The first two questions use the following hierarchy of Java classes for simple geometric shapes. (This is the same hierarchy you used for Homework 6.)

```java
public interface GeometricShape {
    public void describe();
}

public interface TwoDShape extends GeometricShape {
    public double area();
}

public interface ThreeDShape extends GeometricShape {
    public double volume();
}

public class Circle implements TwoDShape {
    private double radius;

    public Circle(double radius) {
        this.radius = radius;
    }

    public double area() {
        return Math.PI * radius * radius;
    }

    public double circumference() {
        return Math.PI * 2.0 * radius;
    }

    public void describe() {
        System.out.print("Circle[radius=");
        System.out.print(radius);
        System.out.println("]");
    }
}

public class Cone implements ThreeDShape {
    private double radius;
    private double height;
```
public class Rectangle implements TwoDShape {
    private double width, height;

    public Rectangle (double width, double height) {
        this.width = width;
        this.height = height;
    }

    public double area() {
        return width*height;
    }

    public double perimeter() {
        return 2.0*(width+height);
    }

    public void describe() {
        System.out.print("Rectangle[width=");
        System.out.print(width);
        System.out.print("],height=");
        System.out.print(height);
        System.out.println("]");
    }
}

public class Sphere implements ThreeDShape {
    private double radius;

    public Sphere (double radius) {
        this.radius = radius;
    }

    public double volume() {
        return (1.0/3.0)*Math.PI*radius*radius*height;
    }

    public void describe() {
        System.out.print("Cone[radius=");
        System.out.print(radius);
        System.out.print("],height=");
        System.out.print(height);
        System.out.println("]");
    }
}

public class Cone (double radius, double height) {
    this.radius = radius;
    this.height = height;
}

public class Rectangle implements TwoDShape {
    private double width, height;

    public Rectangle (double width, double height) {
        this.width = width;
        this.height = height;
    }

    public double area() {
        return width*height;
    }

    public double perimeter() {
        return 2.0*(width+height);
    }

    public void describe() {
        System.out.print("Rectangle[width=");
        System.out.print(width);
        System.out.print("],height=");
        System.out.print(height);
        System.out.println("]");
    }
}

public class Sphere implements ThreeDShape {
    private double radius;

    public Sphere (double radius) {
        this.radius = radius;
    }

    public double volume() {
        return (1.0/3.0)*Math.PI*radius*radius*height;
    }

    public void describe() {
        System.out.print("Cone[radius=");
        System.out.print(radius);
        System.out.print("],height=");
        System.out.print(height);
        System.out.println("]");
    }
}
```java
this.radius = radius;
}

public double volume() {
    return (4.0/3.0)*Math.PI*radius*radius*radius;
}

public void describe() {
    System.out.print("Sphere[radius=");
    System.out.print(radius);
    System.out.println("");
}
}
```

1. (8 points) Consider the following Java code fragments. For each fragment, say whether it results in a compile time error, a run time error, or executes without error.

   (a) TwoDShape[] shapes;
       shapes = new Rectangle[5];
       shapes[0] = new Circle(10.0);

       run-time error -- trying to store a circle into an array of rectangles

   (b) TwoDShape[] shapes;
       shapes = new TwoDShape[5];
       shapes[0] = new Circle(10.0);

       executes without error

   (c) ArrayList<TwoDShape> shapes;
       shapes = new ArrayList<Rectangle>();
       shapes.add(new Circle(10.0));

       compile time error -- trying to assign an arraylist of rectangle to an arraylist of 2-d shapes

   (d) ArrayList<TwoDShape> shapes;
       shapes = new ArrayList<TwoDShape>();
       shapes.add(new Circle(10.0));

       executes without error

2. (9 points) Consider three alternate implementations of a `total_volume` method to find the total volume of some shapes.

   ```java
   public static double total_volume1(ArrayList<ThreeDShape> shapes) {
       double sum = 0;
       for(ThreeDShape shape : shapes) {
```
public static double total_volume2(ArrayList<? extends GeometricShape> shapes) {
    double sum = 0;
    for (ThreeDShape shape : shapes) {
        sum = sum + shape.volume();
    }
    return sum;
}

public static double total_volume3(ArrayList<? extends ThreeDShape> shapes) {
    double sum = 0;
    for (ThreeDShape shape : shapes) {
        sum = sum + shape.volume();
    }
    return sum;
}

Which of these will compile correctly, and which will give a compile error?

total_volume1 and total_volume3 compile correctly;
total_volume2 gives an error

Of the ones that compile correctly, do they provide different functionality? In other words, are there calls to the total_volume method that work for some of the correct versions but not for others? If so, give an example of a call that works for some versions but not others, and say which versions it works for. Also give an example of a call that works for all of the versions that compile correctly.

