

# CSE 401 Final Exam

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**December 15, 2011**

**Name** \_\_\_\_\_ **Sample Solution**

You may have one sheet of handwritten notes plus the handwritten notes from the midterm. Otherwise, the exam is closed book, closed notes, closed electronics, closed neighbors, open mind, ... .

Please wait to turn the page until everyone has their exam and you have been told to begin.

If you have questions during the exam, raise your hand and someone will come to you.

Legibility is a plus as is showing your work. We can't read your mind, but we'll try to make sense of what you write.

1	/ 9
2	/ 22
3	/ 16
4	/ 12
5	/ 12
6	/ 12
7	/ 6
8	/ 10
9	/ 1
Total	/ 100

**Question 1.** (9 points) Compiler phases. For each of the following tasks, indicate the *earliest* stage of the compiler that can *always* perform that task or detect the situation. Assume that the compiler is a conventional one that generates native code for a single target machine (say, x86-64) for a source language with a static type system like C++ or Java. Use the following abbreviations to identify the stages:

scan – scanner

parse – parser

sem – semantics/type check

opt – optimization

instr – instruction selection & scheduling

reg – register allocation

run – runtime (i.e., when the compiled code is executed)

can't – can't always be done during compilation or execution

sem Detect circular inheritance hierarchies (class A extends B and class B extends A)

sem Detect possible use of an uninitialized variable in a Java method

scan Detect that an integer constant is too large to be stored in a variable of type `int`

instr Decide that using a `lea` instruction would be the best choice to multiply a value by 5 instead of using an `imul` instruction

sem In a method call `x.f(...)`, verify that the class of the object referenced by `x` actually does contain a method `f` with the correct number and types of parameters

run In a method call `x.f(...)`, verify that `x` actually refers to an object and is not `null`

parse Discover that the program source file ends in the middle of an incomplete assignment statement like `x=a*b+` (i.e., end of file after the `+` symbol)

reg Discover that registers do not need to be saved and restored in a function because all calculations can be done with registers the function is allowed to change without restoring

sem Warn the programmer that the declaration of a method in a subclass is overloading a method declaration in a superclass and not overriding the superclass method as the programmer may have intended

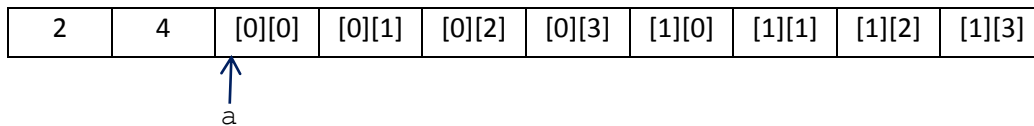
**Question 2.** (22 points) Compiler hacking: a question of several parts. Vulture Ventures, a new startup in South Lake Union, would like to buy our MiniJava compiler, but only if we add 2-dimensional arrays to it. To do this we will make the following additions to the existing rules in the MiniJava grammar:

```
Type ::= "int" "[" "]" "[" "]"
Expression ::= "new" "int" "[" Expression "]" "[" Expression "]"
Expression ::= Expression "[" Expression "]" "." "length"
Expression ::= Expression "[" Expression "]" "[" Expression "]"
```

This adds a new type for 2-D arrays (`int [ ] [ ]`), another version of “new” to allocate 2-D arrays, a way to access the number of columns in a 2-D array (`a [row] .length`), and an expression to access individual elements of a 2-D array (`a [row] [col]`). As in regular Java, `a .length` accesses the number of rows in the array. The elements in a 2-D array are 8-byte integer values, as is true of all other integer values in MiniJava.

Our customer requires us to store 2-D arrays as a single block of memory, not as an array of pointers to individual array rows as in regular Java. The array elements are stored in row-major order, as in C, C++, and other languages. When an array is allocated, the `new` operator returns a pointer to element `[0][0]` of the array. The number of rows and columns in the array are stored in the two preceding 8-byte quadwords right before element `[0][0]`.

For example, if we execute `a = new int [2] [4];` the variable `a` will refer to element `[0][0]` in a new array that has 2 rows of 4 elements each. The number of rows (2) and number of columns (4) are stored just before the array elements.



**Note:** The question accidentally omitted the array assignment `id [exp] [exp] =exp;` that would be needed to add 2-D arrays to MiniJava in the same style that 1-D arrays were originally included. During the exam we announced that the question should be answered ignoring that omission.

