The purposes of this project are (1) to review Java, (2) to give you a taste of what CSE 332 will be like, (3) to implement various “WorkList” data structures, (3) to learn a new important data structure, and (4) to implement a real-world application.

Overview
A WorkList is a generalization of Stacks, Queues, etc. A WorkList contains items to be processed in some order. The WorkList ADT is defined as follows:

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>add(work)</td>
<td>Notifies the worklist that it must handle work</td>
</tr>
<tr>
<td>peek()</td>
<td>Returns the next item to work on</td>
</tr>
<tr>
<td>next()</td>
<td>Removes and returns the next item to work on</td>
</tr>
<tr>
<td>hasWork()</td>
<td>Returns true if there’s any work left and false otherwise</td>
</tr>
</tbody>
</table>

A Trie is a type of dictionary made for storing “words” (types made up of letters). If you took CSE 143, you’ve actually already seen tries; you just didn’t know it yet. We will describe them in full detail later, but for now, here’s an example:

```
      a
     /|
    b c
   /  |
  d   g
 /    |
| a   e|
|      |
|      |
T T T T T T T T T T
```

This trie represents the dictionary: {adam, add, app, bad, bag, bags, beds, bee, cab}, because if we go from the root of the trie reading in letters until we hit a “true” node, we get a word. Recall that in huffman, we had two possibilities (0 and 1) and we read from the root to a leaf.

In this project, you will implement several different types of WorkLists and a generic and specialized trie. Then, you will run code that uses your data structure to compress inputs into a *.zip file which can interoperate with the standard zip programs!

Project Restrictions
- The design and architecture of your code are a part of your grade.
- Your WorkList implementations may not use any classes in java.util.* (including the Arrays class).
- You may not edit any file in the cse332.* packages.
- For better or worse, this project goes up against the limits of Java’s implementation of generics. You will have to deal with this, but it is not a goal of this project for you to completely understand how these work. If you get stuck with generics, please ask for help immediately!
- Make sure to not duplicate fields that are in super-classes (e.g., size). This will lead to unexpected behavior and failures of tests.
Provided Code

- **cse332.interfaces.misc**
  - Set.java: An interface representing a generic Set data structure.
  - SimpleIterator.java: An interface representing an iterator for a data structure.

- **cse332.interfaces.worklist**
  - WorkList.java: An interface representing a generic WorkList.
  - FIFOWorkList.java: An interface representing a WorkList that stores items in FIFO order.
  - LIFOWorkList.java: An interface representing a WorkList that stores items in LIFO order.
  - FixedSizeFIFOWorkList.java: An interface representing a WorkList with a fixed-size buffer that stores items in a FIFO order.
  - PriorityWorkList.java: An interface representing a WorkList that stores items in order of their priorities (given by compareTo).

- **cse332.interfaces.trie**
  - BString.java: An interface representing a type that is made up of individual characters (examples include arrays, strings, etc.)
  - TrieMap.java: An interface representing an implementation of Dictionary using a trie.
  - TrieSet.java: An interface representing an implementation of a Set using a trie.

- **cse332.jazzlib.**: This is the implementation of the DEFLATE specification and Zip file io.
- **cse332.main.**: These are clients of the code you will be writing. Feel free to use them for testing.

Part 1: Implementing The WorkLists

In this part, you will write several implementations of the WorkList ADT: ArrayStack, ListFIFOQueue, CircularArrayFIFOQueue, and FourHeap. Make sure all of your WorkLists implement the most specific interface possible among the WorkList interfaces. These interfaces will help the user ensure correct behavior when the order of the elements in the WorkList matters. The WorkList interfaces have specific implementation requirements. Make sure to read the javadoc.

1. **ListFIFOQueue**
   Your ListFIFOQueue should be a LinkedList under the hood. You should implement your own Node class as an inner class in your ListFIFOQueue class. All operations should be $O(1)$.

