Let bindings

Motivation: Functions without local variables can be poor style and/or really inefficient.

Syntax: `let b1 b2 ... bn in e end` where each `bi` is a binding.

Typing rules: Type-check each `bi` and `e` in context including previous bindings. Type of whole expression is type of `e`.

Evaluation rules: Evaluate each `bi` and `e` in environment including previous bindings. Value of whole expression is result of evaluating `e`.

Elegant design worth repeating:

- Let-expressions can appear anywhere an expression can.
- Let-expressions can have any kind of binding.
  - Local functions can refer to any bindings in scope.

More than style

Exercise: hand-evaluate `bad_max` and `good_max` for lists `[1,2]` `[1,2,3]` and `[3,2,1]`.

Extra Credit Exercise: As a function of `n`, how long will it take to calculate

- `bad_max([1, 2, ..., n])`?
- `bad_max([n, n-1, ..., 1])`?

Summary and general pattern

Major progress: recursive functions, pairs, lists, let-expressions

Each has a syntax, typing rules, evaluation rules.

Functions, pairs, and lists are very different, but we can describe them in the same way:

- How do you create values? (function definition, pair expressions, empty-list and `::`)
- How do you use values? (function application, #1 and #2, `nil`, `1d`, and `t1`)

This (and conditionals) is enough for your homework though:

- `and`, `also` and `or`, `else` help
- You need options (next slide)
- Soon: much better ways to use pairs and lists (pattern-matching)
Options

“Options are like lists that can have at most one element.”

- Create a t option with NONE or SOME φ where φ has type t.
- Use a t option with isSome and valOf

Why not just use (more general) lists? An interesting style trade-off:

- Options better express purpose, enforce invariants on callers, maybe faster.
- But cannot use functions for lists already written.