Set-up:
For this assignment, you will complete and extend two implementations of an interpreter for a small “lan-
guage” for two-dimensional geometry objects. One implementation is in SML and is mostly completed for
you. The other implementation is in Ruby and you will do most of it. The SML solution is structured with
functions and pattern-matching. The Ruby solution is structured with subclasses and methods, including
some mind-bending double dispatch and other dynamic dispatch to stick with an OOP style even where your
instructor thinks the ML-style design is easier to understand.
Download and edit hw7.sml and hw7.rb from the course website. Some example tests are also provided.

Language Semantics:
Our “language” has five kinds of values and four other kinds of expressions. The representation of expressions
depends on the metalanguage (SML or Ruby), with this same semantics:

- A **NoPoints** represents the empty set of two-dimensional points.
- A **Point** represents a two-dimensional point with an x-coordinate and a y-coordinate. Both coordinates
  are floating-point numbers.
- A **Line** is a non-vertical infinite line in the plane, represented by a *slope* and an *intercept* (as in
  \( y = mx + b \) where \( m \) is the slope and \( b \) is the intercept), both floating-point numbers.
- A **VerticalLine** is an infinite vertical line in the plane, represented by its x-coordinate.
- A **LineSegment** is a (finite) line segment, represented by the x- and y-coordinates of its endpoints (so
  four total floating-point numbers).
- An **Intersect** expression is not a value. It has two subexpressions. The semantics is to evaluate the
  subexpressions (in the same environment) and then return the value that is the intersection (in the
  geometric sense) of the two subresults. For example, the intersection of two lines could be one of:
  - **NoPoints**, if the lines are parallel
  - a **Point**, if the lines intersect
  - a **Line**, if the lines have the same slope and intercept (see the note below about what we mean
    by “the same” for floating-point numbers)
- A **Let** expression is not a value. It is like let-expressions in other languages we have studied: The first
  subexpression is evaluated and the result bound to a variable that is added to the environment for
  evaluating the second subexpression.
- A **Var** expression is not a value. It is for using variables in the environment: We look up a string in
  the environment to get a geometric value.
- A **Shift** expression is not a value. It has a *deltaX* (a floating-point number), a *deltaY* (a floating-point
  number), and a subexpression. The semantics is to evaluate the subexpression and then *shift* the result
  by *deltaX* (in the x-direction; positive is “to the right”) and *deltaY* (in the y-direction; positive is
  “up”). More specifically, shifting for each form of value is as follows:
  - **NoPoints** remains **NoPoints**
  - A **Point** representing \((x, y)\) becomes a **Point** representing \((x + \text{deltaX}, y + \text{deltaY})\).
  - A **Line** with slope \(m\) and intercept \(b\) becomes a **Line** with slope \(m\) and an intercept of
    \(b + \text{deltaY} - m \cdot \text{deltaX}\).
- A \texttt{VerticalLine} becomes a \texttt{VerticalLine} shifted by \textit{deltaX}; the \textit{deltaY} is irrelevant.
- A \texttt{LineSegment} has its endpoints shift by \textit{deltaX} and \textit{deltaY}.

\textbf{Note on Floating-Point Numbers:}

Because arithmetic with floating-point numbers can introduce small rounding errors, it is rarely appropriate to use equality to decide if two floating-point numbers are “the same.” Instead, the provided code uses a helper function/method to decide if two floating-point numbers are “real close” (for our purposes, within \texttt{.00001}) and all your code should follow this approach as needed. For example, two points are the same if their x-coordinates are within \texttt{.00001} and their y-coordinates are within \texttt{.00001}.

\textbf{Expression Preprocessing:}

To simplify the interpreter, we first preprocess expressions. Preprocessing takes an expression and produces a new, equivalent expression with the following invariants:

- No \texttt{LineSegment} anywhere in the expression has endpoints that are the same as (i.e., real close to) each other. Such a line-segment should be replaced with the appropriate \texttt{Point}. For example in ML syntax, \texttt{LineSegment(3.2,4.1,3.2,4.1)} should be replaced with \texttt{Point(3.2,4.1)}.

- Every \texttt{LineSegment} has its first endpoint (the first two real values in SML) to the left (lower x-value) of the second endpoint. If the x-coordinates of the two endpoints are the same (real close), then the first endpoint has its first endpoint below (lower y-value) the second endpoint. For any \texttt{LineSegment} not meeting this requirement, replace it with a \texttt{LineSegment} with the same endpoints reordered.

\textbf{The SML Code:}

\textit{Most of the SML solution is given to you.} All you have to do is add preprocessing (problem 1) and \texttt{Shift} expressions (problem 2). The sample solution added much less than 50 lines of code. As always, line counts are just a rough guide.

Notice the SML code is organized around a datatype-definition for expressions, functions for the different operations, and pattern-matching to identify different cases. The interpreter \texttt{eval prog} uses a helper function \texttt{intersect} with cases for every combination of geometric value (so with 5 kinds of values there are 25 cases though some are handled together via pattern-matching). The surprisingly complicated part is the algorithm for intersecting two line segments.

\textbf{The Ruby Code:}

\textit{Much of the Ruby solution is not given to you.} To get you started in the desired way, we have defined classes for each kind of expression in our language, as well as appropriate superclasses. We have implemented parts of each class and left comments with what you need to do to complete the implementation as described in more detail in problems 3 and 4. The sample solution added about 200 lines of Ruby code, many of which were \texttt{end}. As always, line counts are just a rough guide.

Notice the Ruby code is organized around classes where each class has methods for various operations. All kinds of expressions need methods for preprocessing and evaluation. They are subclasses of \texttt{GeometryExpression} just like all ML constructors are part of the \texttt{geom_exp} datatype (though the \texttt{GeometryExpression} class turns out not to be so useful). The value subclasses also need methods for shifting and intersection and they subclass \texttt{GeometryValue} so that some shared methods can be inherited (in analogy with some uses of wildcard patterns and helper functions in ML).

Your Ruby code should follow these general guidelines:

- All your geometry-expression objects should be \textit{immutable}: assign to instance variables only when constructing an object. To “change” a field, create a new object.
- The geometry-expression objects have public getter methods: like in the SML code, the entire program can assume the expressions have various coordinates, subexpressions, etc.
• Unlike in SML, you do not need to define exceptions since without a type-checker we can just “assume” the right objects are used in the right places. You can also use raise with just a string as appropriate.

• Follow OOP-style. In particular, operations should be instance methods and you should not use methods like is_a?, instance_of?, class, etc. This makes problem 4 much more difficult, which is the purpose of the problem.

Advice for Approaching the Assignment:

• Understand the high-level structure of the code and how the SML and Ruby files are structured in different ways before diving into the details.

• Approach the questions in order even though there is some flexibility (e.g., it is possible to do the Ruby problems before the SML problems).

• Because almost all the SML code is given to you, for much of the Ruby implementation, you can port the corresponding part of the SML solution. Doing so makes your job much easier (e.g., you need not re-figure out facts about geometry). Porting existing code to a new language is a useful and realistic skill to develop. It also helps teach the similarities and differences between languages.

• Be sure to test each line of your Ruby code. Dynamically typed languages require testing things that other languages catch for you statically. Compared to Racket, Ruby will not even tell you statically if you misspell a method name or instance variable.

The Problems (Finally):

1. Implement an SML function preprocess_prog of type geom_exp -> geom_exp to implement expression preprocessing as defined above. The idea is that evaluating program e would be done with eval_prog (preprocess_prog e, []) where the [] is the empty list for the empty environment.

2. Add shift expressions as defined above to the SML implementation by adding the constructor Shift of real * real * geom_exp to the definition of geom_exp and adding appropriate branches to eval_prog and preprocess_prog. (The first real is deltaX and the second is deltaY.) Do not change other functions. In particular, there is no need to change intersect because this function is used only for values in our geometry language and shift expressions are not geometry values.

