CSE331 Fall 2014, Midterm Examination
October 31, 2014

Please do not turn the page until 2:30.

Rules:

- The exam is closed-book, closed-note, etc.
- Please stop promptly at 3:20.
- There are 110 points (not 100 points), distributed unevenly among 8 questions (many with multiple parts):

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Advice:

- Read questions carefully. Understand a question before you start writing.
- Write down thoughts and intermediate steps so you can get partial credit. But clearly indicate what is your final answer.
- The questions are not necessarily in order of difficulty. Skip around. Make sure you get to all the questions.
- If you have questions, ask.
- Relax. You are here to learn.
1. (16 points) Here is a correct Java method:

```java
@requires: arr != null and arr.length > 0
@returns: number of elements in arr that are strictly greater than all elements earlier in the arr
int f(int[] arr) {
    int max = arr[0];
    int count = 1;
    int i = 1;
    while(i != arr.length) {
        if(arr[i] > max) {
            max = arr[i];
            count = count + 1;
        }
        i = i + 1;
    }
    return count;
}
```

To prove this method correct would require a loop invariant for the loop in the code. For each suggested loop invariant below, indicate which of the following is true (no explanation required):

A. The invariant is correct and is strong enough to prove the method correct.
B. The invariant is correct but is not strong enough to prove the method correct.
C. The invariant is false because it may not hold initially.
D. The invariant is false because it holds initially but may not hold after the loop body.

(a) count holds the number of elements in arr[0]..arr[i] inclusive that are greater than all earlier elements in the array
(b) count holds the number of elements in arr[0]..arr[i-1] inclusive that are greater than all earlier elements in the array
(c) count holds the number of elements in arr[0]..arr[i] inclusive that are greater than all earlier elements in the array
   and max holds the largest value in arr[0]..arr[i] inclusive
(d) count holds the number of elements in arr[0]..arr[i-1] inclusive that are greater than all earlier elements in the array
   and max holds the largest value in arr[0]..arr[i-1] inclusive
(e) count holds the number of elements in arr[0]..arr[i-1] inclusive that are greater than all earlier elements in the array
   and max holds the largest value in arr[0]..arr[i-1] inclusive
   and count >= 1
(f) count < max
(g) count = 1 and max >= arr[0]
(h) true

Solution:
(a) C
(b) B (Note (D) is probably a common answer because this is too weak to prove that it is a loop invariant, but it is a (true) invariant)
(c) C
(d) A
(e) A
(f) C
(g) D
(h) B
2. (16 points) Fill in the blanks below so that the program is correct and the assertions you write down are true and sufficient to prove the program is correct. Put assertions in the blanks with "{" and "}" and code in the other blanks. For code, use Java syntax. For assertions, use syntax similar to the provided assertions. Assume `arr` is an array of ints and `x`, `y`, and `i` are ints. Notice the initial pre-condition, final post-condition, and a little of the code are provided to you. You need to understand the post-condition to determine what the program should do.

```java
{arr != null and arr.length > 1}
arr[0] = x;
arr[1] = y;
{ }
```

```
{ }
```

```
{inv: }
```

```
while (i != arr.length) {
    
    { }

    { }

    { }

    { }

    { arr[0] = x and arr[1] = y and 
      for all j from 2..(arr.length-1) inclusive, arr[j] = arr[j-2] + arr[j-1] }
```
Other solutions possible, but this is probably the simplest. Stronger assertions are fine and possible in some places.

\{ arr != null \land arr.length > 1 \} \\
arr[0] = x; \\
arr[1] = y; \\
{ arr[0] = x \land arr[1] = y } \\
i = 2; \\
{ arr[0] = x \land arr[1] = y \land i = 2 } \\
{inv: arr[0] = x \land arr[1] = y \land \}
   for all j from 2..(i-1) inclusive, arr[j] = arr[j-2] + arr[j-1] 

while (i != arr.length) { 
   // don't require an assertion here but fine if one is added 
   arr[i] = arr[i-1] + arr[i-2]; 
   {arr[0] = x \land arr[1] = y \land 
      for all j from 2..i inclusive, arr[j] = arr[j-2] + arr[j-1]} 
   i = i + 1; 
   {arr[0] = x \land arr[1] = y \land 
      for all j from 2..(i-1) inclusive, arr[j] = arr[j-2] + arr[j-1]} 
} 
{ arr[0] = x \land arr[1] = y \land 
   for all j from 2..(arr.length-1) inclusive, arr[j] = arr[j-2] + arr[j-1] }
Background: Problems 3–5 involve an ADT for the state of a checkerboard during a game of checkers. You do not need to know how to play checkers, and even if you do, do not use any information beyond what is listed here:

- There are two sides, “red” and “black.”
- Each side has a total number of pieces between 0 and 12 inclusive. If one side has 0 pieces, the game is over. Both sides cannot have 0 pieces.
- In addition to color, each piece is either “regular” or a “king.”
- There are 32 positions on a checkerboard. We assume these positions are numbered 0,1,...,31 and this numbering is part of the (public) specification, but what each position number means will not matter on this exam.
- Each position holds 0 or 1 piece.

3. (18 points) In this problem, we consider an implementation of a checkerboard where the concrete representation is an array of length 32 and the abstract values are the state of a checkers game as described above.

```java
class CheckerBoardProblem3 {
    private int[] board = new int[32];

    ... many methods not shown ...
}
```

In the concrete implementation, the value in `board[i]` indicates what piece, if any, is at board-position `i` as follows:

- 0 means no piece
- 1 means a regular red piece
- 2 means a king red piece
- -1 means a regular black piece
- -2 means a king black piece

(a) Write a `checkRep` method for class `CheckerBoardProblem3`.
(b) Write an `equals` method for class `CheckerBoardProblem3`.
(c) Explain in approximately 1-2 English sentences what is wrong with this method for `CheckerBoardProblem3` and how to fix it:

```java
@returns the board positions of all red kings
public List<Integer> redKingPositions() {
    List<Integer> ans = new ArrayList<Integer>();
    for(int i=0; i<board.length; i++) {
        if(board[i] == 2) {
            ans.add(board[i]);
        }
    }
    return ans;
}
```

The next page has room for your answers.
Solution:

(a) private void checkRep() {
    int numBlack = 0;
    int numRed = 0;
    assert(board.length == 32);
    for(int i=0; i < board.length; i++) {
        assert(board[i] >= -2 && board[i] <= 2);
        if(board[i] < 0) numBlack++;
        if(board[i] > 0) numRed++;
    }
    assert(numBlack > 0 || numRed > 0);
    assert(numBlack <= 12 && numRed <= 12);
}

(b) @Override
    public boolean equals(Object o) {
        if(! o instanceof CheckerBoardProblem3)
            return false;
        CheckerBoardProblem3 c = (CheckerBoardProblem3)o;
        for(int i=0; i < board.length; i++)
            if(board[i] != c.board[i])
                return false;
        return true;
    }

(c) The line ans.add(board[i]) should be ans.add(i) — we want to add the board position. The code as written adds a 2 for every red king.
4. (10 points) In this problem, we consider a different implementation of the same abstraction of a checkerboard. In this approach, the concrete implementation has a list of the positions for each kind of piece:

```java
class CheckerBoardProblem4 {
    private List<Integer> regularBlackPositions;
    private List<Integer> kingBlackPositions;
    private List<Integer> regularRedPositions;
    private List<Integer> kingRedPositions;

    ... many methods not shown ...
}
```

(a) In English, describe two things a `checkRep` for `CheckerBoardProblem4` should check that your implementation of `checkRep` in Problem 3 did not have to check.

(b) Explain in approximately 1-2 English sentences what is wrong with this method for `CheckerBoardProblem4` and how to fix it:

```java
@returns the board positions of all red kings
public List<Integer> redKingPositions() {
    return kingRedPositions;
}
```

Solution:

(a) Here are 4: (1) No duplicates in any of the 4 concrete fields comprising the representation. (2) No duplicates across the 4 concrete fields (i.e., two different kinds of pieces in the same position), (3) no nulls in the lists, (4) no values in the list other than the `Integer` values for -2,-1,0,1,2.

(b) It suffers from representation exposure. We should return a copy of the list, for example `return new ArrayList<Integer>(kingRedPositions);`
5. (12 points) This problem uses both CheckerBoardProblem3 and CheckerBoardProblem4.

