Please read through the entire examination first! We designed this exam so that it can be completed in 50 minutes and, hopefully, this estimate will prove to be reasonable.

There are 4 problems for a total of 90 points. The point value of each problem is indicated in the table below. Write your answer neatly in the spaces provided. If you need more space, you can write on the back of the sheet where the question is posed, but please make sure that you indicate clearly the problem to which the comments apply. If you have difficulty with part of a problem, move on to the next one. They are independent of each other.

The exam is CLOSED book and CLOSED notes (no summary sheets, no calculators, no mobile phones, no laptops). Please do not ask or provide anything to anyone else in the class during the exam. Make sure to ask clarification questions early so that both you and the others may benefit as much as possible from the answers.

Good Luck!

Name: ____________________________
UWNet ID: _________________________
Quiz Section: _______________________

<table>
<thead>
<tr>
<th>Problem</th>
<th>Max Score</th>
<th>Score</th>
</tr>
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<tbody>
<tr>
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<td>30</td>
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</tr>
<tr>
<td>TOTAL</td>
<td>90</td>
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</tr>
</tbody>
</table>
1. Integers and Floats (20 points)

We define two new types as follows:

- **Nine_ints** are 9-bit signed two’s complement integers.
- **Nine_floats** are 9-bit floating point numbers with 4 bits for the exponent, 4 bits for the fraction, and 1 bit for the sign. **Nine_floats** are similar to IEEE floating point as far as layout of sign, exponent and fraction and represent special values (e.g. 0, pos and neg infinity, NAN) similar to how they are represented in 32 bit IEEE floating point.

A. What is the largest positive number we can represent with **Nine_ints**?

   Bit pattern in binary:

   Value in decimal:

B. What is the bias for **Nine_float**?
C. What is the largest positive number we can represent with Nine_floats?

Bit pattern in binary:

Value in decimal:

D. Assuming rules similar to those for conversions between IEEE floats and ints and addition in C, circle all the statements below that are TRUE.

a. It is possible to lose precision when converting from Nine_ints to Nine_floats.

b. It is possible to lose precision when converting from Nine_floats to Nine_ints.

c. The smallest negative number representable as a Nine_int < The smallest negative number representable as a Nine_float. (Reminder: -4 < -3)

d. Adding a negative Nine_float to a positive Nine_float will not result in a loss of precision.
2. Arrays (10 points)

Given the following C function:

```c
long int sum_pair(long int z[16], long int dig)
{
    return z[dig] + z[dig + 1];
}
```

Write x86-64 bit assembly code for this function here. You can assume that 0 <= dig < 15. Comments are not required but could help for partial credit.

`sum_pair`:
3. Assembly to C (30 points)

Given the C code for the function `trick()`, determine which IA32 and x86-64 code snippet corresponds to a correct implementation of `trick()`.

```c
int trick (int *x, int y) {
    int temp = *x * 5;
    int result = temp & y;
    return result - y;
}
```
A. Circle all of the IA-32 implementations below that correctly implement trick() (there could be more than one). For implementations that are not correct give at least one reason each why it is not correct. (You do not need to give reasons why the correct ones are correct.)

i) pushl %ebp
    movl %esp, %ebp
    leal 8(%ebp), %eax
    movl %eax, %edx
    sall $2, %eax
    addl %edx, %eax
    andl 12(%ebp), %eax
    subl 12(%ebp), %eax
    popl %ebp
    ret

Reason:

ii) pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %eax
    movl (%eax), %edx
    movl %edx, %eax
    addl %eax, %edx
    addl %edx, %eax
    andl 12(%ebp), %eax
    subl 12(%ebp), %eax
    popl %ebp
    ret

Reason:

iii) pushl %ebp
    movl %esp, %ebp
    movl 12(%ebp), %edx
    movl 8(%ebp), %eax
    movl (%eax), %eax
    leal (%eax,%eax,4), %eax
    andl %edx, %eax
    subl %edx, %eax
    popl %ebp
    ret

Reason:
B. Circle all of the x86-64 implementations below that correctly implement \texttt{trick()} (there could be more than one). For implementations that are not correct give at least one reason each why it is not correct. (You do not need to give reasons why the correct ones are correct.)

\begin{enumerate}
\item \texttt{movl} (%rdi), %eax  
\texttt{addl} (%rax), %eax  
\texttt{addl} %eax, %eax  
\texttt{andl} %esi, %eax  
\texttt{subl} %esi, %eax  
\texttt{ret}
\textbf{Reason:}

\item \texttt{movl} (%rdi), %eax  
\texttt{leal} (%rax,%rax,4), %eax  
\texttt{andl} %esi, %eax  
\texttt{subl} %esi, %eax  
\texttt{ret}
\textbf{Reason:}

\item \texttt{movl} (%rdi), %eax  
\texttt{leal} (%eax,%eax,2), %eax  
\texttt{addl} %eax, %eax  
\texttt{andl} %esi, %eax  
\texttt{subl} %esi, %eax  
\texttt{ret}
\textbf{Reason:}
\end{enumerate}
4. Stack Discipline (30 points)

Examine the following recursive function:

```c
long int treat(long int a, long int *b) {
    if (a <= 0) {
        return *b;
    } else {
        return treat(a-*b, b);
    }
}
```

Here is the x86_64 assembly for the same function:

```
4005fc <treat>:
4005fc:   sub    $0x18,%rsp
400600:   mov    %rdi,0x8(%rsp)
400605:   mov    %rsi,(%rsp)
400609:   cmpq   $0x0,0x8(%rsp)
40060f:   jg     0x40061a <treat+30>
400611:   mov    (%rsp),%rax
400615:   mov    (%rax),%rax
400618:   jmp    0x400638 <treat+60>
40061a:   mov    (%rsp),%rax
40061e:   mov    (%rax),%rax
400621:   mov    0x8(%rsp),%rdx
400626:   sub    %rax,%rdx
400629:   mov    (%rsp),%rax
40062d:   mov    %rax,%rsi
400630:   mov    %rdx,%rdi
400633:   callq  0x4005fc <treat>
400638:   add    $0x18,%rsp
40063c:   retq
```
Suppose we call `treat(7, &val)` from `main()`, with registers `%rsi = 0x7ff...ffb00` and `%rdi = 7`. The value stored at address `0x7ff...ffb00` is the long int value 5. We set a breakpoint just before the statement “`return *b`” executes (i.e. we are just about to return from `treat()` without making another recursive call but have not yet executed the `add` instruction before `retq`). Draw what the stack will look like when the program hits that breakpoint. Start at the top of the stack and go all the way down to the return address back to `main()` shown currently on the stack. Give both a description of the item stored at that location and the value stored at that location. If a location on the stack is not used, write “unused” in the Description for that address and put “-----” for its Value. You may list the Values in hex or decimal. Unless preceded by `0x` we will assume decimal. It is fine to use `f...f` for sequences of `f`’s as shown above for `%rsi`. Add more rows to the table as needed.

<table>
<thead>
<tr>
<th>Memory address on stack</th>
<th>Name/description of item</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x7fffffffffffffffffad0</td>
<td>Return address back to main</td>
<td>0x400827</td>
</tr>
<tr>
<td>0x7fffffffffffffffffac8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffffac0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffffab8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffffab0</td>
<td></td>
<td></td>
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<tr>
<td>0x7fffffffffffffffffaa8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffffaa0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffff98</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffff90</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffff88</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffff80</td>
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<td>0x7fffffffffffffffff78</td>
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<td>0x7fffffffffffffffff70</td>
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<tr>
<td>0x7fffffffffffffffff68</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0x7fffffffffffffffff60</td>
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<td></td>
</tr>
</tbody>
</table>
B. What is the value stored in register $rsp at the start of the procedure (in hex or decimal)?

C. What is the value stored in register $rsp when the breakpoint is reached (in hex or decimal)?

D. What value is returned by \texttt{treat(7, \&val)}?

E. Where will that return value be found?
# REFERENCES

## Powers of 2:

<table>
<thead>
<tr>
<th>Power</th>
<th>Value</th>
<th>Fraction</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2^0$</td>
<td>1</td>
<td>.5</td>
</tr>
<tr>
<td>$2^1$</td>
<td>2</td>
<td>.25</td>
</tr>
<tr>
<td>$2^2$</td>
<td>4</td>
<td>.125</td>
</tr>
<tr>
<td>$2^3$</td>
<td>8</td>
<td>.0625</td>
</tr>
<tr>
<td>$2^4$</td>
<td>16</td>
<td>.03125</td>
</tr>
<tr>
<td>$2^5$</td>
<td>32</td>
<td>.015625</td>
</tr>
<tr>
<td>$2^6$</td>
<td>64</td>
<td>.0078125</td>
</tr>
<tr>
<td>$2^7$</td>
<td>128</td>
<td>.00390625</td>
</tr>
<tr>
<td>$2^8$</td>
<td>256</td>
<td>.001953125</td>
</tr>
<tr>
<td>$2^9$</td>
<td>512</td>
<td>.0009765625</td>
</tr>
<tr>
<td>$2^{10}$</td>
<td>1024</td>
<td>.00048828125</td>
</tr>
</tbody>
</table>

## Assembly Code Instructions:

- **push**: push a value onto the stack and decrement the stack pointer
- **pop**: pop a value from the stack and increment the stack pointer
- **call**: jump to a procedure after first pushing a return address onto the stack
- **ret**: pop return address from stack and jump there
- **mov**: move a value between registers and memory
- **lea**: compute effective address and store in a register
- **add**: add src (1\(^{st}\) operand) to dst (2\(^{nd}\) with result stored in dst (2\(^{nd}\)
- **sub**: subtract src (1\(^{st}\) operand) from dst (2\(^{nd}\) with result stored in dst (2\(^{nd}\)
- **and**: bit-wise AND of src and dst with result stored in dst
- **or**: bit-wise OR of src and dst with result stored in dst
- **sar**: shift data in the dst to the right (arithmetic shift) by the number of bits specified in 1\(^{st}\) operand

- **jmp**: jump to address
- **jne**: conditional jump to address if zero flag is not set
- **cmp**: subtract src (1\(^{st}\) operand) from dst (2\(^{nd}\) and set flags
- **test**: bit-wise AND src and dst and set flags
Register map for x86-64:

Note: all registers are caller-saved except those explicitly marked as callee-saved, namely, rbx, rbp, r12, r13, r14, and r15. rsp is a special register.

<table>
<thead>
<tr>
<th>Register</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>%rax</td>
<td>Return value</td>
</tr>
<tr>
<td>%rbx</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%rcx</td>
<td>Argument #4</td>
</tr>
<tr>
<td>%rdx</td>
<td>Argument #3</td>
</tr>
<tr>
<td>%rsi</td>
<td>Argument #2</td>
</tr>
<tr>
<td>%rdi</td>
<td>Argument #1</td>
</tr>
<tr>
<td>%rsp</td>
<td>Stack pointer</td>
</tr>
<tr>
<td>%rbp</td>
<td>Callee saved</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Register</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>%r8</td>
<td>Argument #5</td>
</tr>
<tr>
<td>%r9</td>
<td>Argument #6</td>
</tr>
<tr>
<td>%r10</td>
<td>Caller saved</td>
</tr>
<tr>
<td>%r11</td>
<td>Caller Saved</td>
</tr>
<tr>
<td>%r12</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%r13</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%r14</td>
<td>Callee saved</td>
</tr>
<tr>
<td>%r15</td>
<td>Callee saved</td>
</tr>
</tbody>
</table>