(a) (3 points) What new lexical tokens, if any, need to be added to the scanner and parser of our MiniJava compiler to add these new 2-dimensional arrays to the original MiniJava language? Just describe any necessary changes; you don’t need to give JFlex or CUP specifications or code.

None

(continued next page)

**Question 2. (cont.)** (b) (6 points) What changes are needed to the MiniJava abstract syntax tree (AST) data structures to add these new 2-dimensional arrays to MiniJava? Again, you do not need to give any Java or CUP code, just describe the changes (what kinds of new or changed nodes, what children would they have, etc.).

As usual in a question like this there are several possibilities. Correct answers needed to include at least the following:

- Add a new type descriptor for the type of 2-D arrays `int [][]`, or modify the existing `int []` type descriptor to include the number of dimensions.
- Add an additional AST expression node for the operator `new int [e1] [e2]`, with two expression AST nodes as children.
- Add a new or modified node for the length expression `e1 [e2] .length` with appropriate expression AST nodes as children.
- Add a new expression node for 2-D array element references `e1 [e2] [e3]`, with three expression AST nodes as children.

(c) (4 points) Suppose a reference to an array element `e1[e2][e3]` appears as a value in a MiniJava expression. Describe the checks that need to be performed to verify that this array element expression has no type errors or other static semantic errors.

- Verify that the type of `e1` is `int [][]`
- Verify that the types of `e2` and `e3` are `int`

(continued next page)

**Question 2. (cont.)** (d) (9 points) Describe the x86-64 code shape that the compiler would generate to evaluate the array element expression  $e1[e2][e3]$  and load the value of the correct array element into register `rax`. Be sure to show where the code to evaluate expressions  $e1$ ,  $e2$ , and  $e3$  should appear in the generated code. You should assume that the code generated for expressions  $e1$ ,  $e2$ , and  $e3$  will leave the value of the corresponding expression in `rax`, as we did in the MiniJava project. Also, assume that the stack is aligned on a 16-byte boundary at the beginning of the code sequence, and if you change the size of the stack you need to be sure this alignment is preserved if any of the expressions  $e1$ ,  $e2$ , or  $e3$  contain a method call.

Use the Linux/AT&T/gcc x86-64 assembler syntax for your code.

Hint: Remember that elements of the array occupy 8 bytes each, and the number of rows and columns in the array are stored in the 8-byte quadwords just prior to array element `[0][0]`.

The byte address of the array element  $e1[e2][e3]$  is computed by adding the address in the array pointer  $e1$  to  $8 * (e2 * \text{number of columns} + e3)$

```

subq $16,%rsp           # allocate temp space for e1, e2; leaves rsp 16-byte aligned
<code for e1>
movq %rax,8(%rsp)       # save value of e1
<code for e2>
movq %rax,0(%rsp)       # save value of e2
<code for e3>          # value of e3 in rax (pointer to element [0][0])
movq 0(%rsp),%rdx       # value of e2 in rdx
movq 8(%rsp),%rcx       # value of e1 in rcx
addq $16,%rsp           # free temp space (can be done here or later)
imulq -8(%rcx),%rdx     # rdx = e2 * number of columns
addq %rax,%rdx          # rdx = e3 + e2* num cols.
salq $3,%rdx           # multiply rdx by 8 (imulq by 8 would also be fine)
addq $rdx,%rcx         # add byte offset to array [0][0] address
movq 0($rcx),%rax      # load e1[e2][e3] into rax

```

A few people noticed that the last three instructions (`salq/addq/movq`) could be replaced by one `movq` instruction, taking advantage of the x86 addressing arithmetic:

```

movq 0(%rcx,%rdx,8),%rax

```

However, in that instruction it is important that the register containing the base address of the array appear first and the offset appear second, since the second operand is the one multiplied by the scale factor 8.

