1. (9 points) Evaluate each of the following. If the evaluation raises an exception, say so.

(a) (fn x => 42) (hd [])
(b) (fn x => 42) (fn () => hd [])
(c) let val x=0;
    val y=x+1
    in
    let val x=5
    in
    x+y
    end
    end

2. Consider a function last that takes a list as its argument and that returns the last element
in the list. If the argument is the empty list, it raises an exception EmptyList.

(a) (12 points) Write a definition of last.

(b) (3 points) What is the type of last?

(c) (3 points) Is your function last tail-recursive? (It doesn’t need to be — you just need
to be able to say whether your definition is or is not tail-recursive.)
3. (27 points) Suppose the following functions and exception have been defined:

```
exception UnequalLengthLists;

fun map2 (f, [], []) = []
| map2 (f, (x::xs), (y::ys)) = f(x,y) :: map2 (f,xs,ys)
| map2 _ = raise UnequalLengthLists;

fun map2curried f [] [] = []
| map2curried f (x::xs) (y::ys) = f x y :: map2curried f xs ys
| map2curried _ _ _ = raise UnequalLengthLists;

fun average x y = (x+y)/2.0;
```

What is the **value** of each of the following expressions? (If evaluating it raises an exception, say so.)

(a) `map2( (op +), [1,2,3], [10,11,12] )`
(b) `map2( (op +), [1,2,3], [10] )`
(c) `map2curried average [] []`

What is the **type** of each of the following expressions? Some of them may give type errors — if so, say that.

(a) `average`

(b) `map2`

(c) `map2curried`

(d) `map2 (average, [], [])`

(e) `map2curried average [] []`

(f) `map2curried average`
4. (12 points) Consider the following code in an Algol-like language.

begin
  integer m;
  procedure clam(k: integer);
  begin
    print(k,m);
    m := m+3;
    print(k,m);
  end;
  m := 5;
  clam(2*m);
end;

Assume that the statement print(k,m) prints two numbers on the same line, separated by a space. (But we’re not worried about the details of spacing for this question!) What is the output when m is passed using:

(a) call by value

(b) call by name

5. (9 points) In ML, a program can be ill-typed (so that it doesn’t compile at all), it can execute and terminate normally, or it can fail at runtime (either by halting with an exception, going into an infinite loop, or running out of memory).

Consider a new language, DynML, that is like ML except that it is dynamically typed rather than statically typed. There are no type declarations in DynML – all type checking is done at run time when the particular expression involved is being evaluated. For example, the expression 3+"clam" would give a runtime error if you try to evaluate it; but until it’s evaluated, there is no indication that something might be wrong.

Are there any programs that have different behavior with ML and DynML? If so, give an example and describe the behavior in both ML and DynML. If not, explain why not.