2. **ArrayStack**
   The default capacity of your ArrayStack should be 10. If the array runs out of space, you should double the size of the array. When growing your array, you must do your copying “by hand” with a loop; do not use Arrays.copyOf or other similar methods. It is good to know that these methods exist, but for now we want to focus on understanding everything that is going on “under the covers” as we talk about efficiency. Using the length property of an array is perfectly fine. All operations should be amortized $O(1)$.

3. **CircularArrayFIFOQueue**
   Your CircularArrayFIFOQueue should be an array under the hood. The purpose of this class is to represent a buffer that is being processed. It is essential to the later parts of the project that all of the operations be as efficient as possible. Note that there are some extra methods that a subclass of FixedSizeFIFOWorkList must implement.
(4) MinFourHeap
Your MinFourHeap should be an implementation of the heap data structure we’ve discussed in class. It should be an array-based implementation which starts at index 0. Unlike the implementation discussed in lecture, it should be a four-heap (not a two-heap). In other words, each node should have four children, not two. All operations should have the efficiencies we’ve discussed in class.

Part 2: Implementing The Tries
In this part, you will implement another data structure: HashTrieMap

Tries and TrieMaps
As briefly discussed above, a Trie is a set or dictionary which maps “strings” to some type. You should be familiar with using a HashMap and a TreeMap from CSE 143 (or equivalent). So, we’ll start with a comparison to those.

Comparing TrieMap to HashMap and TreeMap
It helps to compare it with dictionaries you’ve already seen: HashMap and TreeMap. Each of these types of maps takes two generic parameters K (for the “key” type) and V (for the “value” type). It is important to understand that Tries are NOT a general purpose data structure. There is an extra restriction on the “key” type: namely, it must be made up of characters (it’s tempting to think of the Character type here, but really, we mean any alphabet–chars, alphabetic letters, bytes, etc. Example of types that Tries are good for include: String, byte[], List<E>. Examples of types that Tries cannot be used for include int and Dictionary<E>.

In our implementation of Tries, we encode this restriction in the generic type parameters:

• A: An “alphabet type”. For a String, it would be Character. For a byte[], it would be Byte.

• K: A “key type”. We insist that all the “key types” extend BString which encodes exactly the restriction that there is an underlying alphabet.

• V: A “value type”. There are no special restrictions on this type.

For reasons that are not worth going into, Java’s implementation of generics causes us issues here. The constructor for a TrieMap takes as a parameter a Class. For our purposes, all you need to understand is that this is our way of figuring out what the type of the alphabet is. To instantiate this class, just feed in <key type class name>.class.

As an example, to create a new HashTrieMap (one of the classes you will implement) which has a byte[] as the key type and a String as the value type, we would write:

TrieMap<Byte, ByteString, String> map = new HashTrieMap<>(ByteString.class);

We also use different method names than the standard Java library: get becomes find, put becomes insert, and remove becomes delete.

(5) HashTrieMap
A HashTrieMap is an implementation of a trie where the “pointers” are made up of a HashMap. An array would work as well, but you should think about why that might not be a good idea if the alphabet size is large (like 5 or more). Consider the following TrieMap:

```
  o
 / \  
 a   e  
|     |
\-----/-----
   d          d
      / \      / \  
     p  p  l  l
```

for a phone
We could manually construct this as a HashTrieMap as follows:

```java
1   this.root = new HashTrieNode();
2   this.root.pointers.put('a', new HashTrieNode("hello"));
3   this.root.pointers.get('a').pointers.put('d', new HashTrieNode());
4   this.root.pointers.get('a').pointers.get('d').pointers.put('d', new HashTrieNode("1 + 1"));
5   this.root.pointers.get('a').pointers.put('p', new HashTrieNode());
6   this.root.pointers.get('a').pointers.get('p').pointers.put('p', new HashTrieNode("for a phone"));
```

Notice that the pointers variables in each of the nodes are just standard HashMaps!

