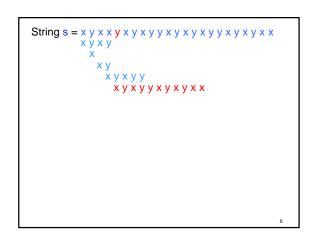
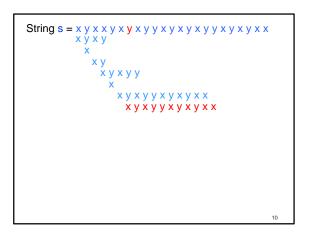


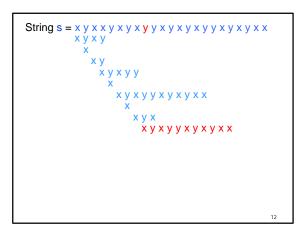
Pattern Matching

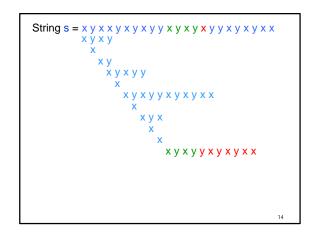
- Given
 - a string, s, of n characters
 - a pattern, p, of m characters
 - usually m<<n</p>
- Find
 - all occurrences of the pattern **p** in the string **s**
- Obvious algorithm:
 - try to see if p matches at each of the positions in s, stopping at a failed match

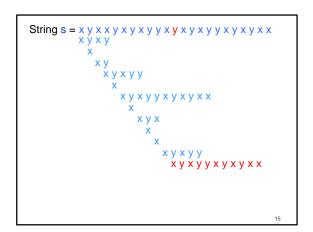
2

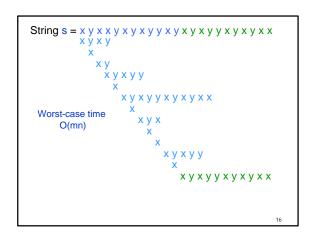


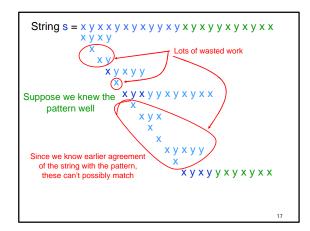












Preprocess the Pattern

- After each character in the pattern figure out ahead of time what the next useful work would be if it failed to match there
 - i.e. how much can one shift over the pattern for the next match

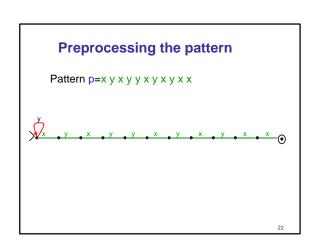
18

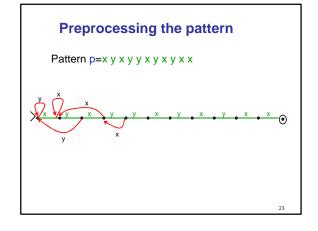
Preprocessing the pattern

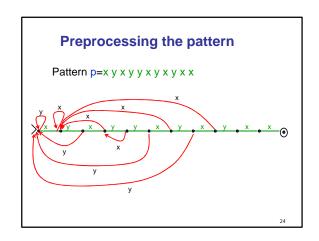
- At each mismatch
 - Look at the last part that matched plus extra mismatched character
 - Try to fit pattern as far to the left in this as possible
 - i.e. look for the longest prefix of the pattern that matches the end of the sequence so far.

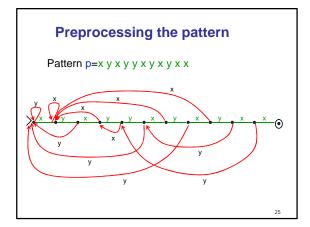
20

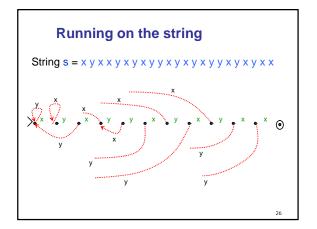
Preprocessing the pattern Pattern p=x y x y y x y x y x x > x y x y x y x y x y x x Each dot represents how far in the pattern things are matched











Knuth-Morris-Pratt Algorithm

- Once the preprocessing is done there are only n steps on any string of size n
 - just follow your nose
- Obvious algorithm for doing preprocessing is O(m²) steps
 - still usually good since m<<n
- Knuth-Morris-Pratt Algorithm can do the pre-processing in O(m) steps
 - Total O(m+n) time

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Finite State Machines

- The diagram we built is a special case of a finite automaton
 - start state
 - goal or accepting state(s)
 - an arc out of each state labeled by each of the possible characters
- Finite automata take strings of characters as input and decide what to do with them based on the paths they follow

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Finite State Machines

- Many communication protocols, cachecoherency protocols, VLSI circuits, userinterfaces, even adventure games are designed by making finite state machines first.
 - The "strings" that are the input to the machines can be
 - a sequence of actions of the user
 - the bits that arrive on particular ports of the chip
 - a series of values on a bus

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Finite State Machines

- Can search for arbitrary combinations of patterns not just a single pattern
 - Given two finite automata can build a single new one that accepts strings that either of the original ones accepted
- Typical text searches are based on finite automata designs
 - Perl builds this in as a first-class component of the programming language.

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