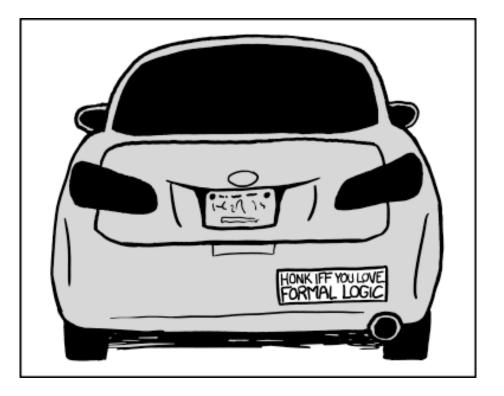
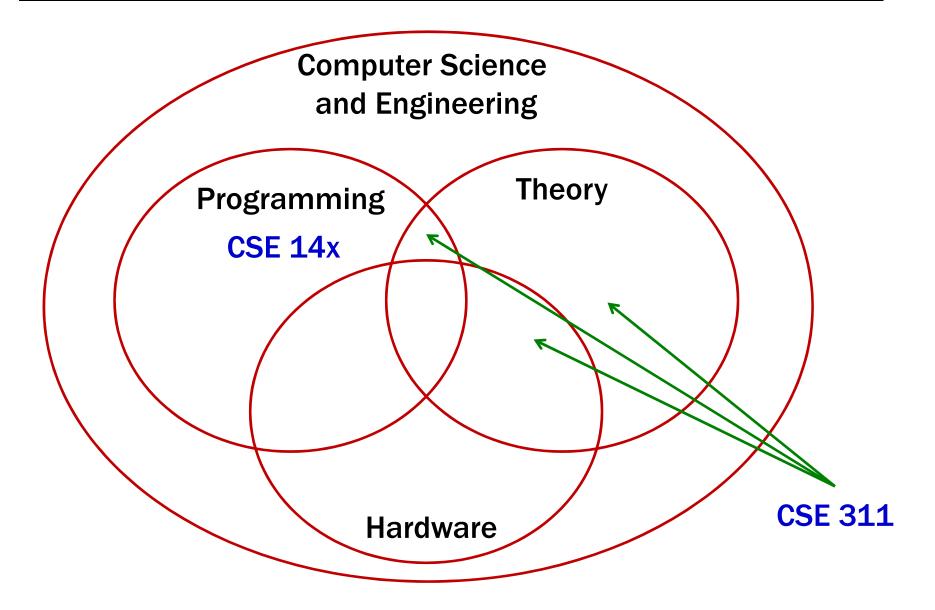
CSE 311: Foundations of Computing I

Lecture 1: Propositional Logic



Some Perspective



We will study the *theory* needed for CSE:

Logic:

How can we describe ideas *precisely*? **Formal Proofs**:

How can we be *positive* we're correct?

Number Theory:

How do we keep data secure?

Relations/Relational Algebra:

How do we store information?

Finite State Machines:

How do we design hardware and software? Turing Machines:

Are there problems computers *can't* solve?

It's about perspective!

- Tools for reasoning about difficult problems
- Tools for communicating ideas, methods, objectives...
- Tools for automating difficult problems
- Fundamental structures for computer science

It's about perspective!

- Tools for reasoning about difficult problems
- Tools for communicating ideas, methods, objectives...
- Tools for automating difficult problems
- Fundamental structures for computer science

This is NOT a programming course!

Instructors

Paul Beame



Section B MWF 10:30-11:20 in MUE 153

Office Hours: MF 11:30-12:00 and M 3:00-4:00 CSE 668

Kevin Zatloukal



Section A MWF 1:30-2:20 in SIG 134

Office Hours: WF 2:30-3:00 and M 12:00-1:00 CSE 212

Office hours are for students in both sections

TAs and Administrivia

Teaching Assistants:

Darin Chin Daniel Fuchs Yuqi Huang Joy Ji Kaiyu Zheng Joshua Fan Kush Gupta Sean Jaffe Cheng Ni

Homework:

Due WED at 11:59 pm online Write up individually Extra Credit

Grading (roughly): 50% Homework 15-20% Midterm 30-35% Final Exam

(Optional) Book: Rosen: Readings for 6th (used) or 7th (cut down) editions. Good for practice with solved problems

All Course Information @ cs.uw.edu/311

Section:

Thursdays

starting this week

Office Hours: TBA

Administrivia

CSE 311: Foundations of Computing I

Spring, 2018

Paul Beame

Section A: MWF 10:30-11:20, MUE 153 Office hours: MF 11:30-12:00 and TBA CSE 668

Kevin Zatloukal

Section B: MWF 1:30-2:20, SIG 134 Office hours: TBA CSE 212

Email and discussion:

email list: cse311_sp18 [archives] Please send any e-mail about the course to cse311-staff@cs.

