

Quicksort Description

Quicksort Algorithm:

- 1. Partition array into left and right sub-arrays such that:
- Elements in left sub-array < elements in right sub-array
- 2. Recursively sort left and right sub-arrays
- 3. Concatenate left and right sub-arrays with pivot in middle

✦ How to Partition the Array:

1. Choose an element from the array as the pivot 2. Move all elements < pivot into left sub-array and all elements > pivot into right sub-array

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• Pivot? One choice \rightarrow use first element in array

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- Algorithm for In Place Partitioning: ٠ Swap pivot with last element \rightarrow swap pivot and A[N-1] Set pointers i and j to beginning and end of array
- 1. 2.
- Increment i until you hit an element A[i] > pivot
 Decrement j until you hit an element A[j] < pivot
- 5.
- Swap A[i] and A[j] Repeat until i and j cross (i exceeds or equals j) Swap pivot (= A[N-1]) with A[i] 6. 7.
- On-Board Example: Partition in place: $\Rightarrow 9 16 4 15 2 5 17 1$ (pivot (pivot = A[0] = 9)

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Quicksort Performance Analysis

- ★ Best Case Performance: Algorithm always chooses best pivot and keeps splitting sub-arrays in half at each recursion
 ⇒ T(0) = T(1) = O(1) (constant time if 0 or 1 element)
 - \Rightarrow T(N) = 2T(N/2) + O(N) (Constant time in our recention) \Rightarrow For N > 1, 2 recursive calls plus linear time for partitioning \Rightarrow T(N) = 2T(N/2) + O(N) (Same recurrence relation as Mergesort) \Rightarrow T(N) = ?

Quicksort Performance Analysis

- <u>Best Case Performance</u>: Algorithm always chooses best pivot and keeps splitting sub-arrays in half at each recursion
 - \Rightarrow T(0) = T(1) = O(1) (constant time if 0 or 1 element)
 - \Rightarrow For N > 1, 2 recursive calls plus linear time for partitioning \Rightarrow T(N) = 2T(N/2) + O(N) (Same recurrence relation as Mergesort) \Rightarrow T(N) = <u>O(N log N)</u>

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• <u>Worst Case Performance</u>: What is the worst case?

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Quicksort Performance Analysis

- ★ Best Case Performance: Algorithm always chooses best pivot and keeps splitting sub-arrays in half at each recursion
 ⇒ T(0) = T(1) = O(1) and T(N) = 2T(N/2) + O(N)
 ⇒ T(N) = O(N log N)
- <u>Worst Case Performance</u>: Algorithm keeps picking the worst pivot – one sub-array empty at each recursion

 - \Rightarrow T(N) = ?

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Quicksort Performance Analysis

- ★ Best Case Performance: Algorithm always chooses best pivot and keeps splitting sub-arrays in half at each recursion
 ⇒ T(0) = T(1) = O(1) and T(N) = 2T(N/2) + O(N)
 ⇒ T(N) = O(N log N)
- ★ <u>Worst Case Performance</u>: Algorithm keeps picking the worst pivot – one sub-array empty at each recursion
 - \Rightarrow T(0) = T(1) = O(1)
 - \Rightarrow T(N) = T(N-1) + O(N)
 - = T(N-2) + O(N-1) + O(N) = ... = T(0) + O(1) + ... + O(N) $\Rightarrow T(N) = O(N^2)$
- Fortunately, average case performance is O(N log N) (see text for proof)

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Can We Sort Any Faster?

- ✤ Heapsort, Mergesort, and Quicksort all run in O(N log N) best case running time
- ✦ Can we do any better?
- ♦ Can Joe Smartypants from Softwareville, USA come up with an O(N log log N) sorting algorithm?

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Answer in next class...

To do:

Finish reading chapter 7 Start reading chapter 8

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