Please read through the entire examination first! We designed this exam so that it can be completed in 50 minutes and, hopefully, this estimate will prove to be reasonable.

There are 5 problems for a total of 90 points. The point value of each problem is indicated in the table below. Write your answer neatly in the spaces provided. If you need more space (you shouldn't), you can write on the back of the sheet where the question is posed, but please make sure that you indicate clearly the problem to which the comments apply. Do NOT use any other paper to hand in your answers. If you have difficulty with part of a problem, move on to the next one. They are independent of each other.

The exam is CLOSED book and CLOSED notes (no summary sheets, no calculators, no mobile phones, no laptops). Please do not ask or provide anything to anyone else in the class during the exam. Make sure to ask clarification questions early so that both you and the others may benefit as much as possible from the answers.

Name: ______________________
ID#: ______________________

<table>
<thead>
<tr>
<th>Problem</th>
<th>Max Score</th>
<th>Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>15</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>10</td>
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<td>3</td>
<td>20</td>
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<tr>
<td>4</td>
<td>30</td>
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<tr>
<td>5</td>
<td>15</td>
<td></td>
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<tr>
<td>TOTAL</td>
<td>90</td>
<td></td>
</tr>
</tbody>
</table>
1. Warm-up (15 points)

A. If we have six (6) bits in which to represent integers, what is largest unsigned number and what is largest 2s complement number we can represent (in decimal)?

Largest unsigned number: ________________

Largest 2s complement number: ________________

B. If %eax stores x and %ebx stores y, what do the following lines of assembly compute?
Note that the result is in %eax.

```assembly
mov   %ebx, %ecx
add   %eax, %ebx
je    .L1
sub   %eax, %ecx
je    .L1
xor   %eax, %eax
jmp   .L2
.L1:
   mov   $1, %eax
.L2:
   ...
```
2. **Floating Point Representation (10 points)**

Suppose we have 16-bit floating point numbers where 6 bits are assigned to the exponent and 9 bits to the fraction and 1 to the sign bit.

A. What is the bias for this float?

B. Given the decimal number 3.625, calculate the fraction (frac) and exponent (exp) that would appear in the floating point representation. (Note: you may leave your answer in decimal for the exponent.)
3. C and Assembly Code (20 points)

Given the C code for the function foo, determine which IA32 and x86-64 code snippet corresponds to a correct implementation of foo.

```c
int foo (int x, int y) {
    int c = x << (y + 3);
    if (x != 0) {
        return c;
    } else {
        return 1;
    }
}
```
A. Which of the following IA-32 implementations is correct for foo()? Circle the correct one and give at least one reason why the other two are not correct.

i) push %ebp
mov %esp, %ebp
mov 0xc(%ebp), %ecx
add $0x3, %ecx
mov 0x8(%ebp), %eax
shl %eax, %ecx
mov %ecx, %eax
cmp $0x8(%ebp), $0
jne $0x808472 // two lines down to leave
mov $0x1, %eax
leave
ret

ii) push %ebp
mov %esp, %ebp
mov 0xc(%ebp), %ecx
add $0x3, %ecx
mov 0x8(%ebp), %eax
shl %ecx, %eax
cmp $0x8(%ebp), $0
jne $0x808472 // two lines down to leave
mov $0x1, %eax
leave
ret

iii) push $ebp
mov %esi, %ecx
add $0x3, %ecx
mov %edi, %eax
shl %ecx, %eax
test %edi, $0
jne $0x808472 // two lines down to leave
mov $0x1, %eax
leave
ret
B. Which of the following x86-64 implementations is correct for foo()? Circle the correct one and give at least one reason why the other two are not correct.

i) add $0x3, %rsi  
   mov %rdi, rax  
   shr %rsi, %rax  
   test %rdi, %rdi  
   jne $0x808472 // two lines down to leave  
   mov $0x1, %rax  
   leave  
   ret

ii) push $rbx  
    mov %rsi, %rbx  
    add $0x3, %rbx  
    mov %rdi, %rax  
    shr %rbx, %rax  
    test %rdi, %rdi  
    jne $0x808472 // two lines down to leave  
    mov $0x1, %rax  
    leaveq  
    ret

iii) mov %rdi, %rdx  
     add $0x3, %rdx  
     mov %rsi, %rax  
     shr %rdx, %rax  
     test $0, %rdi  
     jne $0x808472 // two lines down to leave  
     mov $0x1, %rax  
     ret
4. Stack Discipline (30 points)

The following function recursively computes the greatest common divisor of the integers $a$, $b$:

```c
int gcd(int a, int b) {
    if (b == 0) {
        return a;
    } else {
        return gcd(b, a % b);
    }
}
```

Here is the x86_64 assembly for the same function:

```
4006c6 <gcd>:
4006c6:  sub     $0x18, %rsp
4006ca:  mov     %edi, 0x10(%rsp)
4006ce:  mov     %esi, 0x08(%rsp)
4006d2:  cmpl    $0x0, %esi
4006d7:  jne     4006df <gcd+0x19>
4006d9:  mov     0x10(%rsp), %eax
4006dd:  jmp     4006f5 <gcd+0x2f>
4006df:  mov     0x10(%rsp), %eax
4006e3:  cltd
4006e4:  idivl   0x08(%rsp)
4006e8:  mov     0x08(%rsp), %eax
4006ec:  mov     %edx, %esi
4006ee:  mov     %eax, %edi
4006f0:  callq   4006c6 <gcd>
4006f5:  add     $0x18, %rsp
4006f9:  retq
```

Note: `cltd` is an instruction that sign extends %eax into %edx to form the 64-bit signed value represented by the concatenation of [ %edx | %eax ].

