



Functions and abstraction

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UW CSE 160

Autumn 2022

Functions

In math:

- you use functions: sine, cosine, ...
- you define functions: $f(x) = x^2 + 2x + 1$

Python:

- Lets you **use** and **define** functions
- We have already seen some Python functions:
 - `len`, `float`, `int`, `str`, `range`

Python Functions

In Python:

- A function packages up and **names** a computation
- Enables re-use and, through parameters, generalization of the computation to other scenarios
- Allows you to reduce repetition in your programs
 - Don't Repeat Yourself (DRY principle)
- Makes your programs:
 - Shorter
 - Easier to understand
 - Easier to modify and debug



Similar to what we saw
with loops

Using (“calling”) a function

`len("hello")`

`len("")`

`math.sqrt(9)`

`math.sqrt(7)`

`range(1, 5)`

`range(8)`

`math.sin(0)`

`str(17)`

- Some need no input: `random.random()`
- All of the functions above **return** a value
- We did not have to write these functions ourselves!
We get to re-use code someone else wrote.

[See in python tutor](#)[See in python tutor](#)

Function call examples

```
import math  
  
x = 8  
y = 16  
z = math.sqrt(16)  
u = math.sqrt(y)  
v = math.sqrt(8 + 8)  
w = math.sqrt(x + x)
```

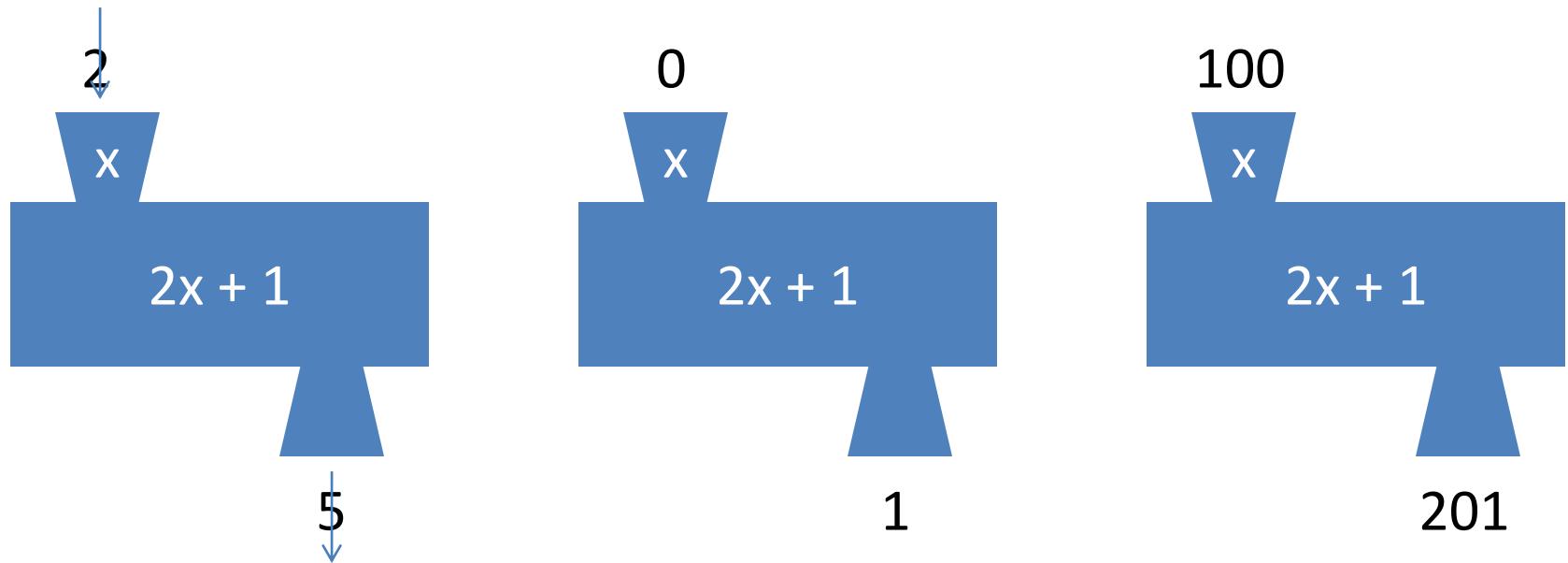
```
greeting = "hi"  
  
name = "Ruth"  
  
a = len("hello")  
b = len(greeting)  
c = len("hello" + "Ruth")  
d = len(greeting + name)  
  
print("hello")  
  
print()  
  
print(len(greeting + name))
```

What are the:

- **Function calls** or “function invocations” or “call sites”?
- **arguments** or **actual parameters** for each function call?
- **math.sqrt** and **len** take input and return a value.
- **print** produces a side effect (it prints to the terminal).

Some functions are like a machine

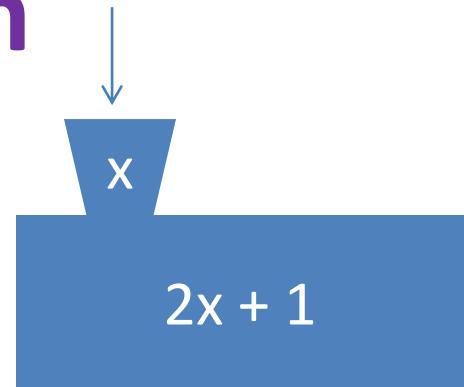
- You give it input
- It produces a result, “returns” a value



In math: $\text{func}(x) = 2x + 1$

Defining a function

Define the machine,
including the input and the result



```
def dbl_plus(x):  
    return 2 * x + 1
```

Name of the function.
Like “y = 5” for a variable

Keyword that means:
I am **def**ining a function

Input variable name,
or “formal parameter”

Keyword that means:
This is the result

Return expression
(part of the **return** statement)

How Python executes a function call

Function definition

```
def square(x):  
    return x * x
```

Formal parameter
(a variable)

Example function call:

```
y = 1 + square(3 + 4)  
y = 1 + square(7)
```

evaluate this expression

```
y = 1 + 49  
y = 50
```

```
return x * x  
return 7 * x  
return 7 * 7  
return 49
```

square(3 + 4)

Argument or
“actual parameter”

Function call or
function invocation,
the “call site”

Variables:
x: 7

1. Evaluate the **argument(s)** at the **call site** – the place where we are calling the function from in our program
2. Assign the **argument's value** to the **formal parameter name**
 - This is a *new* variable, only usable inside of the function body
3. Evaluate the **statements** in the **body of the function** one by one
4. At a **return** statement:
 - **Formal parameter variable** disappears – exists only during the call!
 - Execution continues at the call site. The function call expression evaluates to the “returned” value

Function definition examples

```
def dbl_plus(x):  
    return 2 * x + 1
```

```
def instructor_name():  
    return "Ruth Anderson"
```

```
def square(x):  
    return x * x
```

```
def calc_grade(points):  
    grade = points * 10  
    return grade
```

For each **function definition**, identify:

- Function **name**
- Function **body**
- **formal parameters**

grade is a local variable.
A *temporary* variable that only exists inside of the function body.

[See in python tutor](#)

Function definitions and calls

```
def dbl_plus(x):
    return 2 * x + 1

def instructor_name():
    return "Ruth Anderson"

def calc_grade(points):
    grade = points * 10
    return grade

# main program
dbp3 = dbl_plus(3)
dbp4 = dbl_plus(4)
print(dbp3 + dbp4)
print(instructor_name())
my_grade = calc_grade(dbp3)
```

Identify:

- Function **definitions**
- **formal parameters**
- **Function calls** or
“function invocations” or
“call sites”?
- **arguments** or
actual parameters?

