

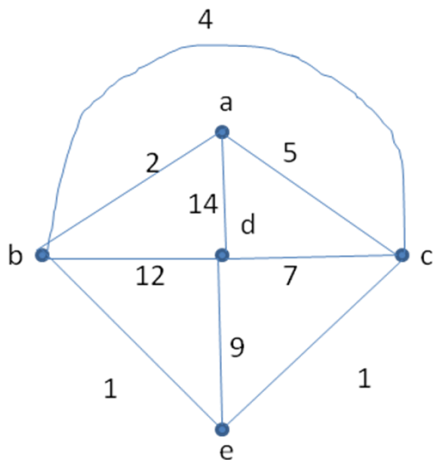
## 1. Run-times

|                  | Run-time                                |
|------------------|---|
| Kruskal's MST    | $ E  \log V $                           |
| Dijkstra's       | $ E  \log V  +  V  \log  V $ or $ V ^2$ |
| Topological sort | $ V  +  E $                             |

## 2. Graphs

a. Draw the following graph:  $V=\{a,b,c,d,e\}$

$E=\{(a,b):2, (a,c): 5, (a,d): 14, (b,c): 4, (b,d): 12, (b,e): 1, (c,d): 7, (c,e): 1, (d,e): 9\}$   
 where  $(x,y):z$  represents an undirected edge between  $x$  &  $y$  with weight  $z$ .

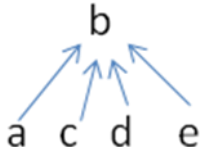


b. Find a minimal spanning tree using Kruskal's algorithm.

Only the final table & up-tree are shown here:

Table of edges by weights:

- 1: (b,e) - accepted
- 1: (c,e) -accepted
- 2: (a,b) - accepted
- 4: (b,c) - rejected
- 5: (a,c) - rejected
- 7: (c,d) - accepted
- 9: (d,e)
- 12: (b,d)
- 14: (a,d)



c. Find the shortest path from a to each vertex using Dijkstra's algorithm.

|   | Known | Cost | Path |
|---|-------|------|------|
| a | Y     | 0    | -    |
| b | Y     | 2    | a    |
| c | Y     | 5    | a    |
| d | Y     | 12   | e    |
| e | Y     | 3    | b    |

d. Dijkstra's algorithm does not necessarily work when the graph possesses negative weights. Will Kruskal's algorithm work with negative weights?

Yes – negative weights won't cause any errors in Kruskal's algorithm.