



# CSE341: Programming Languages Lecture 25 Subtyping for Records and Functions

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# Last major course topic: more types

- SML and Java have static type systems to prevent some errors
  - ML: No such thing as a "treated number as function" error
  - Java: No such thing as a "message missing" error
  - Etc.
- · What should the type of an object be?
  - Theory
    - What fields it has (and what types of things they hold)
    - What methods it has (and argument/result types)
      - With Ruby style getters/setters, no need to treat fields separately
  - Common practice:
    - · Use the names of classes and interfaces instead
      - Has plusses and minuses; see next lecture

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# Being more flexible

- ML's type system would be much more painful (reject safe programs you want to write) without parametric polymorphism
  - Also known as generics
  - Example: A separate length function for int list and string list
- Java's type system would be much more painful (reject safe programs you want to write) without subtype polymorphism
  - Also known as subtyping
  - Example: Couldn't pass an instance of a subtype when expecting an instance of a supertype
  - (Yes, Java also has generics as a separate concept)

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So which is better?

- · Generics and subtyping are best for different things
  - And you can combine them in interesting ways
  - But that's for next lecture because...
- · First we need to learn how subtyping works!
  - Classes, interfaces, objects, methods, etc. will get in the way at first (we'll get there)
  - So start with just subtyping for records with mutable fields
  - We will make up our own syntax
    - · ML has records, but no subtyping or field-mutation
    - · Racket and Ruby have no type system
    - Java uses class/interface names and rarely fits on a slide

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# Records (half like ML, half like Java)

Record expression (field names and contents):

{f1=e1, f2=e2, ..., fn=en} Evaluate ei, make a record

Record field access:

e.f Evaluate e to record v with an f field, get contents

Record field update

e1.f = e2

Evaluate e1 to a record v1 and e2 to a value v2; Change v1's f field (which must exist) to v2; Return v2 A Basic Type System

Record types: What fields a record has and type of contents

{f1:t1, f2:t2, ..., fn:tn}

Type-checking expressions:

- If e1 has type t1, ..., en has type tn,
   then {f1=e1, ..., fn=en} has type {f1:t1, ..., fn:tn}
- If e has a record type containing f : t, then e.f has type t
- If e1 has a record type containing f : t and e2 has type t,
   then e1.f = e2 has type t

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#### This is safe

These evaluation rules and typing rules prevent ever trying to access a field of a record that does not exist

Example program that type-checks (in a made-up language):

```
fun distToOrigin (p:{x:real,y:real}) =
  Math.sqrt(p.x*p.x + p.y*p.y)

val pythag : {x:real,y:real} = {x=3.0, y=4.0}
val five : real = distToOrigin(pythag)
```

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# Motivating subtyping

But according to our typing rules, this program does not type-check

- It does nothing wrong and seems worth supporting

```
fun distToOrigin (p:{x:real,y:real}) =
   Math.sqrt(p.x*p.x + p.y*p.y)

val c : {x:real,y:real,color:string} =
   {x=3.0, y=4.0, color="green"}

val five : real = distToOrigin(c)
```

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# A good idea: allow extra fields

Natural idea: If an expression has type

{f1:t1, f2:t2, ..., fn:tn}

Then it can also have a type missing some of the fields

This is what we need to type-check these function calls:

```
fun distToOrigin (p:{x:real,y:real}) = ...
fun makePurple (p:{color:string}) = ...

val c :{x:real,y:real,color:string} =
   {x=3.0, y=4.0, color="green"}

val _ = distToOrigin(c)
val _ = makePurple(c)
```

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# Keeping subtyping separate

A programming language already has a lot of typing rules and we don't want to change them

 Example: The type of an actual function argument must equal the type of the function parameter

We can do this by adding "just two things to our language"

- Subtyping: Write t1 <: t2 for t1 is a subtype of t2</p>
- One new typing rule that uses subtyping:
   If e has type t1 and t1 <: t2,</li>
   then e (also) has type t2

So now we just have to define t1 <: t2

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Subtyping is not a matter of opinion

- Misconception: If we are making a new language, we can have whatever typing and subtyping rules we want
- · Well, not if you want to prevent what you claim to prevent
  - Here: No accessing record fields that don't exist
- · Our typing rules were sound before we added subtyping
  - So we better keep it that way
- Principle of substitutability: If t1 <: t2, then any value of type t1 must be able to be used in every way a t2 can be
  - Here: It needs all the same fields

# Four good rules

For our record types, these rules all meet the substitutability test:

- "Width" subtyping: A supertype can have a subset of fields with the same types
- "Permutation" subtyping: A supertype can have the same set of fields with the same types in a different order
- 3. Transitivity: If t1 <: t2 and t2 <: t3, then t1 <: t3
- 4. Reflexivity: Every type is a subtype of itself
- (4) may seem unnecessary, but it composes well with other rules in a full language and "can't hurt"

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#### But this still is not allowed

[Warning: I'm tricking you into doing a bad thing ©]