This is all in the same file

[See in python tutor](#)

More function definitions and calls

```
def square(x):  
    return x * x  
  
def print_greeting():  
    print("Hello, world")  
  
def calc_grade(points):  
    grade = points * 10  
    return grade  
  
def print_grade(points):  
    grade = points * 10  
    print("Grade is:", grade)  
  
# main program  
sq1 = square(3)  
print_greeting()  
my_grade = calc_grade(sq1)  
print_grade(5)
```

No **return** statement
Returns the value **None**
Executed for side effect

No **return** statement
Returns the value **None**
Executed for side effect

This is all in the same file

In a function body, assignment creates a local variable

grade is a **local variable**.
A *temporary* variable that only exists inside of the function body.

```
def calc_grade(points):  
    grade = points * 10  
    return grade
```

formal parameter

```
score = 10  
final_grade = calc_grade(score)
```

argument or “actual parameter”

- **points** and **grade** can only be used in the body of the **calc_grade** function
 - Their **scope** is the body of the **calc_grade** function
- **grade** is a **local variable**
- **points** is a **formal parameter**
 - **formal parameters** are similar to local variables in terms of scope, but they start off with an initial value, provided by the argument or actual parameter to the function call
- **score** and **final_grade** are variables in the **global scope**

Local variables exist only while the function is executing

```
def cent_to_fahr(cent):  
    result = cent / 5.0 * 9 + 32  
    return result
```

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```
tempf = cent_to_fahr(15)  
print(result)
```

How to look up a variable

1. Check whether the variable is defined in the **local scope**. If not, go to step 2.
2. Check whether the variable is defined in the **global scope**

If a local and a global variable have the **same name**, the global variable is inaccessible (“**shadowed**”)

This is confusing; try to avoid such shadowing!

```
def lookup():
    x = 42
    return stored + x
x = 22
stored = 100
val = lookup()
```

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How many **x** variables?

```
def square(x):
    return x * x

def abs(x):
    if x < 0:
        return -x
    else:
        return x

# main program
x = 42
sq3 = square(3)
sq4 = square(4)
print(sq3 + sq4)
print(x)
x = -22
result = abs(x)
print(result)
```

This is all in the same file

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Shadowed variables

```
x = 22
stored = 100
def lookup():
    x = 42
    return stored + x
val = lookup()
x = 5
stored = 200
val = lookup()
```

Poor style. In general
we declare functions at
the top of a program.

```
def lookup():
    x = 42
    return stored + x
x = 22
stored = 100
val = lookup()
x = 5
stored = 200
val = lookup()
```

[See in python tutor](#)

Functions can call functions

```
def fahr_to_cent(fahr):  
    return (fahr - 32) / 9.0 * 5
```

```
def cent_to_fahr(cent):  
    result = cent / 5.0 * 9 + 32  
    return result
```

```
def print_fahr_to_cent(fahr):  
    result = fahr_to_cent(fahr)  
    print(result)
```

```
# main program  
boiling = fahr_to_cent(212)  
cold = cent_to_fahr(-30)  
print(print_fahr_to_cent(32))
```

No `return` statement
Returns the value `None`
Executed for side effect

This is all in the same file

Digression: Two types of output

- An expression evaluates to a value
 - Which can be used by the containing expression or statement
- A `print` statement writes text to the screen
- The Python **interpreter** (used the first week of class) reads statements and expressions, then executes them, like a calculator
- If the **interpreter** executes an expression, it prints its value
- In a **program (VSCode, Python Tutor)**, evaluating an expression does not print it
- In a **program**, printing an expression does not permit it to be used elsewhere

In a function body, assignment creates a temporary variable

```
def store_it(arg):  
    stored = arg  
    return stored  
  
stored = 0  
  
y = store_it(22)  
print(y)  
print(stored)
```

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Use only the local and the global scope!

