

- · Many different forms of "Machine Learning"
  - We focus on the problem of prediction
- · Want to make a prediction based on observations
  - Vector X of m observed variables: <X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>m</sub>>
     X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>m</sub> are called "input features/variables"
     Also called "independent variables," but this can be misleading!
  - X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>m</sub> need not be (and usually are not) independent
    Based on observed X, want to predict unseen variable Y
  - Y called "output feature/variable" (or the "dependent variable")
  - Seek to "learn" a function g(X) to predict Y: Ŷ = g(X)
     When Y is discrete, prediction of Y is called "classification"
    - When Y is continuous, prediction of Y is called "regression"

## A (Very Short) List of Applications

- · Machine learning widely used in many contexts
  - Stock price prediction
     Using economic indicators, predict if stock with go up/down
  - Computational biology and medical diagnosis
    - Predicting gene expression based on DNA
    - Determine likelihood for cancer using clinical/demographic data
  - Predict people likely to purchase product or click on ad
    - "Based on past purchases, you might want to buy..."
  - Credit card fraud and telephone fraud detection

     Based on past purchases/phone calls is a new one fraudulent?
     Saves companies *billions(!)* of dollars annually
  - Spam E-mail detection (gmail, hotmail, many others)











$$E[(Y - g(X))^{2}] = E[(Y - (aX + b))^{2}] = E[(Y - aX - b)^{2}]$$



## A Simple Classification Example • Predict Y based on observing variable X • X has discrete value from {1, 2, 3, 4} • X denotes temperature range today: <50, 50-60, 60-70, >70 • Y has discrete value from {rain, sun} • Y denotes general weather outlook tomorrow • Given training data, estimate joint PMF: $\hat{p}_{X,Y}(x, y)$ • Note Bayes rule: $P(Y|X) = \frac{p_{X,Y}(x, y)}{p_X(x)} = \frac{p_{X,Y}(x|y)p_Y(y)}{p_X(x)}$ • For new X, predict $\hat{Y} = g(X) = \arg \max \hat{P}(Y|X)$ • Note $p_x(x)$ is not affected by choice of y, yielding:











## **Email Classification**

- · Want to predict is an email is spam or not
  - Start with the input data
    - Consider a lexicon of *m* words (Note: in English  $m \approx 100,000$ )
    - Define *m* indicator variables  $\mathbf{X} = \langle X_1, X_2, ..., X_m \rangle$
    - Each variable X<sub>i</sub> denotes if word i appeared in a document or not
    - $_{\circ}~$  Note: *m* is huge, so make "Naive Bayes" assumption
  - Define output classes Y to be: {spam, non-spam}
  - Given training set of N previous emails
    - For each email message, we have a training instance:
       X = <X<sub>1</sub>, X<sub>2</sub>, ..., X<sub>m</sub>> noting for each word, if it appeared in email
    - Each email message is also marked as spam or not (value of Y)







## Coincidence, You Ask? San Francisco Chronicle, Oct. 28, 2009: "Schwarzenegger's press secretary, Aaron McLear, insisted Tuesday it was simply a 'weird coincidence'." Steve Piantadosi (grad student at MIT) blog post, Oct. 28, 2009:

- "...assume that each word starting a line is chosen independently..."
- "...[compute] the (token) frequency with which each letter appears at the start of a word..."
- Multiply probabilities for letter starting each word of each line to get final answer: "one in 1 trillion"
- 50,000 times *less* likely than winning CA lottery