(Please continue your answer on the back of this page if you need more space.)

total_volume3 is more general than total_volume1. total_volume3 will accept as a parameter an arraylist of ThreeDShape or any subclass of ThreeDShape, while total_volume1 will only accept an arraylist of ThreeDShape (but not a subclass).

3. (10 points) Write a CLP(\(\mathcal{R}\)) rule \(\text{last}(S,L)\) that succeeds if \(L\) is the last element of the list \(S\). Naturally, you should also be able to use the rule to find the last element of a list, or find all the lists of which \(L\) is the last element. Fail if \(S\) is empty.

\[
\text{last}([X],X).
\text{last}([X|Xs],L) :- \text{last}(Xs,L).
\]

Here is an alternate version — either is OK.
last([X],X).
last([X,Y|Ys],L) :- last([Y|Ys],L).

4. (10 points) Show the output from CLP(R) for the following goals. If backtracking will produce additional answers, give all the additional answers (or the first three if there are infinitely many).
   (a) last([1,2,3,4],L).
   (b) last(S,squid).

last([1,2,3,4],L) => L=4.
lst(S,squid) => S=[squid]; S=[_h1,squid];
   S=[_h1,_h2,squid]; S=[_h1,_h2,_h3,squid]; ... .

5. (16 points) Consider the following CLP(R) rules to find the sum of a list of numbers:
   sum([],0).
   sum([X|Xs],X+S) :- sum(Xs,S).
   (a) Draw the simplified derivation tree for the goal sum([3,4],A).
   (b) Draw the simplified derivation tree for the goal sum([5,1,10],50).
   (Answer on separate diagram.)

6. (10 points) Write a last function in Miranda that takes a list and returns the last element in the list (analogous to the last rule in Question 3). What is its type? Signal an error if the list is empty.
   (Hint: use the Miranda function error.)

last :: [*] -> *

last [] = error "can’t find the last element of an empty list"
last [x] = x
last (x:y:ys) = last (y:ys)

7. (10 points)
   (a) What is the result of evaluating the following expressions in Scheme? (Just give the value of the final expression.)
   (define b '(squid))
   (define (f a) (cons a b))
   (let ((a 'clam)
          (b 'octopus))
     (f 'mollusc))
   (mollusc squid)
(b) Suppose Scheme used dynamic scoping rather than lexical scoping. In that case, what would be the value of the final expression?

(mollusc octopus)

8. (12 points) There are tradeoffs between having a language that is statically typed and one that is dynamically typed. Give two advantages of static typechecking, and two advantages of dynamic typechecking. Give application contexts in which one or the other might be particularly advantageous.

One advantage of static typing is that it detects type errors earlier, at compile time, rather than at run time (perhaps after an application has been shipped and is in operation). A second advantage is that it provides machine-checked documentation of the types that are expected (unlike a comment, which can get out of date).

One advantage of dynamic typing is that it facilitates rapid program development, in which the code is changing quickly. There are fewer places that need editing when a change is made. A second advantage is that it allows more flexible use of data structures — for example, in Scheme a list can contain elements of different types, while in Miranda they must all be the same.

Static typing is traditionally regarded as advantageous for applications with strong requirements for reliability and that are relatively stable. Dynamic typing is traditionally regarded as advantageous for rapid prototyping and experimentation.