Discussion Board (moderated by TBA)

Use this board to discuss the content of the course. That includes everything **except** the solutions to current homework problems. Feel free to discuss homeworks and exams from past incarnations of the course, and any confusion over topics discussed in class. It is also acceptable to ask for *clarifications* about the statement of homework problems, but not about their solutions.

Textbook:

There is no required text for the course. Especially over the first 6-7 weeks of the course, the following textbook can be a useful companion: Rosen, *Discrete Mathematics and Its Applications*, McGraw-Hill. We will support two versions equally: (1) a special reduced version of the 7th edition which at \$60 costs < 1/4 of the ridiculous price of the full text, and (2) the 6th edition, which is available used through the bookstore for even less money. It should also be available on short-term loan from the Engineering Library.



Lectures

#	date	topic	slides	inked (A)	inked (B)	reading (Rosen)
1	Mon, Mar 26	Propositional Logic	pdf			1.1, 1.2 (7th) 1.1 (6th)
2	Wed, Mar 28	Logic/Gates				1.1-1.3 (7th) 1.1-1.2 (6th)
3	Fri, Mar 30	More Logic/Circuits				12.1-12.3 (7th) 11.1-11.3 (6th)
4	Mon, Apr 2	Boolean Algebra/Circuits				12.1-12.3 (7th) 11.1-11.3 (6th)
5	Wed, Apr 4	Canonical Forms, Predicate Logic				1.4-1.5 (7th) 1.3-1.4 (6th)
6	Fri, Apr 6	Predicate Logic				1.6-1.7 (7th) 1.5-1.7 (6th)
7	Mon, Apr 9	Logical Inference and Proofs				1.6-1.7 (7th) 1.5-1.7 (6th)
8	Wed,	Predicate Logic Proofs				1 6-1 7 (7th) 1 5-1 7 (6th)

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TA	Office	hours	Room	
Section	Day	y/Time	Ro	om
Section Ma	toriale	Date	Problems	Solns

Homeworks [Grading guidelines, Submission guidelines]:

Exams:

- Midterm exam: In class, Wednesday 2-May-2018,
- Final exam: Monday, 4-June-2018 The final exam has been rescheduled so that both lectures can take a common exam. The times will be 2:30-4:20 pm (the original exam time for the 1:30 section) and 4:30-6:20 pm both in . Students

All Course Information @ cs.uw.edu/311

Administrivia

CSE 311: Foundations of Computing I

Spring, 2018

Paul Beame

Section A: MWF 10:30-11:20 MUE 153 Office hours: MF 11:30-12:00 and TBA CSE 668

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Midterm: Wed, May 2 in class Final Exam: Mon, Jun 4 A section 2:30-4:20 • B section 4:30-6:20 • Not at 8:30-10:20 time in • exam schedule **Location TBA** Exams: • Midterm exam: In class, Wednesday 2-May-2018, • Final exam Monday 4-June-2018

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All Course Information @ cs.uw.edu/311

Logic: The Language of Reasoning

Why not use English?

- Turn right here...
- Buffalo buffalo Buffalo buffalo buffalo buffalo
- We saw her duck

Logic: The Language of Reasoning

Why not use English?

– Turn right here...

Does "right" mean the direction or now?

Buffalo buffalo Buffalo buffalo buffalo buffalo

This means "Bison from Buffalo, that bison from Buffalo bully, themselves bully bison from Buffalo.

- We saw her duck

Does "duck" mean the animal or crouch down?

Logic: The Language of Reasoning

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Does "duck" mean the animal or crouch down?

"Language" like Java or English

- Words, sentences, paragraphs, arguments...
- Today is about *words* and *sentences*

Logic, as the "language of reasoning", will help us...

- Be more precise
- Be more concise
- Figure out what a statement means more quickly

Propositions

A proposition is a statement that

- has a truth value, and
- is "well-formed"



"If I were to ask you out, would your answer to that question be the same as your answer to this one?"

2 + 2 = 5

The home page renders correctly in Chrome.

Turn in your homework on Wednesday.

This statement is false.

Akjsdf!

Who are you?

Every positive even integer can be written as the sum of two primes.

2 + 2 = 5

This is a proposition. It's okay for propositions to be false.

The home page renders correctly in Chrome.

This is a proposition. It's okay for propositions to be false.

Turn in your homework on Wednesday.

This is a "command" which means it doesn't have a truth value.

