## Section 07: Graphs

## 1. Graph traversal

(a) Consider the following graph. Suppose we want to traverse it, starting at node $A$.


If we traverse this using breadth-first search, what are two possible orderings of the nodes we visit? What if we use depth-first search?
(b) Same question, but on this graph:


## 2. Checking for Cycles

Given a graph as an adjacency list, design an algorithm that checks whether the graph has a cycle or not. The runtime of the algorithm must be $O(|V|+|E|)$, where $V$ is the vertex set and $E$ is the edge set. You may assume that the graph is unweighted, has no parallel edges and has no self loops.

## 3. Simulating Dijkstra's

(a) Consider the following graph:


Suppose we run Dijkstra's algorithm on this graph starting with vertex $s$. What are the final costs of each vertex and the shortest paths from $s$ to each vertex?
(b) Here is another graph. What are the final costs and shortest paths if we run Dijkstra's starting on node $A$ ?


## 4. Topological Sort

Find a topological sort of the following graph:


