1. (10 points) Write a Haskell function \texttt{mapfns}, and a type declaration for it (the most general type possible). \texttt{mapfns} takes a list of functions and a list of items, and that returns a new list consisting of the result of applying each function to the corresponding item. If there are a different number of functions and items, the resulting list is the same length as the shorter of the two. Examples:

\[
\text{ \texttt{mapfns \[\text{(+1), (*2), \text{sqrt}]\[2.0, 3.5, 4.0]\} \Rightarrow [3.0, 7.0, 2.0]}}
\]
\[
\text{\texttt{mapfns \[(+1), (+1)\] [1..] \Rightarrow [2, 3]}}
\]
2. (10 points) Write a Racket function `twice` that takes a list as an argument, and returns `#t` if there is at least one adjacent repeated element in the list, and otherwise `#f`. You can assume that the argument is a proper list. Use `equal?` to test whether one element is a repeat of the previous one. Examples:

```racket
(twice '()) => #f
(twice '(a b b c d e)) => #t
(twice '(a b c a b)) => #f
```

3. (8 points) Consider the `my-or` macro discussed in class. This works exactly the same as the built-in `or` macro in Racket.

```racket
(define-syntax my-or
  (syntax-rules ()
    ((my-or) #f)
    ((my-or e) e)
    ((my-or e1 e2 ...) (let ((temp e1))
                         (if temp temp
                             (my-or e2 ...))))))
```

It relies on macro hygiene. Demonstrate this by writing Racket code that would result in a wrong answer from `my-or` if Racket didn’t have macro hygiene. Also say both what the correct answer is, and what the answer would be if Racket didn’t have macro hygiene.
4. (8 points) Is MUPL statically typed? If it is, give a MUPL expression that has a type error that would be detected statically. If it is not, just say “no”. (For both this and the following question, you don’t need to remember the exact MUPL structs to build MUPL expressions; but if you’re not sure you’ve got the names correct say what they are and what they do so that we can grade these.)

Is MUPL type-safe? If it is, give a MUPL expression that has a type error that would be detected dynamically. If it is not, give a MUPL expression that would be evaluated incorrectly due to the type error.
As in the assignment, you should assume MUPL programs are syntactically correct, e.g., do not worry about wrong things like (int "hi") or (int (int 37)). Think of (int 3) as part of the program’s syntax its how you write the number 3 in MUPL.

5. (10 points) Consider a twice rule in Prolog, which looks for an element that occurs twice in a row in a list:

\[
\text{twice}([X,X|Xs],X).
\text{twice}([X|Xs],Y) :- \text{twice}(Xs,Y).
\]

What are all the answers returned for the following goals? If there are an infinite number, say that, and include at least the first 3 answers.

(a) twice([1,2,2],B).

(b) twice([1,2,2,1],B).

(c) twice([1,2,3,2,1],B).

(d) twice([1,2,2,2,3,1,1],B).

(e) twice(As,1).
6. (10 points) Now consider the `twice` rule again, but with cut:

\[
\text{twice}([X,X|Xs],X) :- !.
\text{twice}([X|Xs],Y) :- \text{twice}(Xs,Y).
\]

What are all the answers returned for the following goals? (These are the same as for Question 5.) If there are an infinite number, say that, and include at least the first 3 answers.

(a) `twice([1,2,2],B)`.

(b) `twice([1,2,2,1],B)`.

(c) `twice([1,2,3,2,1],B)`.

(d) `twice([1,2,2,2,3,1,1],B)`.

(e) `twice(As,1)`.

7. (6 points) Which of the following lists represent valid difference lists? For valid difference lists, what list do they represent?

- `[a,b,c]\[c]`
- `[a,b,c]\[a,b,c]`
- `[a,b,c]\[a,b]`
- `[a,b,c|T]\T`
- `[a,b,c|T]\[b,c|T]`
- `T\T`
8. (12 points) This question asks you to write some Prolog facts and rules — but as a twist, the facts and rules concern inheritance in an object-oriented lanugage.

(a) Write Prolog facts to represent that the class octopus is a subclass of seacreature, seacreature is a subclass of animal, and animal is a subclass of object. (Since we don’t want Prolog to think your names are Prolog variables, we’re using lower-case letters for the class names.)

(b) Write one or more Prolog rules for the ancestor relation. This is defined recursively: a class is an ancestor of itself, and also its superclass, the superclass of its superclass, etc. So the goal ancestor(seacreature,X) should succeed with X=seacreature. If you backtrack, it should succeed with X=animal, then X=object, and then fail. For full credit you need to produce the answers in exactly that order.

(c) Now suppose that our object-oriented language has multiple inheritance. Add rules for two more classes: dolphin and mammal, with dolphin a subclass of both mammal and seacreature, and mammal a subclass of animal. Do you need to modify your ancestor rule(s) to make them work with multiple inheritance? If so, write down the new version here; if not, say that no modification is needed.

