Do not turn the page until 11:30.

Instructions

- This exam contains 10 pages, including this cover page. Show scratch work for partial credit, but put your final answers in the boxes and blanks provided.
- The last page is a reference sheet. Feel free to detach it from the rest of the exam.
- The exam is closed book (no laptops, tablets, wearable devices, or calculators). You are allowed one page (US letter, double-sided) of handwritten notes.
- Please silence and put away all cell phones and other mobile or noise-making devices. Remove all hats, headphones, and watches.
- You have 50 minutes to complete this exam.

Advice

- Read questions carefully before starting. Skip questions that are taking a long time.
- Read all questions first and start where you feel the most confident.
- Relax. You are here to learn.

<table>
<thead>
<tr>
<th>Question</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Possible Points</td>
<td>12</td>
<td>12</td>
<td>8</td>
<td>11</td>
<td>12</td>
<td>55</td>
</tr>
</tbody>
</table>
Question 1: Number Representation [12 pts]

(A) What is the value of the char 0b 1101 1101 in decimal? [1 pt]
If \( x = 0xDD \), \( -x = 0x23 = 2^5 + 3 = 35 \)
Also accepted unsigned: \( 0xDD = (16+1)*13 = 221 \)
-35 or 221

(B) What is the value of char \( z = (0xB << 7) \) in decimal? [1 pt]
\( 0xB << 7 = 0b 1000 0000 = \text{TMin}_\text{char} = -128 \)
Also accepted unsigned: \( 0x80 = 128 \)
-128 or 128

(C) Let char \( x = 0xC0 \). Give one value (in hex) for char \( y \) that results in both signed and unsigned overflow for \( x+y \). [2 pt]
\( x < 0 \), so need large enough (in magnitude) neg num for signed overflow. Unsigned overflow comes naturally along with this.
\( 0x80 \leq y \leq 0xBF \)

For the rest of this problem we are working with a floating point representation that follows the same conventions as IEEE 754 except using 8 bits split into the following vector widths:

<table>
<thead>
<tr>
<th>Sign (1)</th>
<th>Exponent (3)</th>
<th>Mantissa (4)</th>
</tr>
</thead>
</table>

(D) What is the magnitude of the bias of this new representation? [2 pt]
Bias = \(-(2^{3-1} - 1) = -3 \)
3

(E) Translate the floating point number 0b 1110 1010 into decimal. [3 pt]
\( S = 1, E = 110_2, M = 1010_2 \). Notice that E indicates this is not a special case.
Exp = 6 + (-3) = 3, Man = 1.1012.
\((-1)^1 \times 1.1012 \times 2^3 = -1101_2 = -(8 + 4 + 1) = -13.\)
-13

(F) What is the smallest positive integer that can’t be represented in this floating point encoding scheme? Hint: For what integer will the “one’s digit” get rounded off? [3 pt]
Max norm number = \(1.1111 \times 2^{6-3} = 15.5\), so 16.
Based on hint: Look for number such that the \(2^0\)-1 bit is just off the end of the mantissa, so of the form \(1.00001\times2^\text{Exp}\), with the underlined bit being \(2^0\).
Counting to the left, we find that \(\text{Exp} = 5\), and \(1.00001 \times 2^5 = 33.\)
16 or 33
Question 2: Pointers & Memory [12 pts]

For this problem we are using a 64-bit x86-64 machine (little endian). The initial state of memory (values in hex) is shown below:

<table>
<thead>
<tr>
<th>Word Addr</th>
<th>+0</th>
<th>+1</th>
<th>+2</th>
<th>+3</th>
<th>+4</th>
<th>+5</th>
<th>+6</th>
<th>+7</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x00</td>
<td>AC</td>
<td>AB</td>
<td>03</td>
<td>01</td>
<td>BA</td>
<td>5E</td>
<td>BA</td>
<td>11</td>
</tr>
<tr>
<td>0x08</td>
<td>5E</td>
<td>00</td>
<td>AB</td>
<td>0C</td>
<td>BE</td>
<td>A7</td>
<td>CE</td>
<td>FA</td>
</tr>
<tr>
<td>0x10</td>
<td>1D</td>
<td>B0</td>
<td>99</td>
<td>DE</td>
<td>AD</td>
<td>60</td>
<td>BB</td>
<td>40</td>
</tr>
<tr>
<td>0x18</td>
<td>14</td>
<td>CD</td>
<td>FA</td>
<td>1D</td>
<td>D0</td>
<td>41</td>
<td>ED</td>
<td>77</td>
</tr>
<tr>
<td>0x20</td>
<td>BA</td>
<td>B0</td>
<td>FF</td>
<td>20</td>
<td>80</td>
<td>AA</td>
<td>BE</td>
<td>EF</td>
</tr>
</tbody>
</table>

char* cp = 0x12  
short* sp = 0x0C  
unsigned* up = 0x2C

(A) What are the values (in hex) stored in each register shown after the following x86 instructions are executed? Remember to use the appropriate bit widths. [6 pt]

<table>
<thead>
<tr>
<th>Register</th>
<th>Value (hex)</th>
</tr>
</thead>
<tbody>
<tr>
<td>%rdi</td>
<td>0x0000 0000 0000 0000 0004</td>
</tr>
<tr>
<td>%rsi</td>
<td>0x0000 0000 0000 0000 0000</td>
</tr>
<tr>
<td>%ax</td>
<td>0x0004</td>
</tr>
<tr>
<td>%bl</td>
<td>0xBE</td>
</tr>
<tr>
<td>%rcx</td>
<td>0x0000 0000 FFFF B0BA</td>
</tr>
</tbody>
</table>

leaw (%rsi, %rdi), %ax
movb 8(%rdi), %bl
movswl (%rdi, 8), %ecx

movb instruction pulls byte from memory at address 8 + 4 = 12 = 0x0C.
movswl instruction pulls 2 bytes from memory starting at addresses 8 * 4 = 32 = 0x20.

Remember little-endian! Then sign extended to 32 bits, zero out top 32 bits.

(B) It’s a memory scavenger hunt! Complete the C code below to fulfill the behaviors described in the comments using pointer arithmetic. [6 pt]

```c
long v1 = (long) *(cp + __3__); // set v1 = 0x60
unsigned* v2 = up + __5__; // set v2 = 64
long v3 = *(long *)(sp + __1__); // set v3 = 0xB01DFACE
```

v1: Byte 0x60 is at address 0x15. 0x15 - cp = 3.
v2: No dereferencing, just pointer arithmetic (scaled by sizeof(unsigned)=4).
    up = 0x2C = 44. To get to 64, need to add 20 (5 by pointer arithmetic).
v3: The correct bytes can be found (in little-endian order) in addresses 0x0E-0x11.
    Want (0x0E - sp)/sizeof(short) = 1.
Question 3: Computer Architecture Design  [8 pts]

Answer the following questions in the boxes provided with a single sentence fragment. Please try to write as legibly as possible.

(A) Why can’t we upgrade to more registers like we can with memory?  [2 pt]

Registers are part of the CPU (and the architecture) and are not modular like RAM.

(B) Why don’t we see new assembly instruction sets as frequently as we see new programming languages?  [2 pt]

Hard to implement/get adopted – need to build new hardware. (by comparison, a new programming language only needs a new compiler – software)

(C) Name one reason why a program written in a CISC language might run slower than the same program written in a RISC language and one reason why the reverse might be true:  [4 pt]

CISC slower: Complicated instructions take longer to execute (fewer instructions, but each is slower).

RISC slower: Need more instructions to do complicated computations (faster instructions, but more numerous).
Question 4: C & Assembly [11 pts]

We are writing the function toLower, which takes a char pointer and converts a string of letters (assume only letters and spaces) to lowercase, leaving spaces as spaces. Example: If the pointer p points to “TeST oNe”, then after toLower(p), p now points to “test one”.