You will implement all the standard Dictionary operations (insert, and find). For each of these, read the javadoc for Dictionary for the particulars. There are two methods (delete and findPrefix) which are special for TrieMaps and have additional information/restrictions:

- **findPrefix(Key k)** should return true iff k is a prefix of some key in the trie. For example, if “add” were a key in the trie, then:

  ```java
  findPrefix("") = findPrefix("a") = findPrefix("ad") = findPrefix("add") = true.
  ```

  This method is arguably one of the major reasons to use a TrieMap over another implementation of Dictionary. (You saw a similar trade-off between HashMap (faster) and TreeMap (ordered) in your CSE 143 equivalent.) Unlike in a normal Dictionary, it is possible (and in fact, easy) to implement this method.

- (Optional - will not impact your grade.) **delete(Key k)** should delete k from the trie as well as all of the nodes that become unnecessary. One implementation of delete (called lazy deletion) would be to find k in the map and set its value to null (since null is not a valid value in the map). You may not implement delete as lazy deletion. Instead, you must ensure that all leaves of your trie have values. The reason we insist you write this version of deletion is that the ultimate client (zip) would be far too slow with lazy deletion.

Your implementations of insert, find, findPrefix, and delete must have time complexity \(\Theta(d)\) where \(d\) is the number of letters in the key argument of these methods. These methods work on the entire key (the whole “string” of “letters”); make sure to only remove/add/find the exact key asked for.

**Above and Beyond**

The following list of suggestions are meant for you to try only if you finish the requirements early. Recall that any extra credit you complete is noted and kept separate in the gradebook and may be used to adjust your grade at the end of the quarter, as detailed in the course grading policy.

(6) **SuffixTrie**

Now that you’ve done everything else, you should have a solid understanding of the various WorkLists and the idea behind a Trie. This last data structure, which is a type of HashTrieSet (but will be implemented directly as a HashMap with Boolean values), will use all of this knowledge. This data structure will back the LZ77Compressor which is the first phase of the compression used in zip files. It might help to skim the Wikipedia article on LZ77 (https://en.wikipedia.org/wiki/LZ77_and_LZ78) to understand the reasoning behind how this data structure works.

**Tries are Prefix Trees**

Another name for a trie is a “prefix tree”, because they are dictionaries where looking up prefixes is easy. There are plenty of applications of standard tries: word games, predictive text, spell checking, auto-complete, etc. You will see some of these in P2, but in P1 we will focus on a specialization of the trie data structure called a SuffixTrie.
What is a SuffixTrie?

Imagine that we have a String of text which we would like to search through. The SuffixTrie for a particular String of text contains all of the suffixes of that text as entries. Consider the following example:

```
<table>
<thead>
<tr>
<th>a</th>
<th>a</th>
<th>b</th>
<th>c</th>
<th>a</th>
<th>b</th>
<th>c</th>
<th>c</th>
<th>a</th>
<th>a</th>
</tr>
</thead>
</table>
```

A SuffixTrie for text would contain the following:

```
{“aabcabccaa”, “abcabccaa”, “bcabccaa”, “cabccaa”, “abccaa”, “bcca”, “c”, “aa”, “a”, “”}
```

One (annoying) snag with a SuffixTrie is that we would like every suffix to end at a leaf. The solution to this snag is to add a “terminator” character to every suffix that actually ends the word. (Think about what the trie would look like without the null terminator.) We use null for this as follows:

Thus, to look for a word \([a_1, a_2, \ldots, a_n]\) in a SuffixTrie, we look for \([a_1, a_2, \ldots, a_n, \text{null}]\).

This data structure is useful for several reasons. First of all, it’s relatively compact (see above and beyond for an even more compact version), because it avoids storing characters multiple times. Second of all, we can stop the search for a piece of text as soon as the prefix doesn’t match!