**Question 3.** (16 points) A bit of coding. Consider the following Java function that computes the greatest common divisor of its arguments. This code uses the Java and gcc convention that `long` is a 64-bit integer type.

```
/* return gcd(x,y) for x, y > 0 */
long gcd(long x, long y) {
    if (x > y) {
        return gcd(x-y, y);
    } else if (y > x) {
        return gcd(x, y-x);
    } else /* x==y */
        return x;
    }
}
```

This question involves translating this function to x86-64 assembler code. Ground rules:

- You must use the Linux/AT&T/gcc assembly language, and must follow the x86-64 function call, register, and stack frame conventions.
  - Argument registers: `rdi`, `rsi`, `rdx`, `rcx`, `r8`, `r9` in that order
  - Called function must save and restore `rbx`, `rbp`, and `r12-r15` if they are used
  - Function result returned in `rax`
  - `rsp` must be aligned on a 16-byte boundary when a `call` instruction is executed
- Pointers and long ints are 64 bits (8 bytes) each.
- Your x86-64 code must implement all of the statements in the original function, including the recursive function calls. You may *not* rewrite the function into a different form that produces equivalent results (i.e., no tail recursion optimizations). Other than that, you can use any reasonable x86-64 code that follows the standard function call and register conventions.
- You are not required to use register `rbp` as a frame pointer register. If you do use it, you must use it correctly.
- Please include *brief* comments in your code to help us understand what the code is supposed to be doing (which will help us assign partial credit if it doesn't do exactly what you intended.)

(You may detach this page from the exam if convenient.)

**Question 3. (cont.)** Translate function `gcd` to x86-64 assembly language. Be sure to follow the rules given on the previous page (hint: read the rules again after you've finished your answer.) Code repeated for reference.

```
/* return gcd(x,y) for x, y > 0 */
long gcd(long x, long y) {
    if (x > y) {
        return gcd(x-y,y);
    } else if (y > x) {
        return gcd(x, y-x);
    } else /* x==y */
        return x;
    }
}
```

Most people did a good job on this question. The most common error was getting the operand order in the compare instructions reversed (these instructions set the condition code by subtracting the source [1<sup>st</sup> operand] from the destination [2<sup>nd</sup> operand]).

The question should have stated that this was intended to be a simple, non-member (static) function with no `this` pointer, but most people guessed that, and it was announced during the exam.

There are, of course, many possible answers. This one is a fairly literal translation of the original code.

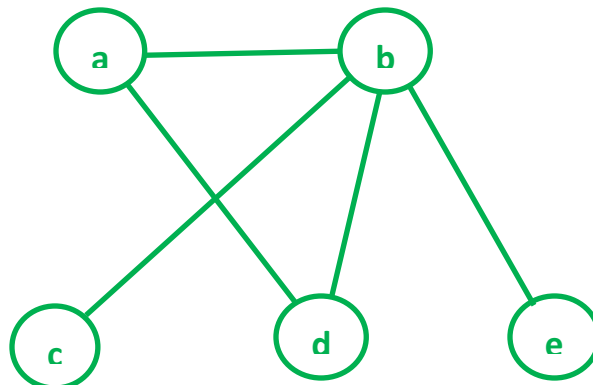
```
gcd:
    subq $8,%rsp      # align stack on 16-byte boundary (may possible ways to do this)
    cmpq %rsi,%rdi    # compare y to x
    jle elseif       # jump if x <= y, fall through if x > y
    subq %rsi,%rdi    # subtract y from x
    call gcd          # call gcd with x-y, y; result in rax
    jmp  done         # return
elseif:              # arrive here if x <= y
    cmpq %rsi,%rdi    # compare y, x (can omit since condition codes still set from last cmpq)
    jge else         # jump if x >= y, fall through if y > x
    subq %rdi,%rsi    # subtract x from y
    call gcd          # call gcd with x, y-x; result in rax
    jmp  done         # return
else:                # arrive here if x==y
    movq %rdi,%rax    # result = x
done:
    addq $8,%rsp      # restore stack
    ret
```

Another very common solution was to use the usual prologue code to push `%rbp` at the beginning of the function and pop it just before the return. That would also have left the stack aligned properly.

**Question 4.** (12 points) Register allocation. Considering the following code:

```
a = read();
b = read();
if (a > b) {
    c = read();
    e = c - b;
} else {
    d = b;
    e = a + d;
}
print(b);
print(e);
```

(a) Draw the interference graph for the variables in this code. You are not required to draw the control flow graph, but it might be useful to sketch it out to help find the solution and to leave clues about what might have happened if the graph is not quite correct. (The next page contains additional blank space if you would like to use it, but please put your final answer on this page.)