```
myvar = 1

def outer():
    myvar = 1000
    temp = inner()
    return temp

def inner():
    return myvar

print(outer())
```

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Aside: The Evaluation Rules have a more precise rule, which applies when you define a function inside another function (which we will not be doing in this class!!!).



Functions are an Abstraction

- Abstraction = ignore some details
- Generalization = become usable in more contexts
- Abstraction over **computations**:
 - functional abstraction, a.k.a. procedural abstraction
- As long as you know what the function **means**, you don't care **how** it computes that value
 - You don't care about the *implementation* (the function body)

Defining absolute value

```
def abs(x):  
    if x < 0:  
        return -1 * x  
    else:  
        return 1 * x
```

```
def abs(x):  
    if x < 0:  
        result = -x  
    else:  
        result = x  
    return result
```

```
def abs(x):  
    if x < 0:  
        return -x  
    else:  
        return x
```

```
def abs(x):  
    return math.sqrt(x * x)
```

Defining round (for positive numbers)

```
def round(x):  
    return int(x + 0.5)
```

```
def round(x):  
    fraction = x - int(x)  
    if fraction >= 0.5:  
        return int(x) + 1  
    else:  
        return int(x)
```

Two types of documentation

1. Documentation for **users/clients/callers**
 - Document the *purpose* or *meaning* or *abstraction* that the function represents
 - Often called the “docstring”
 - Tells **what** the function does
 - Should be written for *every* function
2. Documentation for **programmers** who are reading the code
 - Document the *implementation* – specific code choices
 - Tells **how** the function does it
 - Only necessary for tricky or interesting bits of the code

For **users**: a string as the first element of the function body

```
def square(x):  
    """Returns the square of its argument."""  
    # Uses "x*x" instead of "x**2"  
    return x * x
```

For **programmers**:
arbitrary text after #

Multi-line strings

- Ways to write strings:
 - "hello"
 - 'hello'
 - """hello"""
 - '''hello'''
- Triple-quote version:
 - can include newlines (carriage returns),
so the string can span multiple lines
 - can include quotation marks
 - Use """hello""" version for docstrings

Don't write useless comments

- Comments should give information that is not apparent from the code
- Here is a counter-productive comment that merely clutters the code, which makes the code *harder* to read:

```
# increment the value of x  
x = x + 1
```



DO NOT write comments like this.

Where to write comments

- By convention, write a comment *above* the code that it describes (or, more rarely, on the same line)
 - First, a reader sees the English intuition or explanation, then the possibly-confusing code

```
# The following code is adapted from
# "Introduction to Algorithms", by Cormen et al.,
# section 14.22.

while (n > i):
    ...
    ...
```
- A comment may appear anywhere in your program, including at the end of a line:

```
x = y + x      # a comment about this line
```
- For a line that starts with #, indentation should be consistent with surrounding code

Decomposing a problem

- Breaking down a program into functions is *the fundamental activity* of programming!
- How do you decide when to use a function?
 - One rule: DRY (Don't Repeat Yourself)
 - Whenever you are tempted to copy and paste code, don't!
- Now, how do you design a function?

How to design a function

1. Wishful thinking:

Write the program as if the function already exists

2. Write a specification:

Describe the inputs and output, including their types

No implementation yet!

3. Write tests:

Example inputs and outputs

4. Write the function body (the implementation)

First, write your plan in English, then translate to Python

```
def fahr_to_cent(fahr):
    """Input: a number representing degrees Farenheit
    Return value: a number representing degrees centigrade
    """
    result = (fahr - 32) / 9.0 * 5
    return result

assert fahr_to_cent(32) == 0
assert fahr_to_cent(212) == 100
assert fahr_to_cent(98.6) == 37
assert fahr_to_cent(-40) == -40

# Main program
tempf = 32
print("Temperature in Farenheit:", tempf)
tempc = fahr_to_cent(tempf)
print("Temperature in Celsius:", tempc)
```

More Examples

```
def cent_to_fahr(cent):
    print(cent / 5.0 * 9 + 32)

print(cent_to_fahr(20))
```

```
def myfunc(n):
    total = 0
    for i in range(n):
        total = total + i
    return total

print(myfunc(4))
```

```
def c_to_f(c):
    print "c_to_f"
    return c / 5.0 * 9 + 32
```

```
def make_message(temp):
    print("make_message")
    return "The temperature is " +
str(temp)

for tempc in [-40, 0, 37]:
    tempf = c_to_f(tempc)
    message = make_message(tempf)
    print(message)
```

double(7)

abs(-20 - 2) + 20

Use the Python Tutor:
<http://pythontutor.com/>

What does this print?

