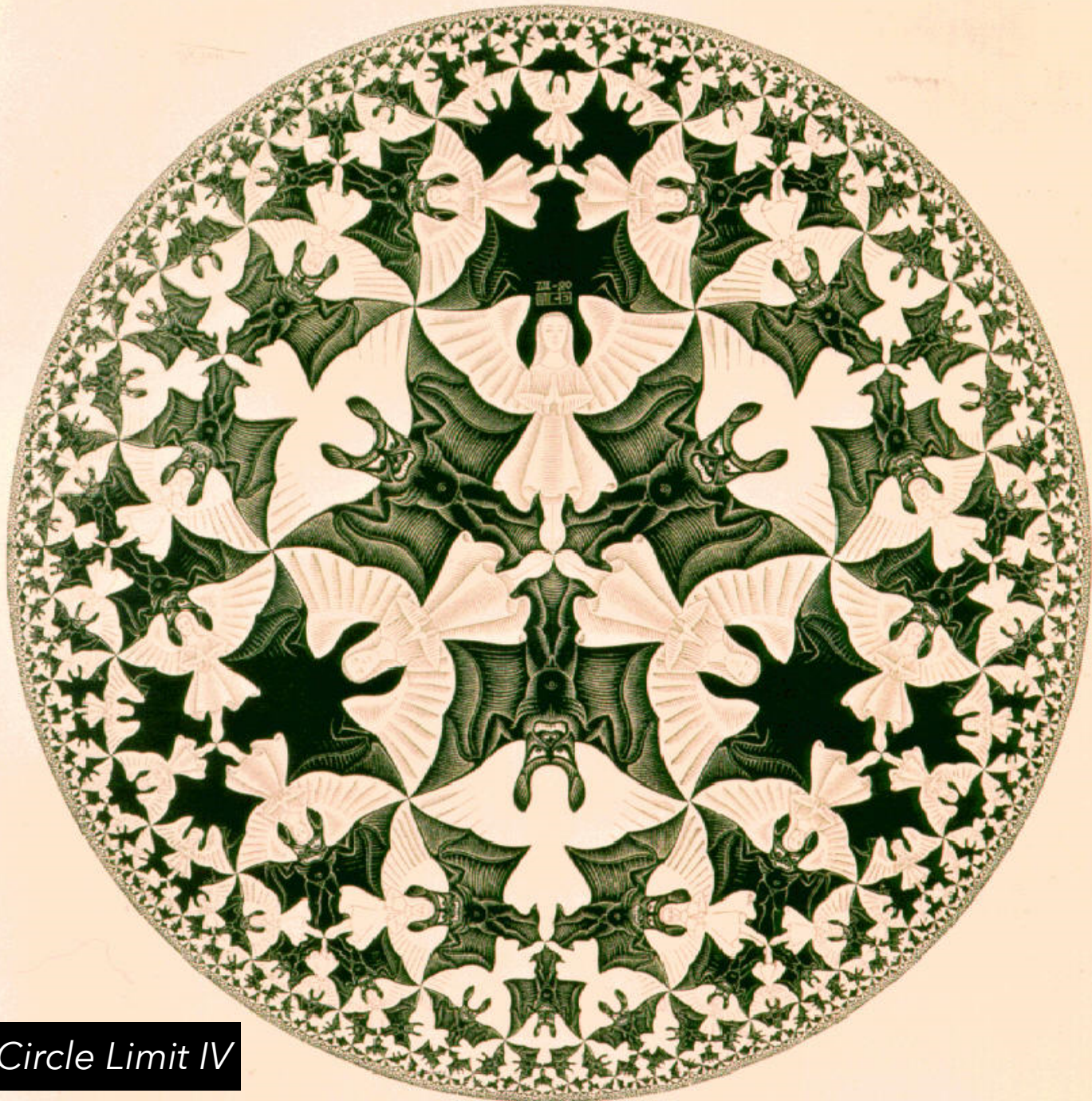
Focus+Context

Scrolling or Panning

Zooming

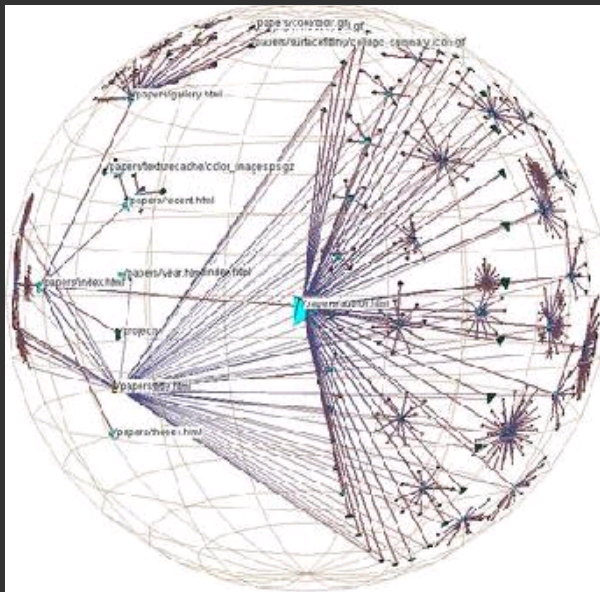
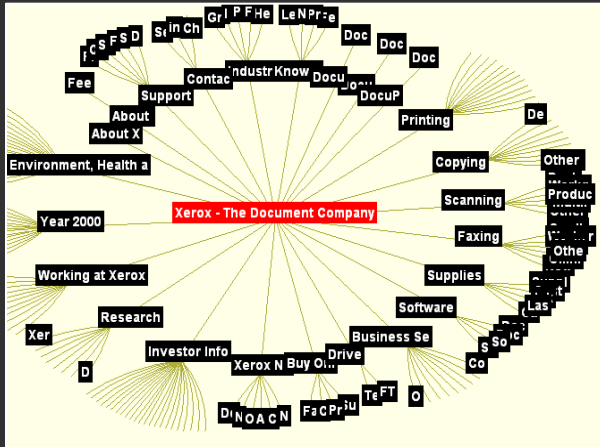
Aggregation





MC Escher, *Circle Limit IV*

# Hyperbolic Layout

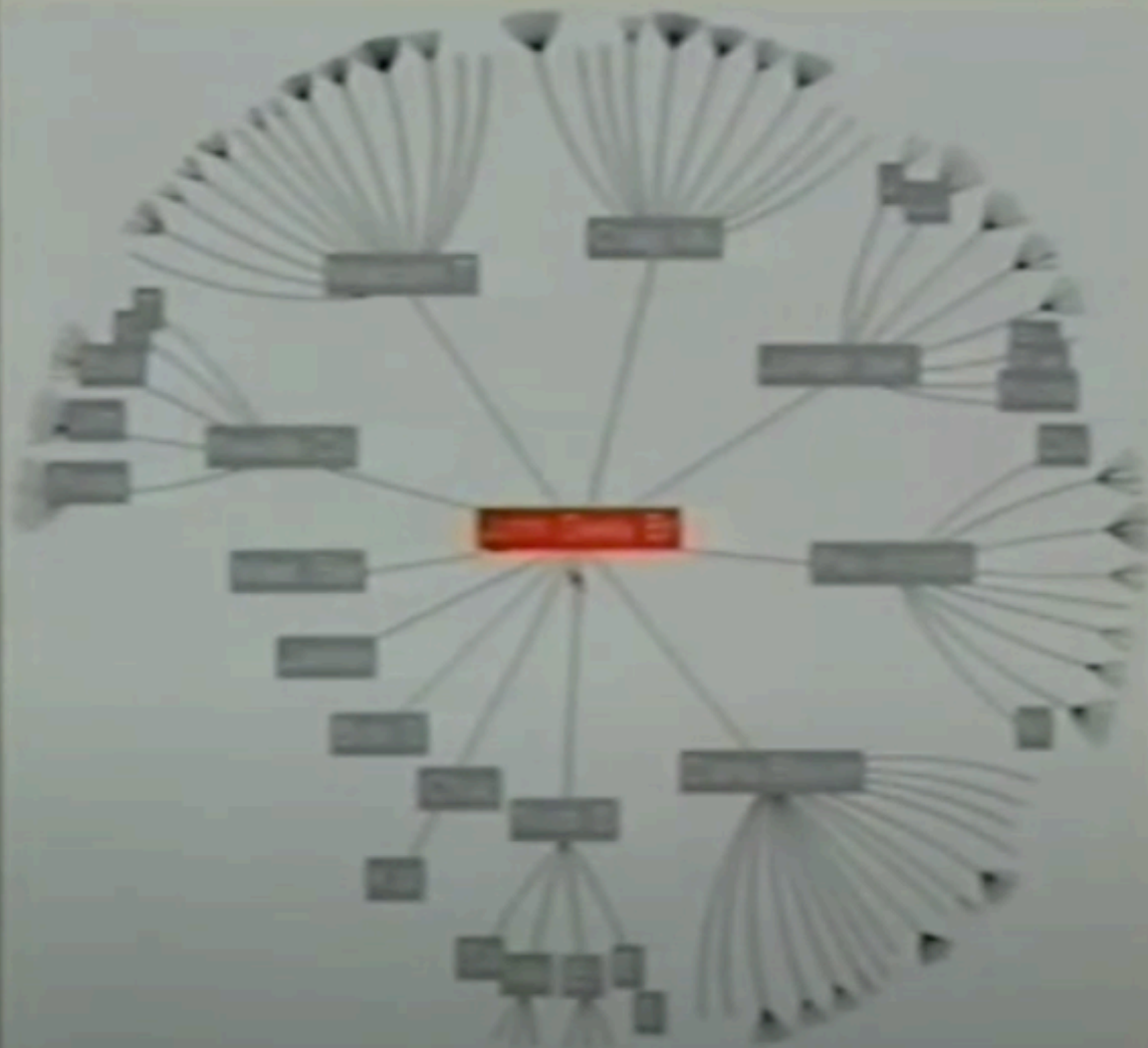


Perform tree layout in hyperbolic geometry, project the result on to the Euclidean plane.

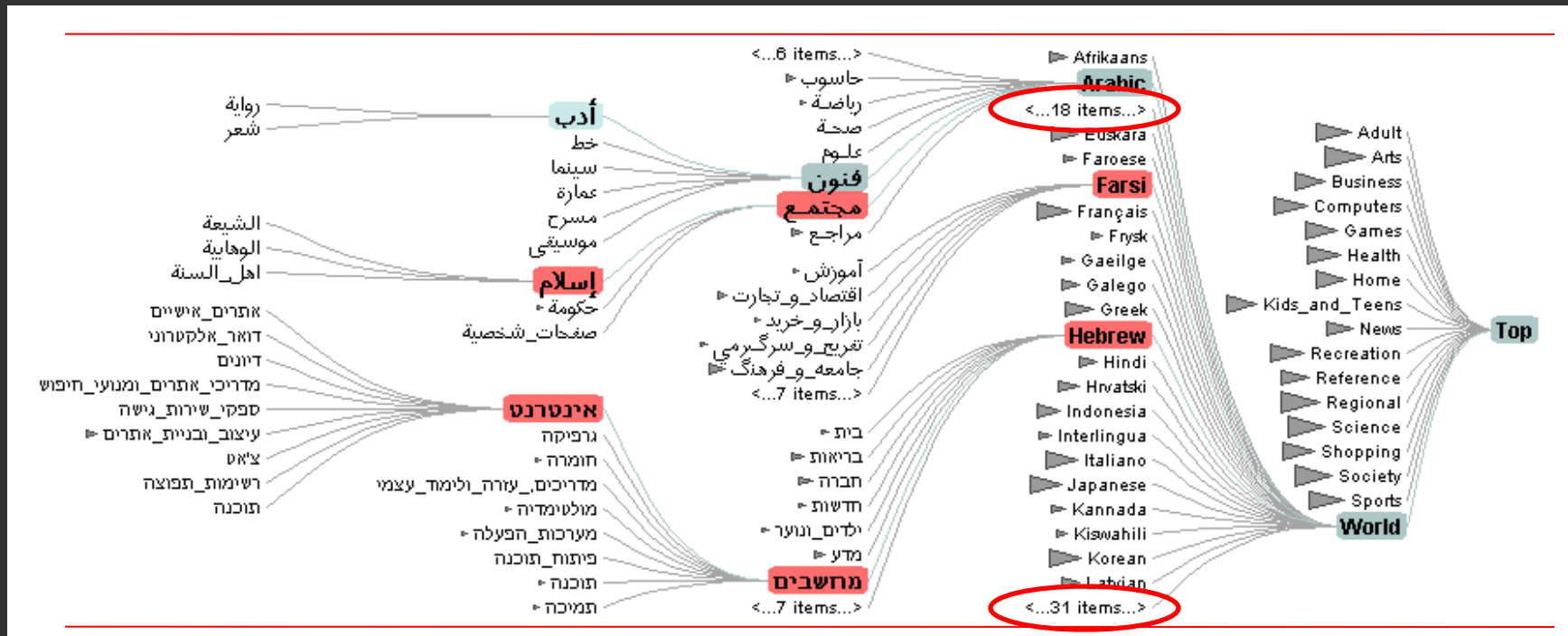
Why? Like tree breadth, the hyperbolic plane expands exponentially!

Also computable in 3D, projected into a sphere.

# Hyperbolic Layout

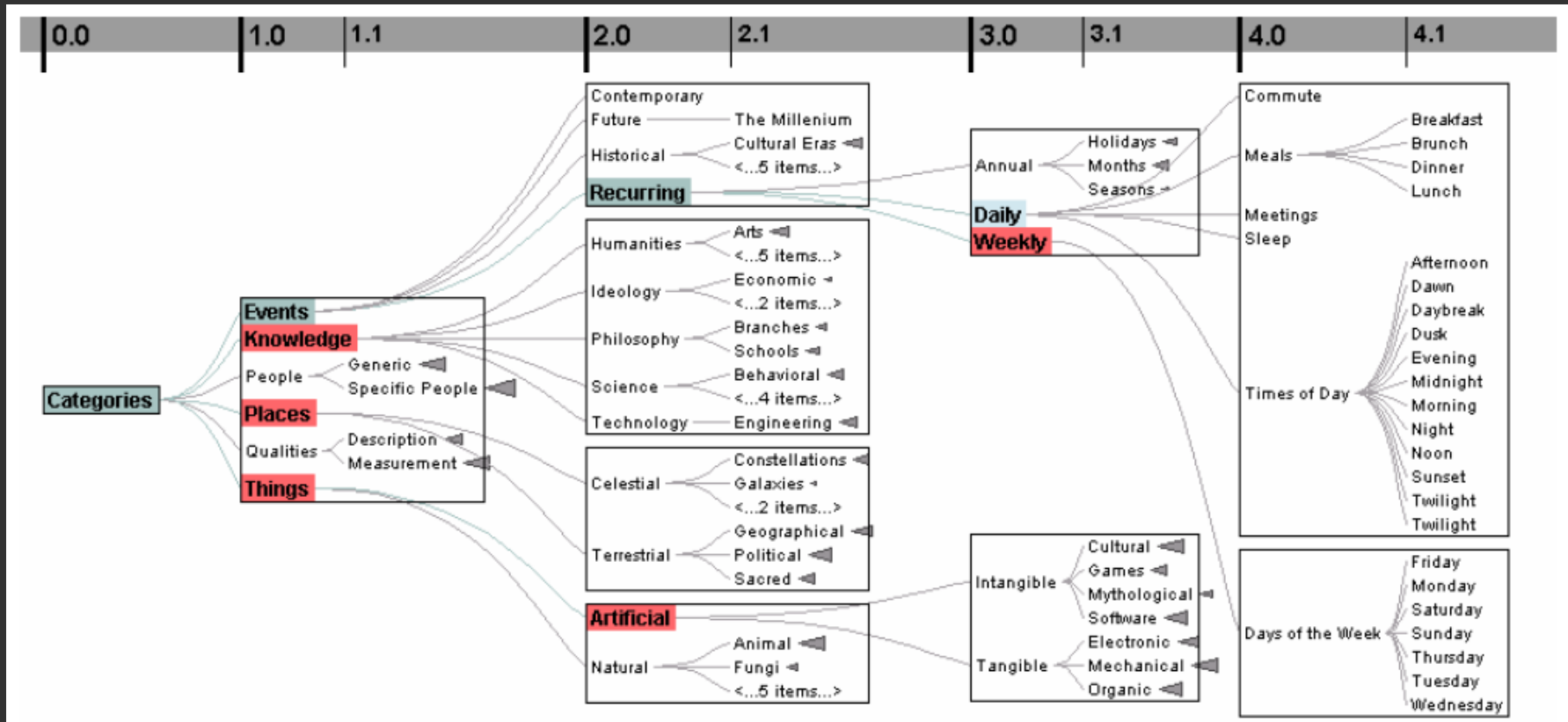


# Degree-of-Interest Trees



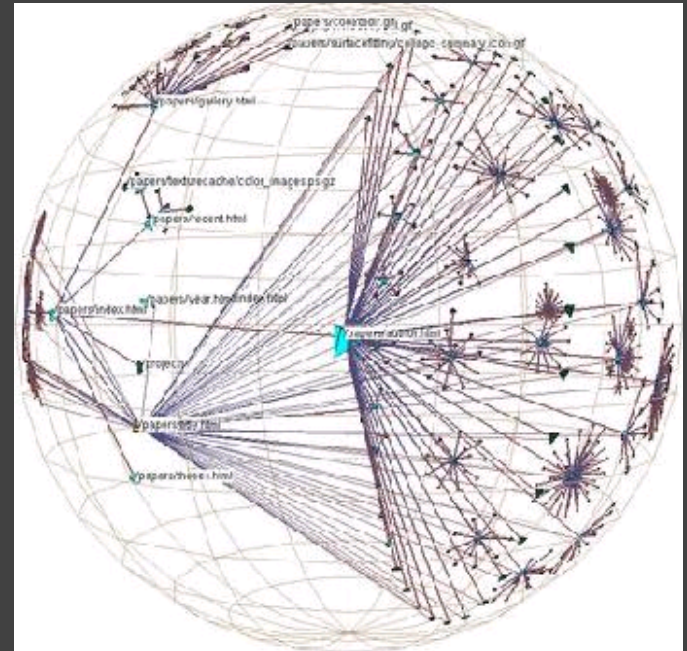
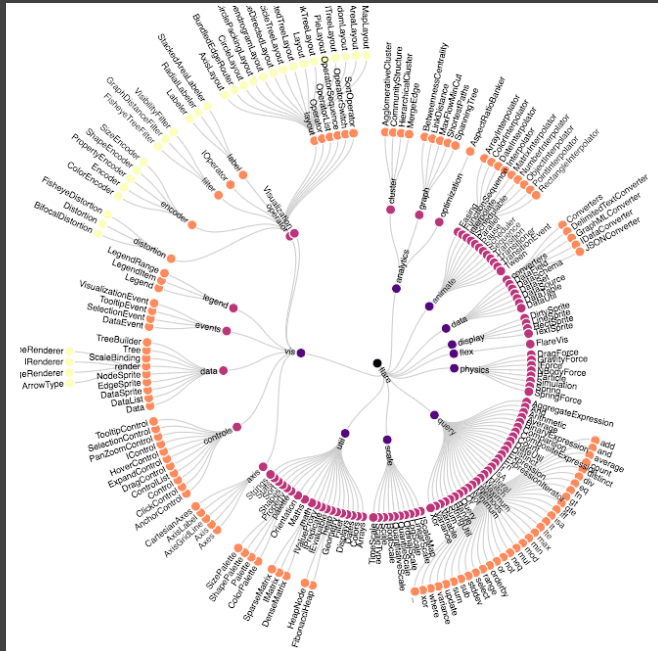
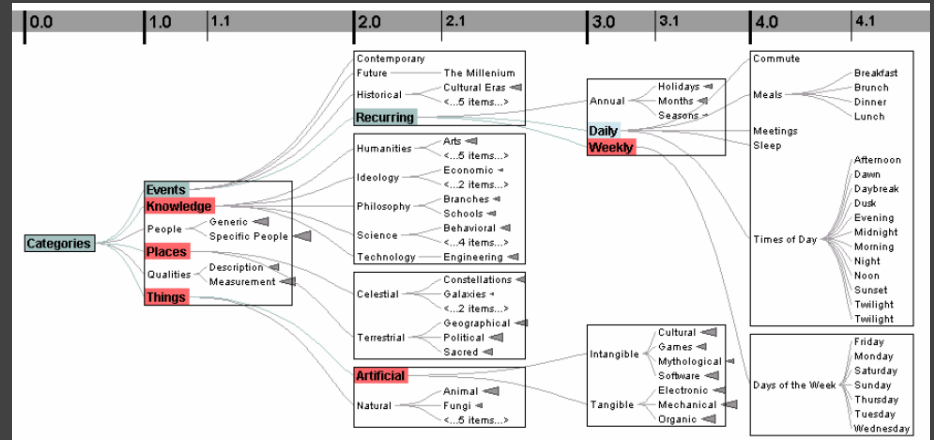
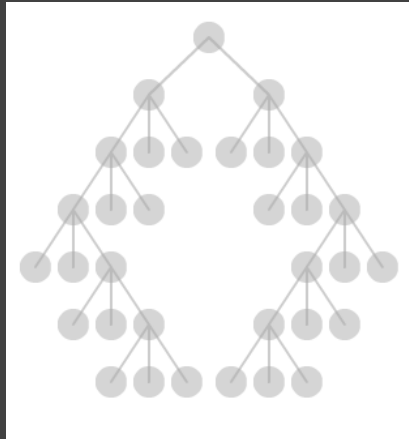
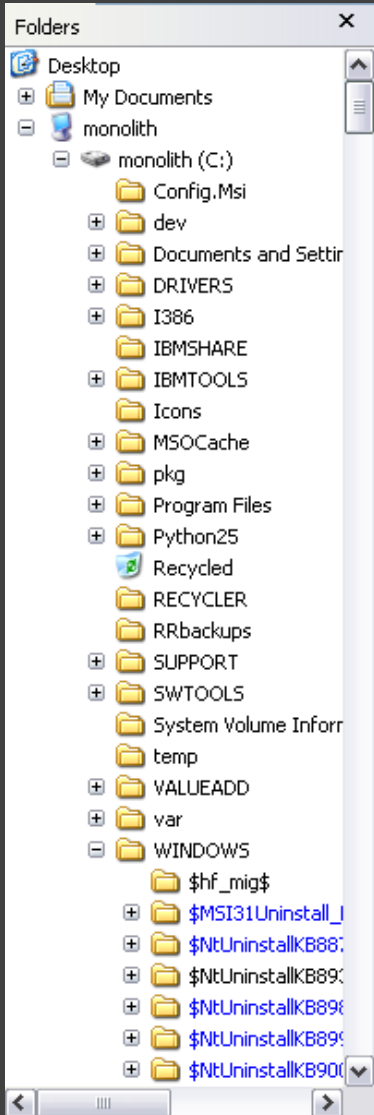
Space-constrained, multi-focal tree layout

