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# CSE 331

## Software Design & Implementation

Spring 2023  
Section 10 – Final Review

# Administrivia

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- Final Exam on Tuesday (6/6) in KNE 110
  - **Lecture B**: 2:30-4:20 pm
  - **Lecture A**: 4:30-6:20 pm
  - Primarily focused on loop reasoning and ADTs
- HW9 due tomorrow at 11:00 pm (6/2)

# Subtypes – Review

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- Recall that subtypes are **substitutable** for supertype
  - If B is a subtype of A, can send B where A is expected

```
function f(s: A): void { ... }  
function g(): B { ... }
```

```
const x: B = 3;  
f(x); // okay
```

```
const y: A = g(); // okay
```

A  
↑  
B

- For ADTs, we use this as our definition of subtypes
- For B to be substitutable for A, must satisfy 2 conditions:
  - 1) B must provide all methods of A
  - 2) B's corresponding methods must...
    - Accept all inputs that A's does
    - Must also promise everything in A's postcondition
    - i.e., B must have the same or **stronger spec**

# Equality – Review

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- Often useful / necessary to define your own equals
- **Properties of equals method:**
  - 1)  $\text{equal}(a,a) = \text{T}$  reflexive
  - 2)  $\text{equal}(a,b) = \text{equal}(b,a)$  symmetric
  - 3) if  $\text{equal}(a,b)$  and  $\text{equal}(b,c)$ ,  
then  $\text{equal}(a,c)$  transitive

# Design Patterns – Review

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- **3 categories of patterns:**
  - **Creational:**
    - **Builder:** Object that helps with creation of another object
      - lets you describe what you want bit by bit
      - Good for immutable types
  - **Structural:**
    - **Adaptor:** often needed with nominal typing
      - Design pattern for working around language issue
  - **Behavioral:**
    - **Interpreter:** Collects code for similar objects, spreads apart code for operations
      - Easy to add objects, hard to add methods
    - **Procedural:** Collects code for similar operations, spreads apart code for objects
      - Easy to add methods, hard to add objects

# Loop Reasoning – Review

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Fill in the missing parts of the implementation of `insert`. Your code must be correct with the **provided invariant**. (You do not need to include a proof, but it must be correct).

```
/**
 * Returns the value in A that is the smallest out of all values in A that are larger than x
 * @param x A number to compare to the values in A.
 * @param A A list of numbers
 * @param requires A != null
 * @returns the smallest of all values in A larger than x
 */
public int nextLargest(A: number[], x: number): number {
    hasLarger: boolean = ____;
    minLarger: number = _____;
    i: number = __;

    {{ Inv: minLarger = the min value in A[0..i-1] that is larger than x. If no such value exists, hasLarger = false}}
    while (i < A.length) {

    }
    if (!hasLarger) {
        throw new Error("nothing smaller");
    }
    return minLarger;
}
```

# Loop Reasoning – Midterm

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Remember this definition from the previous midterm:

```
/**
 * Returns a set that includes all the current elements and x also
 * @param x a string to insert into the set (if not already present)
 * @returns obj if contains(obj, x) = T
 *          L   if contains(obj, x) = F
 *   where L = A ++ [x] ++ B with obj = A ++ B (i.e., L is an array
 *   containing the strings from obj with x inserted somewhere)
 */
insert(x: string): StringSet;
```

We will implement it with the following class, whose concrete representation is an array sorted in decreasing order.

```
class ArrayStringSet implements StringSet {

    // RI: elems[j] > elems[j+1] for any 0 <= j < elems.length - 1
    // AF: obj = this.elems
    readonly elems: readonly string[];

    // @requires elems is sorted in decreasing order, with no duplicates
    constructor(elems: readonly string[]) {
        this.elems = elems;
    }

    ...
}
```

Fill in the missing parts of the implementation of `insert`. Your code must be correct with the **provided invariant**. (You do not need to include a proof, but it must be correct).

# Loop Reasoning – Midterm

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```
insert = (x: string): StringSet => {
  const k = findIndex(this.elems, x);
  if (_____ ) {
    return this;
  }
  // Create an array one longer than this.elems.
  const E: string[] = new Array(this.elems.length + 1);
  // Define A := this.elems[0..k-1]
  let i: number = __;
  // Inv: E[0..i-1] = A[0..i-1]
  while (_____) {

  }
  // Now we have E[0..i-1] = A and i = k

  // Now we have E[0..i-1] = A ++ [x] and i = k + 1
  // Define B := this.elems[k..this.elems.length-1]. Thus we have this.elems = A ++ B
  let j: number = __;
  // Inv: E[0 .. i - 1] = A ++ [x] ++ B[0 .. j - 1] and i = k + 1 + j
  while (_____) {

  }
  return new ArrayStringSet(E);
}
```



# Loop Reasoning – Midterm

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Remember this definition from the previous midterm:

The following function `findIndex` searches for a string in an array of strings that is promised to be sorted in **decreasing** order. In other words, we are promised that  $A[0] \geq A[1] \geq \dots \geq A[n-1]$ , where the ordering of strings is according to  $\geq$  in TypeScript, (reverse) alphabetical ordering.