```
def cent_to_fahr(cent):  
    print(cent / 5.0 * 9 + 32)  
  
print(cent_to_fahr(20))
```

What does this print?

```
def myfunc(n):  
    total = 0  
  
    for i in range(n):  
        total = total + i  
  
    return total  
  
  
print(myfunc(4))
```

What does this print?

```
def c_to_f(c) :  
    print("c_to_f")  
    return c / 5.0 * 9 + 32  
  
def make_message(temp) :  
    print("make_message")  
    return "The temperature is " + str(temp)  
  
for tempc in [-40, 0, 37] :  
    tempf = c_to_f(tempc)  
    message = make_message(tempf)  
    print(message)
```

What does this print?

```
def c_to_f(c) :  
    print("c_to_f")  
    return c / 5.0 * 9 + 32  
  
def make_message(temp) :  
    print("make_message")  
    return "The temperature is " + str(temp)  
  
for tempc in [-40, 0, 37] :  
    tempf = c_to_f(tempc)  
    message = make_message(tempf)  
    print(message)
```

c_to_f	
make_message	The temperature is -40.0
c_to_f	
make_message	The temperature is 32.0
c_to_f	
make_message	The temperature is 98.6

Each variable should represent one thing

```
def atm_to_mbar(pressure):
    return pressure * 1013.25

def mbar_to_mmHg(pressure):
    return pressure * 0.75006

# Confusing
pressure = 1.2 # in atmospheres
pressure = atm_to_mbar(pressure)
pressure = mbar_to_mmHg(pressure)
print(pressure)

# Better
in_atm = 1.2
in_mbar = atm_to_mbar(in_atm)
in_mmHg = mbar_to_mmHg(in_mbar)
print(in_mmHg)
```

```
# Best
def atm_to_mmHg(pressure):
    in_mbar = atm_to_mbar(pressure)
    in_mmHg = mbar_to_mmHg(in_mbar)
    return in_mmHg
print(atm_to_mmHg(1.2))
```

Corollary: Each variable should contain values of only one type

```
# Legal, but confusing: don't do this!
x = 3
...
x = "hello"
...
x = [3, 1, 4, 1, 5]
...
```

If you use a descriptive variable name, you are unlikely to make these mistakes

Review: how to evaluate a function call

1. Evaluate the function and its arguments to values
2. Create a new stack frame
 - The parent frame is the one where the function is defined
 - In CSE 160, this is always the global frame
 - A frame has bindings from variables to values
 - Looking up a variable starts in the local frame
 - Proceeds to its parent frame (the global frame) if no match in local frame
 - All the frames together are called the “environment”
3. Assign the actual argument values to the formal parameter variable
 - Add these as bindings in the new stack frame
4. Evaluate the body
 - Execute the statements in the function body
 - At a return statement, return the value and exit the function
 - If reach the end of the body of the function without encountering a return statement, then return the value **None**
(It is also fine to explicitly have a statement: `return None`)
5. Remove the stack frame
6. The call evaluates to the returned value

Bonus Slides: Extra Function Calls

Example of function invocation

<code>def square(x):</code>	
<code>return x * x</code>	
	Variables:
<code>square(3) + square(4)</code>	(none)
<code>return x * x</code>	x: 3
<code>return 3 * x</code>	x: 3
<code>return 3 * 3</code>	x: 3
<code>return 9</code>	x: 3
<code>9 + square(4)</code>	(none)
<code>return x * x</code>	x: 4
<code>return 4 * x</code>	x: 4
<code>return 4 * 4</code>	x: 4
<code>return 16</code>	x: 4
<code>9 + 16</code>	(none)
<code>25</code>	(none)

Expression with nested function invocations:

Only one executes at a time