Note: `idivl <mem>` is an instruction divides the 64-bit value [ %edx | %eax ] by the long stored at <mem>, storing the quotient in %eax and the remainder in %edx.
A. Suppose we call gcd(144, 64) from another function (i.e. main()), and set a breakpoint just before the statement “return a”. When the program hits that breakpoint, what will the stack look like, starting at the top of the stack and going all the way down to the saved instruction address in main()? Label all return addresses as "ret addr", label local variables, and leave all unused space blank.

<table>
<thead>
<tr>
<th>Memory address on stack</th>
<th>Value (8 bytes per line)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x7fffffffffffffffad0</td>
<td>Return address back to main</td>
</tr>
<tr>
<td>0x7fffffffffffffffac8</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffac0</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffab8</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffab0</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffaa8</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffaa0</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff98</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff90</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff88</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff80</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff78</td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffff70</td>
<td></td>
</tr>
</tbody>
</table>

<%rsp points here at start of procedure
B. How many total bytes of local stack space are created in each frame (in decimal)?

_________________

C. When the function begins, where are the arguments (a, b) stored?

D. From a memory-usage perspective, why are iterative algorithms generally preferred over recursive algorithms?
5. Structs (15 points)

A. Draw a picture of the following struct, specifying the byte offset of each of the struct's fields and the size of any areas of fragmentation. Assume a 64-bit architecture.

```c
typedef struct blah {
    char b;
    int l;
    char *a;
    char h;
} blahblahblah;
```

B. How many bytes of internal fragmentation does the struct contain? External fragmentation?

Internal fragmentation:__________________

External fragmentation:__________________
C. Reorder the fields of the struct to minimize fragmentation:

```c
typedef struct blah {
    __________
    __________
    __________
    __________
    __________
} blah blah blah;
```

D. What is the size of the reordered struct?

```
_________________
```

E. How many bytes of internal fragmentation does the struct contain? External?

```
Internal fragmentation:_________________

External fragmentation:_________________
```
Powers of 2:

| $2^0$ = 1 | $2^{-1} = .5$ |
| $2^1$ = 2 | $2^{-2} = .25$ |
| $2^2$ = 4 | $2^{-3} = .125$ |
| $2^3$ = 8 | $2^{-4} = .0625$ |
| $2^4$ = 16 | $2^{-5} = .03125$ |
| $2^5$ = 32 | $2^{-6} = .015625$ |
| $2^6$ = 64 | $2^{-7} = .0078125$ |
| $2^7$ = 128 | $2^{-8} = .00390625$ |
| $2^8$ = 256 | $2^{-9} = .001953125$ |
| $2^9$ = 512 | $2^{-10} = .0009765625$ |

Assembly Code Instructions:

- **push**: push a value onto the stack and decrement the stack pointer
- **pop**: pop a value from the stack and increment the stack pointer
- **call**: jump to a procedure after first pushing a return address onto the stack
- **ret**: pop return address from stack and jump there
- **mov**: move a value between registers and memory
- **lea**: compute effective address and store in a register
- **add**: add src (1st operand) to dst (2nd) with result stored in dst (2nd)
- **sub**: subtract src (1st operand) from dst (2nd) with result stored in dst (2nd)
- **and**: bit-wise AND of src and dst with result stored in dst
- **or**: bit-wise OR of src and dst with result stored in dst
- **sar**: shift data in the dst to the right (arithmetic shift) by the number of bits specified in 1st operand
- **jmp**: jump to address
- **jne**: conditional jump to address if zero flag is not set
- **cmp**: subtract src (1st operand) from dst (2nd) and set flags
- **test**: bit-wise AND src and dst and set flags
Register map for x86-64:

Note: all registers are caller-saved except those explicitly marked as callee-saved, namely, rbx, rbp, r12, r13, r14, and r15. rsp is a special register.

<table>
<thead>
<tr>
<th>Register</th>
<th>Description</th>
<th>Register</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>%rax</td>
<td>Return value</td>
<td>%r8</td>
<td>Argument #5</td>
</tr>
<tr>
<td>%rbx</td>
<td>Callee saved</td>
<td>%r9</td>
<td>Argument #6</td>
</tr>
<tr>
<td>%rcx</td>
<td>Argument #4</td>
<td>%r10</td>
<td>Caller saved</td>
</tr>
<tr>
<td>%rdx</td>
<td>Argument #3</td>
<td>%r11</td>
<td>Caller Saved</td>
</tr>
<tr>
<td>%rsi</td>
<td>Argument #2</td>
<td>%r12</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%rdi</td>
<td>Argument #1</td>
<td>%r13</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%rsp</td>
<td>Stack pointer</td>
<td>%r14</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%rbp</td>
<td>Callee saved</td>
<td>%r15</td>
<td>Callee saved</td>
</tr>
</tbody>
</table>