

Polynomial Division

 $(5x^6 + 4x^4 - x^3 + 5) / (x^3 - 2x - 5)$

 $x^3 - 2x - 5$ $5x^6 + 4x^4 - x^3 + 5$

		Pol	yn	on	nia	l D)iv	isi	on	
			5				5	0	14	24
	1	0 -2	-5	5	0	4	-1	0	0	5
				- 5	0	-10	-25			
					0	14	24	0		
					- 0	0	0	0		
+	- 3					14	24	0	0	
	$5x^{3} + 14x + 24$				- 14	0	-28	-70		
	28x ² + 118x + 125					24	28	70	5	
	$x^3 - 2x - 5$				-	24	0	-48	-120	
							0	28	118	125

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Definitions

- Abstract Value: what an instance of a class is supposed to represent

 Line represents a given line
- Abstract State: the information that defines the abstract value
 - Each line has a start point and an end point
- Abstract Invariant: the conditions that must remain true over the abstract state for all instances
 Start point and end point must be distinct

Definitions (cont.)

Specification Fields: describes components of the abstract state of a class

• Line has specification fields startPoint, endPoint

• Derived Specification Fields: information that can be derived from specification fields but useful to have

 \circ length = sqrt((x1-x2)^2 + (y1-y2)^2)

ADT Example: Line





ADT Example: Line

* This class represents the mathematical concept of a line segment.

- * Specification fields:
- * @specfield start-point : point // The starting point of the line.
 - @specfield end-point : point // The ending point of the line.
- * Derived specification fields:
- * @derivedfield length : real // The length of the line.
- * Abstract Invariant:
- * A line's start-point must be different from its end-point. * /

public class Line {

Abstract State

Specification Fields

ADT Example: Line

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Abstract Invariant

ADT Example: Line

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public class Line {

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ADT Example: Line

* This class represents the mathematical concept of a line segment. * Specification fields: @specfield start-point : point // The starting point of the line. @specfield end-point : point // The ending point of the line. * Derived specification fields: * @derivedfield length : real $//% \left({{\mathbb{T}}_{{\mathbb{T}}}} \right)$) $//% \left({{\mathbb{T}}_{{\mathbb{T}}}} \right)$ The length of the line. * Abstract Invariant: * A line's start-point must be different from its end-point. public class Line { **Derived Fields**

ADT Example: Circle

Suppose we want to make a Circle class that represents circles on the Cartesian plane



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ADT Example: Circle

Specification Fields:

- Option #1: r and center
- Option #2: center and edgePoint
- Option #3: corner1 and corner2

Derived Specification Fields:

- Circumference
- Diameter
- o Area
- o ...

Abstraction

- Abstract values, state, and invariants specify the behavior of classes and methods
 What should my class do?
- We have not implemented any of these ADTs yet
 Implementation should not affect abstract state
 - As long as Circle represents the circle we are interested in, nobody cares how it is implemented

Abstract vs. Concrete

- We'll talk later about representation invariants, which specify how the abstract invariant is implemented
- We'll also discuss how abstraction functions map the concrete representation of an ADT to the abstract value

Javadoc Documentation

- Tool made by Oracle for API documentation
- We've already seen Javadoc for external class specification
- Method specifications will describe method behavior in terms of preconditions and postconditions

Javadoc Method Tags

- **@requires**: the statements that must be met by the method's caller
- @return: the value returned by the method, if any
- @throws: the exceptions that may be raised, and under which conditions
- **@modifies**: the variables that may change because of the method
- **@effects**: the side effects of the method

Javadoc Method Tags

- If **@requires** is not met, anything can happen • False implies everything
- The conditions for @throws must be a subset of the precondition
 - $\circ~$ Ex: If a method <code>@requires</code> x > 0, <code>@throws</code> should not say anything about x < 0
- **@modifies** lists what may change, while **@effects** indicates how they change
 - If a specification field is listed in the @modifies clause but not in the @effects clause, it may take on any value (provided that it follows the abstract invariant)
 - If you mention a field in @modifies, you should try to specify what happens in @effects