You will write 11 SML functions (and tests for them) related to calendar dates. In all problems, a “date” is an SML value of type `int*int*int`, where the first part is the year, the second part is the month, and the third part is the day. A “reasonable” date would have a positive year, a month between 1 and 12, and a day no greater than 31 (or less depending on the month). However, most problems do not assume “reasonable” dates; solutions should work for any `int*int*int` except where noted. A “day of year” is a number from 1 to 365 where, for example, 33 represents February 2. (We ignore leap years except in one challenge problem.)

The sample solution contains roughly 75–80 lines of code. See page 2 for additional instructions.

1. Write a function `is_older` that takes two dates and evaluates to true or false. It evaluates to true if the first argument is a date that comes before the second argument. (If the two dates are the same, the result is false.)

2. Write a function `number_in_month` that takes a list of dates and a month (i.e., an `int`) and returns how many dates in the list are in the given month.

3. Write a function `number_in_months` that takes a list of dates and a list of months (i.e., an `int` list) and returns the number of dates in the list of dates that are in any of the months in the list of months. Assume the list of months has no number repeated. Hint: Use your answer to the previous problem.

4. Write a function `dates_in_month` that takes a list of dates and a month (i.e., an `int`) and returns a list holding the dates from the argument list of dates that are in the month. The returned list should contain dates in the order they were originally given.

5. Write a function `dates_in_months` that takes a list of dates and a list of months (i.e., an `int` list) and returns a list holding the dates from the argument list of dates that are in any of the months in the list of months. Assume the list of months has no number repeated. Hint: Use your answer to the previous problem and SML’s list-append operator (\@).

6. Write a function `get_nth` that takes a list of strings and an `int` \( n \) and returns the \( n \)th element of the list where the head of the list is 1st. Do not worry about the case where the list has too few elements: your function may apply `hd` or `tl` to the empty list in this case, which is okay.

7. Write a function `date_to_string` that takes a date and returns a string of the form January 20, 2013 (for example). Use the operator \(^\) for concatenating strings and the library function `Int.toString` for converting an `int` to a `string`. For producing the month part, do not use a bunch of conditionals. Instead, use a list holding 12 strings and your answer to the previous problem. For consistency, put a comma following the day and use capitalized English month names: January, February, March, April, May, June, July, August, September, October, November, December.

8. Write a function `number_before_reaching_sum` that takes an `int` called `sum`, which you can assume is positive, and an `int` list, which you can assume contains all positive numbers, and returns an `int`. You should return an int \( n \) such that the first \( n \) elements of the list add to less than \( sum \), but the first \( n + 1 \) elements of the list add to \( sum \) or more. Assume the entire list sums to more than the passed in value; it is okay for an exception to occur if this is not the case.

9. Write a function `what_month` that takes a day of year (i.e., an `int` between 1 and 365) and returns what month that day is in (1 for January, 2 for February, etc.). Use a list holding 12 integers and your answer to the previous problem.

10. Write a function `month_range` that takes two days of the year `day1` and `day2` and returns an `int` list \([m1,m2,\ldots,mn]\) where \( m1 \) is the month of `day1`, \( m2 \) is the month of `day1+1`, ..., and \( mn \) is the month of day `day2`. Note the result will have length `day2 - day1 + 1` or length 0 if `day1 > day2`.

11. Write a function `oldest` that takes a list of dates and evaluates to an `(int*int*int)` option. It evaluates to `NONE` if the list has no dates and `SOME d` if the date \( d \) is the oldest date in the list.
12. **Challenge Problem:** Write functions `number_in_months_challenge` and `dates_in_months_challenge` that are like your solutions to problems 3 and 5 except having a month in the second argument multiple times has no more effect than having it once. (Hint: Remove duplicates, then use previous work.)

13. **Challenge Problem:** Write a function `reasonable_date` that takes a date and determines if it describes a real date in the common era. A “real date” has a positive year (year 0 did not exist), a month between 1 and 12, and a day appropriate for the month. Solutions should properly handle leap years. Leap years are years that are either divisible by 400 or divisible by 4 but not divisible by 100. (Do not worry about days possibly lost in the conversion to the Gregorian calendar in the Late 1500s.)

Note: Remember the course policy on challenge problems.

**Summary**

Evaluating a correct homework solution should generate these bindings:

```sml
val is_older = fn : (int * int * int) * (int * int * int) -> bool
val number_in_month = fn : (int * int * int) list * int -> int
val number_in_months = fn : (int * int * int) list * int list -> int
val dates_in_month = fn : (int * int * int) list * int -> (int * int * int) list
val dates_in_months = fn : (int * int * int) list * int list -> (int * int * int) list
val get_nth = fn : string list * int -> string
val date_to_string = fn : int * int * int -> string
val number_before_reaching_sum = fn : int * int list -> int
val what_month = fn : int -> int
val month_range = fn : int * int -> int list
val oldest = fn : (int * int * int) list -> (int * int * int) option
```

Of course, generating these bindings does not guarantee that your solutions are correct. **Test your functions:** Put your testing code in a separate file. We will not grade the testing file, but you must turn it in.

**Assessment**

Solutions should be:

- Correct
- In good style, including indentation and line breaks
- Written using features discussed in class. In particular, you must not use SML’s mutable references or arrays. (Why would you?) Also do not use pattern-matching; it is the focus of the next assignment.

**Turn-in Instructions**

- Put all your solutions in one file, `lastname_hw1.sml`, where `lastname` is replaced with your last name. Put tests you wrote in `lastname_hw1_test.sml`.
- Follow the dropbox link on the course website (homework section), follow the “Homework 1” link, and upload your files.
- If you have trouble using the dropbox, contact the course staff before the deadline.

**Syntax Hints**

Small syntax errors can lead to strange error messages. Here are 3 examples for function definitions:

1. `int * int * int list` means `int * int * (int list)`, not `(int * int * int) list`.
2. `fun f x : t` means the result type of `f` is `t`, whereas `fun f (x:t)` means the argument type of `f` is `t`.
   There is no need to write result types (and in later assignments, no need to write argument types).
3. `fun (x t), fun (t x), or fun (t : x)` are all wrong, but the error message suggests you are trying to do something much more advanced than you actually are (which is trying to write `fun (x : t)`).