Where are we

- Done features: functions, tuples, lists, local bindings, options
- Done concepts: syntax vs. semantics, environments, mutation-free
- Today features: records, datatypes, case expressions (pattern-matching)
- Today concepts: “One-of” types, constructors/extractors, case-coverage
Base types and compound types

Languages typically provide a small number of “built-in” types and ways to build compound types out of simpler ones:

- Base types examples: int, string, unit
- Type builder examples: tuples, lists, records (see code)

Base types clutter a language definition; better to make them libraries when possible.

- ML does this to a remarkable extent (e.g., we will soon define away bool and conditionals)
Compound-type flavors

Conceptually, just a few ways to build compound types:

1. “Each-of”: A t contains a t1 and a t2
2. “One-of”: A t contains a t1 or a t2
3. “Self-reference”: The definition of t may refer to t

Examples:

- int * bool (syntactic sugar for a record type in ML)
- int option
- int list

Remarkable: A lot of data can be described this way.

(optional jargon: product types, sum types, recursive types)
User-defined types

There are many reasons to define your own types:

1. Using a tuple with 12 fields is incomprehensible

2. Writing down large types is unpleasant; we have computers for that

3. Large programs can use *abstract types* to be robust to change
   • A couple weeks ahead

4. So the language doesn't have to "bake in" lists and options and ...
Datatype

One-of types are less similar across languages

- We’ll discuss OO’s approach to one-of in a few weeks

In ML, we make a new type with a datatype binding, e.g.:

```ml
datatype mytype = TwoInts of int * int
                 | Str of string
                 | Pizza
```

Semantics: Extend the environment with three constructors (in part, functions/constants that produce values of type mytype)

- TwoInts has type int * int -> mytype
- Str has type string -> mytype
- Pizza has type mytype.

So we have a way to build them... what's missing?
The old way

For lists and options, we had a way to:

- Test which *variant* a value was (e.g., null)
- Extract the values from *value-carrying* variants (e.g., hd, tl)
  - Makes no sense if you have the *wrong* variant

What would this look like for mytype?
The new way

Rather than add *variant-tests* and *data-extractors* (non-standard jargon), ML has a *case expression* that uses *pattern-matching*.

In its simplest form, case has one *pattern* for each constructor in a datatype and binds one variable for each value carried. Example:

```
case e of
  TwoInts(i1,i2) => e1
  | Str s => e2
  | Pizza => e3
```

What are the typing rules?
What are the evaluation rules?

*Patterns* are not types nor expressions (despite syntactic similarity)
Type-checking case

In addition to binding local variables and requiring branches to have the same type, the typing rules for case prevent some run-time errors:

- Exhaustiveness: No test can “fail” (a warning)
- Redundancy: No test can be “impossible” (an error)
Expression trees

datatype arith_exp = Constant of int
   | Negate of arith_exp
   | Add of arith_exp * arith_exp

Think of values of type arith_exp as trees where nodes are

- Constant with one int child
- Negate with one child that can be any arith_exp tree.
- Add with two children that can be any arith_exp trees.

In general, a type describes a set of values, which are often trees. One-of types give you different variants for nodes. Constructors evaluate arguments to values (trees) and create bigger values (i.e., taller trees).
Where we’re going

So far, case gives us what we need to use datatypes:

- A (combined) way to test variants and extract values
- Powerful enough to define our own tests and data-extractors

In fact, pattern-matching is far more general and elegant:

- Can use it for datatypes already in the top-level environment (e.g., lists and options)
- Can use it for any type (Wednesday; also tail recursion)
- Can have deep patterns (Friday; also course motivation)