(b) Give an assignment of (groups of) variables to registers using the minimum number of registers possible, based on the information in the interference graph. You do not need to go through the steps of the graph coloring algorithm explicitly, although that may be helpful as a guide to assigning registers. If there is more than one possible answer that uses the minimum number of registers, any of them will be fine. Use R1, R2, R3, ... for the register names. (Again, there is additional work space on the next page if needed, but please write your answer here.)

**There are many possible assignments that use three registers. a, b, and d need to be in separate registers; c and e can be in either register not used by b. One possible assignment:**

**R1: b; R2: a, c, and e; R3: d**



**Question 5.** (12 points) Thinking optimally. In most production compilers, optimization is done using intermediate code that consists of simple 3-address instructions like the following:

$$r5 = r3 + r7$$
$$r6 = r5 * 8$$

Some of the instructions in the intermediate code may be *dead code* because the results of the instructions are never used later in the program. An important optimization in compilers is *dead-code elimination*, where we remove such instructions to save space and execution time.

(a) (8 points) What *data flow analysis* should be used to discover which instructions are dead code? Describe the appropriate data flow problem to use and explain how to use its results to identify dead instruction(s).

**Live variable analysis.**

**For each statement  $a=b \text{ op } c$ , if variable  $a$  is not live at that point in the program, the statement can be deleted.**

(b) (4 points) After performing the data flow analysis in part (a) and removing the dead code that it identifies, will there be any dead code in the remaining instructions? If so, why, and what needs to be done to remove them? If not, why not?

**No. Live variable analysis will only mark a variable as live if it is used directly or indirectly to compute some value that is live on exit from the code being analyzed. If a variable is used only to compute the value of some other variable that is not itself live, neither variable will be marked as live and both statements will be removed by dead code elimination.**

**(This does not mean that later optimization passes might not generate further dead code by eliminating uses of some variables. That is entirely possible, and for that reason dead code elimination is often done repeatedly during optimization.)**

**Question 6.** (12 points) SSA. Here is a simple program that reads two numbers and prints their greatest common divisor as long as both numbers are positive.

```
x = read();
y = read();
while (x != y) {
    if (x > y) {
        x = x - y;
    } else { /* y > x */
        y = y - x;
    }
}
print(x);
```

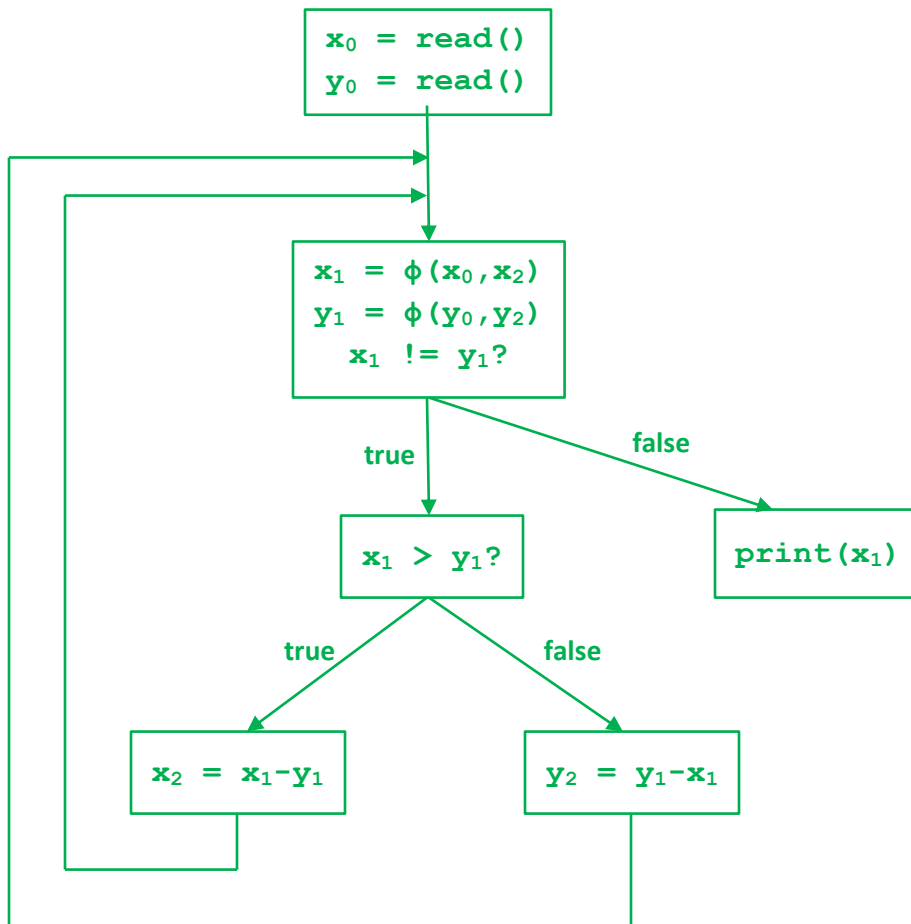
Draw a control flow graph for this program (nodes = basic blocks, edges = possible control flow), using Static Single Assignment (SSA) form as described in section. You should include  $\phi$ -functions where needed to merge different versions of the same variable. For full credit you should only include necessary  $\phi$ -functions and not have extraneous ones scattered everywhere, but we will give generous partial credit if all of the necessary  $\phi$ -functions are included and there are a minimal number of extra ones.