This statement is false.

This statement does not have a truth value! (If it's true, it's false, and vice versa.)

Akjsdf!

This is not a proposition because it's gibberish.

Who are you?

This is a question which means it doesn't have a truth value.

Every positive even integer can be written as the sum of two primes.

This is a proposition. We don't know if it's true or false, but we know it's one of them!

A proposition is a statement that

- has a truth value, and
- is "well-formed"

We need a way of talking about *arbitrary* ideas...

Propositional Variables: Truth Values:

A proposition is a statement that

- has a truth value, and
- is "well-formed"

We need a way of talking about *arbitrary* ideas...

Propositional Variables: *p*, *q*, *r*, *s*, ...

Truth Values:

- T for true
- F for false

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine then you can't get either."

We'd like to understand what this proposition means.

This is where logic comes in. There are pieces that appear multiple times in the phrase (e.g., "you can get measles").

These are called **atomic propositions**. Let's list them:

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine then you can't get either."

We'd like to understand what this proposition means.

This is where logic comes in. There are pieces that appear multiple times in the phrase (e.g., "you can get measles").

These are called **atomic propositions**. Let's list them:

Measles: "You can get measles" Mumps: "You can get mumps" MMR: "You had the MMR vaccine" "You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine then you can't get either."

Measles: "You can get measles"

Mumps: "You can get mumps"

MMR: "You had the MMR vaccine"

Now, we put these together to make the sentence:

((Measles and Mumps) if not MMR) but (if MMR then not (Measles or Mumps))

((Measles and Mumps) if not MMR) and (if MMR then not (Measles or Mumps))

This is the general idea, but now, let's define our formal language.

Logical Connectives

Negation (not)	$\neg p$
Conjunction (and)	$p \land q$
Disjunction (or)	$p \lor q$
Exclusive Or	$p\oplus q$
Implication	$p \longrightarrow q$
Biconditional	$p \leftrightarrow q$

Logical Connectives

Negation (not)	$\neg p$	
Conjunction (and)	$p \wedge q$	Measles:
		"You can get measles"
Disjunction (or)	$p \lor q$	Mumps:
Exclusive Or	$p \oplus q$	"You can get mumps"
lasalisatisa		MMR:
Implication	$p \rightarrow q$	"You had the MMR vaccine"
Biconditional	$p \leftrightarrow q$	

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine then you can't get either."

((Measles and Mumps) if not MMR) and (if MMR then not (Measles or Mumps))

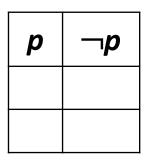
Logical Connectives

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Biconditional	$p \leftrightarrow q$	L

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine then you can't get either."

((Measles and Mumps) if not MMR) and (if MMR then not (Measles or Mumps)) ((Measles \land Mumps) if \neg MMR) \land (if MMR then \neg (Measles \lor Mumps))

Some Truth Tables

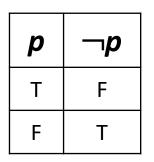


p	q	p ^ q

р	q	$p \lor q$

р	q	p ⊕ q

Some Truth Tables



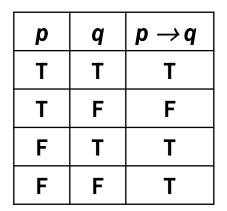
p	q	$p \wedge q$
Т	Т	Т
Т	F	F
F	Т	F
F	F	F

р	q	$p \lor q$
Т	Т	Т
Т	F	Т
F	Т	Т
F	F	F

p	q	p ⊕ q		
Т	Т	F		
Т	F	Т		
F	Т	Т		
F	F	F		

It's useful to think of implications as promises. That is "Did I lie?"

	It's raining	It's not raining
l have my umbrella		
l do not have my umbrella		



It's useful to think of implications as promises. That is "Did I lie?"

p	q	$p \rightarrow q$	
Т	Т	Т	
Т	F	F	
F	Т	Т	
F	F	Т	

	It's raining	It's not raining
l have my umbrella	No	No
l do not have my umbrella	Yes	No

The only lie is when:

- (a) It's raining AND
- (b) I don't have my umbrella

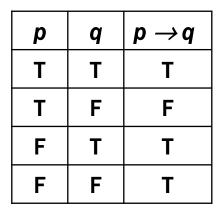
Are these true?

 $2 + 2 = 4 \rightarrow$ earth is a planet

 $2 + 2 = 5 \rightarrow 26$ is prime

р	q	$p \rightarrow q$	
Т	Т	Т	
Т	F	F	
F	Т	Т	
F	F	Т	

Are these true?