<table>
<thead>
<tr>
<th>ASCII</th>
<th>'A'</th>
<th>'Z'</th>
<th>Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>Binary</td>
<td>0b 0100 0001</td>
<td>0b 0101 1010</td>
<td>0b 0010 0000</td>
</tr>
<tr>
<td>Binary</td>
<td>0b 0110 0001</td>
<td>0b 0111 1010</td>
<td>0b 0010 0000</td>
</tr>
</tbody>
</table>

(A) Using the table of ASCII values (in binary) above, complete the function using a bitwise operator: [2 pt]

```c
void toLower(char * p) {
    while(*p != 0) {
        *p = __*_p | 0x20_________;
        p++;
    }
}
```

(B) Fill in the blanks in the x86-64 code below with the correct instructions and operands. *Remember to use the proper size suffixes and correctly-sized register names!* You may assume that Lines 4, 7, and 8 are correctly filled in. [9 pt]

```assembly
toLower(char*):
  1  movzbq (%rdi), %rax # get *p
  2  testb %al, %al     # conditional
  3  je  .Exit          # conditional jump
  .Loop:
  4  <<answer to part (A)>> # to lowercase
  5  movb %al, (%rdi)   # update char in memory
  6  addq $1, %rdi      # increment p
  7  <<same as Line 1>> # get new *p
  8  <<same as Line 2>> # conditional
  9  jne .Loop          # conditional jump
  .Exit:
  10 ret                  # return
```
Grading Notes for Question 4:

Line 1: must be dereference, must be 64-bit register name, p is first argument (%rdi).

Line 2: any width specifier accepted as long as register names match
(testq/%rax, testl/%eax, testw/%ax).
Also accepted cmpq $0, %rax (same idea with width specifiers).

Line 5: points awarded as long as it matched the Line 1 blank.

Line 6: must be q width specifier because destination is %rdi.

Line 9: points awarded as long as it was the opposite of the Line 3 blank.

Line 10: retq also accepted.
**Question 5:** The Stack  [12 pts]

The recursive factorial function `fact()` and its x86-64 disassembly is shown below:

```c
int fact(int n) {
    if(n==0 || n==1) return 1;
    return n*fact(n-1);
}
```

(A) Circle one:  [1 pt] `fact()` is saving `%rdi` to the Stack as a [Caller] [Callee]

(B) How much space (in bytes) does this function take up in our final executable?  [2 pt]

Count all bytes (middle columns) or subtract address of next instruction (0x40054d) from 0x40052d.

32 B

(C) **Stack overflow** is when the stack exceeds its limits (i.e. runs into the Heap). Provide an argument to `fact(n)` here that will cause stack overflow.  [2 pt]

Any negative int

We did mention in the lecture slides that the Stack has 8 MiB limit in x86-64, so since 16B per stack frame, credit for anything between $2^{10}$ and TMax ($2^{31}-1$).
(D) If we use the main function shown below, answer the following for the execution of the entire program: [4 pt]

```c
void main() {
    printf("result = %d\n", fact(3));
}
```

<table>
<thead>
<tr>
<th>Total frames created:</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum stack frame depth:</td>
<td>4</td>
</tr>
</tbody>
</table>

main → fact(3) → fact(2) → fact(1)
→ printf

(E) In the situation described above where main() calls fact(3), we find that the word 0x2 is stored on the Stack at address 0x7fffdc7ba888. At what address on the Stack can we find the return address to main()? [3 pt]

Only %rdi (current n) and return address get pushed onto Stack during fact().

<table>
<thead>
<tr>
<th>Address</th>
<th>Contents</th>
</tr>
</thead>
<tbody>
<tr>
<td>0x7fffdc7ba8a0</td>
<td>Return addr to main()</td>
</tr>
<tr>
<td>0x7fffdc7ba898</td>
<td>Old %rdi (n=3)</td>
</tr>
<tr>
<td>0x7fffdc7ba890</td>
<td>Return addr to fact()</td>
</tr>
<tr>
<td>0x7fffdc7ba888</td>
<td>Old %rdi (n=2)</td>
</tr>
<tr>
<td>0x7fffdc7ba880</td>
<td>Return addr to fact()</td>
</tr>
</tbody>
</table>