Hint: it might be easiest to sketch the flow graph first without converting it into SSA, then add the needed variable version numbers and  $\phi$ -functions to get the final answer.

Write your answer on the next page. You can remove this page from the exam if you wish.

Question 6. (cont.) Write your answer here.

Here is one possible answer.



**Question 7.** (6 points) A little concurrency. In section we discussed the interactions between concurrency and compiler optimizations. Suppose we have the following function that adds the elements of an integer array to the value in global variable `sum`.

```
int sum = 0;

void addarray(int[] a) {
    if (a.length <= 0) return;
    for (int k = 0; k < a.length; k++) {
        sum += a[k];
    }
}
```

We would like to optimize the code by keeping a copy of `sum` in a local register `temp` as follows:

```
void addarray(int[] a) {
    if (a.length <= 0) return;
    temp = sum;
    for (int k = 0; k < a.length; k++) {
        temp += a[k];
    }
    sum = temp;
}
```

(a) (1 point) Is this optimizing transformation always correct and safe in single-threaded code? (circle one)

yes no

(b) (1 point) Assuming that the variable `temp` is a local register that is not shared with other threads, is this optimizing transformation always correct and safe in multi-threaded code (i.e., when other threads are running in the same address space)? (circle one)

yes no

(c) (4 points) Give a brief explanation of your answer to (b) describing why this optimization is or is not safe in multi-threaded code.

If another thread is reading variable `sum` during execution of the loop it can see intermediate values as `sum` is updated in the first version, but will only see the initial or final value in the second version. If another thread writes a new value to `sum` after the first thread reads it, in the second version `sum` will either contain its original value plus the sum of the array elements or the different value written by the other thread. In the original version it may contain the value written by the other thread plus the values of some or all of the elements in the array.

**Question 8.** (10 points, 2 each) The party's almost over. Time to clean up the garbage...

We looked at three major garbage collection algorithms in class: classic mark-sweep collectors, semispace copying collectors, and generational collectors. For each of the following statements or properties, circle the name of the algorithm that is the best match. If more than one algorithm is an equally good "best answer", circle all of the correct answers.

(a) Fastest allocation of new objects (new/malloc/cons):

mark-sweep    copying    generation

(b) Searches entire heap for reachable objects during a routine collection:

mark-sweep    copying    generation

(c) Best heap locality (arrangement of objects for good cache and paging behavior) after a collection:

mark-sweep    copying    generation

(d) Largest percentage of examined objects reclaimed during a routine collection:

mark-sweep    copying    generation

(e) Best overall performance:

mark-sweep    copying    generation

**Question 9.** (1 point) The best Star Trek television series is clearly (circle):

**Number of answers for each given below. Some people voted more than once, but usually multiple votes were for the less popular answers(!). All answers received the point, including the one that wrote in "The one where Luke figures out who his father is".**

- a) The Original Star Trek **10**
- b) Star Trek: The Next Generation **12**
- c) Star Trek: Deep Space Nine **6**
- d) Star Trek: Voyager **4**
- e) Star Trek: Enterprise **3**
- f) All of the above **1**
- g) Just give me my free point, please **21**

*Best wishes for the holidays and New Year!*

The CSE 401 staff