$2 + 2 = 4 \rightarrow$ earth is a planet

The fact that these are unrelated doesn't make the statement false! "2 + 2 = 4" is true; "earth is a planet" is true. T \rightarrow T is true. So, the statement is true.

$2 + 2 = 5 \rightarrow 26$ is prime

Again, these statements may or may not be related. "2 + 2 = 5" is false; so, the implication is true. (Whether 26 is prime or not is irrelevant).

Implication is not a causal relationship!

(1) "I have collected all 151 Pokémon if I am a Pokémon master"(2) "I have collected all 151 Pokémon only if I am a Pokémon master"

These sentences are implications in opposite directions:

(1) "I have collected all 151 Pokémon if I am a Pokémon master"(2) "I have collected all 151 Pokémon only if I am a Pokémon master"

These sentences are implications in opposite directions:

(1) "Pokémon masters have all 151 Pokémon"

(2) "People who have 151 Pokémon are Pokémon masters"

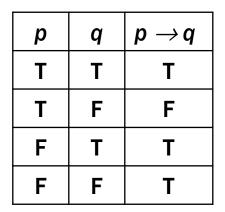
So, the implications are:

(1) If I am a Pokémon master, then I have collected all 151 Pokémon.

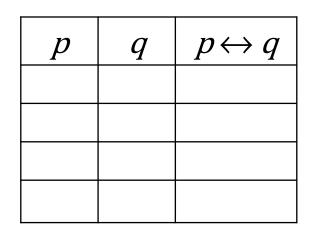
(2) If I have collected all 151 Pokémon, then I am a Pokémon master.

Implication:

- -p implies q
- whenever *p* is true *q* must be true
- if p then q
- -q if p
- -p is sufficient for q
- -p only if q
- q is necessary for p



- *p* iff *q*
- *p* is equivalent to *q*
- *p* implies *q* and *q* implies *p*
- *p* is necessary and sufficient for *q*



Back to our Vaccine Sentence Translation...

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine you can't get either."

((Measles \land Mumps) if \neg MMR) \land (if MMR then \neg (Measles \lor Mumps))

 $(\neg MMR \rightarrow (Measles \land Mumps)) \land (MMR \rightarrow \neg (Measles \lor Mumps))$

Understanding the Vaccine Sentence

"You can get measles and mumps if you didn't have the MMR vaccine, but if you had the MMR vaccine you can't get either."

((Measles \land Mumps) if \neg MMR) \land (if MMR then \neg (Measles \lor Mumps))

 $(\neg MMR \rightarrow (Measles \land Mumps)) \land (MMR \rightarrow \neg (Measles \lor Mumps))$

Define shorthand ...

- $p:\mathsf{MMR}$
- q : Measles
- r: Mumps

 $(\neg p \to (q \land r)) \land (p \to \neg (q \lor r))$

Analyzing the Vaccine Sentence with a Truth Table

p	q	r	$\neg p$	$q \wedge r$	$\neg p \rightarrow (q \wedge r)$	$q \lor r$	$\neg(q \lor r)$	$p \rightarrow \neg (q \lor r)$	$egin{pmatrix} (\neg p ightarrow (q \wedge r)) \land \ (p ightarrow \neg (q \lor r)) \end{pmatrix}$
Т	Т	Т							
Т	Т	F							
Т	F	т							
Т	F	F							
F	Т	т							
F	Т	F							
F	F	Т							
F	F	F							

Analyzing the Vaccine Sentence with a Truth Table

p	q	r	$\neg p$	$q \wedge r$	$\neg p \rightarrow (q \wedge r)$	$q \lor r$	$\neg(q \lor r)$	$p ightarrow \neg (q \lor r)$	$egin{pmatrix} (\neg p ightarrow (q \wedge r)) \land \ (p ightarrow \neg (q \lor r)) \end{pmatrix}$
Т	Т	Т	F	Т	т	Т	F	F	F
Т	Т	F	F	F	т	Т	F	F	F
Т	F	т	F	F	Т	Т	F	F	F
Т	F	F	F	F	Т	F	Т	Т	Т
F	Т	Т	Т	Т	Т	т	F	Т	Т
F	Т	F	Т	F	F	т	F	Т	F
F	F	Т	Т	F	F	Т	F	Т	F
F	F	F	Т	F	F	F	Т	Т	F

- *p* iff *q*
- *p* is equivalent to *q*
- *p* implies *q* and *q* implies *p*
- *p* is necessary and sufficient for *q*

p	q	$p \leftrightarrow q$	
Т	Т	т	
Т	F	F	
F	Т	F	
F	F	Т	