# Degree-of-Interest Trees



Remove “low interest” nodes at a given depth level until all blocks on a level fit within bounds. Attempt to center child blocks beneath parents.

# What tasks are supported/missing?



# Indentation & Node-Link Diagrams

Encode structure in **2D space** (breadth/depth)

## **Benefits**

Clearly depicts node relationships / structure  
Structure-based or browsing tasks

## **Problems**

Even with tidy layout, quickly run out of space

## **Missing**

Attribute-based encodings

# Administrivia



# Reminders!

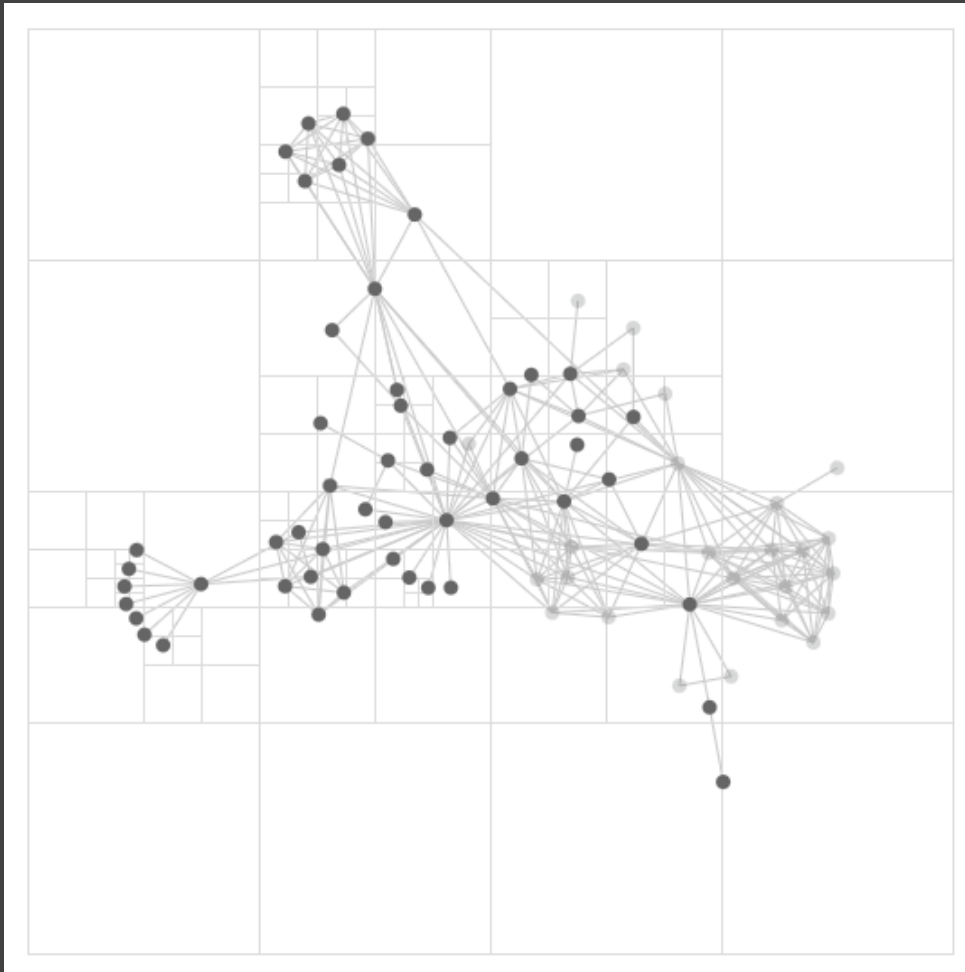
Week 7 Participation Due **tonight Mon 5/17**

*Discussion+quiz or extra peer evaluations*

*Peer evaluation form disabled after tonight*

Final Project Prototype Due **Fri 5/21, 11:59pm PT**

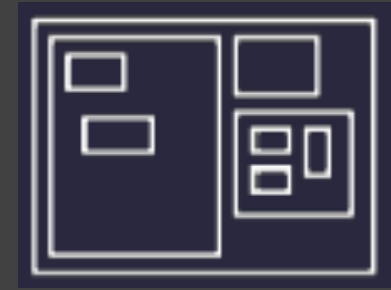
# Required Reading for Wed 5/19



The Barnes-Hut Approximation: Efficient computation of N-body forces. Jeffrey Heer. 2017.

**Enclosure**

# Enclosure Diagrams



Encode structure using **spatial enclosure**  
Popularly known as **treemaps**

## Benefits

Provides a single view of an entire tree  
Easier to spot large/small nodes

## Problems

Difficult to accurately read structure / depth

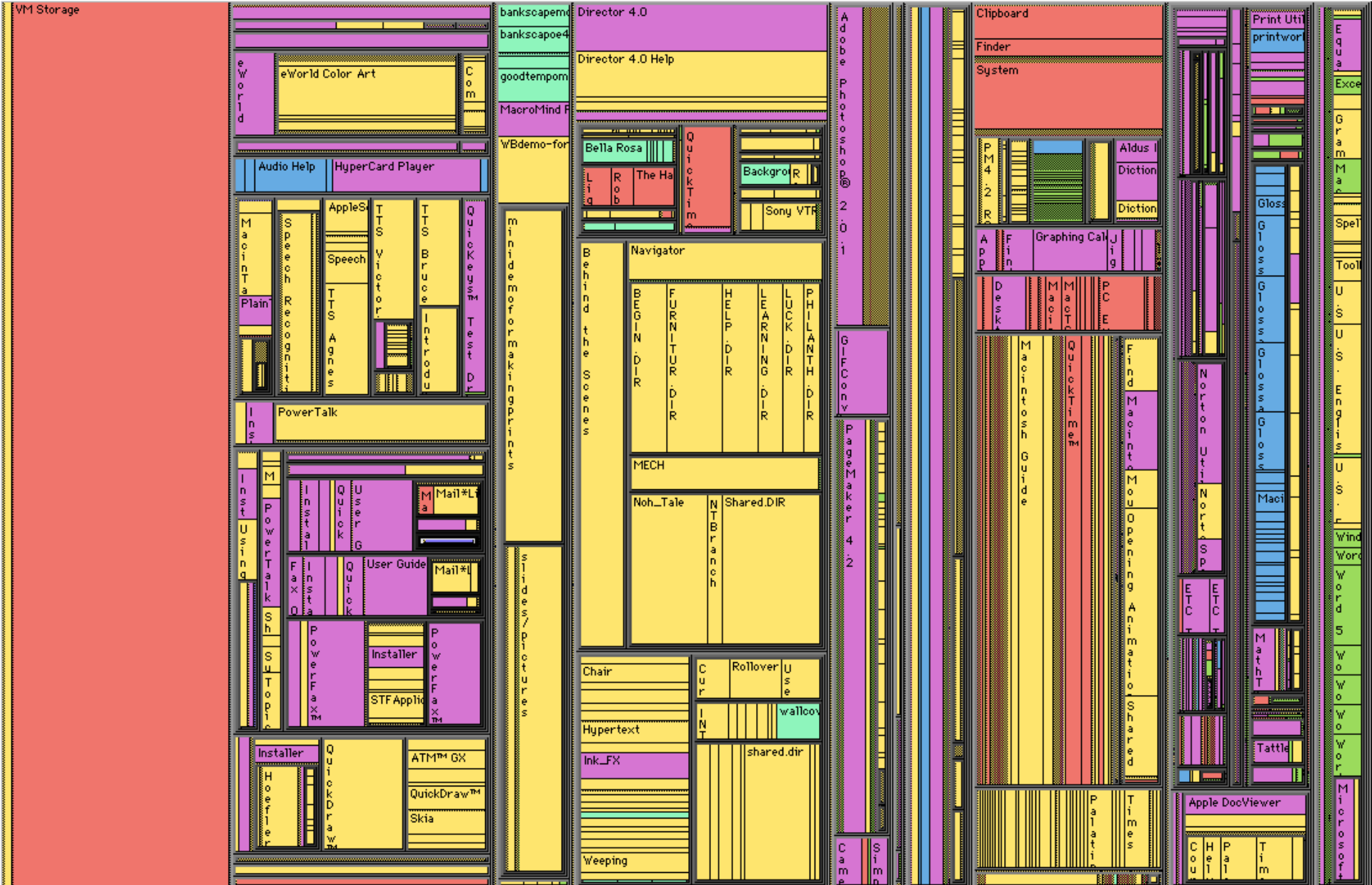


# Treemaps

Hierarchy visualization that emphasizes values of nodes via area encoding.