3. Complete the Ruby implementation except for intersection, which means skip for now additions to the Intersect class and, more importantly, methods related to intersection in other classes. Do not modify the code given to you. Follow this approach:

- Every subclass of GeometryExpression should have a preprocess_prog method that takes no arguments and returns the geometry object that is the result of preprocessing self. To avoid mutation, return a new instance of the same class unless it is trivial to determine that self is already an appropriate result.

- Every subclass of GeometryExpression should have an eval_prog method that takes one argument, the environment, which you should represent as an array whose elements are two-element arrays: a Ruby string (the variable name) in index 0 and an object that is a value in our language in index 1. As in any interpreter, pass the appropriate environment when evaluating subexpressions. (This is fairly easy since we do not have closures.) The result of eval_prog is the result of “evaluating the expression represented by self,” so, as we expect with OOP style, the cases of ML’s eval_prog are spread among our classes, just like with preprocess_arg.

- Every subclass of GeometryValue should have a shift method that takes two arguments dx and dy and returns the result of shifting self by dx and dy. In other words, all values in the language “know how to shift themselves to create new objects.” Hence the eval_prog method in the Shift class should be very short.
4. Implement intersection in your Ruby solution following the directions here, in which we require both double dispatch and a separate use of dynamic dispatch for the line-segment case. Remember all the different cases in ML will appear somewhere in the Ruby solution, just arranged very differently.

- Implement `preprocess_prog` and `eval_prog` in the `Intersect` class. This is not difficult, much like your prior work in the `Shift` class is not difficult. This is because every subclass of `GeometryValue` will have an `intersect` method that “knows how to intersect itself” with another geometry-value passed as an argument.

- Every subclass of `GeometryValue` needs an `intersect` method, but these will be short. The argument is another geometry-value, but we do not know what kind. So we use double dispatch and call the appropriate method on the argument passing `self` to the method. For example, the `Point` class has an `intersect` method that calls `intersectPoint` with `self`.

- So methods `intersectNoPoints`, `intersectPoint`, `intersectLine`, `intersectVerticalLine`, and `intersectLineSegment` defined in each of our 5 subclasses of `GeometryValue` handle the 25 possible intersection combinations:
  - The 9 cases involving `NoPoints` are done for you. See the `GeometryValue` class — there is nothing more you need to do.
  - Next do the 9 remaining cases involving combinations that do not involve `LineSegment`. You will need to understand double-dispatch to avoid `is_a?` and `instance_of?`. As in the ML code, 3 of these 9 cases can just use one of the other cases because intersection is commutative.
  - What remains are the 7 cases where one value is a `LineSegment` and the other is not `NoPoints`. These cases are all “done” for you because all subclasses of `GeometryValue` inherit an `intersectLineSegment` method that will be correct for all of them. But it calls `intersectWithSegmentAsLineResult`, which you need to implement for each subclass of `GeometryValue`. Here is how this method should work:
    * It takes one argument, which is a line segment. (In ML the corresponding variable was a `real*real*real*real`, but here it will actually be an instance of `LineSegment` and you can use the getter methods `x1`, `y1`, `x2`, and `y2` as needed.)
    * It `assumes` that `self` is the intersection of (1) some not-provided geometry-value and (2) the line (vertical or not) containing the segment given as an argument.
    * It `returns` the intersection of the not-provided geometry-value and the segment given as an argument.

Together the 5 `intersectWithSegmentAsLineResult` methods you write will implement the same algorithm as on lines 110–169 of the ML code.

5. **Challenge Problem:** Make a third version of your solution in Java. Follow the structure of your Ruby solution, with no use of Java’s `instanceof` or type casts. Use abstract methods as necessary for type-checking.

**Turn-in Instructions:** Turn in four files using the Catalyst dropbox link on the course website:

- The SML file with your solution
- The Ruby file with your solution
- An SML file used for testing
- A Ruby file used for testing

If you do problem 5, turn in your Java files as well.