



## CSE341: Programming Languages

Lecture 6 Nested Patterns Exceptions Tail Recursion

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## Useful example: zip/unzip 3 lists

fun zip3 lists =	
case lists of	
([],[],[]) => []	
<pre>(hd1::tl1,hd2::tl2,hd3::tl3) =&gt;</pre>	
(hd1, hd2, hd3)::: zip3(t11, t12, t13)	
<pre>  _ =&gt; raise ListLengthMismatch</pre>	
fun unzip3 triples =	
case triples of	

```
[] => ([],[],[])
| (a,b,c)::t1 =>
    let val (11, 12, 13) = unzip3 t1
    in
        (a::11,b::12,c::13)
```

## end More examples in .sml files

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# Nested patterns

- We can nest patterns as deep as we want
  - Just like we can nest expressions as deep as we want
  - Often avoids hard-to-read, wordy nested case expressions
- So the full meaning of pattern-matching is to compare a pattern against a value for the "same shape" and bind variables to the "right parts"
  - More precise recursive definition coming after examples

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## Style

- Nested patterns can lead to very elegant, concise code

   Avoid nested case expressions if nested patterns are simpler
  - and avoid unnecessary branches or let-expressions • Example: unzip3 and nondecreasing
  - A common idiom is matching against a tuple of datatypes to compare them
    - Examples: zip3 and multsign
- Wildcards are good style: use them instead of variables when you do not need the data
  - Examples: len and multsign

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# (Most of) the full definition

The semantics for pattern-matching takes a pattern p and a value v and decides (1) does it match and (2) if so, what variable bindings are introduced.

Since patterns can nest, the definition is elegantly recursive, with a separate rule for each kind of pattern. Some of the rules:

- If *p* is a variable *x*, the match succeeds and *x* is bound to *v*
- If *p* is \_, the match succeeds and no bindings are introduced
- If p is (p1,...,pn) and v is (v1,...,vn), the match succeeds if and only if p1 matches v1, ..., pn matches vn. The bindings are the union of all bindings from the submatches
- If p is C p1, the match succeeds if v is C v1 (i.e., the same constructor) and p1 matches v1. The bindings are the bindings from the submatch.
- ... (there are several other similar forms of patterns)

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# Examples

- Pattern a::b::c::d matches all lists with >= 3 elements
- Pattern a::b::c::[] matches all lists with 3 elements
- Pattern ((a,b), (c,d))::e matches all non-empty lists of pairs of pairs

# Example a set of the set of

## Actually...

Exceptions are a lot like datatype constructors...

- Declaring an exception adds a constructor for type exn
- Can pass values of exn anywhere (e.g., function arguments)
   Not too common to do this but can be useful
- handle can have multiple branches with patterns for type exn

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## Recursion

Should now be comfortable with recursion:

- No harder than using a loop (whatever that is ©)
- · Often much easier than a loop
  - When processing a tree (e.g., evaluate an arithmetic expression)
  - Examples like appending lists
  - Avoids mutation even for local variables
- Now:
  - How to reason about efficiency of recursion
  - The importance of tail recursion
  - Using an accumulator to achieve tail recursion
  - [No new language features here]

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## Call-stacks

While a program runs, there is a *call stack* of function calls that have started but not yet returned

- Calling a function f pushes an instance of f on the stack
- When a call to finishes, it is popped from the stack

These stack-frames store information like the value of local variables and "what is left to do" in the function

Due to recursion, multiple stack-frames may be calls to the same function

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# Example

fun fact n = if n=0 then 1 else n\*fact(n-1)
val x = fact 3
fact 2 fact 2 fact 2 fact 2 fact 2 fact 2 fact 2

fact 3	fact 3: 3*_	fact 3: 3*_	fact 3: 3*_
	fact2	fact 2: 2*_	fact 2: 2*_
		fact1	fact1:1*_
			fact0

fact 3: 3*_	fact 3: 3*_	fact 3: 3*_	fact 3: 3*2
fact 2: 2*_	fact 2: 2*_	fact 2: 2*1	
fact1:1*_	fact 1: 1*1		
fact0: 1	CSE341: Programming Languages		11

## Example Revised



Still recursive, more complicated, but the result of recursive calls *is* the result for the caller (no remaining multiplication)

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And another	Actually much better
fun rev xs =	
case xs of [] => []	fun rev xs =
x::xs' => (rev xs') @ [x]	case xs of [] => []
fun rev xs =	x::xs' => (rev xs') @ [x]
let fun aux(xs,acc) = case xs of	<ul> <li>For fact and sum, tail-recursion is faster but both ways linear time</li> <li>Non-tail recursive rev is quadratic because each recursive call</li> </ul>
[] => acc   x::xs' => aux(xs',x::acc)	uses append, which must traverse the first list
in	<ul> <li>And 1+2++(length-1) is almost length*length/2</li> </ul>
aux (xs,[]) end	<ul> <li>Moral: beware list-append, especially within outer recursion</li> <li>Cons constant-time (and fast), so accumulator version much better</li> </ul>
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Always tail-recursive?	What is a tail-call?
There are certainly cases where recursive functions cannot be	
evaluated in a constant amount of space	The "nothing left for caller to do" intuition usually suffices
Most obvious examples are functions that process trees	<ul> <li>If the result of f x is the "immediate result" for the enclosing function body, then f x is a tail call</li> </ul>
nosi obvious examples are functions that process trees	
In these cases, the natural recursive approach is the way to go	But we can define "tail position" recursively
<ul> <li>You could get one recursive call to be a tail call, but rarely worth the complication</li> </ul>	<ul> <li>Then a "tail call" is a function call in "tail position"</li> </ul>
wordt are complication	
Also beware the wrath of premature optimization	
<ul> <li>Favor clear, concise code</li> </ul>	
<ul> <li>But do use less space if inputs may be large</li> </ul>	
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Draging definition	
Precise definition	
A tail call is a function call in tail position	
If an expression is not in tail position, then no subexpressions are	
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<ul> <li>In fun f p = e, the body e is in tail position</li> <li>If if e1 then e2 else e3 is in tail position, then e2 and e3</li> </ul>	
are in tail position (but e1 is not). (Similar for case-expressions)	
<ul> <li>If let b1 bn in e end is in tail position, then e is in tail position (but no binding expressions are)</li> </ul>	
<ul> <li>Function-call arguments e1 e2 are not in tail position</li> </ul>	
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