Open book and notes. No laptop computers, PDAs, or similar devices. (Calculators OK, although you won’t need one.) Please answer the problems on the exam paper — if you need extra space use the back of a page.
90 points total

1. (10 points) Suppose we have the following definition of the `map` function in Haskell.

   ```haskell
   map f [] = []
   map f (x:xs) = f x : map f xs
   ```

   Circle each type declaration that is a correct type for `map`. (Not necessarily the most general type, just a correct one.)

   The following are correct types:

   ```haskell
   map :: ([Integer] -> [Integer]) -> [[Integer]] -> [[Integer]]
   map :: (a -> a) -> [a] -> [a]
   map :: (a -> b) -> [a] -> [b]
   ```

   This one is incorrect:

   ```haskell
   map :: (a -> b) -> [b] -> [a]
   ```

   Which of the above types, if any, is the most general type for `map`?

   ```haskell
   map :: (a -> b) -> [a] -> [b]
   ```

2. (6 points) Consider the following Scheme expression:

   ```scheme
   (let* ((x a)
           (y (+ x 10)))
     (+ x y))
   ```

   Write an equivalent Scheme expression that binds `x` and `y` to the same values as above and returns the value of `(x + y)` but that only uses `let` and not `let*`.

   ```scheme
   (let ((x a))
     (let (y (+ x 10))
       (+ x y)))
   ```

---

1 Oh no, I hear you cry! Not *this* question again …
3. (10 points) Write a Ruby class `Delay` that implements delays (as we saw in Scheme). The following code shows how it should work:

```ruby
n = 0
d = Delay.new {n=n+1; 3+4}
d.force
v = d.force
e = Delay.new {1/0}
```

After we evaluate these statements `v` should be 7, but `n` should only be 1 (since we only evaluate the block once). Further, since we never force `e`, we shouldn’t get a divide-by-zero error.

class Delay
  def initialize(&p)
    @p = p
    @value = nil
    @unevaluated = true
  end
  def force
    if @unevaluated
      @value = @p.call
      @unevaluated = false
    end
    return @value
  end
end
```

4. (10 points)

(a) Write a `repeat` rule in CLP(R) with three arguments: `N`, `X`, and `Xs`. It succeeds if `Xs` is a list consisting of `N` copies of `X`. Here are some sample goals and results:

?- repeat(3,a,Xs).
   Xs = [a,a,a]

?- repeat(0,a,Xs).
   Xs = []

?- repeat(-2,a,Xs).
   no.

repeat(0,X,[]).
repeat(N,X,[X|Xs]) :- N>0, repeat(N-1,X,Xs).
(b) What answers are returned for the following goals using the rule you just defined for Question 4a? (Part of answering Question 4b is deciding what a reasonable behavior is in these situations.) Continue on the back of this page as needed. If there are a finite number of answers give them all; if an infinite number give at least the first three.

?- repeat(N,Q,[a,a,a,a]).
Q = a
N = 4

?- repeat(N,Q,[a,b,c]).
no

?- repeat(N,a,As).
As = []
N = 0

As = [a]
N = 1

As = [a, a]
N = 2

As = [a, a, a]
N = 3

As = [a, a, a, a]
N = 4

5. (12 points) Consider the following CLP(R) rule:

\[
\text{sum}([],0).
\text{sum}([X|Xs], X+S) :- \text{sum}(Xs, S).
\]

(a) Draw the simplified derivation tree for the goal \text{sum}([100], N).

(b) Draw the simplified derivation tree for the goal \text{sum}(As, 10). (This is an infinite tree; include at least 3 answers in the tree that you draw.)

(answers on a separate scanned page)
6. (10 points) This question uses the following hierarchy of Java classes for simple geometric shapes. (This is the same hierarchy you used for the last homework assignment.)

```java
public interface GeometricShape {
    public void describe();
}

public interface TwoDShape extends GeometricShape {
    public double area();
}

public interface ThreeDShape extends GeometricShape {
    public double volume();
}

public class Circle implements TwoDShape {
    ....
}

public class Cone implements ThreeDShape {
    ....
}

public class Rectangle implements TwoDShape {
    ....
}

public class Sphere implements ThreeDShape {
    ....
}

Suppose we have three different implementations of a `total_area` method to find the total area of some shapes.

```java
public static double total_area1(ArrayList<TwoDShape> shapes) {
    double sum = 0;
    for(TwoDShape shape : shapes) {
        sum = sum + shape.area();
    }
    return sum;
}

public static double total_area2(ArrayList<? extends GeometricShape> shapes) {
    double sum = 0;
    for(GeometricShape shape : shapes) {
        sum = sum + ((TwoDShape) shape).area();
    }
    return sum;
}
```
returnsum;

publicstaticdouble total_area3(
    ArrayList<? extends TwoDShape> shapes)
{
    double sum = 0;
    for(TwoDShape shape : shapes) {
        sum = sum + shape.area();
    }
    returnsum;
}