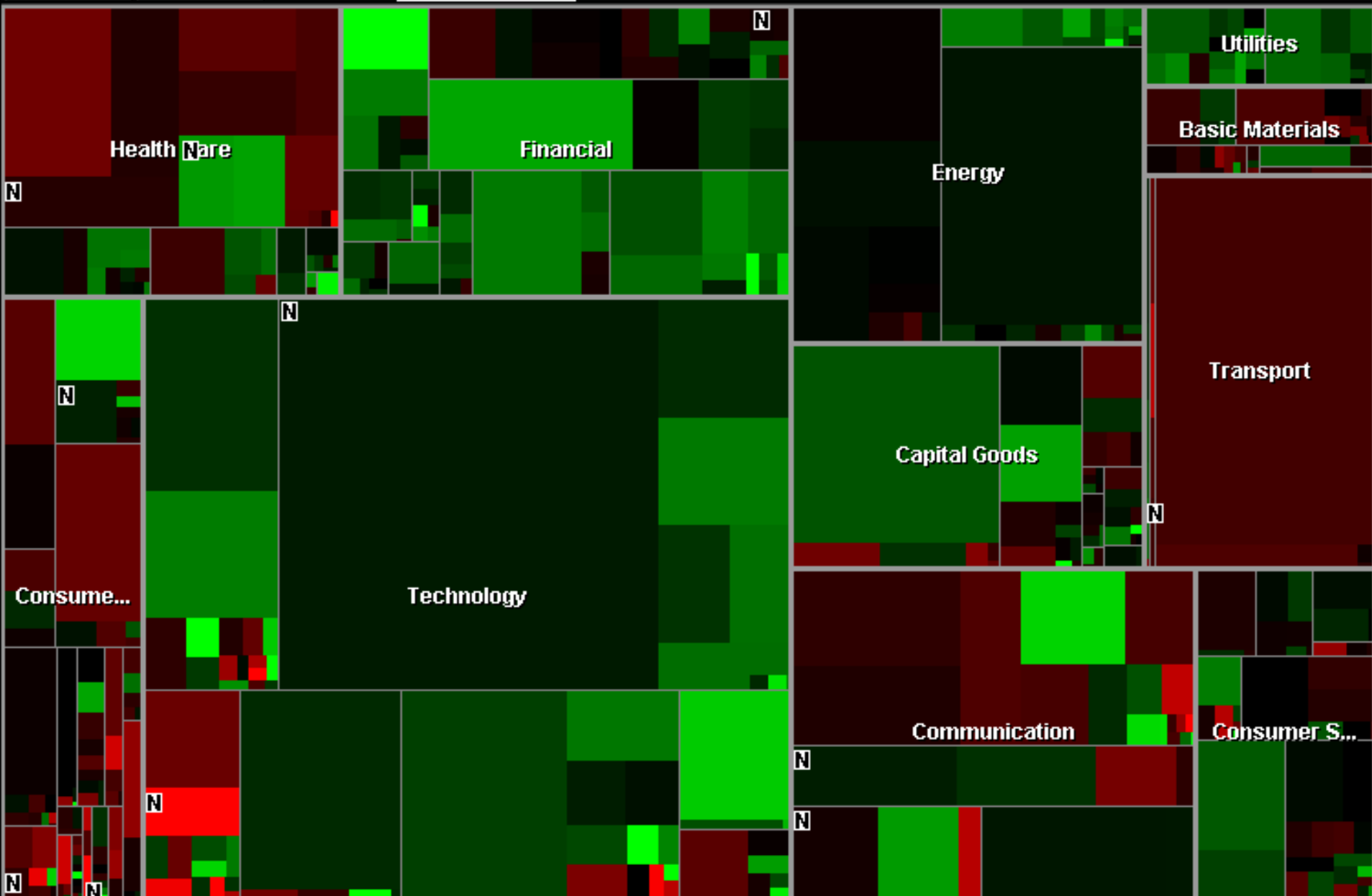
Partition 2D space such that leaf nodes have sizes proportional to data values.

First layout algorithms proposed by Shneiderman et al. in 1990, with focus on showing file sizes on a hard drive.



Name	Size	% Total	Type	Creator	Creation Date	Modification Date
Unknown	Text	Graphics	Archives/Stacks	Programming	Applications	System

*Slice & Dice* layout: Alternate horizontal / vertical partitions.



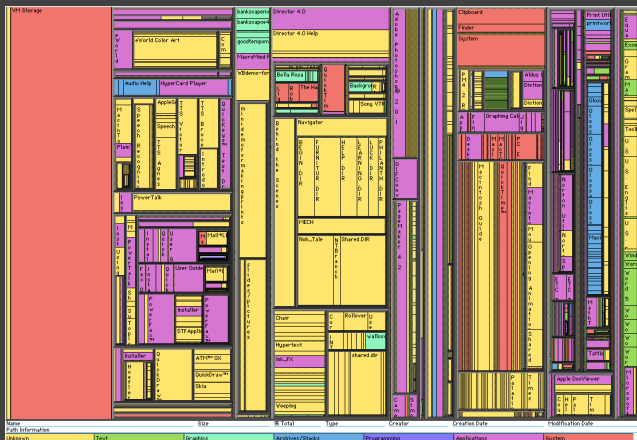
*Squarified* layout: Try to produce square (1:1) aspect ratios



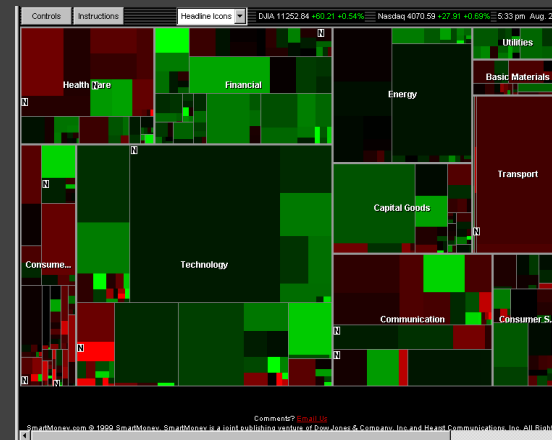
# Squarified Treemaps [Bruls et al. '00]

*Slice & Dice* layout suffers from extreme aspect ratios. How might we do better?

*Squarified* layout: greedy optimization for objective of square rectangles. Slice/dice within siblings; alternate whenever ratio worsens.



VS.

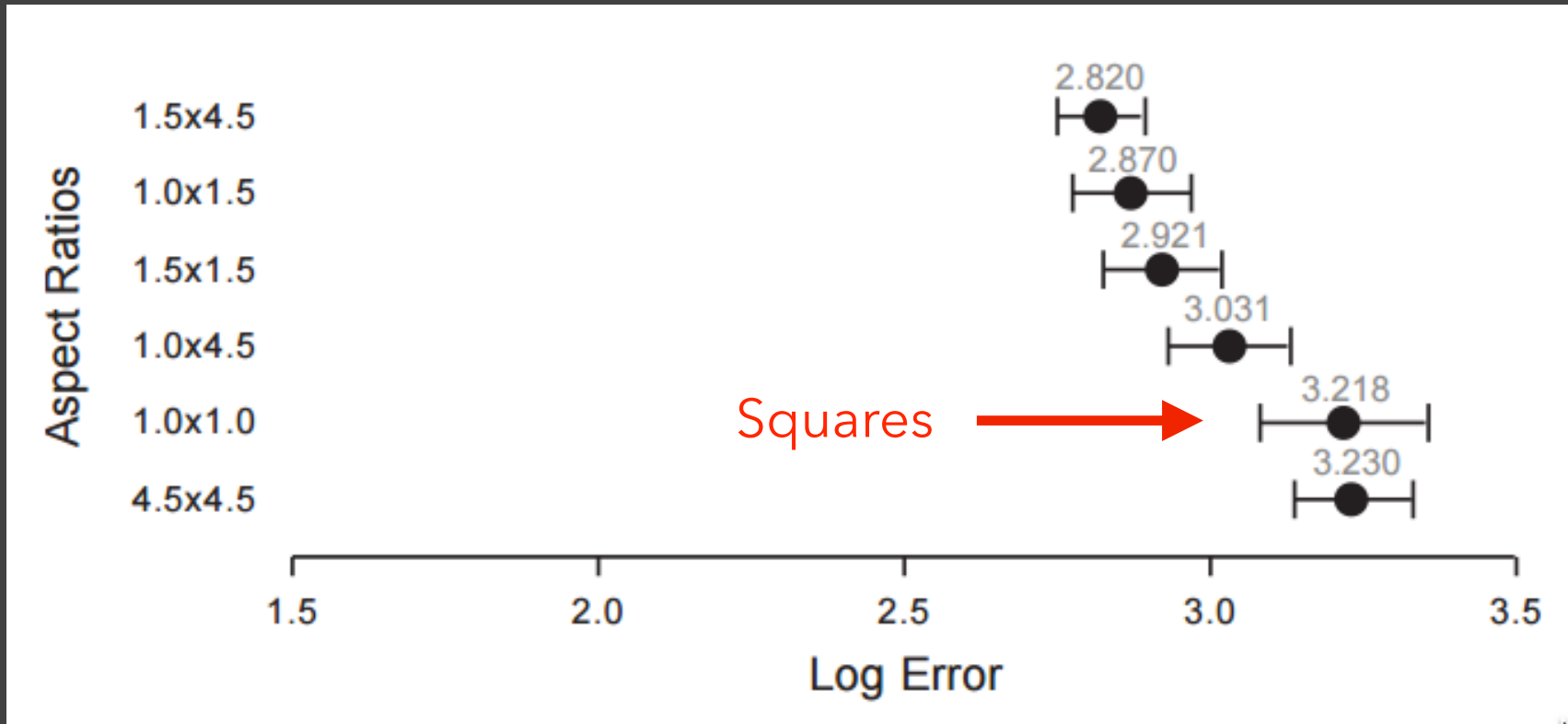


# Why Squares? [Bruls et al. '00]

## Posited Benefits of 1:1 Aspect Ratios

1. Minimize perimeter, reducing border ink.  
*Mathematically true!*
2. Easier to select with a mouse cursor.  
*Validated by empirical research & Fitt's Law!*
3. Similar aspect ratios are easier to compare.  
*Seems intuitive, but is this true?*

# Comparison Error vs. Aspect Ratio



Study by Kong, Heer & Agrawala, InfoVis '10.