(a) Suppose CheckerBoardProblem3 and CheckerBoardProblem4 both implement the same checkerboard abstraction correctly. Would an instance of CheckerBoardProblem3 and an instance of CheckerBoardProblem4 with the same abstract state be reference-equivalent? Answer “always”, “sometimes,” or “never.” No explanation required.

(b) Same question as (a) but replace reference-equivalent with behavior-equivalent.

(c) Can two instances of CheckerBoardProblem3 with different concrete values represent the same abstract value? Answer “yes” or “no” and explain your answer in 1-2 sentences.

(d) Can two instances of CheckerBoardProblem4 with different concrete values represent the same abstract value? Answer “yes” or “no” and explain your answer in 1-2 sentences.

Solution:

(a) Never

(b) Always

(c) No, for any checkerboard, there is only one concrete array value in this implementation that represents it.

(d) Yes, the order of elements in any of the 4 lists does not matter, so there are different concrete representations of the same abstract value.
6. (14 points) Consider these five possible specifications for a method that takes one parameter, an int x:

A. @returns some number between $x - 10$ and $x + 10$
B. @returns some number between $x - 5$ and $x + 5$
C. @requires $x > 0$
   @returns some number between $x - 5$ and $x + 5$
D. @requires $x > 0$ or $x < -5$
   @returns some number between $x - 5$ and $x + 5$
E. @requires $x > 0$
   @throws IllegalArgumentException if $x > 100$
   @returns some number between $x - 10$ and $x + 10$

(a) List all specifications above that are stronger than A.
(b) List all specifications above that are stronger than B.
(c) List all specifications above that are stronger than C.
(d) List all specifications above that are stronger than D.
(e) List all specifications above that are stronger than E.
(f) Yes or no: Is it possible for a single method to satisfy A, B, C, and D?
(g) Yes or no: Is it possible for a single method to satisfy C, D and E?

**Solution:**

(a) B
(b) none
(c) B, D
(d) B
(e) none
(f) Yes
(g) No
7. (10 points) Two questions on testing

(a) Can you use a black-box testing methodology to try to find representation-exposure bugs in an ADT implementation? If so, explain how. If not, explain why not. Aim for 2–3 English sentences.

**Solution:**
Yes: Two approaches, one to catch bugs from not copying-in and one to catch bugs from not copying-out: For the former, pass in objects to methods, then call mutators on the passed in objects, then call other methods on the ADT. For the latter, get objects from observer methods on the ADT, then call mutators on those objects, then call other methods on the ADT.

(b) Consider this method:

```c
int min3(int x, int y, int z) {
    int a;
    if(x < y) {
        a = x;
    } else {
        a = y;
    }
    if(z < a) {
        return z;
    } else {
        return x;
    }
}
```

i. Give a test suite for this method with full branch coverage and where all tests pass.
ii. Give a test that does not pass.

**Solution:**

i. The key is to avoid the path where we take both false branches. For example, a test-suite could be: min3(2,3,4) (expected 2) and min3(3,2,1) (expected 1), though many other answers are possible.
ii. min3(3,2,4) (expected 2, observed 3)
8. (14 points) Short answer (only (e) requires more than a word or letter)

(a) Can defining this method in a Java class violate any contracts specified by `Object`?

```java
int hashCode() {
    return 42;
}
```

(b) In Java, can a method overriding a method defined in a superclass throw a checked exception that is not part of the method signature in the superclass?

(c) In Java, can a method overriding a method defined in a superclass throw an unchecked exception that is not part of the method signature in the superclass?

(d) When is it decided whether Java assertions are executed or ignored:
   A. When code containing assertions is compiled
   B. When the Java program is started
   C. When an assertion is encountered by checking whether there is a `DEBUG` flag that is true
   D. It is not an option: Java assertions are always executed

(e) Rewrite this code to be shorter but do the same thing:

```java
try {
    f();
} catch(Exception e) {
    g();
    throw e;
} catch(Error e) {
    g();
    throw e;
}
g();
return 0;
```

(f) Why should you avoid using strings to store data that is not naturally a string?
   A. So the type system can catch more bugs
   B. Performance
   C. Both (A) and (B)
   D. Neither (A) nor (B)

(g) True or false: Assuming unlimited time and developer resources, a stronger specification is always better than a weaker one.

Solution:

(a) No
(b) No
(c) Yes
(d) B
(e) try {
    f();
} finally {
    g();
}
    return 0;
(f) C
(g) False