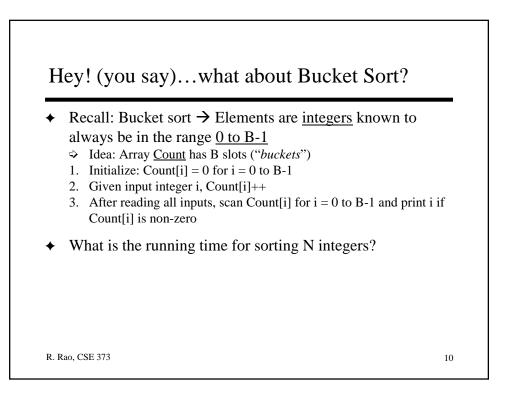


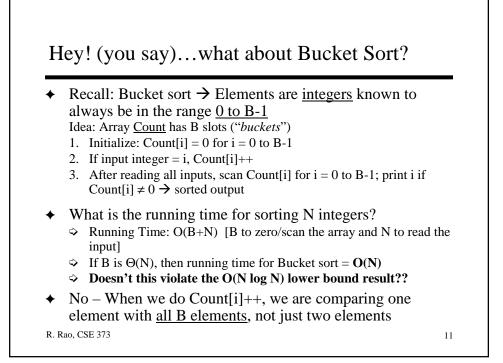
- ◆ Decision tree has L = N! leaves → its depth d ≥ log(N!)
 ◇ What is log(N!)? (first, what is log(A•B)?)
 ◇ log(N!) = log N + log(N-1) + ... log(N/2) + ... + log 1
 ≥ log N + log(N-1) + ... log(N/2) (N/2 terms only)
 ≥ (N/2)•log(N/2) = Ω(N log N)
- <u>Result</u>: Any sorting algorithm based on comparisons between elements requires Ω(N log N) comparisons
 - Run time of any comparison-based sorting algorithm is Ω(N log N)

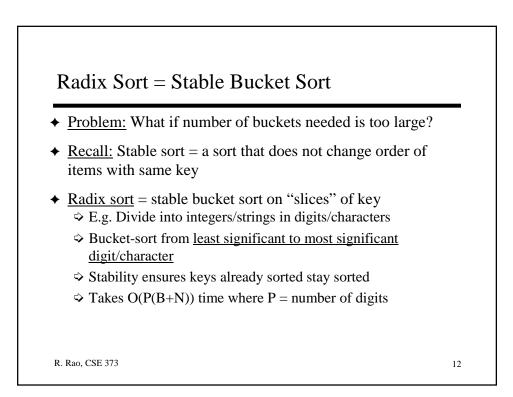
9

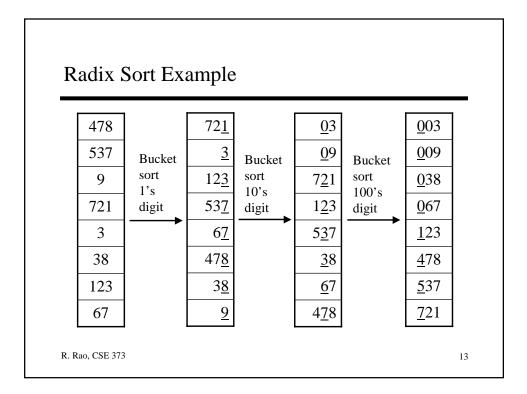
⇔ Can never get an O(N log log N) algorithm (sorry, Pat Swe!)

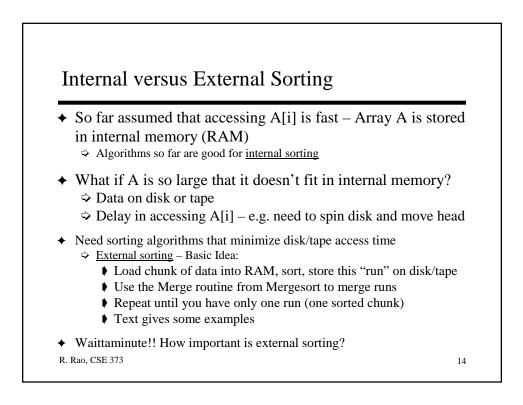
R. Rao, CSE 373

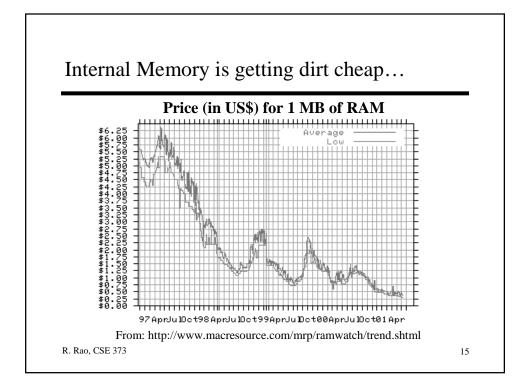


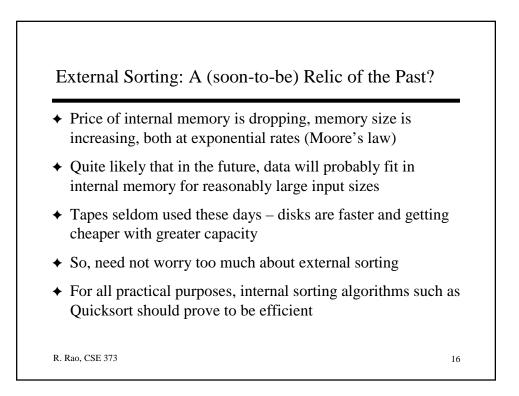


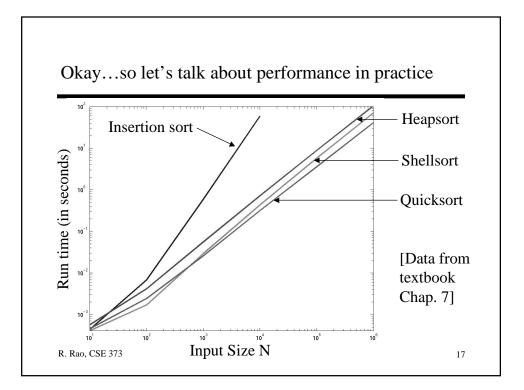


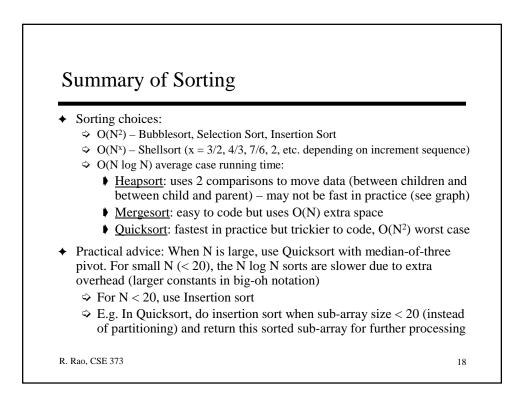












Next time: Union-Find and Disjoint Sets

To do:

Finish reading chapter 7

Start reading chapter 8

Have a great weekend!

R. Rao, CSE 373

19