Another reason that this data structure is interesting is that its easy to update. Imagine that our example word aabcabccaa “shifted forward”. In other words, we removed the first character (“a”) and added on a new character (“x”). To update the SuffixTrie, all we have to do is the following:

- Remove the key representing the entire word. (This is just a remove on the underlying TrieMap.)
- For each leaf in the tree, remove the null terminator and replace it with a new node:
It might not be clear why we remove old suffixes rather than continuing to add them, and, in fact, in a different implementation, we might not remove them at all! In this implementation, we are more concerned about space than keeping track of absolutely everything, and, so, we make this design trade-off.

Implementing SuffixTrie

In our implementation of a SuffixTrie, we will represent the suffixes of a fixed-size buffer. At all times, a SuffixTrie must keep track of the following information:

- The current match (both the letters and the node where the match ended)
- The contents that the trie represents the suffixes of (a buffer of Bytes)
- The current leaves of the trie (to update when the contents advance forwards)

Your SuffixTrie must maintain this information by implementing the following interface:

```java
public int startNewMatch(FIFOWorkList<Byte> buffer)
```

This method starts a new match from the root by consuming Bytes from the provided buffer as long as the Bytes consumed represent a prefix of a key in this trie. The current node pointer (i.e., lastMatchedNode) in the trie should also be updated. This method should return the length of the match if the match is a complete key in the trie. Otherwise, return zero. (That is, if it is a proper prefix of a key in the trie or the empty string, it should return 0.) This method should make sure to leave room in the match buffer for one more Byte.

For example, in the trie above, the following would be the original buffer, the match consumed, and the remaining buffer:

<table>
<thead>
<tr>
<th>Original Buffer</th>
<th>Match WorkList</th>
<th>Remaining Buffer</th>
<th>Return Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>← a b c →</td>
<td>← a b c →</td>
<td>← → → → → → → → →</td>
<td>0</td>
</tr>
<tr>
<td>← a a a →</td>
<td>← a a →</td>
<td>← a → → → → → → →</td>
<td>2</td>
</tr>
<tr>
<td>← c c a b b →</td>
<td>← c c a →</td>
<td>← b b → → → → → →</td>
<td>0</td>
</tr>
</tbody>
</table>

```java
public void addToMatch(Byte b)
```

Appends b to the current match. The current node pointer in the trie should not be updated.

```java
public FIFOWorkList<Byte> getMatch()
```

Returns a deep copy of the stored match. That is, the client should not be able to update the field using the return value.

```java
public int getDistanceToLeaf()
```

Returns the distance from the end of the current match to a leaf. If the match was complete, this method should return 0. Otherwise, it should return the number of (non-terminator) characters to some leaf. It is more important that this method be efficient than that it return a particular leaf. To do this, you should get any element of the pointers map. Your code to do this will look something like:

```java
node.pointers.values().iterator().next()
```
<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>public void advance()</strong></td>
<td>This method advances the contents of the trie using the found match. For each Byte <code>b</code> in match, it should remove the whole word from the trie and append <code>b</code> to the end of every stored word. This is the algorithm described above to advance suffixes applied to an entire buffer. Note that if the stored contents are not yet full, we do not shift anything off. Note that the ordering between removal and appending (that is, removal is first) does matter.</td>
</tr>
<tr>
<td><strong>public void clear()</strong></td>
<td>This method should reset the state of the trie to the same as right after it was originally constructed.</td>
</tr>
</tbody>
</table>
An advanced Example
Suppose that we begin with the following settings:

(max) size: 3

currentMatch: ← a b a b a ←

A single step of \( \text{advance()} \) (1):
For each leaf, we replace the NUL with the new character (here, 'a') followed by a NUL. Then, we add the empty string back into the trie.

currentMatch: ← a b a ←

A single step of \( \text{advance()} \) (2):

currentMatch: ← b a ←

A single step of \( \text{advance()} \) (3):
This time we hit capacity. So, we remove “aab[null]” from the trie before extending the existing words.

currentMatch: ← ←

A single step of \( \text{advance()} \) (4):

currentMatch: ← a ←