```
/**
 * Finds the index where x appears in the given sorted array or where, if
 * it is not in the array, it could be inserted to maintain sorted order.
 * @param A Array of strings in *decreasing* order
 * @param x String to look for in a.
 * @returns an integer k such that  $A[j] > x$  for any  $0 \leq j < k$  and
 *  $x \geq A[j]$  for any  $k \leq j < A.length$ 
 */
function findIndex(A: string[], x: string): number
```

- (a) Use reasoning to fill in all blank assertions. The ‘Pi’s should be filled in with forward reasoning and the ‘Qi’s with backwards reasoning
- (b) Prove  $P_i$  implies  $Q_i$  for  $i = 1, 2, 3$

# Loop Reasoning – Midterm

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The precondition is that  $A[j] \geq A[j + 1]$  for any  $0 \leq j < n-1$ , where  $n$  is  $A.length$

```
let k: number = A.length;
```

```
{{ P1: _____ }}
```

```
{{ Inv:  $x \geq A[j]$  for and  $k \leq j < n$  and  $k \geq 0$  }}
```

```
while (k !== 0 && x >= A[k-1]) {
```

```
    {{ P2: _____ }}
```

```
    {{ Q2: _____ }}
```

```
    k = k - 1;
```

```
    {{ _____ }}
```

```
}
```

```
{{ P3: _____ }}
```

```
{{ Q3:  $A[j] > x$  for any  $0 \leq j < k$  and  $x \geq A[j]$  for any  $k \leq j < n$  }}
```

```
return k;
```

# ADTs – Review

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Suppose we have an implementation of a queue using a list, prove the AF holds after the execution of the function

```
class ArrayQueue {
  // RI:  $0 \leq \text{front} < \text{list.length}$ 
  // AF:  $\text{obj} = \text{list}[\text{front} \dots \text{list.length}-1]$ 
  list: number[];
  front: number = 0;
  // adds element to end of queue
  // @effects  $\text{obj} = \text{obj}_0 ++ [x]$ 
  enqueue = (x: number): void => {
    this.list.push(x);
  }
  // removes element from front of queue
  // @effects  $\text{obj}_0 = [x] ++ \text{obj}$  if queue is not empty, obj otherwise
  // @returns x if queue is not empty, -1 otherwise
  dequeue = (): number => {
    let x: number;
    if (this.front < this.list.length) {
      x = this.list[this.front];
      this.front = this.front + 1;
      return x;
    }
    return -1;
  }
}
```

# Design Pattern – Review

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**Choose the name of the design pattern that best matches the description below.**

- (a) We have a program that uses Complex number objects, but we have two possible implementations of Complex - one uses rectangular coordinates, the other uses Polar. We want the program to be able to select during execution which version to use when a new Complex object is created, and not have that decision fixed when the program is compiled.
- (b) We have a complicated object with many configurations options. We would like to organize constructors with 12 parameters to set all of the configurations options all at once.
- (c) We have a library function that performs calculations using metric units and we want to use it to implement a function that does the same thing, only with U.S. units.

# Subtyping – Review

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Suppose the class `Point3D` is a subtype of `Point`. Which of the functions of `Point3D` below properly override the function of `Point` so that `Point3D` is still substitutable for `Point` (circle all that apply)?

```
interface Point {
    setX(x: number): void;
    setY(y: number): void;
    // @requires this.x != x and this.y != y
    distance(x: number, y: number): number;
}
```

(a)

```
interface Point3D extends Point {
    setX(x: number | string): void;
    setY(y: number | string): void;
    setZ(z: number | string): void;
    // @requires this.x != x and this.y != y
    distance(x: number, y: number): number;
}
```

(b)

```
interface Point3D extends Point {
    setX(x: number): void;
    setY(y: number): void;
    setZ(z: number): void;
    // @requires this.x != x and this.y != y
    distance(x: number, y: number): number | string;
}
```

(c)

```
interface Point3D extends Point {
    setX(x: number): void;
    setY(y: number): void;
    setZ(z: number): void;
    @returns distance that is < 10
    distance(x: number, y: number): number;
}
```