What are all the answers are returned for the goal ancestor(dolphin,X)? For full credit you need to write down the answers in exactly the order that your program will return them. The answer X=dolphin should be produced first, but after that you can return the answers in any order; duplicates are OK.
9. (10 points) Consider the difference list version of reverse as given in the lecture notes:

\[
\text{reverse}(Xs, Rs) :- \text{reverse}\_dl(Xs, Rs\[\]).
\]

\[
\text{reverse}\_dl([], T\T).
\]

\[
\text{reverse}\_dl([X|Xs], Rs\T) :- \text{reverse}\_dl(Xs, Rs\[X|T]).
\]

Draw the derivation tree for the following goal:

\[- \text{reverse}([a,b,c], R).\]
10. (12 points) Consider the following Ruby classes and mixins.

```ruby
class C1
  def print_me
    "C1 print_me"
  end
  def test
    1
  end
end

module M1
  def print_me
    "M1 print_me"
  end
  def test
    10+super
  end
end

module M2
  def print_me
    "M2 print_me"
  end
  def test
    100
  end
end

class C2 < C1
  include M1
end

class C3 < C1
  include M1, M2
end

Now define variables c1, c2, and c3 as follows:

```ruby
c1 = C1.new
c2 = C2.new
c3 = C3.new
```  

What is printed as a result of evaluating the following expressions? (Remember that the value returned by a method is the value of the last expression, if there isn't an explicit return.)

```ruby
c1.print_me

c2.print_me

c3.print_me
```
11. (16 points) Define a Ruby class MySet that represents a set. (There’s already a built-in class Set — define your own however, rather than using the built-in one.) MySet should be a subclass of Object and should mix in Enumerable. Internally, it should use a Ruby array to hold its elements. As a reminder, a set is an unordered collection of elements, with no duplicates. The union of two sets A and B is a new set consisting of all elements that are in either A or B. The intersection of two sets A and B is a new set consisting of the elements that are in both A and B.

MySet should define the following methods:

- **initialize**: Initialize this to be an empty set.
- **add(element)**: Add an element to this set, if it’s not already a member. (This changes the set.)
- **union(other)**: Return a new set that is the union of the receiver and other. This doesn’t change the set (no side effect).
- **intersect(other)**: Return a new set that is the intersection of the receiver and other. This doesn’t change the set (no side effect).
- **each**: Needed for the Enumerable mixin.
12. (12 points) Consider the following Java programs Test1, Test2, and Test3. In each case, does the program compile correctly? If it doesn’t compile, indicate all the lines that result in a compilation error and what the error is. If it does compile, does it execute without error, or is there an exception? If it executes, what is the output, either for the whole program or up until the point where there is an exception? (Except for possible type errors, the programs are legal Java.)

/******************** Test1 *****************/
public class Test1 {
    public static void main(String[] args) {
        String[] a;
        Object[] b;
        a = new String[5];
        b = a;
        a[0] = "oyster";
        test(a, 1);
        test(b, 2);
        test((Object[]) a, 3);
        test((String[]) b, 4);
        for(int i = 0; i<a.length; i++) {
            System.out.print(a[i]);
            System.out.print(" ");
        }
        System.out.print("\n");
    }
    public static void test(Object[] c, int i) {
        c[i] = "clam";
    }
    public static void test(String[] c, int i) {
        c[i] = "squid";
    }
}

/******************** Test2 *********************/

/******************** Test3 *********************/
import java.util.LinkedList;
class Test2 {
    public static void main(String[] args) {
        LinkedList<String> a;
        LinkedList<Object> b;
        a = new LinkedList<String>();
        b = a;
        a.addFirst("oyster");
        test(a,1);
        test(b,2);
        for (String s : a) {
            System.out.print(s);
            System.out.print(" ");
        }
        System.out.print("\n");
    }
    public static void test(LinkedList<Object> c, int i) {
        c.add(i,"clam");
    }
    public static void test(LinkedList<String> c, int i) {
        c.add(i,"clam");
    }
}

class Test3 {
    public static void main(String[] args) {
        String[] a;
        Object[] b;
        a = new String[2];
        b = a;
        a[0] = "oyster";
        System.out.println("added an oyster");
        b[1] = new Integer(5);
        System.out.println("added an integer");
        for(int i = 0; i<a.length; i++) {
            System.out.println(a[i]);
            System.out.println(" ");
        }
        System.out.println("\n");
    }
}
13. (10 points) True or false?

(a) A Haskell expression of type \( \text{IO } t \) can never occur inside another expression of type \( (\text{Num } t) \Rightarrow [t] \) in an expression that typechecks correctly.

(b) In Java, adding an upcast can never change whether or not a program compiles, but could change the behavior of a program that does compile without the upcast.

(c) In Java, \text{Point[]} is a subtype of \text{Object[]}.

(d) In Java, \text{ArrayList<Point>} is a subtype of \text{ArrayList<Object>}.

(e) In Java, \text{ArrayList<Point>} is a subtype of \text{ArrayList<?>}.

(f) In Ruby, class \text{Object} is an instance of itself.

(g) In Ruby, class \text{Object} is a subclass of itself.

(h) In Ruby, class \text{Class} is an instance of itself.

(i) In Ruby, class \text{Class} is a subclass of itself.

(j) A Ruby class can have multiple superclasses, but only one mixin.