9. (9 points) Consider the following example in an Algol-like language.

```algol
begin
integer n;
procedure p(k: integer);
begin
k := k+5;
print(n);
n := n+(2*k);
end;
n := 0;
p(n);
print(n);
end;
```

(a) What is the output when $k$ is passed by value? 0 10
(b) What is the output when $k$ is passed by value result? 0 5
(c) What is the output when $k$ is passed by reference? 5 15

10. (12 points) Aloysius Q. Hacker, CSE grad student, has decided that a quick route to a Ph.D. is to invent a new programming language that combines features of Miranda and CLP($\mathcal{R}$). His first attempt (“CLPanda”, also known as the Giant Panda Language) is like CLP($\mathcal{R}$), except that the constraint solver is lazy. Goals are processed in the same way as in CLP($\mathcal{R}$), but CLPanda postpones solving any constraints until after the last step of a derivation (i.e. until just after the goal is empty). You are doing a CSE 498 project with Aloysius’s advisor. The advisor has great confidence in you, and despite
your protests that you are but an undergraduate, Aloysius’s advisor asks you to straighten Aloysius out on this new language. Your task: to compare CLP(\(\mathcal{R}\)) and CLPanda. Specifically:

- Are there derivations that are infinite in one language and finite in the other? (In other words, is there a derivation that has exactly the same derivation steps in each language up to a particular goal, but in one language the derivation will no longer continue, but in the other it is infinite?)
- If there are derivations that are infinite in one language and finite in the other, is the finite version always a successful derivation, always a failed derivation, or are there cases of both successful and failed derivations?
- Are there any finite derivations that consist of exactly the same derivation steps in each language but that have different answers?

For each of these cases, if there are such derivations, give an example.

There are derivations that are infinite in CLPanda and finite in CLP(\(\mathcal{R}\)) — see examples below. There are no derivations that are finite in CLPanda and infinite in CLP(\(\mathcal{R}\)).

There are derivations that are infinite in CLPanda and finitely failed in CLP(\(\mathcal{R}\)). Here’s an example:

\[
\text{squid}(X) :- X>5, X<5, \text{squid}(X). 
\]

In CLP(\(\mathcal{R}\)), the goal \text{squid}(A) fails, because the constraints are unsatisfiable. CLPanda gets into an infinite recursion because it doesn’t check for unsatisfiable constraints until there are no more goals.

There are also derivations that are infinite in CLPanda and that are finite and terminate with success in CLP(\(\mathcal{R}\)). For example:

\[
\text{squid}(X) :- X>5, X<5, \text{squid}(X).
\]

\[
\text{squid}(10).
\]

Here the goal \text{squid}(A) succeeds in CLP(\(\mathcal{R}\)) with \(A=10\).

There aren’t any finite derivations that consist of exactly the same derivation steps in each language but that have different answers.

11. (10 points) Scheme has built-in constructs \texttt{delay} and \texttt{force} to manage delayed evaluation. For example:

\[
\begin{align*}
\text{(define d (delay (begin (print "evaluating ...") (+ 3 4))))} \\
\text{(force d)} \\
\text{(force d)}
\end{align*}
\]

Write an analogous class \texttt{Delay} in Smalltalk. You can create and initialize a new instance of \texttt{Delay} in any manner that is convenient.

Show the Smalltalk code for delaying the computation of 3+4 (and printing a note to the Transcript), in analogy with the Scheme code shown.
Object subclass: #Delay
  instanceVariableName: 'block cachedValue evaluated'

block: b
  block := b.
  evaluated := false.

force
  evaluated ifFalse:
    [cachedValue := block value. evaluated := true].
  ^cachedValue

(The block: and force methods are both ordinary instance methods.)

Here’s the code for delaying the computation of 3+4 and printing a note to the Transcript:

```smalltalk
d := Delay new block: [Transcript show: 'evaluating ...'. 3+4].
d force.
d force.
```

where you would put these statements in a workspace and print the result of `d force`, then print the result again.

12. (8 points) Extend the class Delay with additional instance and class methods so that you can create and initialize an instance of Delay with one message, namely

```smalltalk
Delay expr: ...
```

where ...is the expression being delayed (however you are representing it). Note carefully which of your methods are instance methods and which are class methods.

We just add one class method to Delay:

```smalltalk
expr: b
  ^self new block: b
```

Then we can rewrite the example as:

```smalltalk
d := Delay expr: [Transcript show: 'evaluating ...'. 3+4].
d force.
d force.
```

13. (12 points) Consider the following Smalltalk class definitions.
What is printed when each of the following expressions is evaluated?

- A new describe
  
  instance of A - no further information available

- B new describe
• C new describe
  instance of C instance of B instance of A – very C-like indeed

• D new describe
  instance of C instance of B instance of A – more like a D

And now for the world’s only known logic programming joke:
Q: How many CLP(\textit{R}) programmers does it take to change a light bulb?

A: Maybe.