Now suppose that we have four variables declared as follows:

ArrayList<Rectangle> rects;
ArrayList<TwoDShape> two_d_shapes;
ArrayList<GeometricShape> geo_shapes;
double area;

We then assign various shapes to the different lists. (So rects will only contain instances of Rectangle, while geo_shapes might contain instances of Circle, Cone, Rectangle, or Sphere.)

Consider the following code that uses these methods and variables. Write “compiles” next to the following statements that compile correctly, and write “doesn’t compile” next to the ones that don’t compile. Finally, if there is a possibility that the statement will cause a cast exception to be raised, write “possible exception” next to it.

area = total_area1(rects); DOESN’T COMPILE
area = total_area1(two_d_shapes); COMPILES
area = total_area1(geo_shapes); DOESN’T COMPILE
area = total_area2(rects); COMPILES
area = total_area2(two_d_shapes); COMPILES
area = total_area2(geo_shapes); COMPILES; POSSIBLE EXCEPTION
area = total_area3(rects); COMPILES
area = total_area3(two_d_shapes); COMPILES
area = total_area3(geo_shapes); DOESN’T COMPILE

7. (6 points) What is something that Ruby mixins can do that Java interfaces can’t?
   Ruby mixins have implementations of the methods they include; Java interfaces just have the method header but no body.

8. (6 points) Consider the following Java code fragments. In each case, does the code compile correctly? If so, does it execute without error, or is there an exception?
(a) Object[] a = new String[10];
a[0] = "hi there";

executes without error

(b) ArrayList<Object> a = new ArrayList<String>();
a.add("hi there");

compile error

(c) Object[] a = new String[10];
a[0] = new Point(10,20);

runtime exception

9. (10 points) What is duck typing? What is an advantage of duck typing over a more standard approach, and what is a potential problem? Finally, could you program in Java in a way that follows the duck typing philosophy? Why or why not?

Duck typing is a philosophy and programming technique used in Ruby. (It could also be used in other dynamically typed object-oriented languages such as Smalltalk, although I’m not requiring this fact as part of your answer.) The term comes from the aphorism “if it walks like a duck and quacks like a duck, it’s a duck.” The idea is that rather than including any runtime checks of what the class is of an object, you just send it the message and let it respond in whatever way it wants. If you aren’t sure whether an object understands a message or not (for example the message squid), rather than testing the receiver’s class, use the respond.to?("squid") message to check if it can handle that message.

An advantage is that duck typing allows more reuse and flexibility. A disadvantage is that programs might have undetected incorrect behavior. For example, suppose that we are assuming we have a bank account object, which includes a “balance” method. If we use a Les Schwab object that also understands “balance” (for balancing a tire) the program might run but have incorrect behavior.

You can’t program in Java in a way that follows the duck typing philosophy, since variables are declared as being of the declared type (and in Java this implies that they are instances of the given class, or a subclass, or a class that implements the interface).

An alternate and acceptable answer is that you can program in Java this way, but only if you essentially simulate a language without static types.

10. (10 points) In Java, a class can be covariant in the return type of an inherited method. It turns out that this feature is new in J2SE 5.0; before that, the return type had to be invariant (i.e., exactly the same as the return type in the method in the superclass or interface).

For a widely used language like Java, the language designers must concern themselves with compatibility issues. What compatibility issues were raised by this change? Are there programs that used to compile without error in pre-5.0 Java that now get a compile error? Are there programs that formerly wouldn’t compile that now do compile? What about runtime behavior? Are there programs that compiled in old and new Java but that can behave differently? If there are such programs with different compile time or run time behavior, give an example, and explain why there is a difference.
There aren’t any compatability issues that will cause problems for old programs. Any program that used to compile in pre-5.0 Java will continue to compile, and will have the same runtime behavior. There are programs that would give a compile error in pre-5.0 Java that now work, but it seems unlikely that would be a problem for anyone. Here is an example of a program that would formerly not compile but that now does. (This is from the lecture notes on this topic.)

```java
interface Octopus {
    Object test();
}

public class BabyOctopus implements Octopus {
    public String test() {
        return "feed me!";
    }
}
```