



# CSE341: Programming Languages Lecture 2 Functions, Pairs, Lists

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#### Review

- Building up SML one construct at a time via precise definitions
  - Constructs have syntax, type-checking rules, evaluation rules
    - And reasons they're in the language
  - Evaluation converts an *expression* to a *value*
- So far:
  - Variable bindings
  - Several expression forms: addition, conditionals, ...
  - Several types: int bool unit
- Today:
  - Brief discussion on aspects of learning a PL
  - Functions, pairs, and lists [*almost* enough for all of HW1]

## Five different things

- 1. Syntax: How do you write language constructs?
- 2. Semantics: What do programs mean? (Evaluation rules)
- 3. Idioms: What are typical patterns for using language features to express your computation?
- 4. Libraries: What facilities does the language (or a well-known project) provide "standard"? (E.g., file access, data structures)
- 5. Tools: What do language implementations provide to make your job easier? (E.g., REPL, debugger, code formatter, ...)

These are 5 separate issues

- In practice, all are essential for good programmers
- Many people confuse them, but shouldn't

### Our Focus

This course focuses on semantics and idioms

- Syntax is usually uninteresting
  - A fact to learn, like "The American Civil War ended in 1865"
  - People obsess over subjective preferences [yawn]
- Libraries and tools crucial, but often learn new ones on the job
  - We're learning language semantics and how to use that knowledge to do great things

## Function definitions

Functions: the most important building block in the whole course

- Like Java methods, have arguments and result
- But no classes, this, return, etc.

Example *function binding*:

```
(* Note: correct only if y>=0 *)
fun pow (x : int, y : int) =
    if y=0
    then 1
    else x * pow(x,y-1)
```

Note: The body includes a (recursive) function call: pow(x,y-1)

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## Function bindings: 3 questions

- Syntax: fun x0 (x1 : t1, ..., xn : tn) = e
   (Will generalize in later lecture)
- Evaluation: *A function is a value!* (No evaluation yet)
  - Adds x0 to environment so *later* expressions can *call* it
  - (Function-call semantics will also allow recursion)
- Type-checking:
  - Adds binding x0 : (t1 \* ... \* tn) -> t if:
  - Can type-check body e to have type t in the static environment containing:
    - "Enclosing" static environment (earlier bindings)
    - x1 : t1, ..., xn : tn (arguments with their types)
    - x0 : (t1 \* ... \* tn) -> t (for recursion)

## More on type-checking

fun x0 (x1: t1, ..., xn: tn) = e

- New kind of type: (t1 \* ... \* tn) -> t
  - Result type on right
  - The overall type-checking result is to give x0 this type in rest of program (unlike Java, not for earlier bindings)
  - Arguments can be used only in **e** (unsurprising)
- Because evaluation of a call to x0 will return result of evaluating
   e, the return type of x0 is the type of e
- The type-checker "magically" figures out t if such a t exists
  - Later lecture: Requires some cleverness due to recursion
  - More magic after hw1: Later can omit argument types too

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## Function Calls

A new kind of expression: 3 questions

Syntax: e0 (e1,...,en)

- (Will generalize later)
- Parentheses optional if there is exactly one argument

Type-checking:

lf:

- e0 has some type (t1 \* ... \* tn) -> t
- e1 has type t1, ..., en has type tn

Then:

- e0(e1,...,en) has type t

Example: **pow(x,y-1)** in previous example has type **int** 

## Function-calls continued

e0(e1,...,en)

Evaluation:

- 1. (Under current dynamic environment,) evaluate e0 to a function fun x0 (x1 : t1, ..., xn : tn) = e
  - Since call type-checked, result will be a function
- 2. (Under current dynamic environment,) evaluate arguments to values v1, ..., vn
- Result is evaluation of *e* in an environment extended to map x1 to v1, ..., xn to vn
  - ("An environment" is actually the environment where the function was defined, and includes x0 for recursion)

#### Example, extended

```
fun pow (x : int, y : int) =
    if y=0
    then 1
    else x * pow(x,y-1)

fun cube (x : int) =
    pow (x,3)
val sixtyfour = cube 4
val fortytwo = pow(2,4) + pow(4,2) + cube(2) + 2
```

## Some gotchas

Three common "gotchas"

- Bad error messages if you mess up function-argument syntax
- The use of **\*** in type syntax is not multiplication
  - Example: int \* int -> int
  - In expressions, \* is multiplication: x \* pow(x,y-1)
- Cannot refer to later function bindings
  - That's what the rules say
  - Helper functions must come before their uses
  - Need special construct for *mutual recursion* (later)

#### Recursion

- If you're not yet comfortable with recursion, you will be soon 
   Will use for most functions taking or returning lists
- "Makes sense" because calls to same function solve "simpler" problems
- Recursion more powerful than loops
  - We won't use a single loop in ML
  - Loops often (not always) obscure simple, elegant solutions