Comparison of squares has higher error!

"Squarify" works because it fails to meet its objective?

# Why Squares? [Bruls et al. '00]

## Posited Benefits of 1:1 Aspect Ratios

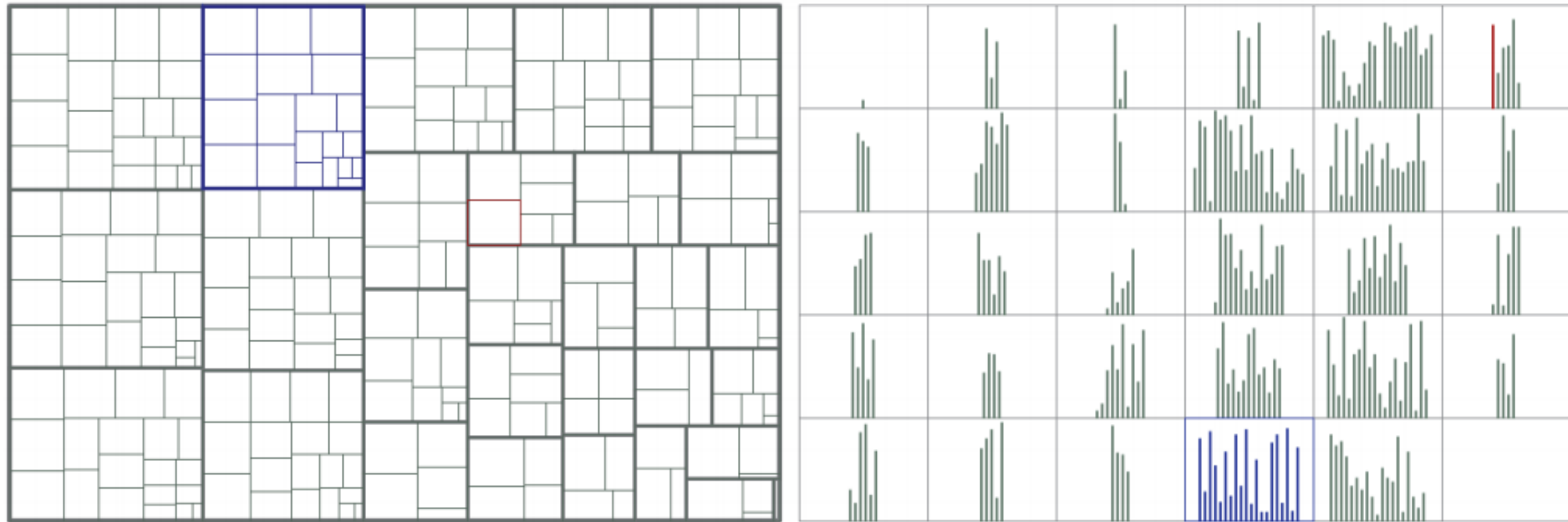
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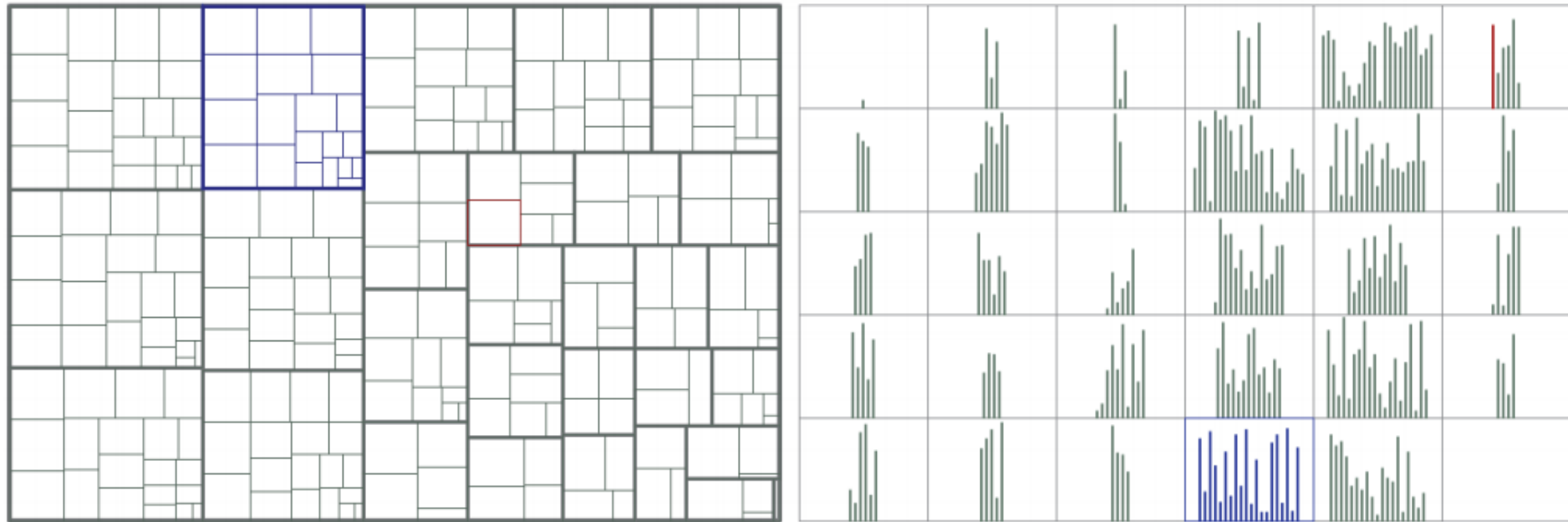
1. Minimize perimeter, reducing border ink.  
*Mathematically true!*
2. Easier to select with a mouse cursor.  
*Validated by empirical research & Fitt's Law!*
3. ~~Similar aspect ratios are easier to compare.~~  
*Extreme ratios & squares-only more inaccurate.*  
*Balanced ratios better? Target golden ratio?*

# Treemaps vs. Bar Charts [Kong et al. '10]



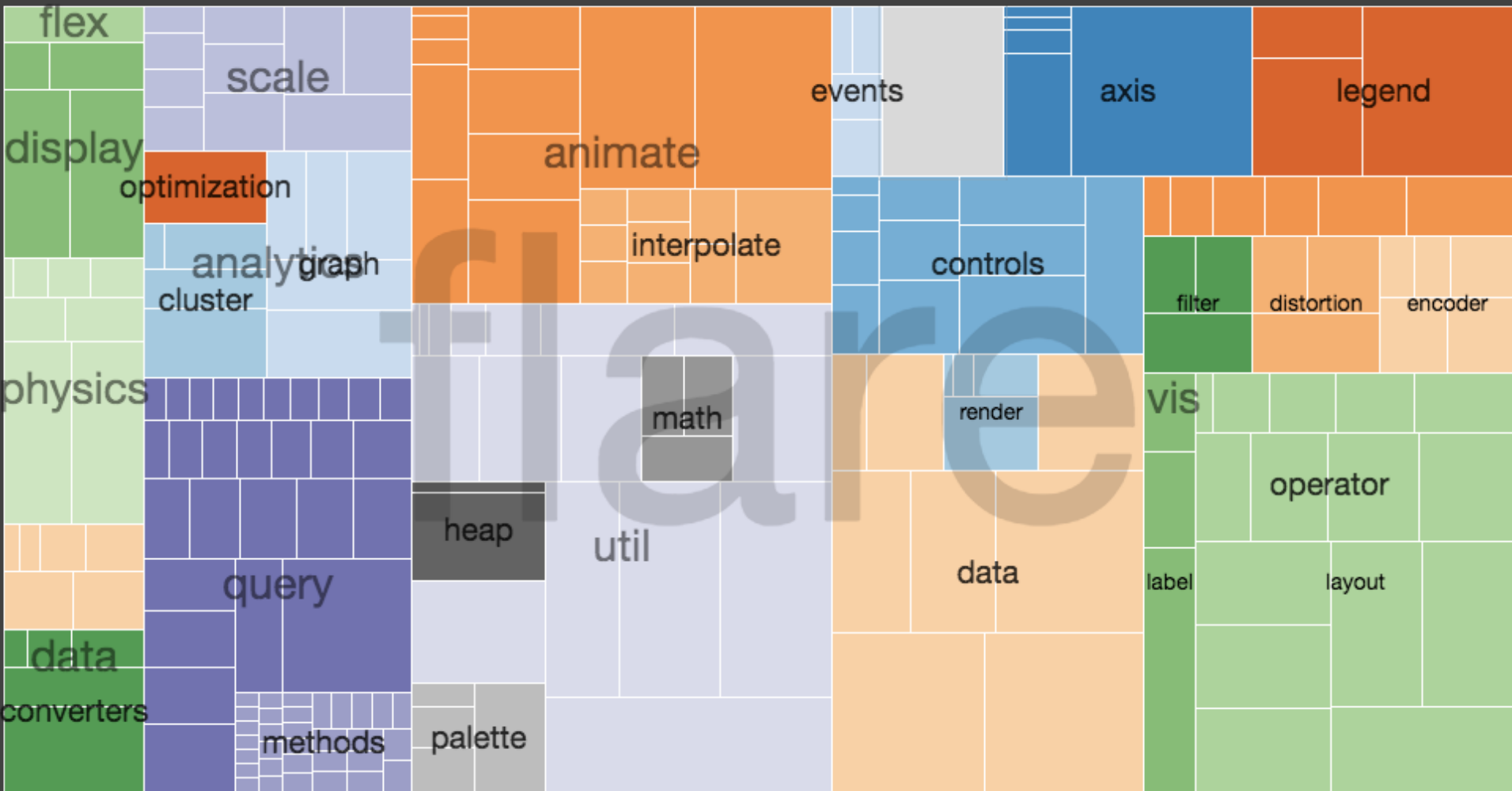
Position is generally more effective than area, but...  
What happens when the element count gets high?  
What happens when comparing groups of elements,  
such as leaf values vs. internal node values?