```
def fahr_to_cent(fahr):  
    return (fahr - 32) / 9.0 * 5
```

```
def cent_to_fahr(cent):  
    return cent / 5.0 * 9 + 32
```

```
fahr_to_cent(cent_to_fahr(20))  
    return cent / 5.0 * 9 + 32  
    return 20 / 5.0 * 9 + 32  
    return 68
```

```
fahr_to_cent(68)  
return (fahr - 32) / 9.0 * 5  
return (68 - 32) / 9.0 * 5  
return 20
```

20

Variables:

(none)

cent: 20

cent: 20

cent: 20

(none)

fahr: 68

fahr: 68

fahr: 68

(none)

Expression with nested function invocations:

Only one executes at a time

```
def square(x):  
    return x * x  
  
square(square(3))  
    return x * x  
    return 3 * x  
    return 3 * 3  
    return 9  
  
square(9)  
    return x * x  
    return 9 * x  
    return 9 * 9  
    return 81
```

Variables:

(none)

x: 3

x: 3

x: 3

x: 3

(none)

x: 9

x: 9

x: 9

x: 9

Function that invokes another function:

Both function invocations are active

```
def square(z):  
    return z * z  
  
def hypotenuse(x, y):  
    return math.sqrt(square(x) + square(y))
```

```
hypotenuse(3, 4)
```

Variables:

(none)

```
    return math.sqrt(square(x) + square(y))
```

x: 3 y:4

```
    return math.sqrt(square(3) + square(y))
```

x: 3 y:4

```
        return z * z
```

z: 3 x: 3 y:4

```
        return 3 * 3
```

z: 3 x: 3 y:4

```
        return 9
```

z: 3 x: 3 y:4

```
return math.sqrt(9 + square(y))
```

x: 3 y:4

```
return math.sqrt(9 + square(4))
```

x: 3 y:4

```
        return z * z
```

z: 4 x: 3 y:4

```
        return 4 * 4
```

z: 4 x: 3 y:4

```
        return 16
```

z: 4 x: 3 y:4

```
return math.sqrt(9 + 16)
```

x: 3 y:4

```
return math.sqrt(25)
```

x: 3 y:4

```
return 5
```

x: 3 y:4

(none)

Shadowing of formal variable names

```
def square(x):  
    return x * x  
  
def hypotenuse(x, y):  
    return math.sqrt(square(x) + square(y))  
  
hypotenuse(3, 4)  
    return math.sqrt(square(x) + square(y))  
    return math.sqrt(square(3) + square(y))  
        return x * x  
        return 3 * 3  
        return 9  
  
    return math.sqrt(9 + square(y))  
    return math.sqrt(9 + square(4))  
        return x * x  
        return 4 * 4  
        return 16  
  
    return math.sqrt(9 + 16)  
    return math.sqrt(25)  
    return 5
```

Same formal parameter name,
but two completely different variables

Variables:

(none)

x: 3 y:4

x: 3 y:4

x: 3 y:4

x: 3 y:4

x: 4 x: 3 y:4

x: 4 x: 3 y:4

x: 4 x: 3 y:4

x: 3 y:4

x: 3 y:4

x: 3 y:4

(none)

Formal parameter
is a *new* variable

Shadowing of formal variable names

```
def square(x):  
    return x * x  
  
def hypotenuse(x, y):  
    return math.sqrt(square(x) + square(y))  
  
hypotenuse(3, 4)  
    return math.sqrt(square(x) + square(y))  
    return math.sqrt(square(3) + square(y))  
        return x * x  
        return 3 * 3  
        return 9  
    return math.sqrt(9 + square(y))  
    return math.sqrt(9 + square(4))  
        return x * x  
        return 4 * 4  
        return 16  
    return math.sqrt(9 + 16)  
    return math.sqrt(25)  
    return 5
```

Same diagram, with
variable scopes or
environment frames
shown explicitly

Variables:

