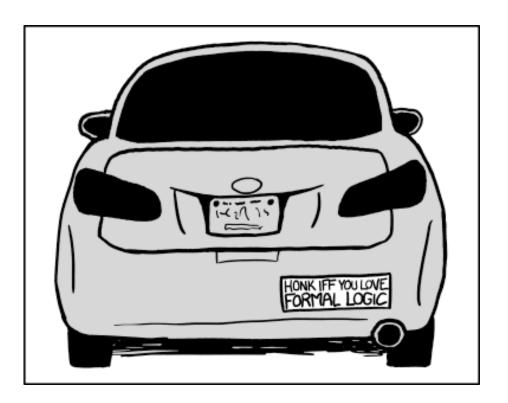
# **CSE 311: Foundations of Computing I**

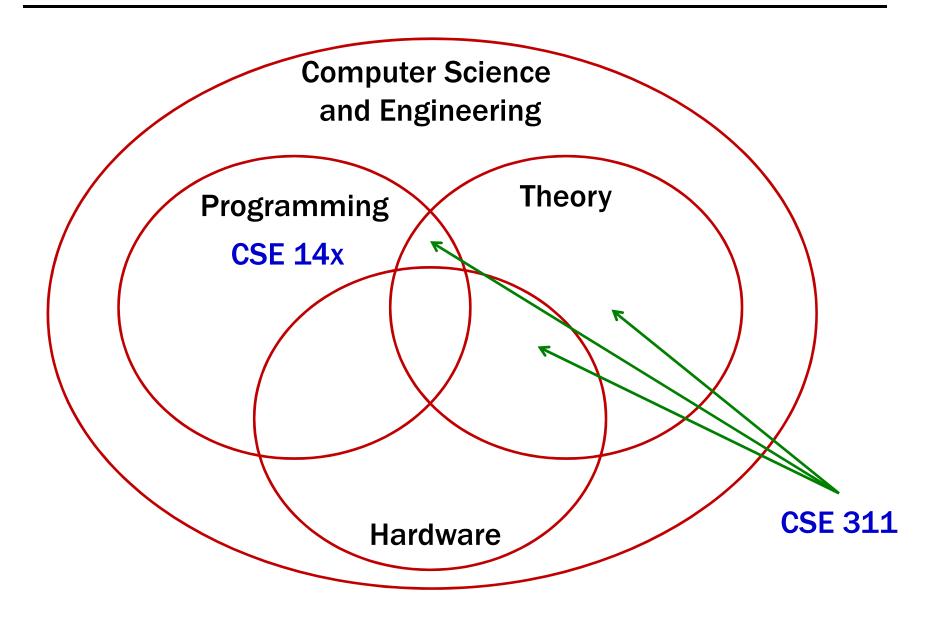
### **Lecture 1: Propositional Logic**





# **About CSE 311**

# **Some Perspective**



#### **About the Course**

### We will study the *theory* needed for CSE:

### Logic:

How can we describe ideas *precisely*?

#### **Formal Proofs:**

How can we be *positive* we're correct?

#### **Number Theory:**

How do we keep data secure?

#### **Relations/Relational Algebra:**

How do we store information?

#### **Finite State Machines:**

How do we design hardware and software?

#### **Turing Machines:**

Are there problems computers can't solve?

#### **About the Course**

#### Will help you become a better programmer

By the end of the course, you will have the tools for....

- reasoning about difficult problems
- automating difficult problems
- communicating ideas, methods, objectives and will understand fundamental structures of CS

# **Course Logistics**

#### Instructor

#### **Paul Beame**



MWF 1:30-2:20 in CSE2 G01

**Office Hours (tentative):** 

M 2:30-4:00 and WF 2:30-3:00 in CSE 668

#### **TAs**

#### **Teaching Assistants:**

Siddharth lyer Josh Shin

Suraj Jagadeesh Xiaoyue Sun

Karishma Mandyam Jason Waataja

**Section:** 

**Thursdays** 

starting this week

**Office Hours: TBD** 

(Optional) Book:

Rosen: Readings for 6<sup>th</sup> or 7<sup>th</sup> editions.

Many used copies available

**Good for practice with solved problems** 

# **Course Webpage**

#### **CSE 311: Foundations of Computing I**

Winter, 2020

#### **Paul Beame**

MWF 1:30-2:20, CSE2 G01 Office hours: TBA CSE 668

#### Email and discussion:

email list: cse311a\_wi20 [archives]

Please send any e-mail about the course to cse311-staff@cs.

#### Textbook

There is no required text for the course. Especially over the first 6-7 weeks of the course, the following textbook can be a useful companion: Rosen, *Discrete Mathematics and Its Applications*, McGraw-Hill. There are many editions of this book and lots of used copies available, new copies are extremely expensive. A copy should be available on short-term loan from the Engineering Library.



#	date	topic	slides	inked	reading (Rosen)
1	Mon, Jan 6	Propositional Logic			1.1, 1.2 (7th) 1.1 (6th)
2	Wed, Jan 8	Logical Equivalence/Gates			1.1-1.3 (7th) 1.1-1.2 (6th)
3	Fri, Jan 10	More Logic/Circuits			12.1-12.3 (7th) 11.1-11.3 (6th)
4	Mon, Jan 13	Boolean Algebra/Circuits			12.1-12.3 (7th) 11.1-11.3 (6th)
5	Wed, Jan 15	Canonical Forms, Predicate Logic			1.4-1.5 (7th) 1.3-1.4 (6th)
6	Fri, Jan 17	Predicate Logic			1.6-1.7 (7th) 1.5-1.7 (6th)
	Mon, Jan 20	Martin Luther King Day NO CLASS			
7	Wed, Jan 22	Logical Inference and Proofs			1.6-1.7 (7th) 1.5-1.7 (6th)
8	Fri, Jan 24	Predicate Logic Proofs			1.6-1.7 (7th) 1.5-1.7 (6th)
9	Mon, Jan 27	Set Theory			2.1-2.3 (6th, 7th)
10	Wed, Jan 29	Modular Arithmetic			4.1-4.2 (7th) 3.4-3.5 (6th)
11	Fri, Jan 31	Applications of Mod, Number Theory, Factoring			4.1-4.3 (7th) 3.4-3.6 (6th)
12	Mon, Feb 3	GCD, Euclid's Algorithm, Modular Equations			4.3-4.4 (7th), 3.5-3.7 (6th)
13	Wed, Feb 5	Induction			5.1 (7th), 4.1 (6th)
14	Fri, Feb	More Induction			5.1 (7th), 4.1 (6th)

LOW 220 LOW 101	TA Office l		hours	Room			
20 DEN 213 20 LOW 220 0 LOW 101	Siddharth Iyer						
20 DEN 213 20 LOW 220 0 LOW 101	Suraj Jagadeesh						
20 DEN 213 20 LOW 220 0 LOW 101	Karishma Mandyam						
20 DEN 213 20 LOW 220 0 LOW 101	Josh Shin						
20 DEN 213 20 LOW 220 0 LOW 101	Xiaoyue Sun						
20 DEN 213 20 LOW 220 0 LOW 101	Jason Waataja						
LOW 220 LOW 101	Section Day/Tir		ime	Room	ı		
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	AD	Th 2:30-3:20		LOW 101			
ate Problems Solns	Section Mate	erials	Date	Problems	Solns		
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	Midterm of In class, F Closed book     Final example The final of Monday 1	riday 14 ok. Close <b>m</b> :	ed notes.	), fficially sched	luled tin		

All Course Information @cs.uw.edu/311

#### Work

#### Homework:

**Due WED at 11:00 pm online (Gradescope)** 

Write up individually

**Extra Credit** 

**Exams:** 

Midterm in class on Friday, Feb 14

**Final exam:** 

Monday, March 16 2:30-4:20 pm

**Grading (roughly):** 

**50% Homework** 

**15-20% Midterm** 

30-35% Final Exam

#### Communication

- You are already on the class e-mail list
  - Major announcements here, archive reachable from the course webpage
- If you want to email to us (me & TAs):

cse311-staff@cs.washington.edu

- Discussion board
  - accept invitation to Ed class discussion board

Grades were very important up until now...

- Grades were very important up until now
- Grades are much less important going forward
  - companies care much more about your interviews
  - grad schools care much more about recommendations

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  - good recommendations involve knowledge beyond the classes
- Please <u>relax</u> and focus on learning

## Please calm down about grades

- Most time spent on questions about grading issues is not worthwhile to either the student or teacher
- Try to avoid asking "will I lose points if..."
- If the thought of losing points worries you, show more work
  - no sense having a 30 minute discussion to save 10 minutes

# **Collaboration Policy**

- Collaboration with others is encouraged
- BUT you must:
  - list anyone you work with
  - turn in only your own work
- Recommended approach for group work
  - do not leave with any solution written down or photographed
  - wait 30 minutes before writing up your solution
- See Allen School Academic Misconduct policy also

# **No Late Days**

 To be accepted, late submission (with good reason) must be arranged in advance 48 hours before the deadline

# If you are worried about Mathy aspects of 311

- Associated 1-credit CR/NC workshop
  - CSE 390ZA (not yet available for enrollment)
  - Extra collaborative practice on 311 concepts, study skills, a small amount of assigned work
  - 1.5 hours Thursdays 3:30 pm
  - Full attendance is required, else NC
  - NOT for help with 311 homework
- Anyone in 311 can sign up but enrollment is limited

# Getting used to being formal

As problems we deal with get harder we need stronger tools...

# Formalism is a tool we apply when problems get difficult

- helps us get through without making mistakes
- sometimes even gives "turn the crank" solutions



# **Propositional Logic**

# What is logic and why do we need it?

Logic is a language, like English or Java, with its own

- words and rules for combining words into sentences (syntax)
- ways to assign meaning to words and sentences (semantics)

Why learn another language when we know English and Java already?

# Why not use English?

– Turn right here...

Buffalo buffalo buffalo buffalo buffalo buffalo

We saw her duck

# Why not use English?

– Turn right here...

Does "right" mean the direction or now?

Buffalo buffalo Buffalo buffalo buffalo buffalo



This means "Bison from Buffalo, that bison from Buffalo bully, themselves bully bison from Buffalo.

We saw her duck

Does "duck" mean the animal or crouch down?

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Natural languages can be imprecise

# Why not use Java?

#### What does this code do:

```
public static boolean mystery(int x) {
   for (int r = 2; r < x; r++) {
     for (int q = 2; q < x; q++) {
        if (r*q == x)
          return false;
     }
   }
   return x > 1;
}
```

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}
```

**Determines if x is a prime number** 

Programming languages can be verbose

# Why learn a new language?

#### We need a language of reasoning to

- state sentences more precisely
- state sentences more concisely
- understand sentences more quickly

# Propositions: building blocks of logic

#### A *proposition* is a statement that

- is either true or false
- is "well-formed"

# Propositions: building blocks of logic

### A *proposition* is a statement that

- is either true or false
- is "well-formed"

#### All cats are mammals

true

#### All mammals are cats

false

# **Are These Propositions?**

$$2 + 2 = 5$$
  
 $x + 2 = 5$ 

$$x + 2 = 5$$

Akjsdf!

Who are you?

Every positive even integer can be written as the sum of two primes.

# **Are These Propositions?**

$$2 + 2 = 5$$

This is a proposition. It's okay for propositions to be false.

$$x + 2 = 5$$

Not a proposition. Doesn't have a fixed truth value

#### Akjsdf!

Not a proposition because it's gibberish.

#### Who are you?

This is a question which means it doesn't have a truth value.

Every positive even integer can be written as the sum of two primes.

This is a proposition. We don't know if it's true or false, but we know it's one of them!

# A first application of logic



"If I were to ask you out, would your answer to that question be the same as your answer to this one?"

## **Propositions**

We need a way of talking about arbitrary ideas...

Propositional Variables: p, q, r, s, ...

#### **Truth Values:**

- T for true
- F for false

# **A Compound Proposition**

"Garfield has black stripes if he is an orange cat and likes lasagna, and he is an orange cat or does not like lasagna"

We'd like to understand what this proposition means.

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- q "Garfield is an orange cat"
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We'd like to understand what this proposition means.

First find the simplest (atomic) propositions:

- p "Garfield has black stripes"
- q "Garfield is an orange cat"
- "Garfield likes lasagna"

```
(p if (q and r)) and (q or (not r))
```

### **Logical Connectives**

Negation (not)  $\neg p$ 

Conjunction (and)  $p \land q$ 

Disjunction (or)  $p \vee q$ 

Exclusive Or  $p \oplus q$ 

Implication  $p \rightarrow q$ 

Biconditional  $p \leftrightarrow q$ 

### **Logical Connectives**

Negation (not)  $\neg p$ 

Conjunction (and)  $p \land q$ 

Disjunction (or)  $p \lor q$ 

Exclusive Or  $p \oplus q$ 

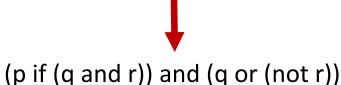
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q "Garfield is an orange cat"

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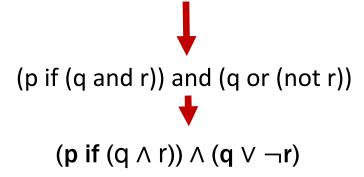
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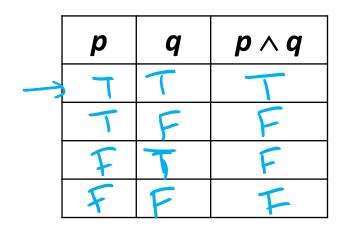
q "Garfield is an orange cat"

"Garfield likes lasagna"



## **Some Truth Tables**

p	$\neg p$
T	4
T	H



p	q	$p \vee q$
		T
	1	T
¥	1	1
F	¥	F

p	q	p⊕q
+	4	F
+	4	+
F	7	1
F	T	F

## **Some Truth Tables**

p	$\neg p$
Т	F
F	Т

p	q	p \ q
Т	Т	Т
Т	F	F
F	Т	F
F	F	F

p	q	$p \vee q$
Т	Т	Т
Т	F	Т
F	Т	Т
F	F	F

p	q	p⊕q
Т	Т	F
Т	F	Т
F	Т	Т
F	F	F

"If it's raining, then I have my umbrella"

It's useful to think of implications as promises. That is "Did I lie?"

	It's raining	It's not raining
I have my umbrella		
I do not have my umbrella		

р	q	$p \rightarrow q$	
Т	Т	Т	•
Т	F	F	(
F	Т	Т	
F	F	Т	
*			

"If it's raining, then I have my umbrella"

It's useful to think of implications as promises. That is "Did I lie?"

р	q	$p \rightarrow q$
Т	T	Т
Т	F	F
F	Т	Т
F	F	Т

	It's raining	It's not raining
I have my umbrella	No	No
I do not have my umbrella	Yes	No

The only lie is when:

- (a) It's raining AND
- (b) I don't have my umbrella

"If it's raining, then I have my umbrella"

р	q	$p \rightarrow q$
Т	Т	Т
Т	F	F
F	Т	Т
F	F	Т

Are these true?

$$2 + 2 = 4 \rightarrow \text{ earth is a planet}$$

$$2 + 2 = 5 \rightarrow 26$$
 is prime

"If it's raining, then I have my umbrella"

р	q	$p \rightarrow q$
Т	T	Т
Т	F	F
F	Т	Т
F	F	Т

Are these true?

$$2 + 2 = 4 \rightarrow \text{ earth is a planet}$$

The fact that these are unrelated doesn't make the statement false! "2 + 2 = 4" is true; "earth is a planet" is true.  $T \rightarrow T$  is true. So, the statement is true.

$$2 + 2 = 5 \rightarrow 26$$
 is prime

Again, these statements may or may not be related. "2 + 2 = 5" is false; so, the implication is true. (Whether 26 is prime or not is irrelevant).

### Implication is not a causal relationship!

#### $p \rightarrow q$

- (1) "I have collected all 151 Pokémon if I am a Pokémon master"
- (2) "I have collected all 151 Pokémon only if I am a Pokémon master"

These sentences are implications in opposite directions:

#### $p \rightarrow q$

- (1) "I have collected all 151 Pokémon if I am a Pokémon master"
- (2) "I have collected all 151 Pokémon only if I am a Pokémon master"

These sentences are implications in opposite directions:

- (1) "Pokémon masters have all 151 Pokémon"
- (2) "People who have 151 Pokémon are Pokémon masters"

#### So, the implications are:

- (1) If I am a Pokémon master, then I have collected all 151 Pokémon.
- (2) If I have collected all 151 Pokémon, then I am a Pokémon master.

- -p implies q
- whenever p is true q must be true
- if p then q
- -q if p
- -p is sufficient for q
- -p only if q
- q is necessary for p

р	q	$p \rightarrow q$
T	Т	Т
T	F	F
F	Т	Т
F	F	Т

# Biconditional: $p \leftrightarrow q$

- p iff q
- p is equivalent to q
- p implies q and q implies p
- p is necessary and sufficient for q

p	q	$p \leftrightarrow q$
-	4	1
1	1	F
F		F
7	4	T

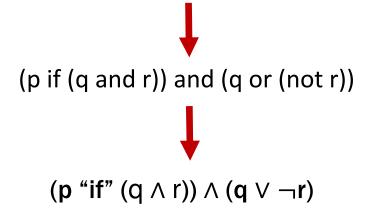
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p	q	$p \leftrightarrow q$	
Т	T	T	
Т	F	F	
F	Т	F	
F	F	Т	

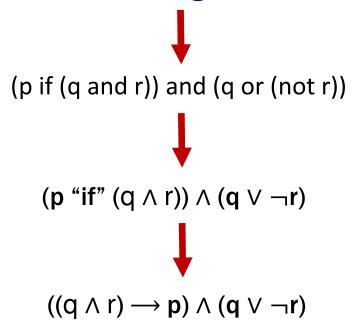
#### **Back to Garfield...**

- p "Garfield has black stripes"
- q "Garfield is an orange cat"
- r "Garfield likes lasagna"



#### **Back to Garfield...**

- "Garfield has black stripes"
- q "Garfield is an orange cat"
- r "Garfield likes lasagna"



### **Analyzing the Garfield Sentence with a Truth Table**

_			/		1	
q	r	$\neg r$	$q \lor \neg r$	$q \wedge r$	$(q \wedge r) \rightarrow p$	$((q \land r) \rightarrow p) \land (q \lor \neg r)$
<b>ш</b>	F	+'	+	4		
F	Т	11	7	+		7
Т	F	1	T	F	7	
Т	Т	4	T	7	F	F
F	F	1	+	7	7	
F	Т	T	F	F	T	F/
Т	F	T	T	F	T	T /
Т	Т	F	1	T		
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### **Analyzing the Garfield Sentence with a Truth Table**

p	q	r	$\neg r$	$q \lor \neg r$	$q \wedge r$	$(q \wedge r) \rightarrow p$	$((q \land r) \rightarrow p) \land (q \lor \neg r)$
F	F	F	Т	Т	F	Т	Т
F	F	Т	F	F	F	Т	F
F	Т	F	Т	Т	F	Т	Т
F	Т	Т	F	Т	T	F	F
Т	F	F	Т	Т	F	Т	Т
Т	F	Т	F	F	F	Т	F
Т	Т	F	Т	Т	F	Т	Т
Т	Т	Т	F	Т	Т	Т	Т