1. ArrayList Mystery

Consider the following method:

```java
public static void mystery(ArrayList<Integer> list) {
    for (int index = 0; index < list.size(); index++) {
        int elementValue = list.remove(index);
        if (elementValue % 2 == 0) {
            list.add(index);
        }
    }
    System.out.println(list);
}
```

Write the output produced by the method when passed each of the following ArrayLists:

<table>
<thead>
<tr>
<th>List</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>a) [5, 2, 5, 2]</td>
<td></td>
</tr>
<tr>
<td>b) [3, 5, 8, 9, 2]</td>
<td></td>
</tr>
<tr>
<td>c) [0, 1, 4, 3, 1, 3]</td>
<td></td>
</tr>
</tbody>
</table>

2. Recursive Tracing

For each of the calls to the following recursive method below, indicate what output is produced:

```java
public static void mystery(int x, int y) {
    if (y <= 0) {
        System.out.print("0 ");
    } else if (x > y) {
        System.out.print(x + " ");
        mystery(x - y, y);
    } else {
        System.out.print(y + " ");
        mystery(x, y - x);
    }
}
```

<table>
<thead>
<tr>
<th>Call</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>a) mystery(6, 3);</td>
<td></td>
</tr>
<tr>
<td>b) mystery(2, 3);</td>
<td></td>
</tr>
<tr>
<td>c) mystery(5, 8);</td>
<td></td>
</tr>
<tr>
<td>d) mystery(21, 12);</td>
<td></td>
</tr>
<tr>
<td>e) mystery(3, 10);</td>
<td></td>
</tr>
</tbody>
</table>
3. Collections

Write a method `byAge` that accepts three parameters: 1) a `Map` where each key is a person's name (a string) and the associated value is that person's age (an integer); 2) an integer for a minimum age; and 3) an integer for a max age. Your method should return a new map with information about people with ages between the min and max, inclusive.

In your result map, each key is an integer age, and the value for that key is a string with the names of all people at that age, separated by "and" if there is more than one person of that age. Include only ages between the min and max inclusive, where there is at least one person of that age in the original map. If the map passed in is empty, or if there are no people in the map between the min/max ages, return an empty map.

For example, if a `Map` named `ages` stores the following key=value pairs:

```
{Paul=28, David=20, Janette=18, Marty=35, Stuart=98, Jessica=35, Helene=40, Allison=18, Sara=15, Grace=25, Zack=20, Galen=15, Erik=20, Tyler=6, Benson=48}
```

The call of `byAge(ages, 16, 25)` should return the following map (the contents can be in any order):

```
{18=Janette and Allison, 20=David and Zack and Erik, 25=Grace}
```

For the same map, the call of `byAge(ages, 20, 40)` should return the following map:

```
{20=David and Zack and Erik, 25=Grace, 28=Paul, 35=Marty and Jessica, 40=Helene}
```

For full credit, obey the following restrictions in your solution. A solution that disobeys them can get partial credit.

- You will need to construct a map to store your results, but you may not use any other structures (arrays, lists, etc.) as auxiliary storage. (You can have as many simple variables as you like.)
- You should not modify the contents of the map passed to your method.
- Your solution should run in no worse than \( O(N \log N) \) time, where \( N \) is the number of pairs in the map.
4. Stacks and Queues

Write a method `isSorted` that accepts a stack of integers as a parameter and returns `true` if the elements in the stack occur in ascending (non-decreasing) order from top to bottom, and `false` otherwise. That is, the smallest element should be on top, growing larger toward the bottom. For example, passing the following stack should return `true`:

```
bottom [20, 20, 17, 11, 8, 8, 3, 2] top
```

The following stack is not sorted (the 15 is out of place), so passing it to your method should return a result of `false`:

```
bottom [18, 12, 15, 6, 1] top
```

An empty or one-element stack is considered to be sorted. When your method returns, the stack should be in the same state as when it was passed in. In other words, if your method modifies the stack, you must restore it before returning.

For full credit, obey the following restrictions in your solution. A solution that disobeys them can get partial credit.

- You may use one queue or one stack (but not both) as auxiliary storage.
  You may not use other structures (arrays, lists, etc.), but you can have as many simple variables as you like.
- Use the Queue interface and Stack/LinkedList classes discussed in class.
- Use stacks/queues in stack/queue-like ways only. Do not use index-based methods such as get, search, or set, or for-each loops or iterators. You may call add, remove, push, pop, peek, isEmpty, and size.
- Your solution should run in O(N) time, where N is the number of elements of the stack.

You have access to the following two methods and may call them as needed to help you solve the problem:

```java
public static void s2q(Stack<Integer> s, Queue<Integer> q) { ... }
public static void q2s(Queue<Integer> q, Stack<Integer> s) { ... }
```
Write a method `minToFront` to be added to the `LinkedIntList` class. Your method should move the smallest element value to the front of the linked list. Suppose a `LinkedIntList` variable named `list` stores these elements:

```
[7, 9, 12, 5, 3, 17]
```

If you made the call of `list.minToFront();`, the list would then store the elements:

```
[3, 7, 9, 12, 5, 17]
```

If the list has more than one occurrence of the minimum value, the first occurrence is the only one that should be moved. For example, `[7, 9, 3, 12, 5, 3, 17, 3]` becomes `[3, 7, 9, 12, 5, 3, 17, 3]`. If the list is empty, calling your method should have no effect.

For full credit, obey the following restrictions in your solution. A solution that disobeys them can get partial credit.

- Do not call any other methods on the `LinkedIntList` object, such as `add`, `remove`, or `size`.
- Do not create new `ListNode` objects (though you may have as many `ListNode` variables as you like).
- Do not use other data structures such as arrays, lists, queues, etc.
- Your solution should run in O(N) time, where N is the number of elements of the linked list.

Assume that you are adding this method to the `LinkedIntList` class (that uses the `ListNode` class) below.

```java
public class LinkedIntList {
    private ListNode front;
    ...
}
```

```java
public class ListNode {
    public int data;
    public ListNode next;
    ...
}
```
6. Recursive Programming

Write a recursive method `moveToEnd` that accepts a `String s` and a `char c` as parameters, and returns a new `String` similar to `s` but with all occurrences of `c` moved to the end. The relative order of the other characters should be unchanged from their order in the original string `s`. If `s` does not contain `c`, it should be returned unmodified.

The following table shows calls to your method and their return values. Occurrences of `c` are underlined for clarity.

<table>
<thead>
<tr>
<th>Call</th>
<th>Returns</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>moveToEnd(&quot;hello&quot;, 'l')</code></td>
<td>&quot;heoll&quot;</td>
</tr>
<tr>
<td><code>moveToEnd(&quot;hello&quot;, 'e')</code></td>
<td>&quot;hlloe&quot;</td>
</tr>
<tr>
<td><code>moveToEnd(&quot;hello there&quot;, 'e')</code></td>
<td>&quot;hlo threee&quot;</td>
</tr>
<tr>
<td><code>moveToEnd(&quot;hello there&quot;, 'q')</code></td>
<td>&quot;hello there&quot;</td>
</tr>
<tr>
<td><code>moveToEnd(&quot;HELLO there&quot;, 'e')</code></td>
<td>&quot;HELLO threee&quot;</td>
</tr>
<tr>
<td><code>moveToEnd(&quot;&quot;, 'x')</code></td>
<td>&quot;&quot;</td>
</tr>
</tbody>
</table>

You may not construct any structured objects other than `Strings` (no array, `List`, `Scanner`, etc.). You will examine the `String` one character at a time but you may not use any loops to solve this problem; you must use recursion.