## Tuples and lists

So far: numbers, booleans, conditionals, variables, functions

- Now ways to build up data with multiple parts
- This is essential
- Java examples: classes with fields, arrays

Rest of lecture:

- Tuples: fixed "number of pieces" that may have different types
- Lists: any "number of pieces" that all have the same type

Later: Other more general ways to create compound data

Pairs (2-tuples)

We need a way to *build* pairs and a way to *access* the pieces

Build:

- Syntax: *(e1,e2)*
- Evaluation: Evaluate e1 to v1 and e2 to v2; result is (v1,v2)
   A pair of values is a value
- Type-checking: If e1 has type t1 and e2 has type t2, then the pair expression has type t1 \* t2
  - A new kind of type, the pair type

Pairs (2-tuples)

We need a way to *build* pairs and a way to *access* the pieces

Access:

- Syntax: **#1 e** and **#2 e**
- Evaluation: Evaluate e to a pair of values and return first or second piece
  - Example: If e is a variable x, then look up x in environment
- Type-checking: If e has type ta \* tb, then #1 e has type ta and #2 e has type tb

#### Examples

Functions can take and return pairs

```
fun swap (pr : int*bool) =
  (#2 pr, #1 pr)
fun sum_two_pairs (pr1 : int*int, pr2 : int*int) =
  (#1 pr1) + (#2 pr1) + (#1 pr2) + (#2 pr2)
fun div_mod (x : int, y : int) =
  (x div y, x mod y)
```

## Tuples

Actually, you can have *tuples* with more than two parts

A new feature: a generalization of pairs

- (e1,e2,...,en)
- t1 \* t2 \* ... \* tn
- #1 e, #2 e, #3 e, ...

Homework 1 uses triples of type int\*int a lot

## Nesting

Pairs and tuples can be nested however you want

– Not a new feature: implied by the syntax and semantics

## Lists

- Despite nested tuples, the type of a variable still "commits" to a particular "amount" of data
- In contrast, a **list** can have any number of elements
- But unlike tuples, all elements have the same type

Need ways to *build* lists and *access* the pieces...

## **Building Lists**

• The empty list is a value:

#### []

 In general, a list of values is a value; elements separated by commas:

[v1,v2,...,vn]

 If e1 evaluates to v and e2 evaluates to a list [v1,...,vn], then e1::e2 evaluates to [v,...,vn]

e1::e2 (\* pronounced "cons" \*)

## Accessing Lists

Until we learn pattern-matching, we will use three standard-library functions

- null e evaluates to true if and only if e evaluates to []
- If e evaluates to [v1, v2, ..., vn] then hd e evaluates to v1
   (raise exception if e evaluates to [])

- If e evaluates to [v1,v2,...,vn] then tl e evaluates to [v2,...,vn]
  - (raise exception if e evaluates to [])
  - Notice result is a list

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## Type-checking list operations

Lots of new types: For any type t, the type t list describes lists where all elements have type t

- Examples: int list bool list int list list (int \* int) list (int list \* int) list
- So [] can have type t list for any type
  - SML uses type `a list to indicate this ("quote a" or "alpha")
- For e1::e2 to type-check, we need a t such that e1 has type t and e2 has type t list. Then the result type is t list
- null : `a list -> bool
- hd : 'a list -> 'a
- tl : `a list -> `a list

### Example list functions

```
fun sum list (lst : int list) =
  if null lst
 then 0
  else hd(lst) + sum list(tl(lst))
fun countdown (x : int) =
  if x=0
  then []
  else x :: countdown (x-1)
fun append (lst1 : int list, lst2 : int list) =
  if null lst1
  then 1st2
 else hd (lst1) :: append (tl(lst1), lst2)
```

#### Recursion again

Functions over lists are usually recursive

- Only way to "get to all the elements"
- What should the answer be for the empty list?
- What should the answer be for a non-empty list?
  - Typically in terms of the answer for the tail of the list!

Similarly, functions that produce lists of potentially any size will be recursive

- You create a list is out of smaller lists

## Lists of pairs

Processing lists of pairs requires no new features. Examples:

```
fun sum pair list (lst : (int*int) list) =
  if null lst
 then 0
  else #1(hd lst) + #2(hd lst) + sum pair list(tl lst)
fun firsts (lst : (int*int) list) =
 if null lst
  then []
  else #1(hd lst) :: firsts(tl lst)
fun seconds (lst : (int*int) list) =
 if null lst
  then []
  else #2(hd lst) :: seconds(tl lst)
fun sum pair list2 (lst : (int*int) list) =
 (sum list (firsts lst)) + (sum list (seconds lst))
```