# Treemaps vs. Bar Charts [Kong et al. '10]



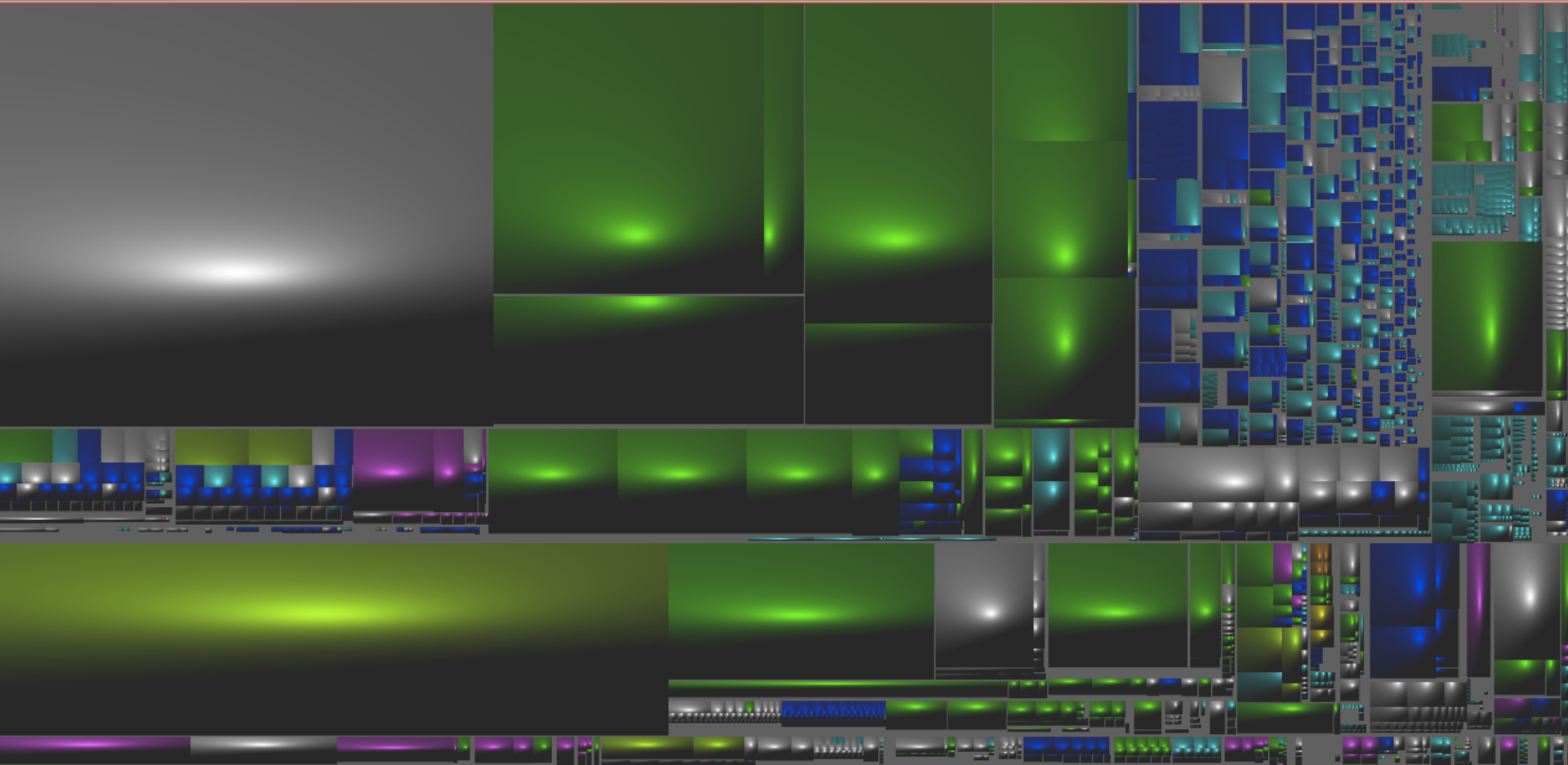
At low densities ( $< 4k$  elements), bar charts more accurate than treemaps for leaf-node comparisons.  
At higher density, treemaps led to faster judgments.  
Treemaps better for group-level comparisons.

# Interactive Example...



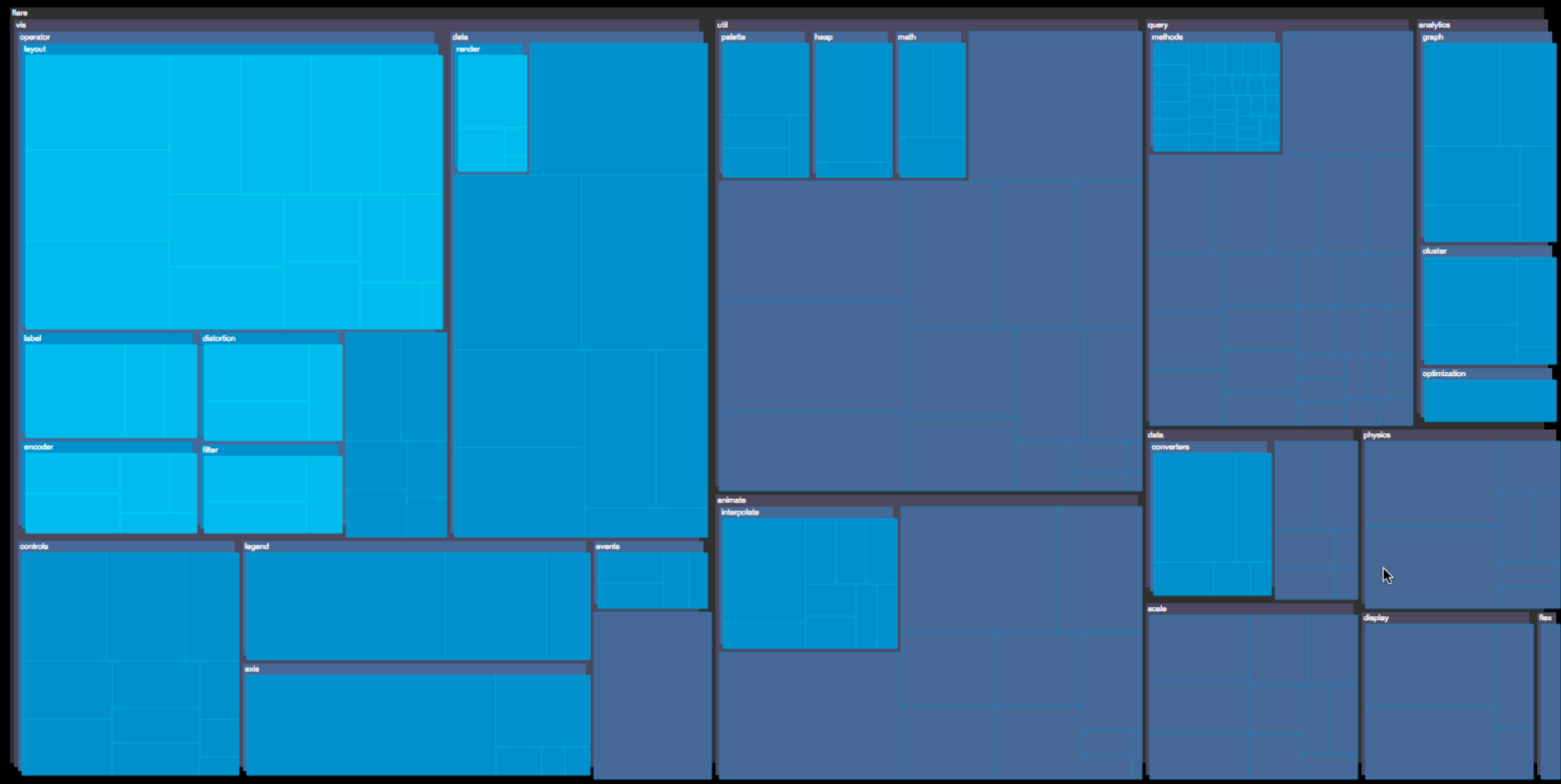


# Cushion Treemaps [van Wijk & Wetering '99]



Uses shading to emphasize hierarchical structure.

# Cascaded Treemaps [Lü & Fogarty '08]

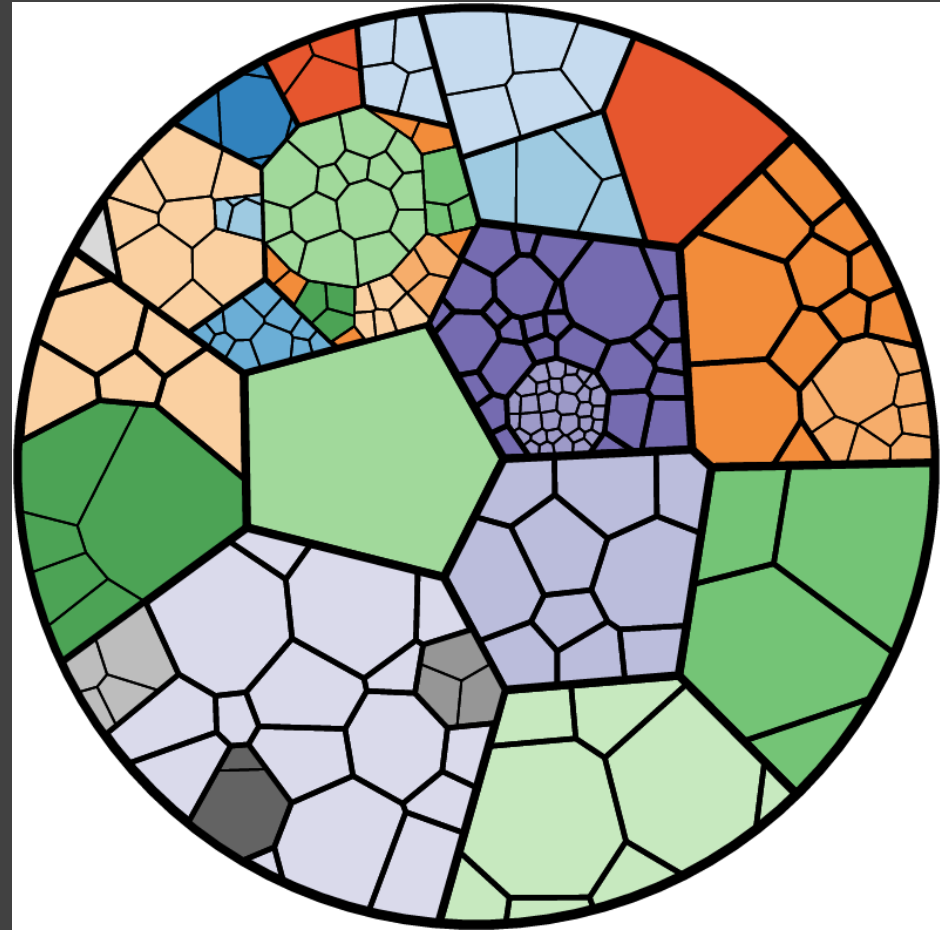


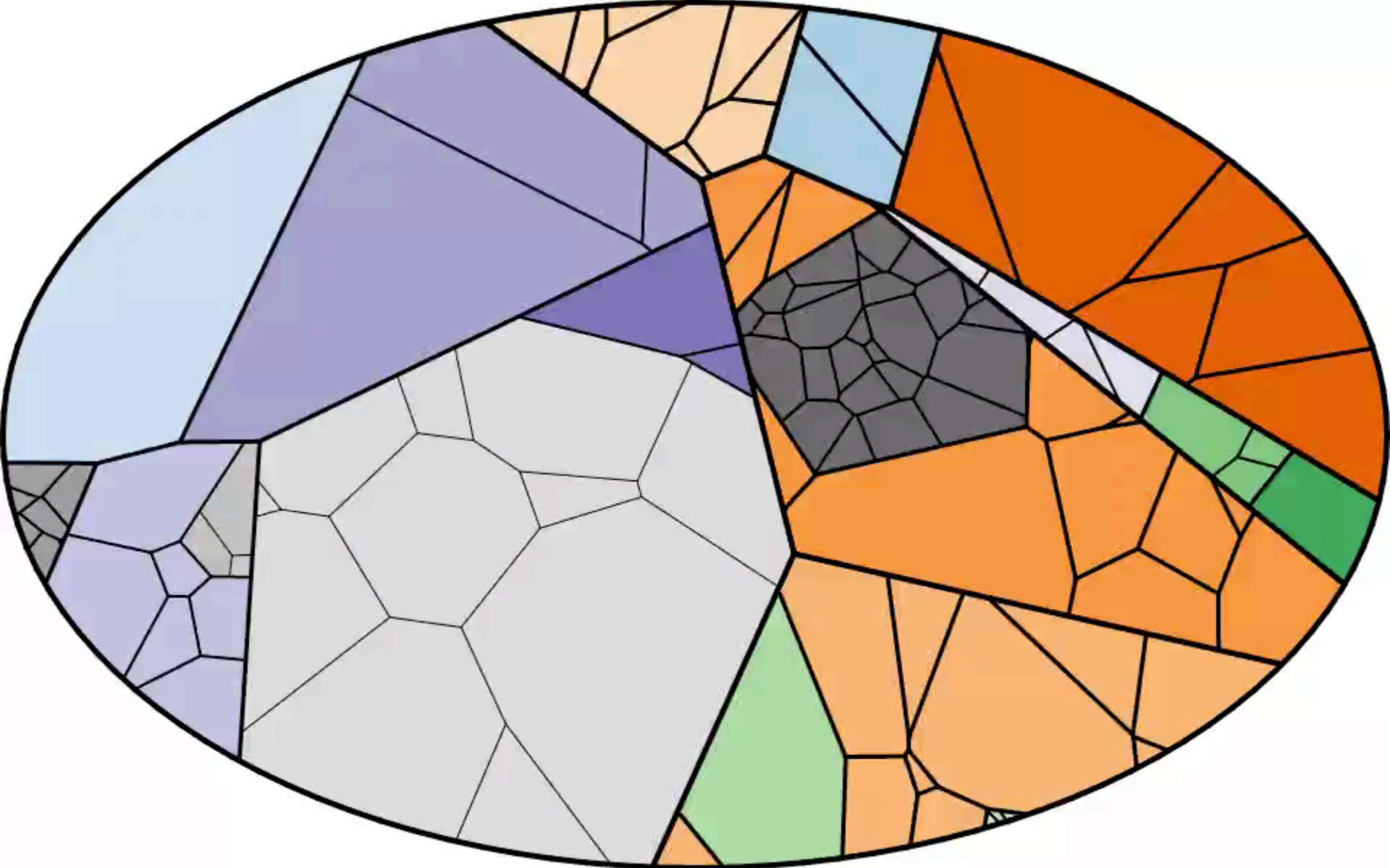
Uses 2.5D effect to emphasize hierarchy relations.

# Voronoi Treemaps [Balzer et al. '05]

Instead of rectangles, create treemaps with arbitrary polygonal shapes and boundary.

Use iterative, weighted Voronoi tessellations to achieve cells with value-proportional areas.

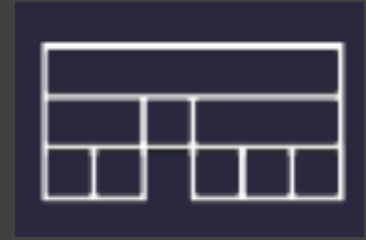




Iterative Voronoi Tessellations [Jason Davies]

# Layering

# Layered Diagrams



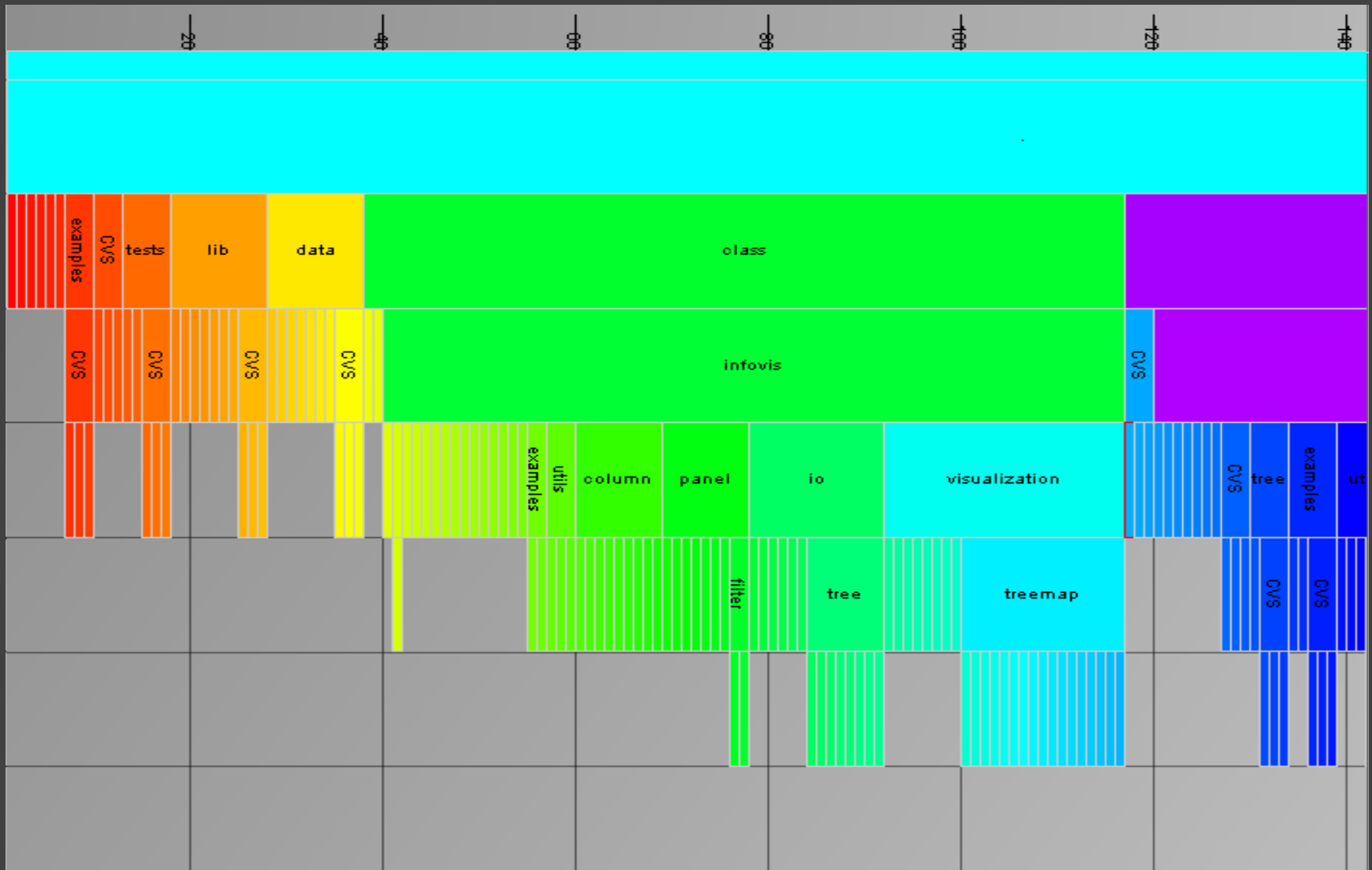
Signify tree structure using:

- Layering
- Adjacency
- Alignment

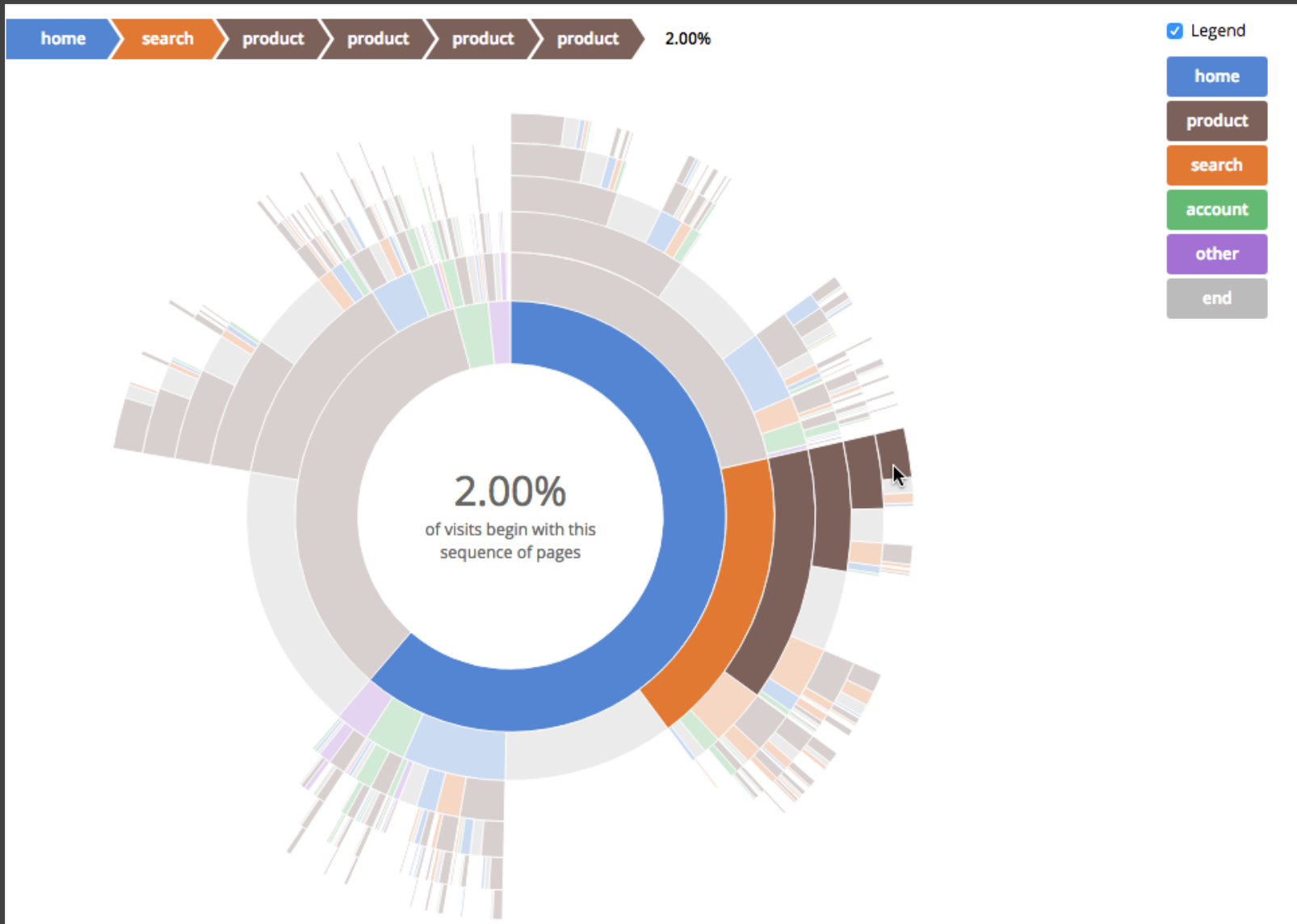
Involves recursive sub-division of space.

Leaf nodes may be sized by value, parent size visualizes sum of descendant leaf values.

# Icicle Trees: Cartesian Partition

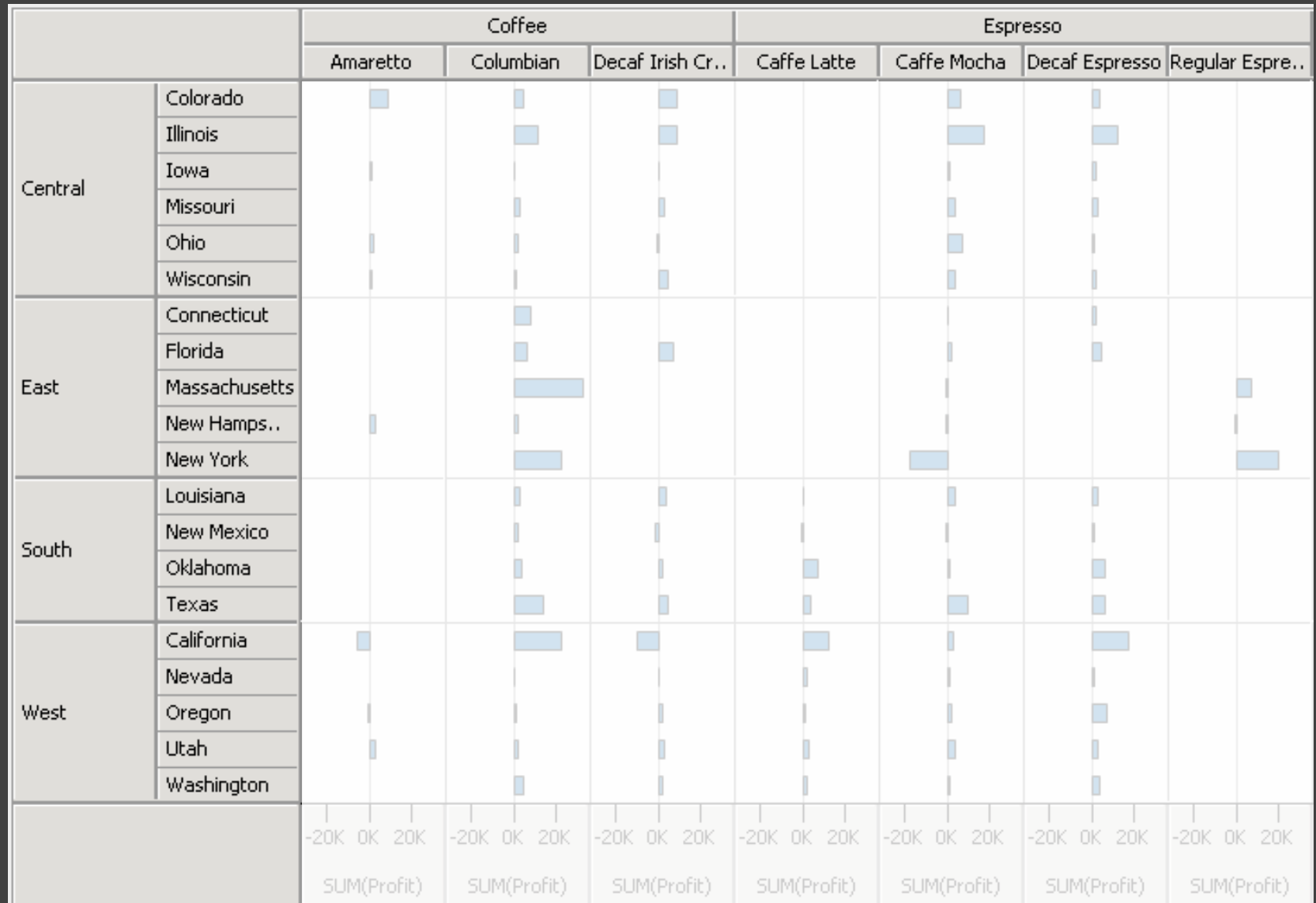


# "Sunburst" Trees: Polar Partition



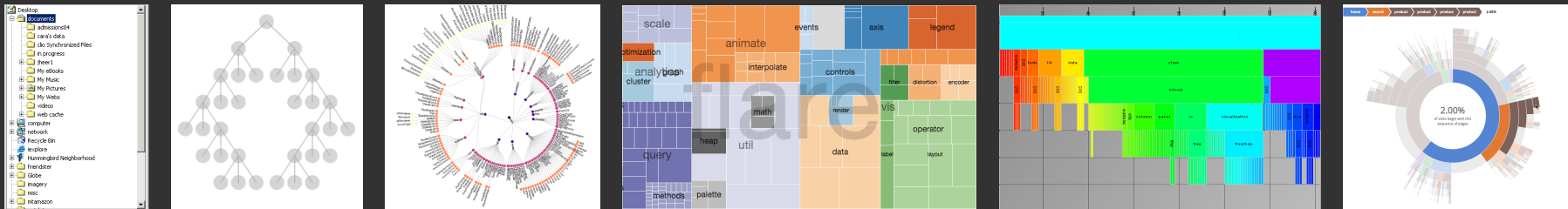


# Layered Trees Useful Elsewhere...

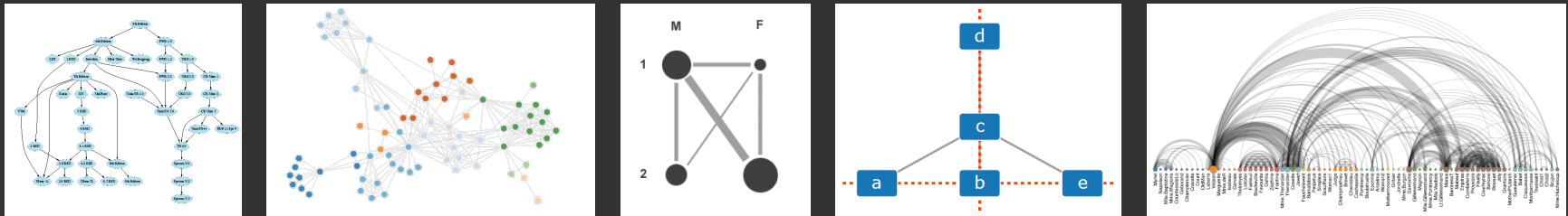


# Topics

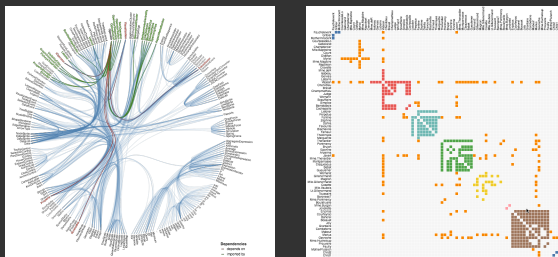
## TODAY - Tree Visualization



## Wed - Graph Layout: Node-Link Diagrams



## Wed - Alternative Visualizations and Techniques



Select an image to jump to those slides.