Subtyping rules so far let us drop fields but not change their types

Example: A circle has a center field holding another record

#### Don't have this subtyping - could we?

- No way to get this yet: we can drop center, drop r, or permute order, but we can't "reach into a field type" to do subtyping
- So why not add another subtyping rule... "Depth" subtyping:
   If ta <: tb, then {f1:t1, ..., f:ta, ..., fn:tn} <:</li>
   {f1:t1, ..., f:tb, ..., fn:tn}
- Depth subtyping (along with width on the field's type) allows our example to type-check
  - Unfortunately, it also allows some things it should not... 🕾

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# Mutation strikes again

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Moral of the story

- In a language with records/objects with getters and setters, depth subtyping is unsound
  - Subtyping cannot change the type of fields
- If fields are immutable, then depth subtyping is sound!
  - So this is the Nth time in the course we have seen a benefit of outlawing mutation
  - Choose two of three: setters, depth subtyping, soundness
- · Remember: subtyping is not a matter of opinion

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# Picking on Java (and C#)

Arrays should work just like records in terms of depth subtyping

- But in Java, if t1 <: t2, then t1[] <: t2[]</pre>
- So this code type-checks, surprisingly

# Why did they do this?

- More flexible type system allows more programs but prevents fewer errors
  - Seemed especially important before Java/C# had generics
- Good news, despite this "inappropriate" depth subtyping
  - e.color will never fail due to there being no color field
  - Array reads e1[e2] always return a (subtype of) t if e1 is a t[]
- Bad news, to get the good news given "inappropriate" subtyping
  - e1[e2]=e3 can fail even if e1 has type t[] and e3 has type t
  - Array stores check the run-time class of e1's elements and do not allow storing a supertype
  - No type-system help to avoid such bugs / performance cost

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# So what happens

```
void m1(Point[] pt_arr) {
  pt_arr[0] = new Point(3,4); // can throw
}
String m2(int x) {
  ColorPoint[] cpt_arr = new ColorPoint[x];
    ...
  m1(cpt_arr); // "inappropriate" depth subtyping
  ColorPoint c = cpt_arr[0]; // fine, cpt_arr
    // will always hold (subtypes of) ColorPoints
  return c.color; // fine, a ColorPoint has a color
}
```

- Causes code in m1 to throw an ArrayStoreException
  - It is awkward at best to blame this code
  - Benefit is run-time checks occur only on array stores, not on field accesses like c.color

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#### null

- Array stores probably the most surprising choice for flexibility over static checking
- But null is the most common one in practice
  - null is not an object; it has no fields or methods
  - But Java and C# let it have any object type (backwards, huh?!)
  - So, in fact, we do *not* have the static guarantee that evaluating e in e.f or e.m (...) produces an object that has an f or m
  - The "or null" caveat leads to run-time checks and errors, as you have surely noticed
- Sometimes null is very convenient (like ML's option types)
  - But having "can't be null" types in the language would be nice

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#### Now functions

- Already know a caller can use subtyping for arguments passed
  - Or on the result
- · More interesting: When is one function type a subtype of another?
  - Important for higher-order functions: If a function expects an argument of type t1->t2, can you pass a t3->t4 instead?
  - Important for understanding methods
    - An object type is a lot like a record type where "method positions" are immutable and have function types
    - Flesh out this connection next lecture, using our understanding of function subtyping

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# Example

No subtyping here yet:

- flip has exactly the type distMoved expects for f
- Can pass in a record with extra fields for p, but that's old news

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# Return-type subtyping

- Return type of flipGreen is {x:real,y:real,color:string}, but distMoved expects a return type of {x:real,y:real}
- Nothing goes wrong: If ta <: tb, then t -> ta <: t -> tb

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- A function can return "more than it needs to"
- Jargon: "Return types are covariant"

### This is wrong

- Argument type of flipIfGreen is {x:real,y:real,color:string}, but it is called with a {x:real,y:real}
- Unsound! ta <: tb does NOT mean ta -> t <: tb -> t

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### The other way works!

- Argument type of flipX\_Y0 is {x:real} but it is called with a
  {x:real,y:real}, which is fine
- If tb <: ta, then ta -> t <: tb -> t
  - A function can assume less than it needs to of arguments
  - Jargon: "Argument types are contravariant"

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# This time with enthusiasm

- If t3 <: t1 and t2 <: t4, then t1->t2 <: t3->t4
  - Function subtyping contravariant in argument(s) and covariant in results
- · Also essential for understanding subtyping and methods in OOP
- · The most unintuitive concept in this course
  - Smart people often forget and convince themselves that covariant arguments are okay
  - These smart people are always mistaken
  - At times, you or your boss or your friend may do this
  - Remember: A guy with a PhD in PL jumped out and down insisting that function/method subtyping is always contravariant in its argument -- covariant is unsound

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#### Can do both

• flipXMakeGreen has type

{x:real} -> {x:real,y:real,color:string}

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Fine to pass a function of such a type as function of type
 {x:real,y:real} -> {x:real,y:real}

• If t3 <: t1 and t2 <: t4, then t1->t2 <: t3->t4

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